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Analysis of Boundary Layer Statistical Properties at 1

Dome C, Antarctica 2

Jean-François Rysman · Sébastien 3

Verrier · Alain Lahellec · Christophe

Genthon 5

Abstract The boundary layer of the Antarctic Plateau is unique on account 6 of its isolated location and extreme stability. This study investigates the char-7 acteristics of this boundary layer using wind and temperature measurements 8 from a 45-m high tower located at Dome C. First, spectral analysis reveals 9 that both fields have a scaling behaviour from 30 minutes to 10 days (spectral 10 slope $\beta \approx 2$). Wind and temperature time series also shows a multifractal 11 behaviour. Therefore, it is possible to fit the moment-scaling function to the 12 universal multifractal model and obtain multifractal parameters for temper-13 ature ($\alpha \approx 1.51$ and $C_1 \approx 0.14$) and wind speed ($\alpha \approx 1.34$ and $C_1 \approx 0.13$). 14 The same analysis is repeated separately in winter and summer at six different 15 heights. The β parameter shows a strong stratification with height especially in

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¹⁷ summer. This means that properties of turbulence change surprisingly rapidly¹⁸ from the ground to the top of the tower.

¹⁹ Keywords Boundary Layer \cdot Dome C \cdot Meteorological tower \cdot Scaling \cdot

20 Statistical properties

21 1 Introduction

The Antarctic surface consists of a plateau ranging from 2000 to 4000 m in 22 altitude and covered 98 % by ice (King and Turner, 1997). One of its local 23 maxima is Dome C (3233 m), where the Concordia station has been installed 24 since 1997. At this station, meteorological measurements are taken at the sur-25 face with an automated weather station, while daily launched balloons pro-26 vide soundings of the troposphere. As snow surface emissivity is higher than 27 atmosphere emissivity, significant temperature inversion exists in this region 28 at night and during winter (Hudson and Brandt, 2005; Genthon et al., 2013). 29 Moreover, surface winds are weak over the Eastern Antarctic Plateau where 30 the surface is smooth. These features, which inhibit turbulence and vertical 31 motions, explain the extremely stable boundary layer at Dome C. The bound-32 ary layer may remain stable for several months almost without interruption, 33 leading to remarkable properties. The analysis of these properties is of high in-34 terest to meteorologists since it provides the opportunity to better understand 35 the characteristics of an extremely stable boundary layer in an unperturbed 36 environment and facilitates the development of parameterizations aimed at 37 global and regional models. 38

Overall, boundary layer properties in Antarctica are poorly studied compared with mid-latitude boundary layer properties because of the difficulty in performing surface measurements. To fill this gap, a tower was installed in 2007 close to the Concordia station. Instruments were set up to measure wind,

temperature, and humidity at six levels along the 45 m tower. At present, this 43 is the highest tower that performs continuous measurements in Antarctica. 44 As the boundary layer depth in Antarctica is very shallow, the vertical vari-45 ability is considerable and, for this reason, a tower is well adapted to study 46 boundary layer characteristics. The continuous measurements along the ver-47 tical are particularly interesting when studying the boundary layer temporal 48 evolution and especially when analyzing the transition between the stable and 49 convective boundary layer that occurs on summer days. 50

In most Antarctic stations, except for the South Pole and Halley stations, in-situ measurements are simply taken at standard meteorological levels (2 and 10 m). In addition, some measurement campaigns at high latitude regions have been performed with an instrumented mast (e.g., King and Turner, 1997; Travouillon et al., 2003; Grachev et al., 2005). As a result, long-term, in-situ, and high-quality measurements of the low atmosphere at high latitude are scarce and extremely valuable.

The present study is based on wind and temperature observations collected 58 from the tower at Dome C between January and December 2009. The objective 59 was to study the statistical properties of wind and temperature of the Dome C 60 boundary layer together with the vertical variability of these properties. The 61 analysis of the boundary layer is often difficult since processes with various 62 spatial and temporal scales occur conjointly. However, statistical properties 63 known as scaling or self-similarity can characterize this complex system with 64 only a few parameters. Experimental measurements have shown that scaling 65 properties are found in most geophysical fields and are related to atmospheric 66 turbulence, notably wind and temperature (Gage and Nastrom, 1986), cloud 67 radiance (Tessier et al., 1993), and rainfall (Verrier et al., 2011; Rysman et al., 68 2013)). As a result, we chose to use this approach in this paper. 69

First, we highlight and analyze the scaling behaviour of wind and temperature fields. In the second part of this analysis, we use the multifractal framework to obtain parameters that describe the fields intrinsic properties. This is the first time that such an innovative analysis is conducted in Antarctica and for such an extremely stable boundary layer. This approach allows us to characterize the full spectrum of signal variability that is not possible with standard approaches.

77 2 Data

The Concordia scientific station is based on a local maxima called Dome C (75° 06' S, 123° 20' E, 3233 m a.s.l.) in the eastern part of the Antarctic Plateau. The nearest coast is located more than 1000 km away. The local slope of the Dome is about 5×10^{-4} toward the north and 1×10^{-3} toward the east (based on NASA measurements at a 10' resolution). At this latitude, the sun culminates at 38° on 21 December, and the winter night extends between April and September.

In this study, we used meteorological instruments deployed along a 45 m 85 tower located 700 m from the Concordia station. The tower position was chosen 86 with respect to the atmospheric flow in order to minimize the influence of 87 station buildings. Six Väisälä hygrometers (4 HMP155 and 2 HMP45AC), 88 six pt100 DIN IEC 751 thermistors, and six Young 45106 aero-vanes were 89 mounted at 3.6 m, 11 m, 18.6 m, 25.9 m, 33.2 m, and 42.4 m. Measurements 90 were performed with a 10-second time step and averaged over 30 minutes. 91 Additional technical details can be found in Genthon et al. (2010, 2013). 92

93 3 Methodology

94 3.1 Scaling

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Initially, approaches based on a single exponent, called monofractal approaches, were used to characterize the scaling properties of a field over a given inertial range. Among these approaches, spectral analysis is widely used. It has been shown that if a physical field presents scaling properties, its power spectral density E (Priestley , 1981), proportional to the square of the modulus of the Fourier transform of the field, follows power-law behaviour as a function of frequency f (i.e., log-log linearity):

$$E(f) \simeq f^{-\beta} \tag{1}$$

¹⁰³ The β value depends on the correlation in a given field: a highly correlated ¹⁰⁴ field has a high β exponent, while a white noise (uncorrelated field) has a β ¹⁰⁵ exponent equal to zero (for details, see Rysman et al. (2013)).

Another way to highlight the scaling behaviour of a field is to test the firstorder structure function log-log linearity. The first-order structure function corresponds to the statistical average of the absolute increments for different lags (this is a first-order function analogue to variograms):

$$S(\delta t) = \langle |X(t+\delta t) - X(t)| \rangle \simeq \delta t^{H}$$
⁽²⁾

where δt is the time lag (varying from 0 to the time series length), S the firstorder structure function and $\langle \rangle$ is the ensemble averaging operator. As for β , H indicates the smoothness of the field.

¹¹⁴ 3.2 Multifractal

Subsequently, refinements were proposed in order to take into account the 115 strong inhomogeneity in the energy fluxes (e.g., Yaglom, 1966). These refine-116 ments rely on multiplicative cascades, that is, the representation of multiscale 117 variability using a sequence of iterative multiplicative modulations of increas-118 ing resolution (e.g., Schertzer and Lovejoy, 1987; She and Leveque, 1994). 119 Such models can usually be parameterized using a few exponents with more 120 or less obvious physical interpretations, thus giving a description of a much 121 wider class of variability than monofractal models (single parameter models). 122 More precisely, multiplicative cascades generate multifractal stochastic fields. 123 To investigate the validity of these theories with geophysical data, multifractal 124 analysis procedures are applied (e.g., Verrier et al., 2011). The latter relies on 125 the remarkable scaling properties of statistical moments of different orders that 126 generalize the spectral scaling properties to a wider class of process intensities. 127 Statistically speaking, a field Φ follows multifractal properties if the statis-128 tical moments of the field depend on the resolution in a power-law manner. The 129 power-law exponent only depends on the moment order, so that the statistical 130 moments of the normalized field can be expressed as: 131

$$\langle \Phi^q_{\lambda} \rangle \simeq \lambda^{K(q)}$$
 (3)

where $\langle \rangle$ is the ensemble averaging operator, q the moment order (nonnecessarily integer), λ the resolution, and K(q) the moment-scaling function, which relates to scaling exponents and moments. In the following, the empirical statistical moments are denoted as $M_q(\lambda)$.

Several parameterizations of the fundamental moment-scaling function K(q)exist (e.g., Schertzer and Lovejoy, 1987; She and Leveque, 1994). In this paper, we consider the two-parameter universal form defined by Schertzer and 142

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¹⁴⁰ Lovejoy (1987). K(q) is thus parametrized by two fundamental parameters, ¹⁴¹ C_1 (intermittency parameter) and α (index of multifractality):

$$K(q) = \frac{C_1}{\alpha - 1}(q^\alpha - q) \tag{4}$$

where $\alpha \in [0:2]$ and $\alpha \neq 1$ and $C_1 \in [0:D]$ with D the dimension of the 143 Euclidean space in which the field is defined (i.e., 1 in the case of time series). 144 A physical understanding of these parameters allows a given geophysical 145 field to be characterized. C_1 can be related to the intermittency of the data, 146 that is, the uniformity of the data around the mean. It increases as most of the 147 measured values depart from the mean. α relates to the presence of extreme 148 fluctuations within the field. High values of α indicate a field with a few large 149 singularities (for details on the interpretation of multifractal parameters, see 150 Pecknold et al., 1993; Purdy et al., 2001; Nykanen, 2008). 151

Often, Φ cannot be directly related to geophysical fields, because most of 152 these fields and atmospheric processes are better described as low-pass filtered 153 versions of multiplicative cascades. Therefore, a scaling filter such as fractional 154 integration is usually applied (Schertzer and Lovejoy, 1987). Consequently, 155 the properties of the conservative multifractal field Φ should be distinguished 156 from the (usually) non-conservative integrated fields (the term integrated is 157 related to the fractional integration needed to transform a conservative (non 158 integrated) multifractal field to a realistic physical field (non conservative and 159 integrated)). 160

The first step of a multifractal analysis is to determine whether the studied field is integrated. To this end, we use spectral analysis: if a field is integrated, its spectral slope is strictly (and notably) greater than 1. We then use the structure function. Indeed, the H exponent gives the order of fractional integration in the field and physically represents the degree of smoothing involved with the integration. For instance, H = 0 is associated with a conservative

¹⁶⁷ cascade (for details, see de Montera et al., 2009).

168 4 Results

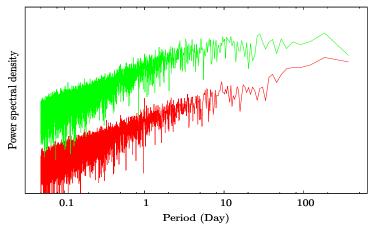


Fig. 1 Power spectral density of temperature (K² s⁻¹, red line) and zonal wind (m² s⁻³, green line) at 42.4 m in a log-log plot

Figure 1 reveals that the power spectral density of zonal wind and temper-169 ature scale with a slope of respectively 2.20 and 2.02 at 42.4 m (from 2 hours 170 up to 10 days). In other words, a high temporal autocorrelation exists be-171 tween these fields, with the temperature at a given time being related to the 172 temperature up to 10 days later. For longer periods of time, both fields ap-173 pear uncorrelated (spectral slope equals zero) because the meteorological noise 174 is greater than the remaining correlation. The region with periods exceeding 175 10 days is often called the spectral plateau. The spectral plateau has been 176 highlighted in various meteorological fields in the past (Fraedrich and Larn-177 der, 1993; Olsson, 1995; Fabry, 1996; Lovejoy and Schertzer, 2011; Rysman 178 et al., 2013), with a decorrelation period ranging from 5 days to 1 month, 179 which reveals a similarity among meteorological fields independent of local 180

characteristics. It must also be emphasized that both spectra are very similar 181 (similar slope and scaling range), suggesting a relationship between both vari-182 ables. This similarity can be related to the influence of wind on temperature; 183 for example, when the wind changes direction, local temperature is affected. 184 Since spectral slopes greater than 1 are notably observed, it means that 185 the fields are integrated. The next step is to determine the degree of fractional 186 integration in the fields. Figure 2 shows the first-order structure functions of 187 the temperature and zonal wind series, averaged over height. Regarding tem-188 perature, data only pertains to the period from January to October because 189 temperature sensors were interrupted for a few hours in October. For both 190 temperature and zonal wind, a scaling behaviour is found between 2 and 16 h 191 with an exponent H of about 0.69 (temperature) and 0.66 (zonal wind). This 192 confirms that for both variables, the observables should perhaps be related to 193 multifractal field only when applying a fractional integration. This is achieved 194 following Lavallée et al. (1993) and de Montera et al. (2009) with the compu-195 tation of the absolute gradient of the time series. 196

The empirical moments of the latter are then estimated in order to confirm 197 the validity of Eq. 3. In a log-log plot, the multiscaling behaviour of moments 198 appears as a sequence of straight lines, each associated with a unique moment 199 order. Figure 3 shows the behaviour of statistical moments (between 0 and 2) 200 of temperature and zonal wind as a function of scale in log-log coordinates. 201 Two regimes thus appear: from 2 h to 2 days and from 2 days to 0.5 month. Red 202 lines at high frequencies show the fit of moment laws in the range 2 h-2 days. 203 In this range of scales, the moments (especially high-order moments) strongly 204 vary with the scale in a way that might be approximated by multifractal 205 laws. Larger scales are characterized by much slighter variations of moments, 206 represented by flat curves at low frequencies. This confirms the findings of 207 the structure function analysis above, wherein a scaling regime was found at 208

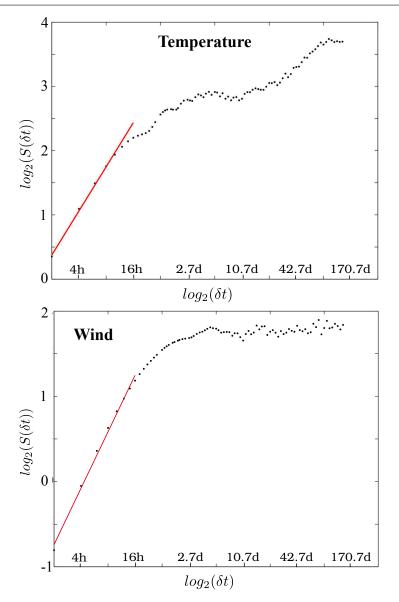


Fig. 2 First-order structure function $(S(\delta t))$ of temperature (K) and zonal wind (m.s-1) averaged over heights as a function of time lag (δt) ranging from 2 h to 170.7 days. Linear regressions between 2 and 16 h are shown as red lines

²⁰⁹ high frequencies, while all statistics had more regular scale behaviour on larger

210 scales.

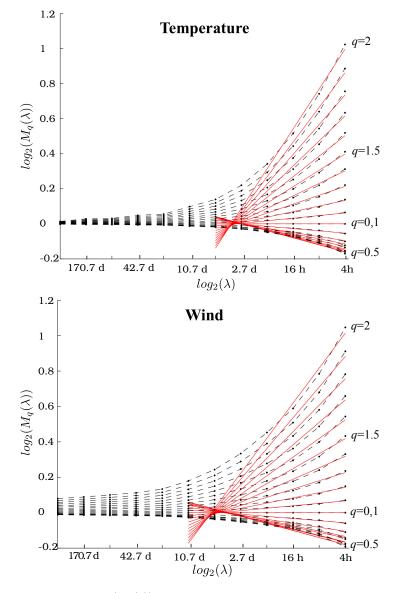


Fig. 3 Empirical moments $(M_q(\lambda))$ of the absolute temperature and zonal wind temporal gradients, averaged over heights as a function of the resolution ranging from 2 h to 170.7 days (log-log plot). Each straight line corresponds to a linear regression of the moments of fixed order q. The orders taken into consideration are q = 0, 0.1, 0.2, ..., 2.0

Previous figures showed that zonal wind and temperature fields have multifractal behaviour. The next step focusses on the multifractal parametrization of the 2 h-2 days regime in order to obtain C_1 and α parameters. Here, the

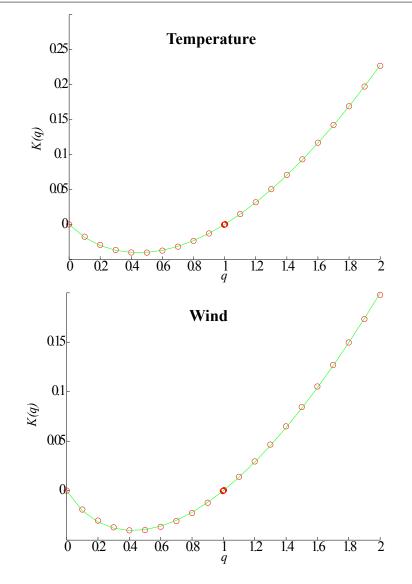


Fig. 4 Empirical moment-scaling function (K(q)) (red points), i.e., log-log slopes of the red fit lines in figure 3 and fit with universal multifractal model (green line) between 2 hours and 2 days for temperature and zonal wind averaged over height

slopes of the red fit lines previously computed are represented as a function K(q) for moment order q (Figure 4). The curve of the empirical scaling exponents K(q) is superimposed to the least-square best fit of the universal (α , C_1) form. First, we observe that the fits are very accurate, thus validating the choice of parameterization proposed by Schertzer and Lovejoy (1987). The best-fit parameters are $\alpha \approx 1.51$ and $C_1 \approx 0.14$ for temperature and $\alpha \approx 1.34$ and $C_1 \approx 0.13$ for zonal wind.

These parameters are consistent with previous multifractal analyses. For 221 instance, Schmitt et al. (1992) using laboratory observations obtained $\alpha \approx 1.2$ 222 and $C_1 \approx 0.15$ for temperature and $\alpha \approx 1.3$ and $C_1 \approx 0.25$ for wind. Further, 223 Stolle et al. (2009); Lovejoy and Schertzer (2010); Stolle et al. (2012) using 224 model outputs from tropical and mid-latitude regions obtained, in average, for 225 wind and temperature $\alpha \approx 1.8$ and $C_1 \approx 0.12$. The most significant difference 226 is found for the α parameter, which is lower in our observations compared to 227 the model outputs in tropical and mid-latitude regions. This could indicate 228 that our observations have less extreme values. However, it is difficult to give 229 further interpretation because of the substantial differences between datasets. 230 Additional analysis and measurements are thus required in order to deter-231 mine whether temperature and wind statistical properties significantly differ 232 at Dome C compared to other parts of the world. 233

Overall, the monofractal and multifractal results reveal the intrinsic quality of the data. Indeed, positive slopes for spectra and moments highlight the organisation (or correlation) within the geophysical field (see Nykanen, 2008; Rysman et al., 2013), meaning that the noise of data is low compared to the meteorological signal. Moreover, most of the fits show a rather low noise.

Turning to the effect of elevation and season on scaling parameters, the same scaling analysis was applied separately to continuous period of summer (January-February) and winter (July-August) seasons for each height (table 1).

Table 1 shows that scaling parameters depend on the season and height. Overall parameters are lower during winter (e.g., for wind $\beta \simeq 2.00\pm0.03$) than during summer (e.g., for wind $\beta \simeq 2.21\pm0.09$). Moreover, during winter,

	Winter			
Height (m)	Wind		Temperature	
	β	H	β	Н
3.6	$2.01{\pm}0.18$	$0.68{\pm}0.09$	$2.25{\pm}0.17$	$0.74{\pm}0.10$
11	$1.95{\pm}0.21$	$0.65{\pm}0.10$	$2.11{\pm}0.20$	$0.72 {\pm} 0.06$
18.4	$1.97{\pm}0.22$	$0.68{\pm}0.13$	-	-
25.9	$2.05{\pm}0.17$	$0.67 {\pm} 0.11$	-	-
33.2	$2.00{\pm}0.14$	$0.65{\pm}0.10$	$1.95{\pm}0.24$	$0.66{\pm}0.09$
42.4	$2.00{\pm}0.23$	$0.64{\pm}0.11$	$2.00{\pm}0.22$	$0.69{\pm}0.09$
	Summer			
3.6	$2.06{\pm}0.17$	$0.68{\pm}0.05$	$2.14{\pm}0.22$	$0.91{\pm}0.03$
11	$2.14{\pm}0.14$	$0.72 {\pm} 0.04$	$2.05{\pm}0.23$	$0.85{\pm}0.06$
18.4	$2.22{\pm}0.13$	$0.75 {\pm} 0.04$	$1.89{\pm}0.28$	$0.75 {\pm} 0.07$
25.9	$2.26{\pm}0.12$	$0.74{\pm}0.04$	$1.91{\pm}0.17$	$0.71{\pm}0.06$
33.2	$2.28{\pm}0.14$	$0.75{\pm}0.04$	$1.92{\pm}0.18$	$0.69{\pm}0.05$
42.4	$2.29{\pm}0.13$	$0.75 {\pm} 0.04$	$1.89{\pm}0.23$	$0.68{\pm}0.06$

 Table 1
 Multifractal parameters as a function of height and season (Summer (January-February) and Winter (July-August)). Missing data are indicated by a - and correspond to periods of interruptions for temperature sensors

 β (2.00±0.03) and H (0.66±0.02) are rather constant with height for zonal 246 wind while β and H decrease from the ground to the top of the tower for tem-247 perature (from 2.25 to 2 for β and from 0.74 to 0.69 for H). During summer, 248 the zonal wind shows a stratification with height for the H (from 0.68 to 0.75) 249 and the β parameters (2.06 to 2.29). Regarding temperature, H parameter 250 goes from 0.91 to 0.68 and β goes from 2.14 to 1.89. The C_1 and α parameters 251 do not seem to be affected by season or height for both fields (not shown in 252 the table). Note that, as the uncertainties in β and H values are significant 253 (see table 1), no definitive conclusions can be drawn on the significance of 254 highlighted tendencies. Because boundary layer is almost continuously stable 255 during winter, scaling parameters are characteristics of stable conditions dur-256 ing this season. During summer, boundary layer is alternatively convective and 257

stable. Therefore scaling parameters are likely to be affected by both stableand convective conditions during this season.

²⁶⁰ 5 Summary and Discussion

This study conducted an analysis of wind and temperature measurements 261 taken at Dome C during the 2009 field campaign. First, the computation of the 262 power spectra of wind and temperature reveals that both fields present scaling 263 properties from 30 minutes to 10 days with a β exponent of approximately 2. 264 Second, the analysis of the first-order structure function provides the degree 265 of fractional integration in both fields (i.e., H=0.69 for temperature and 266 H=0.66 for zonal wind). The computation of the empirical moment for the 267 temporal gradients of the wind and temperature time series reveals multifractal 268 behaviour. Thus, it is possible to use the universal multifractal model to fit 269 the moment-scaling function K(q) and obtain the α and C_1 parameters. The 270 same analysis is repeated for winter and summer seasons for six elevations 271 and provides β and H parameters in these various conditions. While β and 272 H are constant with height during winter for the wind, a stratification of H273 and β parameter is found during summer (e.g., from 2.06 to 2.29 for β). A 274 stratification of β and H parameter also exists for the temperature in both 275 winter and summer. 276

For the first time, this analysis provides scaling parameters in Antarctica for a very stable boundary layer. An important result is the height dependency for β and H especially in summer. For the zonal wind the parameters increase from the ground to the top of the tower while for the temperature the parameters decrease from the ground to the top of the tower. This result is very surprising and to the authors best knowledge, this is the first time that such an effect has been observed in these conditions. This behaviour is probably related to the different properties of turbulence at the ground and at the top of the tower due to the very strong temperature vertical gradient. In particular, a steeper slope indicates a higher correlation within data; that is turbulence could be stronger close to the ground than at higher levels. Further interpretations require additional measurements of turbulence at Dome C.

This analysis could be used to evaluate parametrizations used in simula-289 tions (Stolle et al., 2012, 2009). Indeed, many aspects of a meteorological field 290 can be fully characterized using the multifractal approach with only few coef-291 ficients, e.g., the statistical moments and the probability distribution functions 292 of the field for scales ranging from the data resolution to the time series length. 293 Therefore, following the methodology of this paper, simulation outputs (and 294 associated parametrizations) could be evaluated in a new and innovative way. 295 In particular, this method could help to evaluate the statistical relationships 296 between scales in simulations (which is not usually done to our knowledge). 297 Moreover it will help identifying parametrizations that do not respect scaling-298 laws i.e., that are not physically meaningful. 299

These computed values and our conclusions must be validated with other 300 measurements obtained in similar conditions, but to our knowledge, no previ-301 ous scaling (including multifractal) analysis has been conducted in the region. 302 Finally, this analysis also highlights the intrinsic quality of our data. Indeed, 303 most of the fitted functions were found to have relatively little noise with 304 regard to the extreme atmospheric conditions. Since the tower still provides 305 data, it will be possible in the future to improve the accuracy of the scaling pa-306 rameters. Moreover, measurements from sonic anemo-thermometers recently 307 deployed along the tower will be highly valuable to understand the scaling 308 properties of wind and temperature highlighted in this study. 309

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