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Investigating CH₄ Thermal Activation in Clathrate Nanocages

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Abstract. The energy levels of methane molecule trapped, at low temperature, in small (s) and large (l) nano-cages of cubic sI clathrates are calculated in the Born-Oppenheimer approximation using the Extended Lakhlifi-Dahoo model based on pairwise atom-atom effective interaction potentials. In the s cage, the center of mass of CH₄ exhibits a slightly asymmetrical 3D oscillation motion with small amplitude around the cage center. Two methods were used to calculate the frequencies of such a motion: a 3D harmonic treatment and a 1D Discrete Variable Representation (DVR) treatment in the X, Y and Z directions. They give approximately the same values of, respectively, 133 cm⁻¹, 108 cm⁻¹ and 120 cm⁻¹. In the l cage, the oscillations are anharmonic and characterized by large amplitude motions with frequencies of 63 cm⁻¹, 52 cm⁻¹ and 47 cm⁻¹. In the s and l nano-cages, the molecule exhibits strongly perturbed rotational motion. The rotational level schemes are quite different from that of the molecular free rotational motion, and for each nano-cage, the obtained levels are described as combination of the free rotation levels.

1. Introduction

A great number of research activities in the field of astrophysics are devoted to clathrates, crystalline solids formed by a compact assembly of nano-cages. Clathrates exist as three different kinds of Archimedes polyhedra characterized by two types of cubic structures termed sI and sII with a cage-like structure of water molecules surrounding atoms or small molecules and a hexagonal structure-H (sH) [1], which forms in the presence of large guest molecules. The unit cell of sI consists of 46 water molecules with two types of cages; 2 small 5¹¹ cages (s), and 6 large 5¹¹6¹² cages (l) [4]. In the sII structure unit cell there are 136 water molecules which form 16 small 5¹¹ and 8 large 5¹¹6¹² cages. In this work, we investigate the effect on the thermal properties of clathrates when they trap methane (CH₄) molecules. This effect is studied through the relaxation channels through which an IR excited CH₄ redistributes its energy. These channels are connected to the structure of the energy levels related to its low frequency motions and which are determined by solving the Schrodinger's eigen-value equation based on the

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Hamiltonian of the encaged molecule. In the following, the Extended Lakhlifi-Dahoo model [2][3] based on pairwise atom-atom effective interaction potentials is applied to CH₄ in sI and sII types clathrate and the results discussed by comparison to previous results obtained on CO₅.

2. The Site inclusion model and interaction potential energy

To simulate the spectra of the CH₄ molecule trapped in clathrate nano-cages, the theoretical model is built as an extension of the site inclusion one applied to study C₃, CO₂ and N₂O molecules [4-6] trapped in rare gas matrices. Electrostatic interactions between atoms of CH₄ and H₂O, are modelled by the usual 12-6 Lennard-Jones (LJ) interatomic potentials at short range and mid-range distances and by effective charges placed on the atoms of the molecules at long range distances. The validity of the Born-Oppenheimer approximation is assumed to separate the vibrational degrees of freedom (high frequency motions) from the orientational and translational degrees of freedom (low frequency motions) of the system formed by the molecule and the nano-cage. Then the total potential energy of the trapped molecule inside the nano-cage is written as:

$$V = \sum_{j} V_{Mj} \left(\mathbf{r}_{0j} \right) + \sum_{jj', j \neq j'} V_{jj'} \left(\mathbf{r}_{jj'} \right)$$

$$\tag{1}$$

where the term V_{iij} is the molecule-cage interaction and \mathbf{r}_{0j} is the distance vector between the centre of mass (c.m.) of CH₄ and the j^{ii} atom of the cage (s or l). The second term V_{ii} represents the interaction potential between two atoms of the cage: i) a j^{ii} atom, of one H₂O molecule, located at position \mathbf{r}_{ji} and ii) a j^{ii} atom, of another H₂O molecule of the cage, located at position \mathbf{r}_{ji} with respect to an absolute frame (O, X, Y, Z) tied to the cage.

The interaction potential energy V_{s_i} between the CH₄molecule and an atom of the cage is the sum of 12-6 LJ potentials representing the repulsion-dispersion contributions and the electrostatic interaction from effective charges q_i (i=1,...,5 for CH₄) and q_i on the atoms of the H₂O molecules of the s or l cage, such that:

$$V_{Mj}(\mathbf{r}_{0j}) = \sum_{i=1}^{5} \left[4\varepsilon_{ij} \left\{ \left(\frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left(\frac{\sigma_{ij}}{r_{ij}} \right)^{6} \right\} + \frac{1}{4\pi\varepsilon_{0}} \frac{q_{i}q_{j}e^{2}}{r_{ij}} \right]$$
(2)

where ε_a and σ_a are the mixed LJ potential parameters from the Lorentz-Berthelot combination rules

$$\mathcal{E}_{ij} = \sqrt{\mathcal{E}_{ii}\mathcal{E}_{jj}}$$
 and $\sigma_{ij} = \frac{\sigma_{ii} + \sigma_{jj}}{2}$. The distance vector \mathbf{r}_{ij} between i and j atoms can be expressed in

the molecular frame $(G, \mathbf{x}, \mathbf{y}, \mathbf{z})$ or the crystal frame $(O, \mathbf{X}, \mathbf{Y}, \mathbf{Z})$ as given in reference [2]. The orientational degrees of freedom, $\mathbf{\Omega} = (\varphi, \theta, \chi)$, of the molecule and the position vector of any atom, j, are defined in the absolute crystal frame $(O, \mathbf{X}, \mathbf{Y}, \mathbf{Z})$.

In the rigid crystal approximation, the potential energy hypersurface of the molecule in its cage, n (n = s or l), can then be written as :

$$V_{M}^{(n)}(\boldsymbol{\xi}^{e}, \mathbf{u_{0}}, \boldsymbol{\Omega}, \{Q\}) = V_{M}^{(n)e}(\boldsymbol{\xi}^{e}) + V_{M}^{(n)}(\boldsymbol{\xi}^{e}, \mathbf{u_{0}}) + V_{M}^{(n)}(\boldsymbol{\xi}^{e}, \{Q\}) + V_{M}^{(n)}(\boldsymbol{\xi}^{e}, \boldsymbol{\Omega}) + \Delta V_{M}^{(n)}(\boldsymbol{\xi}^{e}, \mathbf{u_{0}}, \boldsymbol{\Omega}, \{Q\})$$

$$(3)$$

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where $V_M^{(n)e}(\boldsymbol{\xi}^e)$ is the minimum of the potential energy corresponding to the equilibrium configuration; $V_M^{(n)}(\boldsymbol{\xi}^e, \mathbf{u_0})$ is the c.m. translation dependence in terms of the dynamical coordinate vector; $V_M^{(n)}(\boldsymbol{\xi}^e, \{Q\})$ is the vibrational dependence in terms of normal coordinates $\{Q\}$; $V_M^{(n)}(\boldsymbol{\xi}^e, \boldsymbol{\Omega})$ is the orientational dependence in terms of Euler angles $\boldsymbol{\Omega} = (\varphi, \theta, \chi)$; $\Delta V_M^{(n)}(\boldsymbol{\xi}^e, \mathbf{u_0}, \boldsymbol{\Omega}, \{Q\})$ characterizes the translation-orientation-vibration dynamic coupling term, which can induce the relaxation of vibrational modes onto the translational and orientational modes; and $\boldsymbol{\xi}^e$ represents the equilibrium configuration displacement vector of the c.m. of H₂O molecules of the cage and of the trapped CH₄, determined on the basis of the Green's functions of the perfect crystal.

From the potential energies calculated for the low frequency motions, the Hamiltonian can be solved for the eigen-values of the allowed translation and orientation in each cage (s or l);

$$H_{M}^{(n)} = H_{vib}^{(n)} + T_{rot}^{(n)} + T_{trans}^{(n)} + V_{M}^{(n)} (\boldsymbol{\xi}^{e}, \mathbf{u_{0}}, \boldsymbol{\Omega}, \{Q\})$$
(4)

where the sum of the first three terms, $H_{vib}^{(n)} + T_{rot}^{(n)} + T_{trans}^{(n)}$, corresponds to the free CH₄ molecular Hamiltonian.

3. Results and discussion

Calculations were performed for the CH₄ molecule trapped in clathrate matrices: sI containing 4x4x4 unit cells (up to 2,944 water molecules) and sII with 3x3x3 unit cells (up to 3,672 water molecules). In the *s* cage of sI, the equilibrium configuration corresponds to a minimum energy value of -266 meV (-2,145 cm⁴), the molecular c.m. being located nearly at the cage center and oscillating with small amplitude. In the *l* cage, the minimum energy value is of -263 meV (-2,123 cm⁴), and the molecule is displaced from the cage center by about 0.3 Å in a direction parallel to the two hexagonal faces and exhibiting a translational motion of large amplitude. In the sII structure, the minimum energy values are of -238 meV and of -229 meV, respectively, for the *s* and *l* cages. These results show that trapping of CH₄ in sI is more favourable than in sII. As a result, we focus our quantum mechanical (molecular internal vibrational and orientational modes) computations on the CH₄-clathrate sI system, only.

Using the Born-Oppenheimer approximation, the c.m. of the rigid molecule is fixed at its equilibrium position in the cages, the orientational part $V_M^{(n)}(\varphi,\theta)$ of the interaction potential energy minimized with respect to the χ proper rotation (spinning) angle, is analysed. Figure 1 gives the 2D contour plot of the energy calculated for CH₄ trapped in the small (a) and large (b) cages.

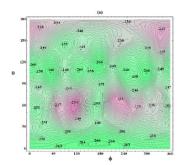


Figure 1 a). Potential energy of CH_4 as a function of orientation in cage s.

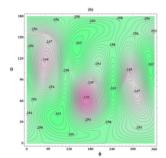


Figure 1 b). Potential energy of CH₄ as a function of orientation in cage l.

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The Figures show that the molecule exhibits a rather perturbed rotational motion such that the calculated rotational eigen-vectors are linear combinations of eigen states linked to the free rotation of the molecule. It is then necessary to define new quantum numbers to label the resulting eigen-states as given by:

$$\left|j\gamma\right\rangle^{(n)} = \sum_{JMK} \Lambda_{JMK}^{j\gamma} \left|JMK\right\rangle \tag{5}$$

where j is an integer number (j=0,1,2,...) and γ takes values: i) $\gamma=0$, for simply degenerate states, for the values $K=0,\pm 3,\pm 6,...$ of the spinning number and ii) $\gamma=\pm$, doubly degenerate states, for the other K values. This is due to the symmetry C_{3v} of the CH_4 molecule. Finally, when the transition elements of the IR rovibrational active modes v_3 and v_4 of CH_4 are calculated, the IR spectra are comprised of an intense Q line associated with vibrational transition surrounded by many R branch (blue shift) and P branch (red shift).

The level schemes in the small (Figure 2a) and in the large (Figure 2b) cages are quite different from that of the CH₄ free rotation motion as shown in Figure 2c.

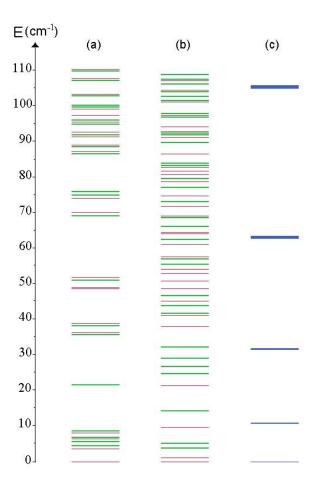


Figure 2. Calculated rotational level schemes of CH₄ in the small (a) and large (b) cages of sI structure. Level scheme (c) corresponds to that of the free molecule. Green levels are doubly degenerate and red ones are simply degenerate.

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In the small cage, the orientational levels are roughly grouped in packets of levels in the range of 2 to 4 cm⁴, separated by energy gaps of 12 to 18 cm⁴ in an interval of 110 cm⁴. In the large cage, the maximum energy gap between the levels is about 7 cm⁴, and in the same interval of 110 cm⁴, the levels appear as almost continuous compared to the small cage case. In comparison, calculations performed on CO₂ [2] led to fewer levels within the same range, with 3 levels separated by a first energy gap of 55 cm⁴ and the next one of about 40 cm⁴ in the small cage and only 8 levels separated by 30 cm⁴ for the first two levels and less than 20 cm⁴ for the other levels. To analyze these structures in terms of thermal properties of the clathrate trapping CH₄ or CO₂, it is necessary to link the redistribution of energy from the excited states of these structures to the solid environment.

Thermal effects are due to the excitation of the phonons that constitutes the quantized thermal bath which absorbs the energy dissipated in the condensed phase matter during a non-radiative transition of an excited molecule. The vibrational or orientational energy of the molecule is thus transferred to this reservoir in the form of kinetic energy to the solid environment thus increasing the temperature of the surroundings. The number of phonons involved in this process is proportional to the energy difference between the levels involved in the transition. This phenomenon has been modelled from two different approaches: one that is based on the short range repulsive forces between the molecule and its environment and assumed to be responsible for the transfer to phonons [7-13] possibly assisted by the rotational motion [14] and one based on the binary collision model [15] initially developed to interpret vibration-translation (V-T) transfers in liquids [16-17] and gases [18].

In the case of CO₂, observations from energy transfer experimental studies carried on low temperature CO₂-rare gas solid systems by laser induced fluorescence and double resonance techniques have shown that radiative relaxation was the main relaxation channel by which the energy from excited vibration-orientational levels was redistributed. Calculations performed on such systems led to energy gaps between the orientational levels corresponding to more than 5 phonons of the different rare gas matrices. Non-radiative relaxation were therefore less probable than radiative relaxation from upper excited levels. Based on these results, it was postulated that since the calculated orientational levels of CO₂ in clathrates had structures similar to those determined in rare gas matrices, then radiative relaxation were the main pathways for redistribution of the energy of excited levels of CO₂ and that the thermal properties of clathrates containing trapped CO₂ were not significantly changed [2].

In the case of CH₄, the situation is quite different because the energy level structures of CH₄ and CO₅ are very different in clathrates. Then, the energy gaps determined for CH₄ should involve 3 or less phonons, which is in favor of non-radiative relaxation in contrast to the CO₅ case which involves more than 5 phonons. The thermal properties of CH₄-clathrate systems should therefore be significantly modified and the nano-cages may free the CH₄ molecules if the temperature rise is significant.

4. Conclusions

In this work, the low frequency energy states of CH₄ trapped in the s and l nano-cages of cubic sI type clathrate are numerically calculated from a theoretical model and analysed by comparison to former studies on CO₅ trapped in clathrates. The results show that although the molecule is rather isolated in its cage, non-radiative relaxation processes are expected to be more important than radiative ones, in contrast to results obtained for CO₅-clathrate systems.

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References

- [1] E. D. Sloan, 2004, Am. Mineral. 89, 1155
- [2] A. Lakhlifi, P. R. Dahoo and E. Chassefière, 2017, J.Q.S.R.T. 187, 124-134
- [3] P. R. Dahoo, R. Puig, A. Lakhlifi, C. Meis and J. D. Gale, 2016, J.P.C.S. 738, 012072
- [4] Lakhlifi A., Dahoo P. R., Vala M., Szczepanski J. and Ekern S., 1997 Chem. Phys. 222, 241.

doi:10.1088/1742-6596/936/1/012071

- [5] Lakhlifi A., Chabbi H., Dahoo P. R. and Teffo J. L., 2000 Eur. Phys. J. D. 12, 435.
- [6] Dahoo P. R., Lakhlifi A., Chabbi H. and Coanga J. M., 2006 J. of Mol. Struc. 786, 157.
- [7] Nitzan A., Jortner J., « Line shape of a molecular resonance », Mol. Phys., vol. 24, p. 109-131, 1972.
- [8] Nitzan A., Mukamel S., Jortner J., « Some features of vibrational relaxation of a diatomic molecule in a dense medium », *J. Chem. Phys.*, vol. 60, p. 3929, 1974.
- [9] Nitzan A., Silbey R.J., « Relaxation in simple quantum systems », *J. Chem. Phys.*, vol. 60, 1974, p. 4070, 1974.
- [10] Mukamel S., Jortner J., « Lifetimes for resonance fluorescence and near resonance Raman scattering », *J. Chem. Phys.*, vol. 62, p. 3609-3615, 1975.
- [11] Berkowitz M., Gerber R.B., « Vibrational relaxation of molecules in solids: The role of rotational and of translational local modes », *Chem. Phys. Lett.*, vol. 49, p. 260-264, 1977.
- [12] Gerber R.B., Berkowitz M., « Role of Rotational and Translational Local Modes in Vibrational Relaxation in Solids: A Study of NH and ND in Solid Ar », *Phys. Rev. Lett.*, vol. 39, p. 1000, 1977.
- [13] Berkowitz M., Gerber R.B., « Rotational mode participation in long-distance vibrational energy transfer in solids », *Chem. Phys. Lett.*, vol. 56, p. 105-108, 1978.
- [14] Legay F., Chemical and Biochemical Applications of Lasers, vol. 2, C.B. Moore, New York, 1977.
- [15] Sun H.Y., Rice S.A., « Conjecture on the Rate of Vibrational Relaxation of a Diatomic Molecule in a Monatomic Lattice », *J. Chem. Phys.*, vol. 42, p. 3826, 1968.
- [16] Zwanzig R.W., « Theory of Vibrational Relaxation in Liquids », *J. Chem. Phys.*, vol. 34, 1961, p. 1931.
- [17] Litovitz T.A., « Theory of Ultrasonic Thermal Relaxation Times in Liquids », *J. Chem. Phys.*, vol. 26, p. 469, 1967.
- [18] Schwartz R.N., Slawsky Z.I., Herzfeld K.F., « Calculation of Vibrational Relaxation Times in Gases », *J. Chem. Phys.*, vol. 20, p. 1591, 1952.