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Worldwide wavelet analysis of geomagnetic jerks

Mioara Alexandrescu,¹ Dominique Gibert,² Gauthier Hulot,¹
Jean-Louis Le Mouél,¹ and Ginette Saracco²

Abstract. Following an earlier study which gives the principles of the method and an example of application to the eastern component of the magnetic field in the European region [Alexandrescu *et al.*, 1995], detection and characterization of geomagnetic jerks using wavelet analysis is generalized to any horizontal component of the field and to a worldwide distribution (involving 97 locations) of observations. This allows for a systematic and global search for such events within the twentieth century and makes it possible to unravel a number of intriguing properties associated with them. Whereas our first study only reveals five such events in Europe, we can now state that seven and only seven events have apparently occurred throughout the world during the present century. Two (1969 and 1978) are unquestionably of global extent, three (1901, 1913, and 1925) being possibly of similar extent, while the remaining two (1932 and 1949) are not seen everywhere at the Earth's surface. We confirm our early result that the events are more singular than previously thought, with a "regularity" systematically closer to 1.5 than to 2, and a common mean value of about 1.6. Furthermore, the 1969 and 1978 events display a two-step spatio-temporal behavior consisting of an "early arrival" in the northern hemisphere, a "late arrival" in the southern hemisphere, and a time lag between the two arrivals of the order of a couple of years. We were also able to show that the 1969 and 1978 events tend to at least partially balance each other. The extent to which this is true remains to be assessed, mainly because our method, although already providing some information about the geometry of the events, does not yet allow the proper recovery of their intensities.

Introduction

Assessing the exact nature of the time changes of the magnetic field of internal origin at the surface of the Earth and at the core-mantle boundary is important, not only for its own sake but also for the information it can give about the deep Earth, such as the electrical conductivity of the lower mantle, the motions at the surface the fluid core, and the interaction between the core and the mantle.

The identification of an abrupt change in the trend of the geomagnetic secular variation, referred to as a "jerk" [Courillot *et al.*, 1978; Malin *et al.*, 1983], and the demonstration that it really is of internal origin, required quite some efforts in the past years. This internal origin now seems to be well established. Malin and Hodder [1982] devised a filter to measure the magnitude of the 1970 discontinuity in the second time derivative

of the field components at 83 observatories; performing a spherical harmonic analysis of these magnitudes led them to conclude that most of the sudden change is indeed of internal origin. Gubbins and Tomlinson [1986] removed the external field effects from the data and attributed the discontinuity in the time derivatives of the resulting time series to an internal origin. Gauthier *et al.* [1986] analyzed monthly mean values and also stressed the internal nature of the phenomenon.

However, the definition and characteristics of the geomagnetic jerks are still a matter of debate in the geomagnetic community. Even the fundamental parameters of a jerk, such as the date at which it occurs, the time duration of the impulse, or the worldwide character of the event are not agreed upon by all the researchers.

The late 1960s event has for instance been reported as occurring in 1969 [Courillot *et al.*, 1978; Courillot and Le Mouél, 1984; McLeod, 1985, 1989; Golovkov *et al.*, 1989], 1970 [Stewart and Whaler, 1995], or 1971/1972 in the Australian region [Gubbins and Tomlinson, 1986; Whaler, 1987]. Another sudden change in the secular acceleration of the geomagnetic field has been reported around 1978 [Gauthier *et al.*, 1986; Gubbins and Tomlinson, 1986; Langel *et al.*, 1986; McLeod, 1989; Stewart and Whaler, 1995]. Stewart [1991] indicated the existence of another jerk in 1983, also detected in South

¹Institut de Physique du Globe de Paris, Paris, France.

²Géosciences Rennes — Centre National de la Recherche Scientifique/Institut National des Sciences de l'Univers, Rennes, France.

Africa by Kotzé *et al.* [1991] and on South Georgia island by Dowson *et al.* [1988]. Other jerks have also been detected earlier in this century: in 1913 [Courillot and Le Mouél, 1984; Ducruix and Le Mouél, 1983; Gire *et al.*, 1984] and in 1925 [McLeod, 1989], and a number of suggestions have been made for some jerks in 1940 [McLeod, 1989], 1937, 1947, and 1958 [Golovkov *et al.*, 1989]. However, in a recent study focusing on the European area and using the wavelet analysis of monthly mean values, five and only five events have been detected since the beginning of this century: around 1902, 1913, 1925, 1969, and 1978 [Alexandrescu *et al.*, 1995]. As this method has been proved to be objective and efficient, we now present a systematic and worldwide analysis in order to exactly assess the existence, timing (and possible regional delays), and general characteristics of such events.

A good determination of the duration (which can be defined as the time needed for the change of slope in the time series of the secular variation to be completed), and time of occurrence of these events is very much required. A change of the core field in a time span of about a year or less would, for instance, shorten the period of variations of internal origin as given by early estimates [Currie, 1967, 1968; Alldredge, 1984]. Also, the effect of the conducting mantle could be addressed with better data. Backus [1983], who discussed the filtering effect of the mantle and suggested that it behaves as a causal time-invariant real linear filter, noted that the centroid date (emergence time) and smoothing time of the jerk could be different at different locations at the Earth surface, even in the case of an ideal jerk occurring at the core-mantle boundary. A study of the jerks using a time sampling which could resolve these differences would therefore prove very valuable.

Up to now most studies focused on the European region [Ducruix *et al.*, 1980; Achache *et al.*, 1980; Gavoret *et al.*, 1986] which has by far the best coverage of observatories and for which the impulse field usually has a strong Y (east) component. But impulses are also known to be found in other components and elsewhere [see Courillot and Le Mouél, 1988]. Analyzing only the usual orthogonal components of the geomagnetic field (X , Y , Z) may mean that impulses might have been masked at some places due to this choice of axes. In the present study we will therefore extend our previous analysis [Alexandrescu *et al.*, 1995] (hereinafter referred to as paper 1) to worldwide data and apply the wavelet analysis to linear combinations of the horizontal components (X and Y), in order to better estimate the characteristics of the jerks.

Method of Analysis

Detection of Singularities With Wavelets

The theoretical background is identical to the one described in paper 1, except for a few details, and the reader is referred to this paper for a full description of wavelet analysis applied to singularity detection. A

brief description of the main aspects of the method is given in the appendix. A significant difference with our previous study is that the present analysis is no longer restricted to the Y component. It is generalized and aims at recovering the direction and sense of the horizontal component of the jerk.

Now, as in paper 1, we will assume that the signal recorded in the observatories is the sum of a main-field signal containing singularities, that is, jerks, an external long-period signal, and noise. In paper 1 we decomposed the analyzed Y component in the following canonical form:

$$Y(t) = \beta j_\alpha(t) + h_Y(t) + n_Y(t), \quad (1)$$

where βj_α is the jerk signal (it represents an abrupt change with a regularity α and intensity β localized at the time t_0):

$$j_\alpha(t) = \begin{cases} 0 & t \leq t_0 \\ (t - t_0)^\alpha & t > t_0 \end{cases}, \quad (2)$$

h_Y is the Y component of the "periodic" external signal and n_Y the noise on the Y component. Let us now generalize this decomposition to the horizontal component $\vec{H}(t)$ of the field. The external signal $\vec{h}$ can reasonably be supposed to be linearly polarized, as it is mainly generated by the ring current. We will also assume that the jerk signal is linearly polarized. This means that the jerk components X and Y are assumed to be proportional and to share the same regularity. This is a strong assumption we might need to reconsider later on. But it will allow us to detect the direction along which the jerk is the strongest. We will then be able to determine its characteristics along this particular direction.

We will therefore assume that

$$X(t) = \beta \cos(\theta) j_\alpha(t) + \cos(\varphi) h(t) + n_X(t), \quad (3)$$

$$Y(t) = \beta \sin(\theta) j_\alpha(t) + \sin(\varphi) h(t) + n_Y(t). \quad (4)$$

The noise will be considered as being isotropic. The angle θ (counted eastward from the geographical north direction) will be called the direction angle of the jerk; φ the direction angle of the external signal.

The first step of the analysis consists in computing a set of linear combinations of the original components:

$$f_{\theta'}(t) = \cos(\theta') X(t) + \sin(\theta') Y(t), \quad (5)$$

where the rotation angle θ' spans $[0, \pi]$. The second step consists of taking the wavelet transform of the signal (see the appendix). The linearity of the wavelet transform implies that

$$\begin{aligned} W f_{\theta'}(t, a) &= \cos(\theta') W X(t, a) + \sin(\theta') W Y(t, a) \\ &= \beta \cos(\theta - \theta') W j_\alpha(t, a) \\ &\quad + \cos(\varphi - \theta') W h(t, a) \\ &\quad + W [n_X \cos(\theta') + n_Y \sin(\theta')] (t, a). \end{aligned} \quad (6)$$

For a rotation angle $\theta' = \theta_e = \theta + \pi/2$, the jerk is removed from the composite signal, and the wavelet trans-

form of the rotated signal $f_{\theta_e}(t)$ is limited to the one of both the harmonic signals and the noise:

$$Wf_{\theta_e}(t, a) = \cos(\varphi - \theta_e)Wh(t, a) + W[n_X \sin(\theta_e) + n_Y \cos(\theta_e)](t, a). \quad (7)$$

In this case, and in view of the results obtained in paper 1, all ridge functions extracted from the wavelet transform $Wf_{\theta_e}(t, a)$ should be either of type 2 (i.e., typical of the harmonic signals) or of type 3 (i.e., strongly altered by the random noise); see the appendix.

If the rotation angle is now $\theta' = \theta_b = \varphi + \pi/2$,

$$Wf_{\theta_b}(t, a) = \beta \cos(\theta - \theta_b)Wj_{\alpha}(t, a) + W[n_X \cos(\theta_b) + n_Y \sin(\theta_b)](t, a), \quad (8)$$

the contribution of the wavelet transform of the harmonic signal disappears and the ridge functions of type 1 associated with the jerk should be better detected in the wavelet transform $Wf_{\theta_b}(t, a)$.

Assessment of the Method

We now give several synthetic examples to illustrate the theoretical considerations developed in the preceding section. As already mentioned, the results presented in this study have been obtained with the same analyzing wavelet as in paper 1. However, in order to obtain the most reliable assessment of the method, we did not use the harmonic signal and synthetic noise described in this previous paper. Instead we used data extracted directly from six European observatories (BFE, CLF, ESK, HAD, LER, NGK) and covering the 1925-1970 period displaying no jerk (in Europe). To these time series, considered to be typical real signals free of any jerks, was superimposed a synthetic jerk with a regularity $\alpha = 1.65$ and a strength $\beta = 0.17 \text{ nT} \times \text{month}^{-\alpha}$ estimated from the 1969 jerk detected in the Chambon-la-Forêt Y series (see equation (12) of paper 1).

We set $\theta = \pi/4$, and the synthetic jerk was successively injected at 1943, 1945, 1947, 1949, and 1951 in order to look for some possible influence of the relative phasing of the external signal with respect to the jerk. From the previous section we can expect that both the date and the regularity of the jerk should be best estimated for $\theta' = \theta_b = \varphi + \pi/2$, and the jerk removed for $\theta' = \theta_e = \theta + \pi/2$. This was checked very efficiently using the movie procedure included in the seismic processing package distributed by the Center for Wave Phenomena at the Colorado School of Mines [Scales, 1995]. This is the way we determine the direction θ of the jerk. The sign of the jerk along this direction can then be recovered by inspection of the sign of the wavelet transform (see the appendix). In this way we finally get local characteristic directions for the jerk.

An example of a movie sequence represented at 10° intervals for the CLF series and the 1947 synthetic jerk is shown on Plate 1. Such sequences have actually been computed for 5° increments (not shown on Plate 1 for reasons of space) in order to accurately detect the extinction of the jerk which is clearly achieved within a limited range (10°) of angles θ' around $\theta + \pi/2$. The signature of the jerk is visible for a wide range of angles θ' centered on θ_b in the form of a conelike patch of large amplitude. A precise determination of both the date and the regularity α of the event can be obtained from the ridge functions displaying the best type 1 behavior (Figure 1, which displays the 18 ridge functions corresponding to the sequence shown in Plate 1).

Since the appearance of the jerk is not as sudden as its extinction, type 1 ridge functions can be observed within an interval of θ' of some tens of degrees. The center of this interval depends on both θ and φ , and

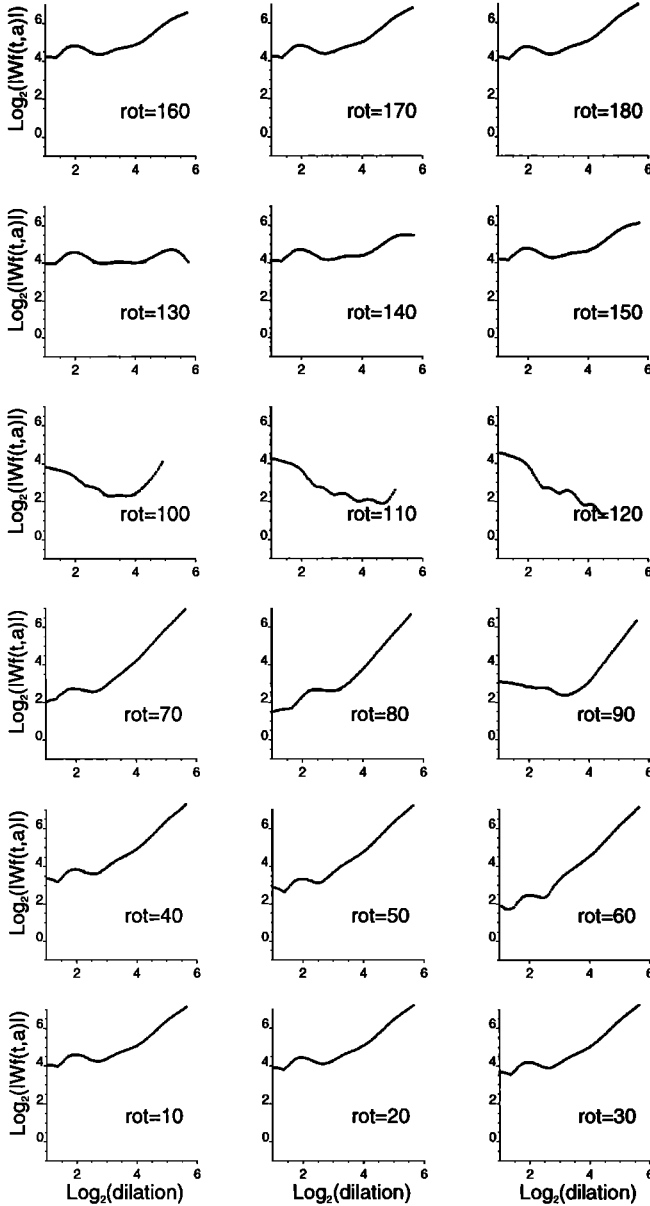


Figure 1. Ridge functions for the 1947 artificial jerk injected in the CLF series and computed for θ' spanning $[0^\circ, 180^\circ]$ in steps of 10° . The ridge functions of type 2 observed for $\theta' = 130^\circ$ and 140° correspond to the extinction of the jerk (as detected in Plate 1). Good quality ridge functions of type 1 are observed for $40^\circ \leq \theta' \leq 90^\circ$.

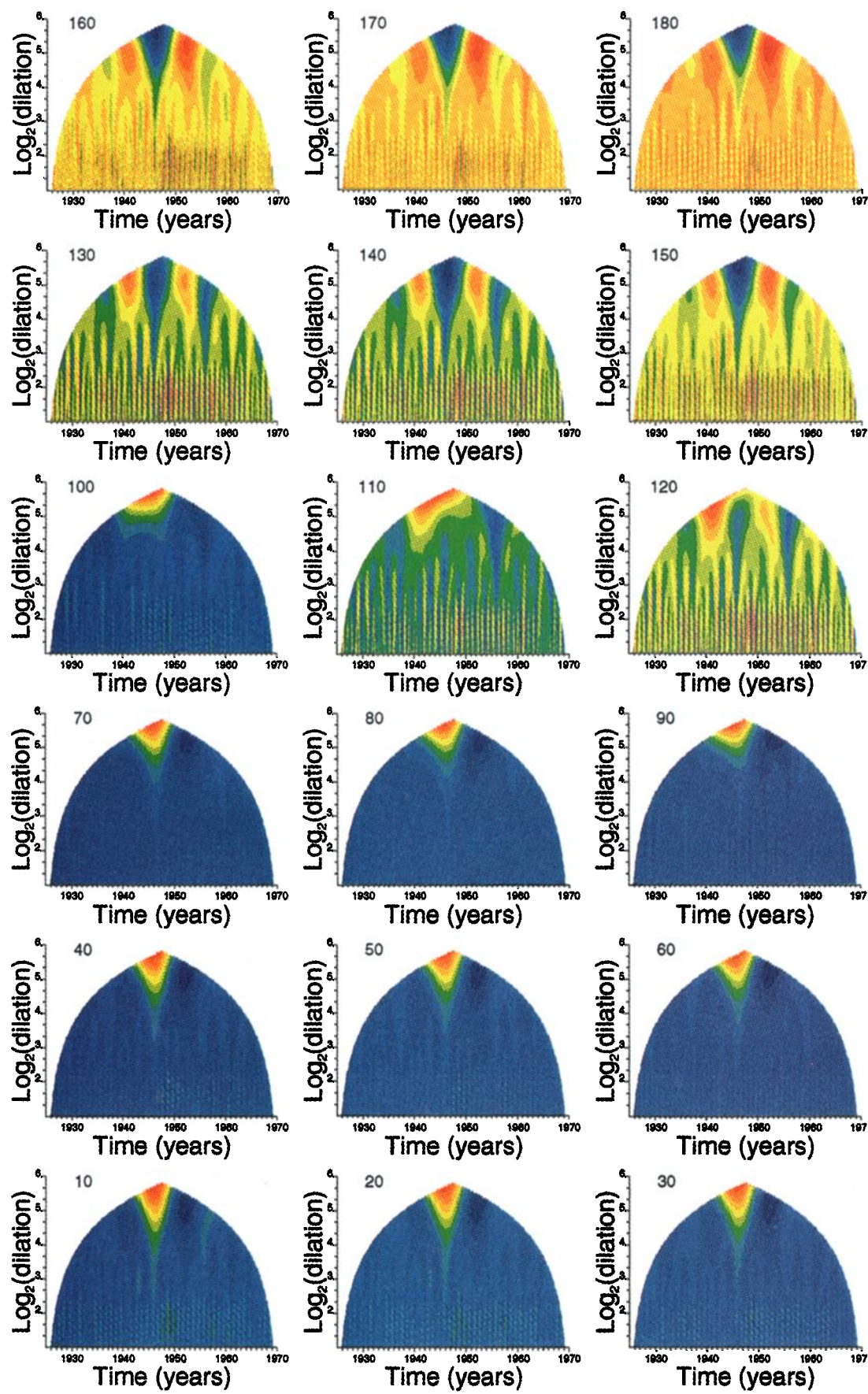


Table 1. Results of the Synthetic Tests

Date	Data	θ_b , deg	Date	α	θ , deg
1943.0	18	77 (9)	1942.6 (0.2)	1.62 (0.10)	47.5 (2.5)
1945.0	18	70 (8)	1944.8 (0.4)	1.75 (0.15)	47.5 (2.5)
1947.0	18	65 (10)	1946.4 (0.3)	1.65 (0.13)	46.1 (3.1)
1949.0	18	70 (8)	1948.8 (0.2)	1.58 (0.10)	44.2 (3.2)
1951.0	18	70 (10)	1950.3 (0.5)	1.70 (0.14)	44.4 (3.0)

Numbers in parentheses are standard deviations.

gives a poor estimate of θ_b (to determine θ_b more accurately, we would symmetrically look for the direction $\varphi + \pi/2$ which extinguishes the harmonic type ridge function).

Now, for the six previously mentioned synthetic series, we retrieved the extinction angle θ_e and examined the best type 1 ridge functions. The statistics of the results for the five injection dates are summarized in Table 1. These statistics include the three best type 1 ridge functions for each observatory. It appears that the method allows the recovery of the regularity α with a relative uncertainty of about 10% and the extinction angle θ_e within an error of the order of 5° . The dating of the jerks should ideally be done using the lines of extrema for very small dilations where the time localization of the wavelets is more precise (see the appendix). In practice, we use the smallest dilations unaffected by the noise and corresponding to the small-dilation end of the linear part of the ridge functions (i.e., $a \simeq 2^{3.5}$ as can be seen in Figure 1). The whole set of lines of extrema corresponding to the analyzed ridge functions of type 1 (Table 1) is shown on Figure 2. At small dilations ($a \lesssim 2^{3.5}$), the lines are controlled by the noise and are scattered. For the dilation range corresponding to the linear part of the ridge functions ($a \gtrsim 2^{3.5}$), the lines characterizing each date of artificial jerk are well localized within a time interval smaller than 1 year. However, this part of the lines of extrema form curved arches with their large-dilation end located at dates about 2 years before the theoretical dates. The statistics show that the dates obtained for the smallest dilation available (i.e., $a \simeq 2^{3.5}$) fall within an interval of about 6 months and that, due to the curvature of the lines of extrema, the average dates obtained are slightly biased (less than 6 months) toward the inferior dates (Table 1). Therefore in what follows, dilations $a \simeq 2^{3.5}$ will be used for dating the real jerks.

Data Selection

The present study has been performed on observatory monthly means (defined as being the average over all days of the month and all times of the day) obtained

from the National Geophysical Data Center (NGDC, Boulder, Colorado) or directly from the observatories. In the latter case the data were either obtained in digital form or digitized from year books. For the purposes of the present study the first criterion in data selection was the length and continuity of the time series of the northward (X) and eastward (Y) components (available or computable from declination (D) and horizontal intensity (H)). Only observatories for which time series were available over a continuous time interval longer than 12 years have been selected. We had to accept some gaps in some of the series and, in these cases, a linear interpolation was used to reconstruct the missing values; the largest gaps we corrected for were 6 months long. In the case of a longer gap the time series was split into two.

Following this initial selection, all time series were subjected to a careful validation procedure using the wavelet transform as in paper 1. When anomalies were

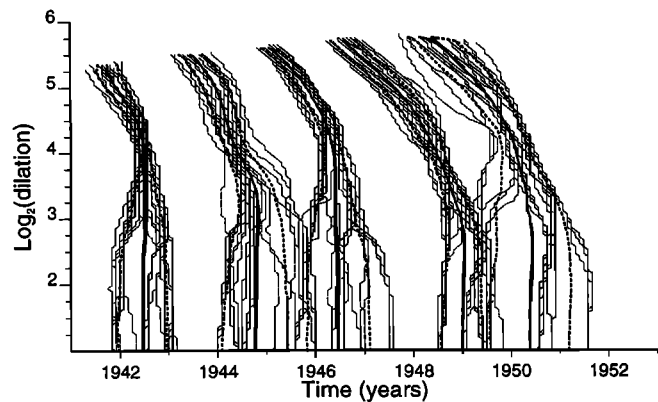


Figure 2. Lines of extrema extracted from the wavelet transforms computed from the five artificial jerks injected at 1943, 1945, 1947, 1949, and 1951 into the BFE, CLF, ESK, HAD, LER, and NGK data series. Only the best three lines are drawn (see text for details). For each artificial jerk the average of the lines of extrema (solid lines) indicates the time of occurrence (see also Table 1). Also shown are the standard deviations of the lines of extrema (dashed curves).

Plate 1. Wavelet transforms of the 1947 artificial jerk injected in the CLF series and computed for θ' spanning $[0^\circ, 180^\circ]$ in steps of 10° . The extinction of the jerk begins for $\theta' = 100^\circ$ and it is complete for $\theta' = 130^\circ$. The color scale represents the sign of the wavelet transform: red indicates positive, blue indicates negative.

Table 2a. Observatories Considered in the Present Study

Code ^a	Name	λ^b	φ^c	Period ^d	Source ^e	Jump ^f
AAE	Addis Abeba	9.030	38.765	1958-1974	obs	...
ABG	Alibag	18.638	76.917	1921-1991	obs	...
AGN	Agincourt	43.783	280.733	1932-1969	wdc	1958
AIA	Faraday Islands	-65.245	295.742	1957-1984	obs	...
AML	Amberley	-43.152	172.722	1923-1978	obs	...
AMS	Martin de Vivies	-37.833	77.567	1981-1991	bcmt	...
AMT	Amatsia	31.550	34.917	1976-1988	obs	...
ANN	Annamalainagar	11.367	79.683	1958-1991	obs	...
API	Apia	-13.807	188.225	1921-1989	obs	...
AQL	L'Aquila	42.383	13.317	1960-1993	obs	...
ARC	Arctowski	-62.160	301.522	1978-1993	obs	...
ARS	Arti	56.433	58.567	1945-1956	obs	...
...	...	...	...	1973-1993	...	...
BEL	Belsk	51.837	20.792	1966-1994	obs	...
BFE	Brorfelde	55.625	11.672	1907-1994	obs	1982
BLC	Baker Lake	64.333	263.967	1960-1994	wdc	1969, 1975, 1977
BNG	Bangui	4.437	18.565	1955-1991	bcmt	1957
BOU	Boulder	40.138	254.762	1967-1985	wdc	...
BRW	Barrow	71.323	203.380	1965-1989	wdc	...
CBB	Cambridge Bay	69.200	255.000	1973-1985	...	...
CLF	Chambon la Forêt	48.023	2.260	1883-1994	obs	1957, 1968, 1983
CMO	College	64.860	212.163	1948-1982	wdc	1947
COI	Coimbra	40.222	351.378	1866-1942	obs	...
...	...	...	...	1952-1992	obs	...
CZT	Port Alfred	-46.433	51.867	1974-1991	bcmt	...
DBN	De Bilt	52.102	5.177	1903-1938	wdc	...
DOU	Dourbes	50.097	4.595	1964-1988	obs	...
DRV	Dumont d'Urville	-66.665	140.007	1962-1991	bcmt	...
EBR	Ebro	40.820	0.493	1910-1937	obs	...
...	...	...	...	1950-1981	obs	...
ESK	Eskdalemuir	55.317	356.800	1911-1994	obs	...
FCC	Fort Churchill	58.767	265.900	1964-1994	wdc	...
FRD	Fredericksburg	38.205	282.627	1901-1989	wdc	1957
FUQ	Fuquene	5.470	286.263	1954-1994	obs	...
FUR	Furstenfeldbruck	48.165	11.277	1940-1993	obs	...
GDH	Godhavn	69.252	306.467	1926-1993	wdc	1975
GNA	Gnangara	-31.783	115.950	1919-1992	obs	1958
GUA	Guam	13.583	144.870	1958-1980	wdc	...
GWC	Great Whale River	55.267	282.217	1966-1984	wdc	...
HAD	Hartland	50.995	356.517	1926-1993	obs	...
HBK	Hartebeeshoek	-25.882	27.707	1964-1986	obs	...
HER	Hermanus	-34.425	19.225	1941-1993	obs	...
HLP	Hel	54.608	18.815	1966-1993	obs	...
HON	Honolulu	21.320	201.998	1902-1976	obs	1947, 1960
HRB	Hurbanovo	47.873	18.190	1893-1914	obs	...
...	...	...	...	1949-1994	...	...
HRN	Hornsund	77.000	15.550	1978-1993	obs	...
HUA	Huancayo	-12.045	286.660	1922-1989	obs	...
HYB	Hyderabad	17.413	78.555	1965-1991	obs	...
IRT	Patrony	52.167	104.450	1959-1990	obs	1977
KAK	Kakioka	36.230	140.190	1897-1917	obs	...
...	...	...	...	1924-1993	obs	1958
KIV	Kiev (Dymer)	50.717	30.300	1958-1992	obs	1964
KNY	Kanoya	31.420	130.882	1958-1993	wdc	...
KOD	Kodaikanal	10.230	77.463	1965-1991	obs	...
LAS	Las Acacias	-35.007	302.310	1962-1993	obs	...
LER	Lerwick	60.133	358.817	1926-1993	wdc	...
LNN	Voyekovo	59.950	30.705	1947-1985	wdc	1963
LRV	Leirvogur	64.183	338.300	1953-1994	obs	...
LVV	Lvov	49.900	23.750	1953-1978	wdc	1969
MAW	Mawson	-67.600	62.880	1961-1992	obs	...
MBC	Mould Bay	76.200	240.600	1963-1994	wdc	...
MBO	M'Bour	14.392	343.042	1952-1991	bcmt	...
MCQ	Macquarie Island	-54.500	158.950	1961-1993	obs	...
MEA	Meanook	54.617	246.667	1932-1994	wdc	...

Table 2a. (continued)

Code ^a	Name	λ^b	φ^c	Period ^d	Source ^e	Jump ^f
MMB	Memambetsu	43.907	144.193	1958-1994	wdc	...
MMK	Loparskoye	68.250	33.083	1959-1980	wdc	1961, 1965
MNK	Pleshenitzi	54.500	27.883	1961-1990	wdc	...
MOS	Krasnaya Pakhra	55.467	37.312	1947-1988	wdc	...
NEW	Newport	48.263	242.880	1966-1989	wdc	...
NGK	Niemegk	52.072	12.675	1890-1994	obs	...
NUR	Nurmijarvi	60.508	24.655	1953-1994	obs	...
NVS	Klyuchi	55.033	82.900	1966-1989	wdc	1972
ODE	Stepanovka	46.783	30.883	1948-1981	obs	...
PAF	Port-aux-Français	-49.350	70.200	1958-1991	bcmt	1980
PAG	Panagyuriste	42.512	24.177	1956-1992	obs	1962
PMG	Port Moresby	-9.408	147.150	1958-1988	wdc	...
POD	Podkamennaya	61.600	90.000	1969-1990	wdc	...
PPT	Pamatai	-17.568	210.425	1969-1991	bcmt	...
RES	Resolute Bay	74.100	265.100	1954-1994	obs	1967
SAB	Sabhawala	30.363	77.798	1965-1991	obs	...
SBA	Scott Base	-77.850	166.783	1964-1989	wdc	...
SIT	Sitka	57.058	224.675	1902-1993	wdc	...
SJG	San Juan	18.113	293.85	1926-1993	wdc	1965
SOD	Sodankyla	67.368	26.6300	1914-1945	wdc	1945
...	...	...	...	1946-1993	...	...
SPA	South Pole	-89.993	346.678	1959-1971	wdc	...
SUA	Surlari	44.680	26.253	1949-1993	obs	...
TEO	Teoloyucan	19.747	260.818	1960-1978	obs	...
TFS	Dusheti	42.092	44.705	1959-1992	wdc	...
THL	Thule	77.483	290.833	1959-1988	wdc	...
THY	Tihany	46.900	17.893	1955-1987	obs	1979
TOO	Toolangi	-37.530	145.470	1953-1979	obs	...
TRD	Trivandrum	8.483	76.950	1958-1991	obs	...
TRW	Trelew	-43.248	294.685	1957-1992	obs	...
TSU	Tsumeb	-19.217	17.700	1964-1989	obs	...
TUC	Tucson	32.247	249.167	1910-1993	wdc	...
VAL	Valentia	51.933	349.750	1954-1993	obs	...
VIC	Victoria	48.517	236.583	1964-1994	wdc	...
VQS	Vieques	18.147	294.552	1903-1925	wdc	...
WIK	Wien Kobenzl	48.265	16.318	1956-1994	obs	...
WIT	Witteveen	52.813	6.668	1938-1987	wdc	...
WNG	Wingst	53.743	9.073	1939-1993	obs	...

^aAccording to the International Association of Geomagnetism and Aeronomy (IAGA) convention.^bLatitude of the observatory, in degrees.^cLongitude of the observatory, in degrees, positive eastward.^dInterval of time with uninterrupted *X* and *Y* series.^eData retrieved from bcmt, Bureau Central de Magnétisme Terrestre (Institut de Physique du Globe, Paris, France); wdc, World Data Center (Boulder, Colorado); obs, data supplied by the observatory.^fDates of changes in the baselines.

detected, we carefully checked the consistency of the monthly mean values with the annual mean values on the same CD-ROM (labeled NGDC 05/1) by computing the annual means from the monthly means and comparing them with the archived values. This revealed that in some observatories and at certain epochs changes in the base level had been applied to the annual means (indicated by "J" in the file called "annual" on NGDC CD-ROM) but not to the monthly means. We corrected for this, by simply applying the required changes to the monthly series. When this correction did not give satisfying results, more information was directly requested from the observatories; several of them acknowledged that corrections due to changes in instrumental baselines had been omitted.

The lists of available observatories with the corre-

sponding code, geographical coordinates, lengths of time series and baseline corrections are given in Tables 2a and 2b (note that further useful data might still be obtained from other observatories). The geographical distribution of these observatories is shown on Figure 3. Let us emphasize that the process of establishing sound time series in the way just described, however time consuming, is both an essential step to the following analysis and a very efficient way of identifying possible problems within the observatory data.

Results

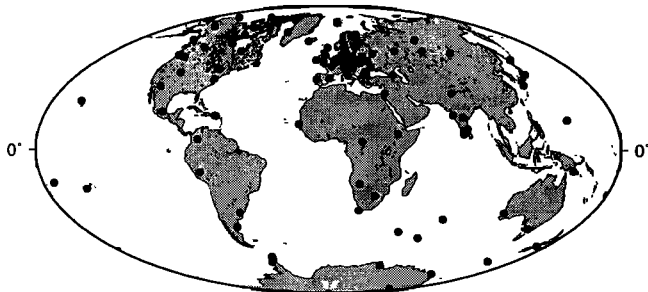
The same analysis procedure as the one used previously for the synthetic tests has been applied to the *X* and *Y* series of the 97 observatories of Table 2a. Only a

Table 2b. Corrections Made to Observatory Baselines in This Study

Code ^a	Name	Jump Date ^b	X ^c	Y ^d	Z ^e
AGN	Agincourt	1958	-239	-547	56
BFE	Brorfelde	1982	137	-1	-266
BLC	Baker Lake	1969	93	-88	8
BLC	Baker Lake	1975	-60	95	3
BLC	Baker Lake	1977	-6	0	60
BNG	Bangui	1957	-111	9	27
CLF	Chambon la Forêt	1957	-34	4	-70
CLF	Chambon la Forêt	1968	1	17	-11
CLF	Chambon la Forêt	1983	1	0	1
CMO	College	1947	22	-49	100
FRD	Fredericksburg	1957	471	186	-413
GDH	Godhavn	1975	40	-36	275
GNA	Gnangara	1958	-909	-50	-1269
HON	Honolulu	1947	224	602	-237
HON	Honolulu	1960	-244	-88	-421
IRT	Patrony	1977	4	8	8
KAK	Kakioka	1958	11	-19	-44
KIV	Kiev (Dymer)	1964	43	-104	-10
LNN	Voyeykovo	1963	17	-6	15
LVV	Lvov	1969	0	0	36
MMK	Loparskoye	1961	150	207	-270
MMK	Loparskoye	1965	-1	0	30
NVS	Klyuchi	1972	6	1	5
PAF	Port-aux-Français	1980	0	0	1
PAG	Panagyuriste	1962	0	-2	0
RES	Resolute Bay	1967	-10	5	-10
SJG	San Juan	1965	-83	207	-257
SOD	Sodankyla	1945	-13	-25	-124
THY	Tihany	1979	0	0	20

^aAccording to the IAGA convention.^bAccording to Table 2a.^cCorrection applied to X component, in nanotesla.^dCorrection applied to Y component, in nanotesla.^eCorrection applied to Z component, in nanotesla.

small number of observatories have long enough records to allow for the detection of the jerks occurring during the first quarter of the century. The whole set of results is given in Tables 3a-g; the dates found for the jerks cluster into seven groups hereinafter referred to as the 1901, 1913, 1925, 1932, 1949, 1969, and 1978 events (Figure 4). For each of the seven jerks detected in the data series, the extinction angle θ_e can be determined with the same accuracy as in the case of the synthetic tests.

**Figure 3.** Distribution of the 97 observatories considered in the present study. See also Table 2a for more details.

Early Events

The 1901 event was successfully detected in all observatories with available data for this epoch. It clearly appears, with well-defined ridge functions of type 1, in three European observatories (CLF, COI, NGK, see Table 3a and Figure 5). It is also present, as a late edge of an energy packet (see the appendix for more details), in the wavelet transforms of the HRB and KAK series. However, the insufficient duration of the records for these two observatories (compare Table 2a) did not allow us to recover the ridge functions over a large range of dilations. Dates (1902.0 ± 0.5) and regular-

Table 3a. Results for the 1901 Event

θ^a	θ_b^b	α^c	Date ^d	Code
125	90	1.60	1901.33	CLF
120	70	1.66	1902.60	COI
130	80	1.55	1902.17	NGK

^aDirection angle of the jerk in degrees.^bEnhancement angle of the jerk in degrees.^cSlope of the ridge function.^dDate of occurrence of the jerk.

Table 3b. Results for the 1913 Event

θ^a	θ_b^b	α^c	Date ^d	Code
65	90	1.41	1913.92	BFE
140	90	1.47	1913.17	CLF
120	80	1.35	1911.14	COI
130	90	1.37	1915.17	DBN
165	50	1.28	1913.33	FRD
160	60	1.26	1913.17	HON
140	90	1.60	1913.75	NGK
25	110	1.61	1915.05	SIT
25	90	1.42	1913.67	VQS

^aDirection angle of the jerk in degrees.^bEnhancement angle of the jerk in degrees.^cSlope of the ridge function.^dDate of occurrence of the jerk.

ities ($\alpha = 1.60 \pm 0.04$) found for this jerk are almost identical for the three observatories where they could be computed. It seems safe to conclude that the 1901 jerk is observed in a large part of the northern hemisphere, but it may be of worldwide extent.

The 1913 event has also been detected in all observatories with sufficient data (see Table 2a). It is clearly observed in five European (BFE, CLF, COI, DBN, NGK) and three North American (FRD, SIT, VQS) observatories and HON (Table 3b and Figure 6). Most dates of this jerk cluster at the average date (1913.6 ± 1.1). However, the dates of the event at COI and DBN are surprisingly far from the average. The regularities estimated from the nine ridge functions (Figure 6) give an average of 1.42 ± 0.12 . This event again could very well be worldwide.

The 1925 event is clearly observed at five European observatories (BFE, CLF, DBN, ESK, NGK) and two North American ones (TUC and SIT), but not at FRD (Table 3c and Figure 7). This jerk has also been detected for the remaining observatories EBR and SOD (with less data) as an energy packet in the wavelet transform. The average date and regularity are 1925.2 ± 0.8 and 1.64 ± 0.19 , respectively. This event could again be worldwide.

The 1932 event does not show up everywhere. It is detected at the FRD and HON observatories and in the

Table 3c. Results for the 1925 Event

θ^a	θ_b^b	α^c	Date ^d	Code
60	80	1.48	1925.08	BFE
55	80	1.67	1924.08	CLF
50	50	1.84	1924.25	DBN
45	80	1.90	1926.42	ESK
55	80	1.52	1925.50	NGK
50	110	1.33	1925.52	SIT
115	90	1.73	1925.50	TUC

^aDirection angle of the jerk in degrees.^bEnhancement angle of the jerk in degrees.^cSlope of the ridge function.^dDate of occurrence of the jerk.**Table 3d.** Results for the 1932 Event

θ^a	θ_b^b	α^c	Date ^d	Code
85	110	1.92	1932.08	AML
45	90	1.55	1931.75	API
10	50	1.57	1932.00	FRD
25	80	1.60	1930.58	GNA
60	80	1.65	1933.83	HON
50	80	1.46	1934.08	HUA

^aDirection angle of the jerk in degrees.^bEnhancement angle of the jerk in degrees.^cSlope of the ridge function.^dDate of occurrence of the jerk.

southern hemisphere at the four observatories (AML, API, GNA and HUA) whose time series are long enough to allow for such a detection (Table 3d and Figure 8). The average date and regularity found for this jerk are 1932.4 ± 1.2 and 1.63 ± 0.14 , respectively. This event is not seen in any of the European observatories.

The 1949 event is again not seen in Europe. It is observed in the Pacific area (ABG, AML, API, GNA, KAK) and in the American region (FRD, HON, HUA, SJG, TUC) (Table 3e and Figure 9). The average date and regularity estimated for this event are 1949.8 ± 1.4 and 1.49 ± 0.27 , respectively. The 1949 jerk covers the same geographical area as the 1932 event. We will not discuss any further those early events which are much less documented than the 1969 and 1978 ones, on which we will now focus.

The 1969 and 1978 Events

The worldwide character of the 1969 event is attested by its presence in a large number of observatories distributed all around the world (at 66 observatories out of the 74 covering the time span around the event (Table 2a)). The ridge functions of this jerk are very clear for 47 observatories where they are linear over a large dilation range (Table 3f and Figure 10). We note evidence of this jerk in the form of conelike energy patches in the wavelet transforms of the series at 19 other ob-

Table 3e. Results for the 1949 Event

θ^a	θ_b^b	α^c	Date ^d	Code
30	80	1.78	1947.67	ABG
75	80	1.36	1949.08	AML
30	70	1.00	1949.25	API
170	50	1.64	1950.00	FRD
120	100	1.63	1949.83	GNA
165	60	1.39	1950.83	HON
115	170	1.44	1951.58	HUA
120	100	1.13	1949.67	KAK
170	40	1.83	1952.42	SJG
155	100	1.74	1947.83	TUC

^aDirection angle of the jerk in degrees.^bEnhancement angle of the jerk in degrees.^cSlope of the ridge function.^dDate of occurrence of the jerk.

Table 3f. Results for the 1969 Event

Sign ^a	θ^b	θ_b^c	α^d	Date ^e	Code
+	25	160	1.52	1972.33	ANN
+	25	70	1.37	1971.84	API
+	80	80	1.30	1968.83	AQL
+	95	80	1.70	1969.42	BFE
+	95	90	1.64	1969.09	CLF
-	60	120	1.46	1969.75	CMO
+	95	90	1.58	1969.50	COI
+	100	100	1.90	1968.92	EBR
+	90	80	1.71	1968.67	ESK
-	160	50	1.46	1969.42	FRD
+	95	80	1.69	1969.09	FUR
+	30	90	1.70	1968.83	GDH
+	30	80	1.65	1972.59	GNA
+	90	90	1.77	1969.42	HAD
-	145	110	1.07	1972.42	HER
-	40	80	1.21	1972.67	HUA
-	80	60	1.71	1969.17	IRT
-	110	90	1.36	1969.42	KAK
+	90	80	1.96	1970.42	KIV
-	115	110	1.86	1970.33	KNY
+	85	100	1.53	1969.09	LER
+	85	80	1.55	1969.58	LNN
+	85	90	1.73	1969.25	LRV
+	100	90	2.05	1969.17	LVV
+	90	130	1.56	1970.09	MBO
-	75	110	1.58	1970.42	MEA
-	160	100	1.87	1970.08	MMB
+	95	100	1.92	1970.08	MMK
+	90	110	1.60	1969.50	MOS
+	80	90	1.74	1969.09	NGK
+	90	90	1.73	1969.25	NUR
+	100	100	1.82	1969.17	ODE
+	70	80	1.46	1969.42	PAG
+	35	90	1.43	1971.92	PMG
-	65	80	1.55	1968.92	RES
-	65	110	1.82	1969.73	SIT
+	25	90	1.00	1968.84	SJG
+	85	90	1.66	1969.42	SOD
+	70	90	1.22	1968.75	SUA
+	75	70	1.65	1968.75	TFS
+	90	90	1.45	1970.92	THY
+	10	160	1.32	1971.75	TRD
-	40	80	1.41	1971.25	TUC
+	90	100	1.95	1969.33	VAL
+	85	80	1.86	1970.00	WIK
+	85	90	1.68	1969.59	WIT
+	90	90	1.83	1969.00	WNG

^aThe sign of jerk detected from the wavelet maps.^bDirection angle of the jerk in degrees.^cEnhancement angle of the jerk in degrees.^dSlope of the ridge function.^eDate of occurrence of the jerk.

servatories (despite their limited records), distributed worldwide (ABG, AML, BLC, DOU, FCC, FUQ, GUA, HBK, HRB, LAS, MAW, MBC, MCQ, MNK, PAF, TEO, THL, TOO, TSU).

The 1978 event displays the same global character, being visible at 71 observatories out of 78. It is detected and shows clear ridge function signatures in 46 observatories, distributed worldwide (Table 3g and Figure 11). For 25 other observatories the event is located close to

the beginning or the end of the available series (ABG, ANN, BNG, BRW, DRV, FUQ, HBK, HYD, IRT, KOD, LAS, MBC, MBO, MNK, NVS, PMG, POD, PPT, RES, SAB, SUA, TFS, TRD, TRW, TSU). For all these observatories the event is detected from energy patches in the wavelet transforms.

A very interesting feature revealed by this analysis is that the distribution of the dates of occurrence is clearly bimodal (Figure 12) for both events. For the 1969 event a first group of dates is centered on 1969.4 ± 0.5 and an-

Table 3g. Results for the 1978 Event

Sign ^a	θ^b	θ_b^c	α^d	Date ^e	Code
-	40	80	1.88	1978.25	API
-	90	80	1.05	1978.00	AQL
-	90	80	1.29	1978.00	BEL
-	60	80	1.46	1978.09	BFE
+	50	90	1.60	1978.17	BLC
+	45	100	1.38	1978.67	BOU
-	60	80	1.89	1978.59	CLF
-	40	100	1.01	1977.67	COI
-	45	80	1.09	1981.75	CZT
-	40	80	1.53	1978.00	DOU
-	40	80	1.37	1977.59	ESK
+	65	100	1.73	1977.92	FCC
+	45	70	1.64	1978.09	FRD
-	40	80	1.83	1978.00	FUR
-	160	50	1.81	1976.84	GDH
+	25	90	1.78	1980.92	GNA
-	45	90	1.64	1978.09	HAD
-	45	90	1.36	1982.00	HER
-	85	90	1.50	1980.80	HLP
-	90	80	1.79	1978.50	HRB
+	145	110	1.63	1977.84	KAK
-	70	70	1.51	1977.75	KIV
+	155	100	1.85	1979.33	KNY
-	45	80	1.67	1977.92	LER
-	50	90	1.42	1977.58	LRV
-	100	70	1.97	1976.42	LNN
-	65	120	1.28	1978.00	MCQ
+	75	110	1.78	1976.67	MEA
+	155	100	1.52	1977.83	MMB
-	110	40	1.89	1976.50	MOS
+	65	90	1.95	1978.37	NEW
-	50	80	1.69	1978.17	NGK
-	40	90	1.40	1977.67	NUR
+	50	70	1.58	1981.92	PAF
-	35	90	1.51	1977.75	PAG
+	50	100	1.58	1977.71	SIT
+	55	70	1.72	1977.92	SJG
-	25	80	1.65	1978.09	SOD
-	10	40	1.63	1976.67	THL
-	60	90	1.44	1977.67	THY
+	50	80	1.66	1978.00	TUC
-	45	90	1.74	1978.25	VAL
+	60	80	1.76	1977.58	VIC
-	40	80	1.83	1979.00	WIK
-	25	80	1.78	1978.17	WIT
-	45	80	1.65	1978.25	WNG

^aThe sign of jerk detected from the wavelet maps.^bDirection angle of the jerk in degrees.^cEnhancement angle of the jerk in degrees.^dSlope of the ridge function.^eDate of occurrence of the jerk.

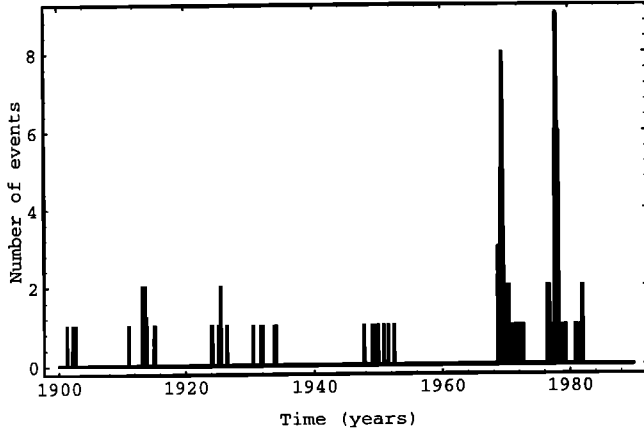


Figure 4. Histogram of the dates of the jerks detected in the present study. Seven clusters can be identified, roughly dated 1901, 1913, 1925, 1932, 1949, 1969, and 1978.

other one on 1972.1 ± 0.5 . In a similar way, the dates of the 1978 event split into a first group centered on 1977.9 ± 0.6 and a second one centered on 1981.5 ± 0.5 . Figure 13, which shows the geographical distribution of the dates of occurrence, further reveals that the bimodal temporal distribution of the 1969 jerk is also associated with a clear geographical pattern: the jerk appears at a later date in the southern hemisphere. This result is corroborated by the analysis of the wavelet maps of eight other observatories located in the southern hemisphere (FUQ, HBK, LAS, MAW, MCQ, PAF, TOO, and TSU) and for which the examination of the energy packet also suggests a date around 1972. Figure 14 shows that exactly the same thing happens to be true for the 1978 event. The occurrence time is again later in the southern than in the northern hemisphere with a similar time lag of about 2 to 3 years (note, however, that the number of analyzed southern series is even smaller than for the 1969 event). Again also, this later date is confirmed by inspecting the cone-like energy patches typical of jerks within the wavelet maps of 12 additional observatories with shorter series (ABG, ANN, DRV, FUQ, HBK, HYD, KOD, LAS, PMG, PPT, TRW, and TSU). Thus the two 1969 and 1978 events seem to share a common spatio-temporal behavior.

To what extent can this similarity be generalized to the regularity α and the local direction θ , both param-

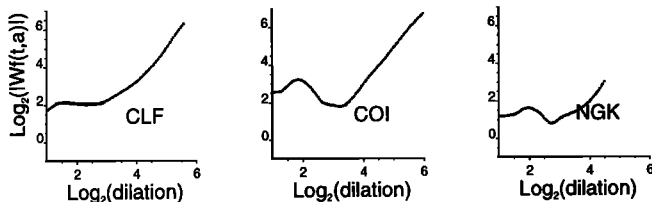


Figure 5. Log-log plots of the ridge functions of the 1901 event (see Table 2a for the code and location of the observatories and Table 3a for ridge function slopes).

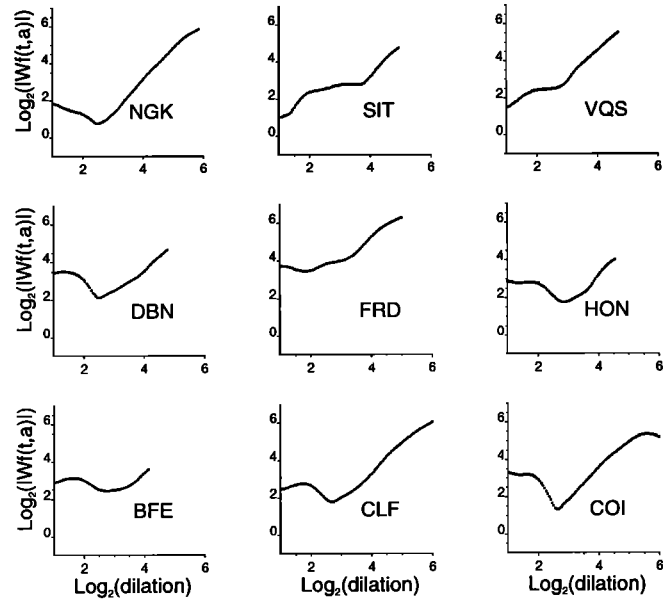


Figure 6. Log-log plots of the ridge functions of the 1913 event (see Table 2a for the code and location of the observatories and Table 3b for ridge function slopes).

eters being available at 47 observatories for the 1969 event, and 46 observatories for the 1978 event? We note that the average values of the α for 1969 and 1978 events happen to be equal ($\alpha = 1.6$). But we also note that within each event, the measured values of α vary significantly from place to place (Tables 3f and 3g). We measured this dispersion in terms of a global standard deviation with respect to the previous average values. Again we found exactly the same value $\sigma_\alpha = 0.23$ for both events. This value is slightly larger than the standard deviation we expected from our synthetic test

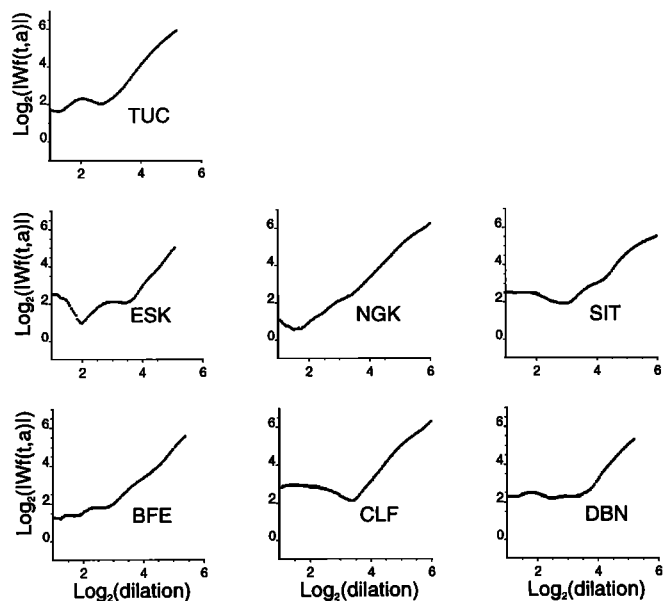


Figure 7. Log-log plots of the ridge functions of the 1925 event (see Table 2a for the code and location of the observatories and Table 3c for ridge function slopes).

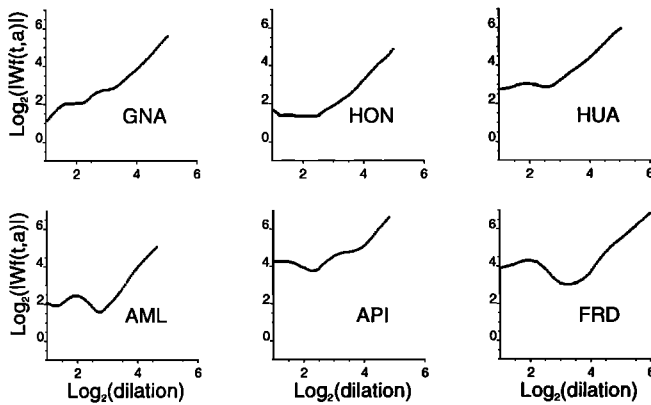


Figure 8. Log-log plots of the ridge functions of the 1932 event (see Table 2a for the code and location of the observatories and Table 3d for ridge function slopes).

(which suggests a value of the order of 0.15; recall Table 1). This could result from the way we estimated the error in α in the synthetic case using only data from close-by European observatories. However, it could also be due to some geophysically relevant regional variations. In order to check this, we produced maps of the departures of the α from the average value 1.6 for each of the two events (Figures 15 and 16). The 1969 event again displays a fairly strong global asymmetry, with the southern hemisphere (crudely speaking) usually showing regularities below the average value, while the northern hemisphere tends to reveal larger regularities. This asymmetry is less obvious for the 1978 event, but this might be due to the tiny number of values recoverable from the southern hemisphere. Hence we may conclude that within the accuracy of our method, the regularities of the two events seem to be identical, with an average value of $\alpha = 1.61 \pm 0.23$, and a common tendency to be slightly larger in the northern than in the southern hemisphere.

The local directions for both jerks (sign and θ in Tables 3f and 3g) are displayed on maps (Figures 17 and 18). In interpreting these maps, one must carefully keep in mind that they give no information about the intensity of the signal, $|\beta|$, a parameter we have not yet been able to recover in a systematic way (which remains a drawback of the present study but will be the subject of further investigation). Both maps show satisfactory regional consistency and reveal that the two events are not simple in geometry. They appear to be large scale but complex phenomena. There is no simple north-south symmetry or antisymmetry. A comparison between the two events shows that in most places the 1978 directions tend to be opposite to the 1969 directions. Figure 19 is a blow up of the planetary map over Europe; the arrows are indeed well organized, have approximately the same directions, but reverse senses in 1969 and 1978.

Concluding Remarks

In paper 1 we focused on the analysis of the Y component observed in European observatories. This allowed

us to uncover five events in the twentieth century, to confirm their internal origin, and to show that they are more singular than previously assumed, with a regularity closer to 1.5 than to 2. The present study confirms and extends these early results.

Allowing for the search to be carried out on any horizontal component made it, for instance, possible to detect the 1978 event which was not seen at GDH observatory when analyzing the Y component (paper 1). It is now seen there on the N250°E direction. Also, the worldwide character of the present analysis allowed for a systematic search for singular events within the twentieth century secular variation. Seven such events have been detected, two being unquestionably of global extent (1969 and 1978), three being of possibly similar extent (1901, 1913, and 1925), while the remaining two are not seen everywhere at the Earth's surface (1932 and 1949).

The two 1969 and 1978 global events display an intriguing spatio-temporal behavior consisting of an early arrival in the northern hemisphere followed by a later arrival in the southern hemisphere. In addition, these two events tend to balance each other, as already noted by Stewart [1991] and Le Huy [1995] on the basis of an entirely different analysis.

The two-step behavior of these two events also accounts for the observations made by previous authors for "late" jerks in the southern hemisphere (Gubbins and Tomlinson [1986] and Whaler [1987] for a 1971/1972

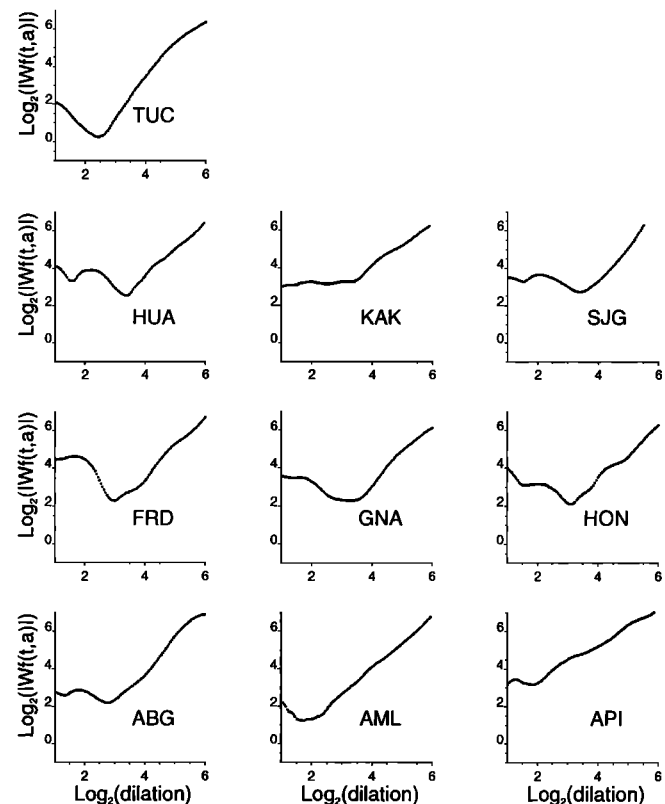


Figure 9. Log-log plots of the ridge functions of the 1949 event (see Table 2a for the code and location of the observatories and Table 3e for ridge function slopes).

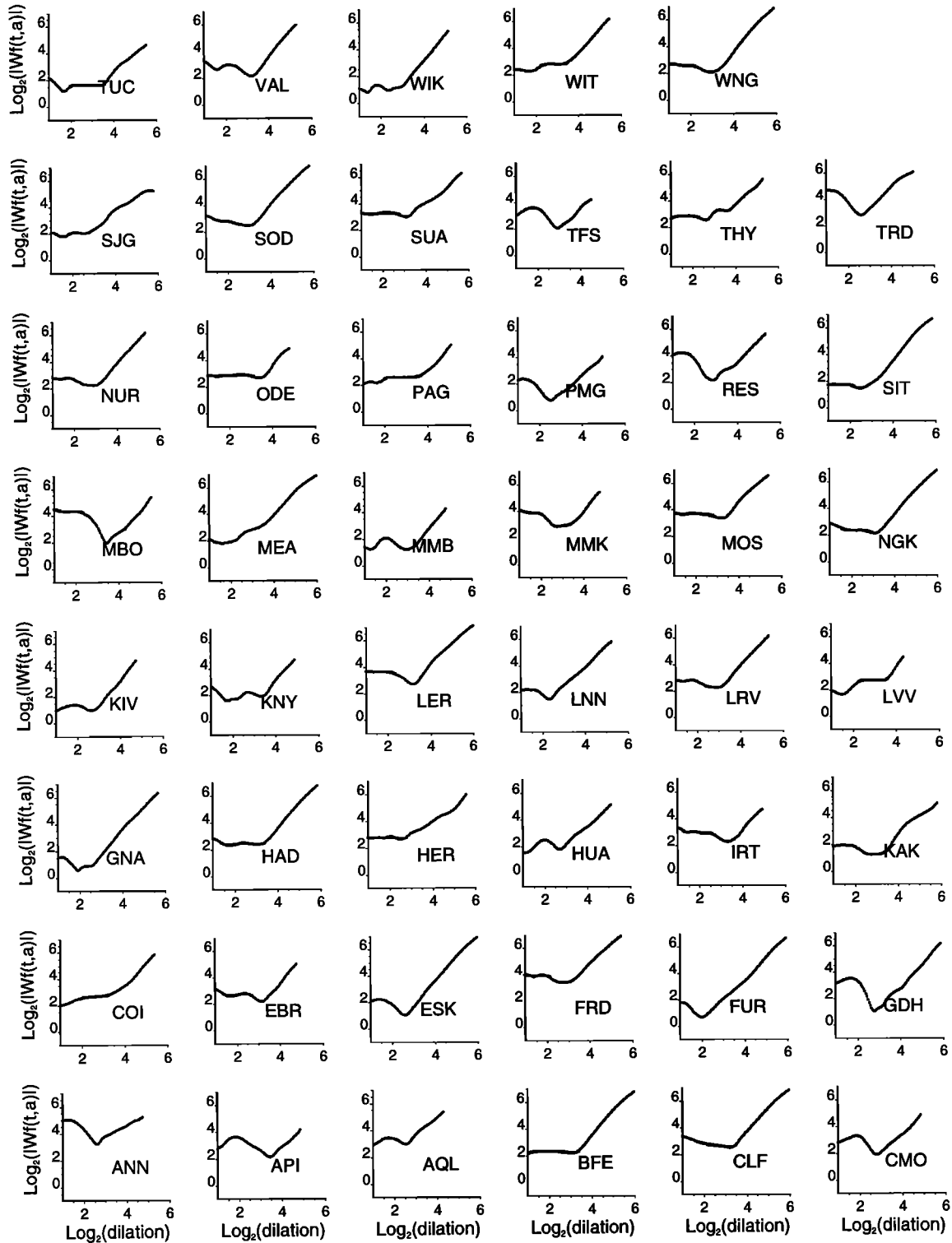


Figure 10. Log-log plots of the ridge functions of the 1969 event (see Table 2a for the code and location of the observatories and Table 3f for ridge function slopes).

jerk and Dowson *et al.* [1988], Kotzé *et al.* [1991], and Stewart [1991] for a 1983 jerk).

Turning now to the regularities, we confirm our early result that they are closer to 1.5 than to 2. We can furthermore state that this is true for all events, with

an overall common value of about $\alpha \approx 1.6$, and for the much better documented 1969 and 1978 events, the regularity seems to be slightly larger for the early northern arrival than for the late southern arrival. This could reflect some general property of the evolution of the flow

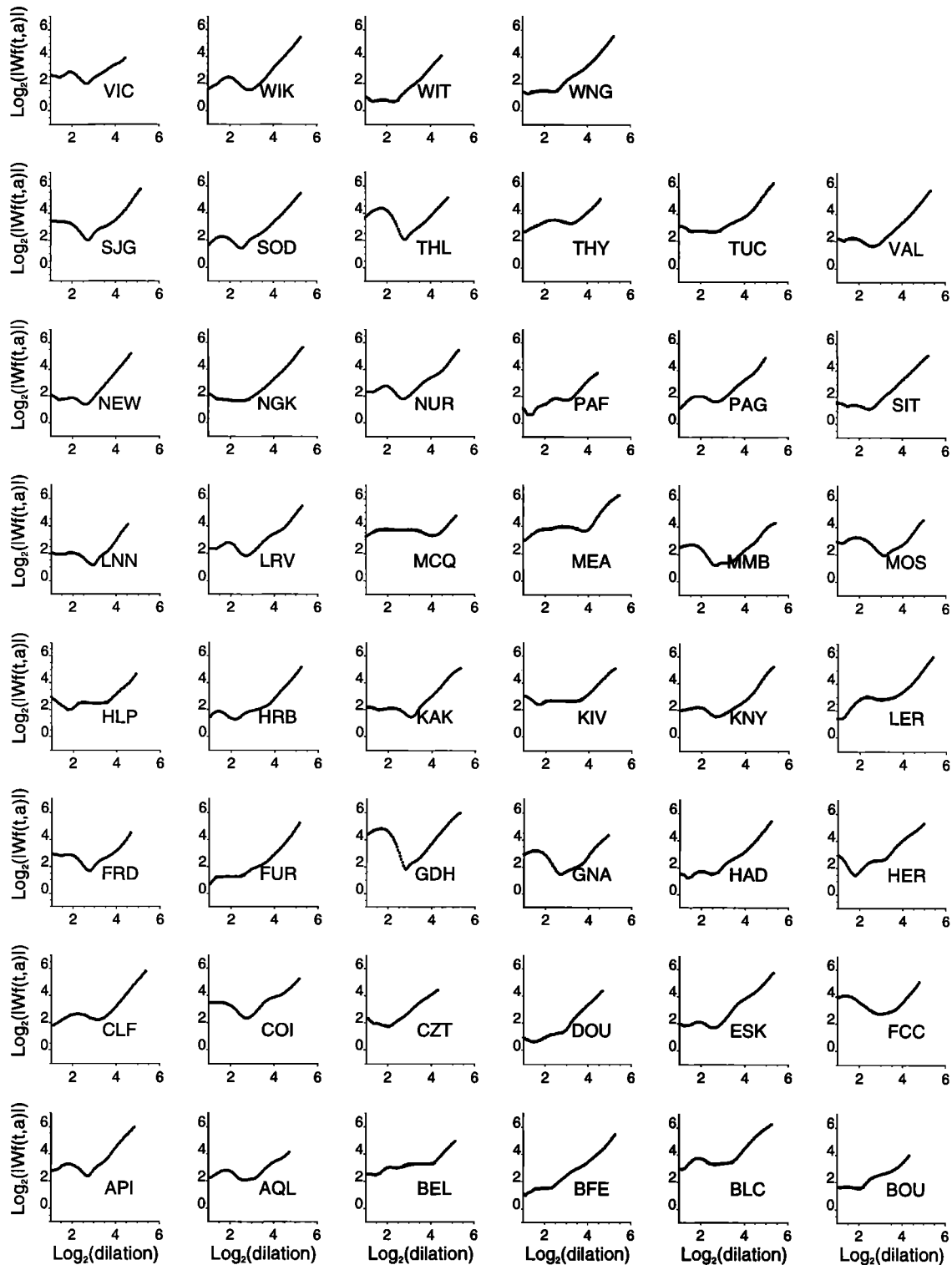


Figure 11. Log-log plots of the ridge functions of the 1978 event (see Table 2a for the code and location of the observatories and Table 3g for ridge function slopes).

at the top of the core. However, this regularity is not so straightforward to interpret. As already pointed out, our analysis relies on the assumption that the jerks be linearly polarized in the horizontal plane. This is not necessarily the case since the geometry of the secular variation is not constant in time at the Earth's sur-

face. This means that what we actually measure could be some kind of combination of two different singularities corresponding to two perpendicular horizontal components. Nevertheless, the fact that we were able to find a direction for which the signal is actually extinguished, and that, perpendicularly to this direction, we

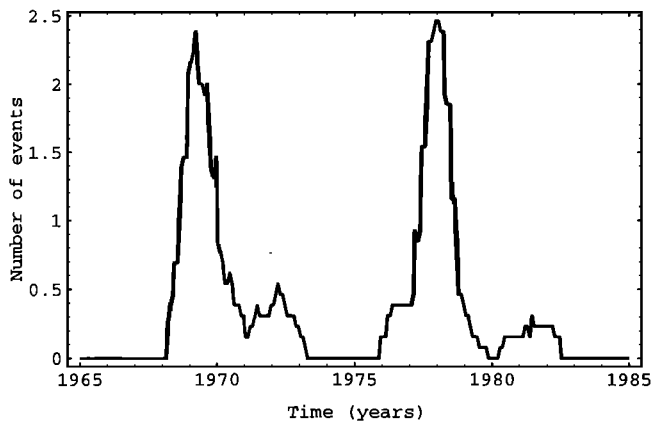


Figure 12. Histogram of the dates of the 1969 and 1978 jerks.

obtained in most cases a reasonably linear behavior of the ridge functions within the range of dilations of interest, validates a posteriori our analysis. Let us recall that the main aim of the present paper was to carefully screen the twentieth century magnetic data for all possible events, to best characterize their temporal behavior, and to sketch their global geometry. A more detailed study of each event, especially with respect to the intensity β of the signal, remains to be done. We again underline the fact that more data could also be recovered to complete our study. Indeed, whereas the number of observatories in operation at the beginning of the century was limited for obvious reasons, it is still disappointingly small for the 1978 event. This stresses the need for an implemented array of magnetic obser-

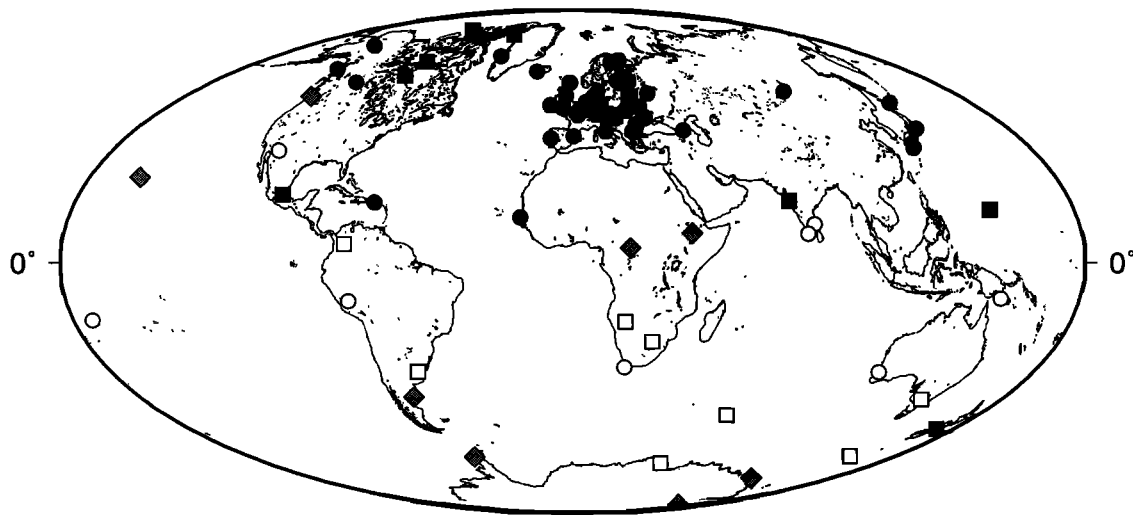


Figure 13. Times of occurrence of the 1969 event. These are detected using either the wavelet transform maps (before 1971, solid squares; after 1971, open squares) or the ridge functions (before 1971, solid circles; after 1971, open circles; see also Table 3f for more details). In some observatories the jerk is not detected (gray diamond).

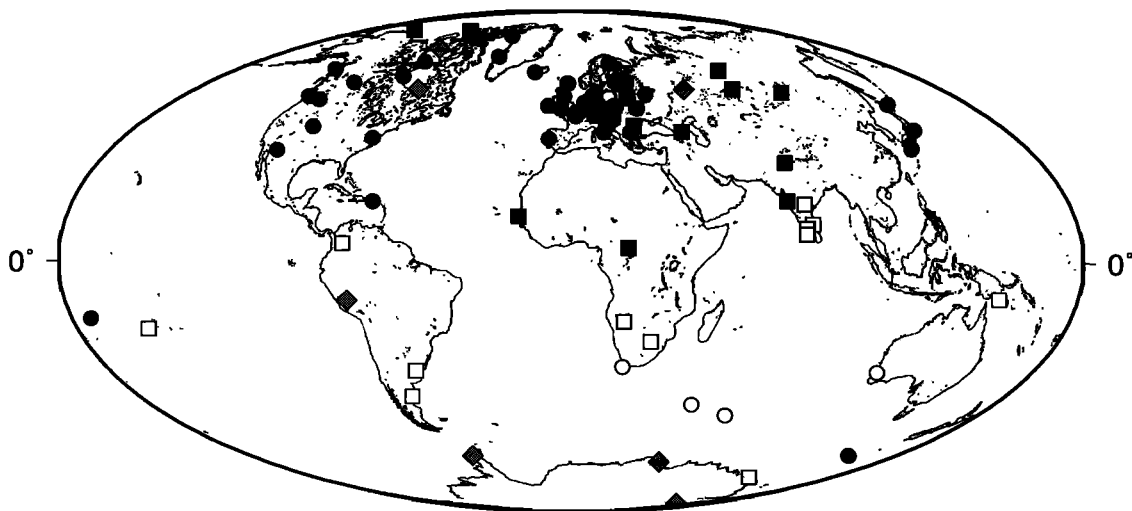


Figure 14. Times of occurrence of the 1978 event. These are detected using either the wavelet transform maps (before 1980, solid squares; after 1980, open squares) or the ridge functions (before 1980, solid circles; after 1980 open circles; see also Table 3g for more details). In some observatories the jerk is not detected (gray diamond).

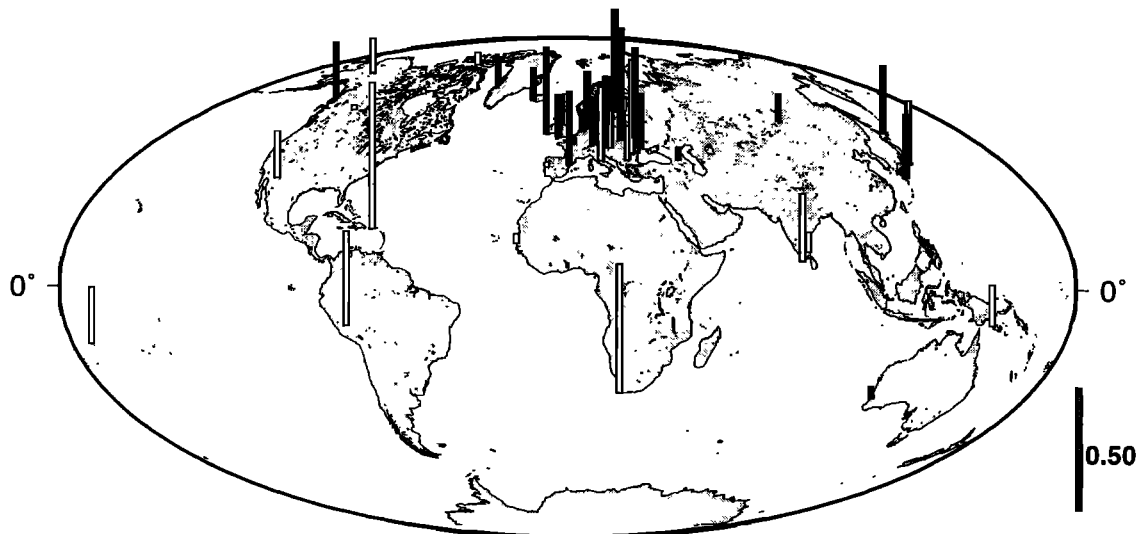


Figure 15. Departures of the regularities from the average value for the 1969 jerk. The black bars indicate positive values, and the white ones indicate negative values.

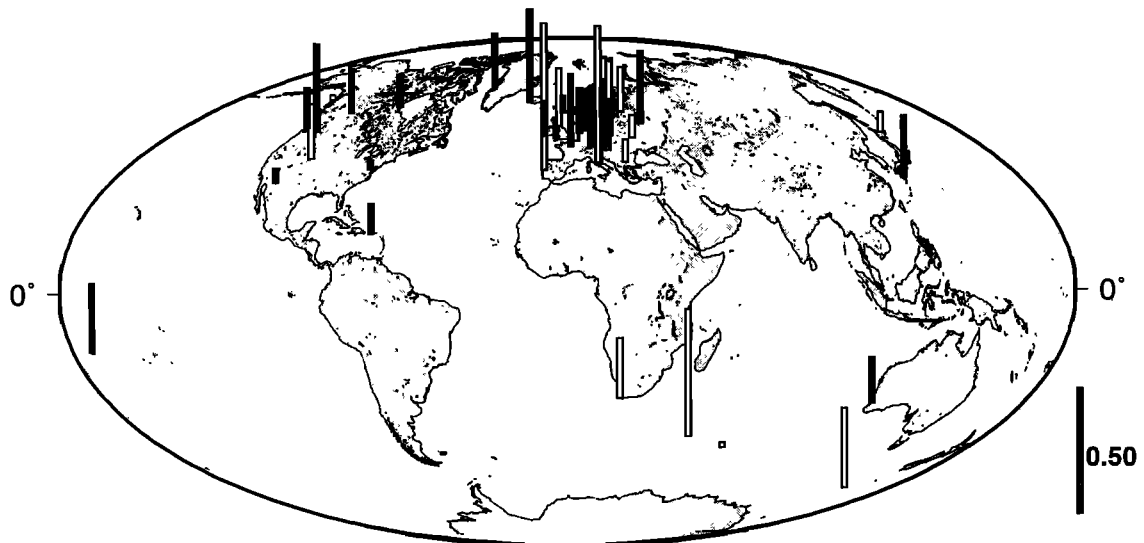


Figure 16. Departures of the regularities from the average value for the 1978 jerk. The black bars indicate positive values, and the white ones indicate negative values.

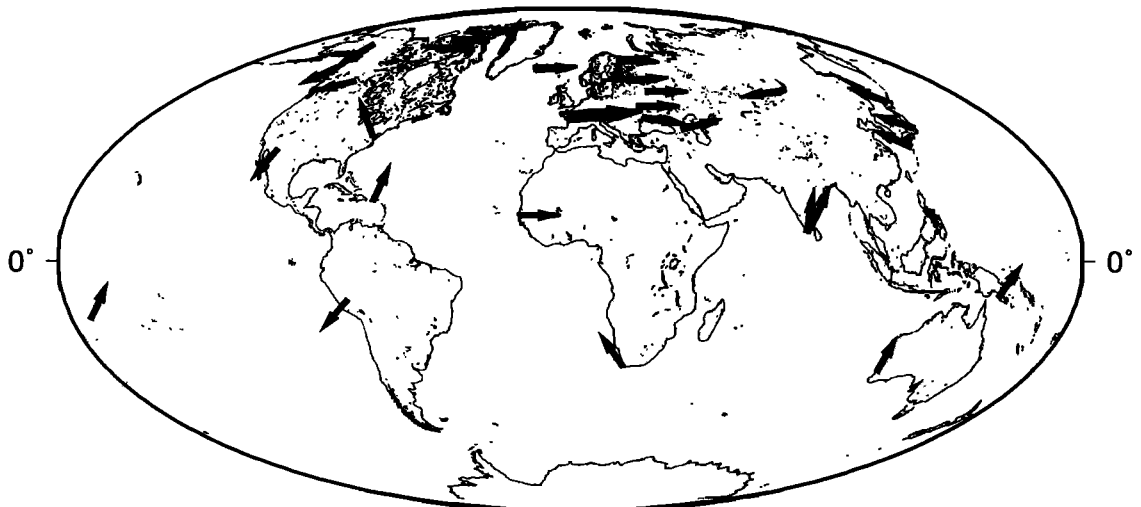


Figure 17. Characteristic directions and senses of the 1969 jerk. The longest arrow indicates the average direction and sense for the European observatories (see also Table 3f for more details).

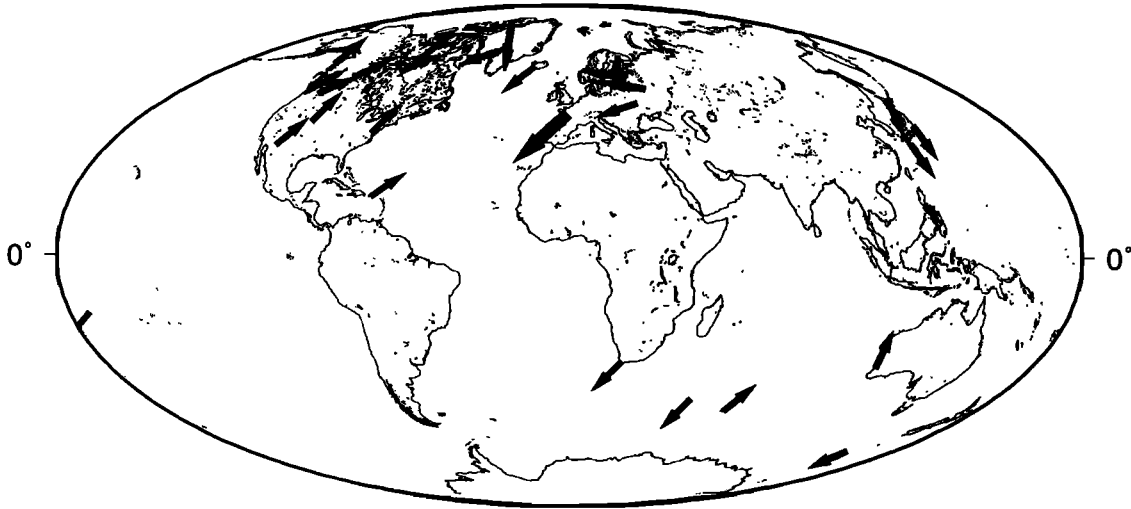


Figure 18. Characteristic directions and senses of the 1978 jerk. The longest arrow indicates the average direction and sense for the European observatories (see also Table 3g for more details).

vatories making their data rapidly available (as in the Intermagnet program).

Finally, let us note that it is now time to try to understand the mechanism of these events: they have a large, sometimes global, extension at the surface of the Earth; they occur simultaneously, within the analysis accuracy, at places tens of thousands of kilometers apart, but can also be observed in one hemisphere a few years before the other one (this might have something to do with

the delays introduced by the conductivity of the mantle [Backus, 1983]); they govern the secular variation for years or decades after they have occurred, as shown also by the observation that they are caused by sudden changes in the evolution of the flow at the top of the core [Hulot *et al.*, 1993]. Any further progress concerning the origin of the secular variation will require that we simultaneously address the origin of the geomagnetic jerks.

Appendix: Wavelet Transform

In order to make this paper self-consistent, we recall the main aspects of the wavelet analysis method used in the present study. A more detailed discussion about both the mathematical aspects and the numerical assessment of the method is given in paper 1 [Alexandrescu *et al.*, 1995]. Only those aspects of the wavelet transform directly relevant to this paper are presented, and the reader interested in the wavelet transform from a more general point of view is referred to Meyer [1990], Daubechies [1992], and Holschneider [1995]. Works on singularity detection with wavelets are given by Grossmann [1986], Grossmann *et al.* [1987], and Mallat and Hwang [1992].

We define the continuous wavelet transform of a signal $f(t)$ by the convolution product

$$Wf[t, a] \equiv [f * \psi_a](t), \quad (\text{A1})$$

where the wavelets $\psi_a(t)$ are obtained by dilating an analyzing wavelet $\psi(t)$,

$$\psi_a(t) \equiv \frac{1}{a} \psi\left(\frac{t}{a}\right) \quad (\text{A2})$$

with a dilation $a > 0$. Equation (A1) shows that the wavelet transform is defined in the (t, a) open half-space and that every voice $Wf(t, a = cst)$ is a filtered version

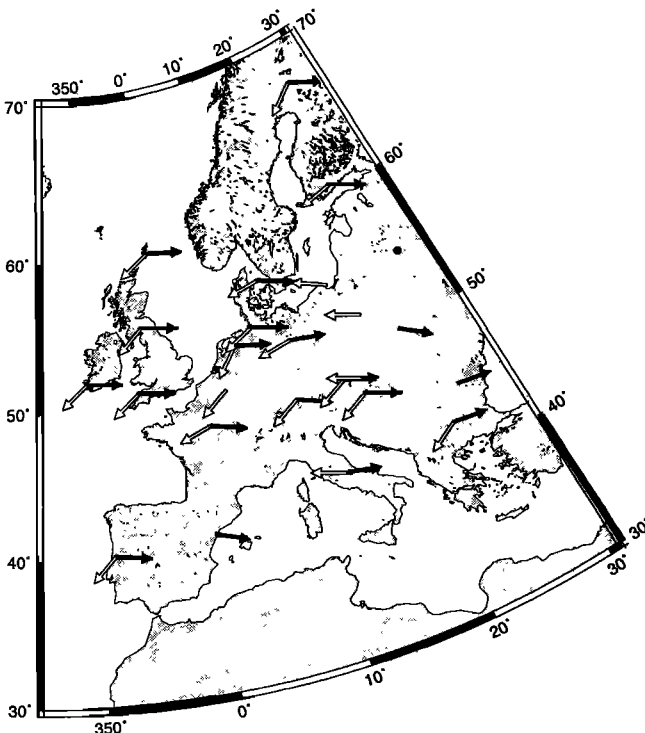


Figure 19. The directions and senses of the 1969 (black arrows) and 1978 (white arrows) jerks for the European observatories (see also Tables 3f and 3g for more details).

of the initial signal $s(t)$. The fact that the wavelet family $\psi_a(t)$ is generated through dilations of an analyzing wavelet $\psi(t)$ being well localized along the time axis makes the wavelet transform a useful tool to analyze the signal $f(t)$ at any timescale and reveal its possible self-similar behavior. In the present study we use the same analyzing wavelet as in paper 1,

$$\psi(t) = \frac{d^3}{dt^3} \exp\left(-\frac{t^2}{2}\right). \quad (\text{A3})$$

Consider now the particular case of a horizontal component of the geomagnetic field, assumed to be of the form

$$f(t) = \beta j_\alpha(t) + h(t) + n(t), \quad (\text{A4})$$

where the jerk is given by

$$j_\alpha(t) = \begin{cases} 0 & t \leq t_0 \\ (t - t_0)^\alpha & t \geq t_0 \end{cases}. \quad (\text{A5})$$

Variable $h(t)$ is a harmonic component of the form

$$h(t) = \sum_i \gamma_i \sin\left(\frac{2\pi t}{T_i} + \varphi_i\right), \quad (\text{A6})$$

where γ_i and φ_i are amplitude and phase terms respectively, and T_i are the main Fourier periods of the external field (i.e., 1/2, 1, 11/3, 11/2, and 11 years). The term $n(t)$ is assumed to be Gaussian-white noise with a zero mean and a variance σ_n^2 . Inserting model (A4) into (A1) we obtain

$$Wf(t, a) = \beta Wj_\alpha(t, a) + Wh(t, a) + Wn(t, a), \quad (\text{A7})$$

which indicates that the wavelet transform of the signal is the superposition of the wavelet transforms of the jerk, of the harmonic components, and of the noise. The task is now to examine under which conditions a possible term Wj_α may be identified in the whole wavelet transform Wf , and how both the regularity α and the date t_0 of the jerk can be recovered.

According to paper 1, and setting $t_0 = 0$,

$$Wj_\alpha(t, a) = \Gamma(\alpha + 1) a^\alpha \psi^{-(\alpha+1)}\left(\frac{t}{a}\right) \quad (\text{A8})$$

where the notation $\psi^{-(\cdot)}$ is for the fractional primitive:

$$\frac{d^{\alpha+1}}{dt^{\alpha+1}} \psi^{-(\alpha+1)} \equiv \psi. \quad (\text{A9})$$

Using (A8), we obtain

$$Wj_\alpha(t, a) = \left(\frac{a}{a'}\right)^\alpha Wj_\alpha\left(t \frac{a'}{a}, a'\right), \quad (\text{A10})$$

which indicates that the wavelet transform $Wj_\alpha(t, a)$ can be recovered by dilating and scaling a single voice $Wj_\alpha(t, a')$. As a consequence, the wavelet transform of a jerk has a conelike pattern pointing toward the date of the jerk (Figure 20). This property implies that the existence of conelike energy patches in the experimental

wavelet transform will indicate that jerks are present in the signal $f(t)$. Clearly, a change of the sign of the jerk (β) will result in a change of a sign in the wavelet transform. This is represented by color or gray scale in the wavelet map (typically red or light gray for positive and blue or dark gray for negative). By comparison with the synthetic test, we can tell whether the jerk is positive ($\beta > 0$) or negative ($\beta < 0$).

Also the focusing of the cone toward the date t_0 when a tends toward 0 makes it possible to date the occurrence of the jerk. The scaling $(a/a')^\alpha$ between two voices of the wavelet transform depends on the regularity α of the jerk which, in practice, is estimated by studying the variation of the wavelet coefficients taken along the lines of extrema of the wavelet transform where the signal-to-noise ratio is the highest (Figure 20). The set of absolute values of the wavelet coefficients belonging to a given line of extrema and ranked with respect to the dilation a defines what will be referred to as a ridge function $r(a)$. When plotted in a log-log diagram, the ridge function are straight lines whose slopes equal the regularity α (Figure 21).

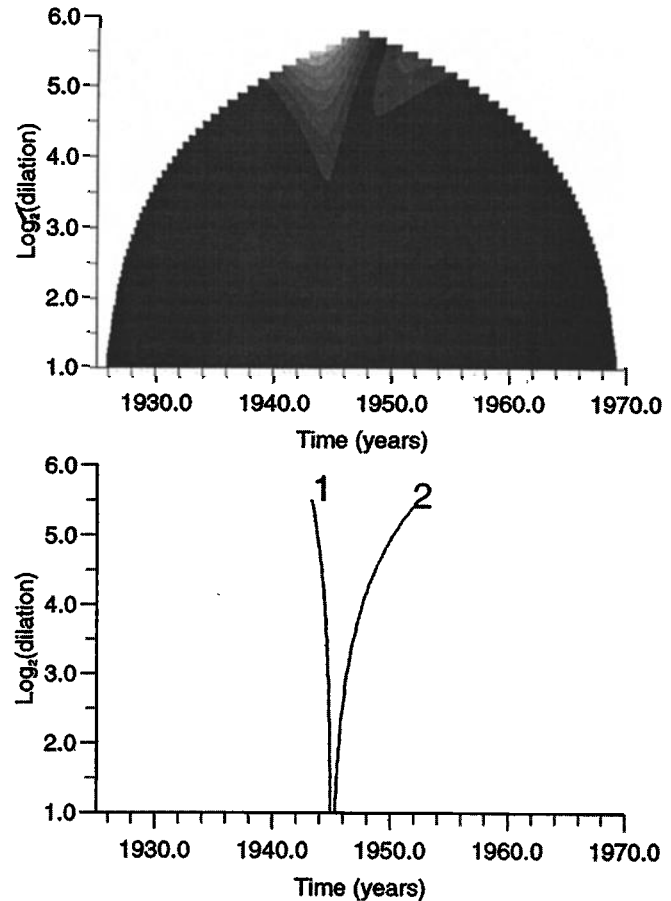


Figure 20. (top) Wavelet transform of a jerk with $\alpha = 1.6$, $\beta = 0.17 \text{ nT} \times \text{month}^{-1.6}$, and $t_0 = 1945$. Note the conelike structure of the wavelet map pointing toward the date of the jerk. The gray scale represents the sign of the wavelet transform: light gray indicates positive, dark gray indicates negative. (bottom) Lines of extrema extracted from the wavelet map of the jerk. These lines converge toward the date of the jerk.

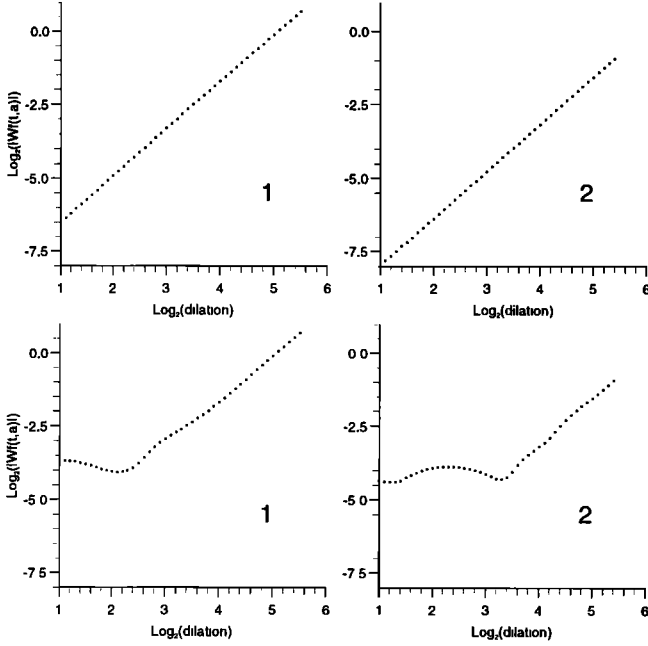


Figure 21. (top) Log-log plots of the ridge functions corresponding to the lines of extrema of Figure 21. The slopes of the ridge functions equal the regularity (here $\alpha = 1.6$) of the jerk. (bottom) Ridge functions corresponding to the same jerk polluted with a Gaussian-white noise with zero mean and variance $\sigma_n^2 = 6 \times 10^{-4}$. The ridge functions are no more linear in a small-dilation range $a \leq a_c \simeq 2^{3.5}$ but remain so for $a > a_c$. The slopes of the linear parts of the ridge functions 1 and 2 are $\alpha = 1.54$ and $\alpha = 1.62$, respectively. Such ridge functions are considered to be of type 1.

The experimental wavelet transforms also contain the effects of both the noise and the harmonic components (equation (A7)). The effect of the noise is essentially limited to a small-dilation range $a \leq a_c$ for which the ridge functions cease to be linear (Figure 21). The value of a_c depends on the relative strengths of both the jerks and the noise present in the data. In the present study as well as in paper 1, when processing real data we found experimentally that $a_c \simeq 2^{3.5}$. The effects of the harmonic components are more complicated and not restricted to such a small-dilation range. Again, due to the linearity of the wavelet transform, we have

$$Wh(t, a) = \sum_i \gamma_i W \left[\sin \left(\frac{2\pi t}{T_i} + \varphi_i \right) \right] (t, a), \quad (\text{A11})$$

where the transform of a single harmonic component reads

$$W \left[\sin \left(\frac{2\pi t}{T_i} + \varphi_i \right) \right] (t, a) = (2\pi)^{7/2} \left(\frac{a}{T_i} \right)^3 \exp \left(-\frac{2\pi^2 a^2}{T_i^2} \right) \cos \left(\frac{2\pi t}{T_i} + \varphi_i \right). \quad (\text{A12})$$

This wavelet transform is extremum for

$$a_i = T_i \sqrt{3}/2\pi \quad (\text{A13})$$

along any line $t = \text{const}$ in the (t, a) half plane. In general, the wavelet transform of the harmonic signal will possess numerous lines of extrema resulting from complicated interference between the transforms of the individual harmonic components. Although very variable in details, all ridge functions due to the harmonic signal share a common wobbling aspect (Figure 22) and an exponential decrease beyond the dilation

$$a_{\max} = T_{\max} \sqrt{3}/2\pi, \quad (\text{A14})$$

where $T_{\max}$ is the largest period present in the sum of (A6). For instance, if $T_{\max} = 11$ years, then $a_{\max} = 2^{5.2}$. This sharp decrease characterizes the ridge functions of the harmonic signal whose behavior is then very different from those of jerks (Figure 22). This provides us with a means of classifying the ridge functions extracted from an experimental wavelet transform (paper 1):

Type 1 ridge functions are linear for large dilations, with a positive slope. They are possibly altered in a small-dilation range $a \leq a_c$ because of the presence of noise. Such type 1 ridge functions may safely be considered as mainly due to jerks.

Type 2 ridge functions have a wobbling appearance and display a sharp decrease for large dilation. This type of ridge functions will be principally due to the harmonic component.

Type 3 ridge functions are those not falling into either type 1 or type 2 and generally correspond to ridge functions caused by complicated interferences between the different terms of the experimental wavelet trans-

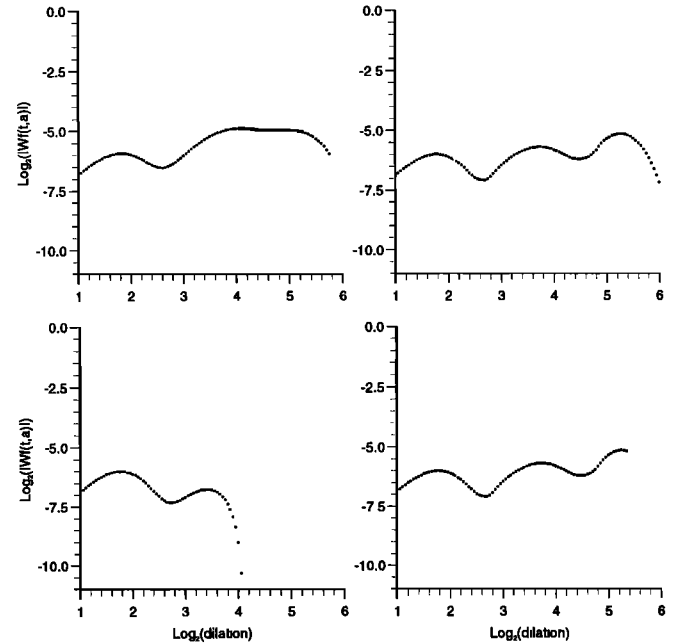


Figure 22. Typical ridge functions extracted from the wavelet maps of pure harmonic components $h(t)$ (equation (A11)) with the longest period $T_{\max} = 11$ years. Note the wobbling aspect of these ridge functions and the sharp decrease beyond $a_{\max} = 2^{5.2}$. Such ridge functions are considered to be of type 2.

form (equation (A7)). Such ridge functions cannot be given a clear origin.

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- M. Alexandrescu, G. Hulot, and J.-L. Le Mouél, Institut de Physique du Globe, B.P. 89, 4 Place Jussieu, 75252 Paris cedex 5, France. (e.mail: mioara@ipgp.jussieu.fr; ghulot@ipgp.jussieu.fr; lemouel@ipgp.jussieu.fr)
- D. Gibert, and G. Saracco, Géosciences Rennes, Université de Rennes 1, Bât. 15 Campus de Beaulieu, 35042 Rennes cedex, France. (e.mail: gibert@univ-rennes1.fr; ginet@univ-rennes1.fr)

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