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Khalifa Nsir, Gerhard Schäfer, Raphaël Di Chiararoupert, Lionel Mercury. Pore scale modelling of DNAPL migration in a water–saturated porous medium. Journal of Contaminant Hydrology, 2018, 215, pp.39-50. 10.1016/j.jconhyd.2018.07.001 . insu-01856217

HAL Id: insu-01856217 https://insu.hal.science/insu-01856217v1

Submitted on 10 Aug 2018

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1	Pore scale modelling of DNAPL migration in a water–saturated
2	porous medium
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10	
11	Abstract
12	A numerical simulator based on the discrete network model approach has been developed
13	to simulate drainage processes in a water-saturated porous medium. To verify the predictive
14	potential of the approach to simulate the unstable migration of adense nonaqueousphase liquid
15	(DNAPL) at the pore scale, the numerical model was applied to laboratory experiments
16	conducted on a sand-filled column. The parameters relative to pore body size and pore throat
17	size used in the construction of the equivalent network were derived from discrete grain-size
18	distribution of the real porous medium. The observed water retention curve (WRC) was first
19	simulated by desaturation of the network model. The good agreement of the modelled WRC
20	with the experimental one highlights that the applied approach reproduces the main
21	characteristics of the real pore space. The numerical model was then applied to rate controlled
22	experiments performed on a homogenous sand-filled column to study the gravity-driven
23	fingering phenomenon of immiscible two-phase flow of water and a DNAPL. The numerical
24	results match within 10% based on the standard deviation with the experiments. They correctly
25	reproduce the effect of several system parameters, such as flow mode (upward flow and

downward flow) and the flow rate, on the stability of the water/DNAPL front in a saturatedporous medium.

Keywords: network model; porous medium; WRC; DNAPL; immiscible displacement;
fingering

30

31 **1. Introduction**

32 Characterization and quantification of the migration of immiscible liquids in groundwater 33 are topics that have received considerable attention in recent years (Alexandra et al.2012; Wu 34 et al.2017). Several studies of two-phase immiscible flows have been motivated by the need to 35 treat spills and leaks of so-called dense nonaqueousphase liquid (DNAPL), which can severely impact the quality of subsurface water supplies (Kueper and Frind 1989; Birovljev et al. 1991; 36 37 Fayers et al. 1996; Bettahar et al. 1999). When infiltrating through the saturated zone, migration 38 of DNAPLcan result in highly fingered fluid distributions. The occurrence of fingering is 39 caused by flow instabilities due to differences in viscosity and density between DNAPL and 40 water (Khataniar and Peters 1992; Riaz and Tchelepia 2006; Essaid et al. 2015; Cheng et al. 41 2016). These fingers propagate rapidly, causing early breakthrough relative to stable 42 displacement (Brailovskyet al. 2006).

Numerical modelling of DNAPL displacement in water-saturated porous media using
continuum models has been performed by many researchers (Nayagum et al. 2004;
Aggelopoulos and Tsakiroglou 2009, Zhang et al. 2011; Erning 2012; Kokkinaki et al. 2013;
Sleep et al. 2015, Schneider et al. 2015). However, the fingering process in a homogenous
porous medium cannot be simulated with these models because they do not explicitly consider
the instability behaviourof the DNAPL-water interface.

To overcome this shortcoming, microscopic approaches such as Stokes' solution for flow
in single pores with a specified geometry or lattice Boltzmann methods(LBM) have been

51 investigated to reproduce unstable displacement experiments. Kiriakidis et al. (1991) developed 52 a 2D algorithm involving Monte Carlo decision-making, random walks, and principles of percolation theory. This algorithm successfully predicted the three distinct behaviours of 53 54 immiscible displacement in porous media, such as viscous fingering, stable displacement, and invasion percolation, but the model did not include the gravity term, and gravity fingering was 55 56 not considered. Ewing and Berkowitz (1998) developed a generalized growth model based on 57 invasion percolation to simulate immiscible displacement in saturated porous media. Even 58 capillary, viscous and gravity forces were incorporated in their 3D algorithm, where viscous 59 forces were expressed stochastically rather than explicitly. Glass et al. (2001) developed a 60 macro-modified invasion percolation (MMIP) model, including also the effects of all 3 forces 61 within the invading phase in a macro-heterogeneous porous medium. The simulated evolving 62 invasion structure during the gravity-destabilized condition matched the experimental 63 distributions quite well.Dong et al.(2011) proposed a LBM model taking into account both 64 wettability and gravity tosuccessfully reproduce flow experiments in Hele Shaw cells. Recently, 65 Liu et al.(2013; 2014; 2015) have developed a Lattice Boltzmann model that was able to 66 simulate the main flow regimes (capillary fingering, viscous fingering and stable displacement). 67 The model was applied to simulate drainage micromodel experiments of the liquid CO₂ displacement of water. The authors obtained a good agreement with the experimental 68 69 measurements and showed that increasing M (viscosity ratio of non-wetting fluid to wetting 70 fluid) or decreasing the media heterogeneity can enhance the stability of the displacement 71 process.

While the lattice Boltzmann method gives a more rigorous description of different physical processes, it is often limited to relatively simple physical situations or to systems encompassing only a few pores. For this reason, pore-scale networks are often used to describe

the flow rate of fluids at the pore scale (Koplick and Lasseter 1985; Aker et al. 1998; Helge et
al. 1999; Jia et al. 1999; Laroche and Visika 2005).

In pore-scale network modelling, local capillary equilibrium via the Young-Laplace equation is generally used to determine multiphase fluid distribution. A set of rules that describes the appropriate physical processes and arrangements of fluid within each pore is developed and then combined to describe the displacement of both fluids in the system. Macroscopic behaviours of the displacement can then be seen in network models, even though they are not coded explicitly.

83 Many network models have been developed to study a wide range of displacement 84 processes, including drainage and imbibition (Nordhaug et al. 2003; Singh and Mohenty 2003; 85 Ferer et al. 2007; Niaser et al. 2009; Tørå et al. 2012; Sheng and Thompson 2013; Bultreys et 86 al. 2015; Kallel et al. 2017). Regular lattice structures are generally used, with pore bodies 87 corresponding to the vertices of the lattice and pore throats connecting the pore bodies. The 88 most important aspects of network models are the dimension and coordination (Gaoet al. 2012; 89 Jivkovet al. 2013). For example, trapping is a dominant process in 2D, less important in 3D, 90 and virtually non-existent in 4D (3D+time) and when an above multi-directional pore-network 91 is used (Raoof and Hassanizadeh 2010). Likewise, networks with high coordination behave 92 quite differently than networks with low coordination. In most early network models, pore 93 space parameters were chosen without reference to a realistic porous medium. Network is 94 equivalent only in a statistical sense to the modelled system. Indeed, they were used to explore 95 network concepts as much as to explore porous media. More modern network models were 96 often built directly from micro-CT scans of the rock, and so they had not only the same pore 97 size distribution but also the same exact structure as the rock they are simulating (Al-Raoush 98 and Willson 2005; Prodanovic et al. 2007; Dong and Blunt 2009; Raoof et al. 2010; Bultreys et 99 al. 2015). In these cases, the ability to reproduce physical measurements is excellent. However,

if the exact rock type has to be used for the network construction, the application of predictive
pore-scale modelling will be severely limited due to the complexity and cost of the methods.
More details about the methods for obtaining pore space information, constructing pore
networks and the application of pore network models in porous media can be found elsewhere
(see Joekar-Niasar and Hassanizadeh(2012) and Xionget al. (2016)).

105 By controlling parameters such as pore-size disorder, viscosity, and flow rate, previously 106 developed dynamic pore network models were used successfully to reproduceviscous fingering 107 phenomena exhibited in laboratory studies.Lenormandet al. (1988) developed a dynamic 108 drainage pore network model and used it to simulate corresponding micromodel experiments. 109 Their model reproduces capillary fingering, viscous fingering and frontal displacement regimes 110 for different capillary number and mobility ratio combinations successfully. The largest 111 network that they used in their simulations consisted of 100×100 nodal junctions and they 112 presented a relatively limited set of simulation results. Aker et al. (1998) developed a two-113 dimensional network simulator and used it to characterize the different flow regimes observed 114 in drainage. They introduced a new method that allowed the simultaneous flow of two liquids 115 into one pore and demonstrated that viscous fingering could be reproduced. However, the 116 approach was highly CPU intensive and a 60×80 network was the largest lattice that could be 117 considered. In addition, they only presented results before a breakthrough of the injected 118 phase.Singh and Mohanty (2003) developed a dynamic network model providing 3D results 119 consistent with the 2D results of Lenormandet al.(1988). Their simulator could reproduce the 120 displacement front structure and dynamics as function of capillary number and viscosity ratio. 121 Whilst their simulator could produce various displacement regimes, including viscous 122 fingering, the largest system used in their study was a 30×8×8 network. Tørå et al. (2012) 123 extended the model developed by Aker et al. (1998) by incorporating the dynamics of the 124 wetting layers using an approach similar to Singh and Mohanty (2003). They used this model to study saturation profiles during imbibition and the resistivity index at different capillary numbers. Their numerical results were in good agreement with experimental data from sandpacks. The simulations were carried out on one realization of model volume of $(4.5 \times 1.5 \times 1.5)$ mm³ consisting of 767 nodes and 1750 tubes.

Most of the previous pore network modelling studies described above were performed in small networks and were followed by a successful benchmarking exercise of the numerical simulations against micromodel experiments. However, the modelling approach is rarely used to simulate such mechanisms at the laboratory core scale. Additionally, very few studies have presented saturation maps after breakthrough under unstable conditions. An integrated effort is needed to connect network models and laboratory tests at the core scale more closely.

The main objective of the present work is to test, at the scale of a few centimetres, the 135 136 capacity of the pore scale network model developed by Nsir and Schäfer (2010) to capture the 137 gravity-driven fingering observed in our own water-DNAPL drainage system. The model is 138 first applied to predict the water retention curve of the model sand used in the experiment. The 139 comparison of the experimental curve and the one modelled will show whether the used 140 network model reproduces the main characteristics of the real pore space. In a second step, the 141 numerical model is then used to simulate the displacement of water by DNAPL during 142 controlled drainage experiments performed in a 68-cm long glass column filled with the 143 homogenous model sand. The numerical results are compared to the observed physical 144 quantities, such as the distribution of arrival times of the DNAPL/water front at a control 145 section, the DNAPL pressure at the inlet as a function of time, and the DNAPL saturation profile 146 at the end of the displacement experiment.

147

148 **2. Laboratory experiments on DNAPL migration**

149 Laboratory experiments were conducted on a 68-cm long glass column with an internal 150 diameter of 10 cm. The used porous medium is a medium-sized quartz sand with a mean grain-151 size diameter of 0.4 mm, a uniformity coefficient of 2.1 and a low fraction of organic content (foc = 0.09%, based on NFT 31–109) (Bohyet al. 2006). The hydraulic properties of the quartz 152 153 sand, such as its moisture characteristics, were quantified in former studies by Cotel(2008). 154 Trichloroethylene (TCE) was chosen as the DNAPL for the experiments because it is among 155 the most frequently detected contaminants in subsurface environments. At 20 °C, TCE has a 156 density of 1.463 g/cm3, a viscosity of 0.0056 g/s/cm, and a solubility in water of 1300 mg/L.

The experimental setup was designed to produce a controlled and well-defined injection of TCE in an initially water-saturated homogeneous porous medium. The outlet section of the column was kept at a constant water pressure. A highaccuracy peristaltic pump with flow rates up to 200 mL/min was used to inject the displacing fluid in the sand-filled column. Pressures at the inlet and outlet were measured using a pressure transducer (Cerabar T-PMC131). Several system parameters (e.g., flow rate, flow mode (upward flow, downward flow) were varied in the experimental programme.

164 The experimental approach is original, as it is based on the use of optical fibres to locally 165 quantify the arrival times of the DNAPL/water front at different points within a control section 166 of the porous medium. Local DNAPL saturations at different depths of the sand column were 167 also quantified by in situ soil sampling. Because of the emplacement of fibres, the sampling 168 was achieved only above the sensor control section of the column (between z=0 and z=-34169 cm). At each sampling depth, one sample was taken on the axis of the column and two others 170 on opposite points of the edges of the column section. More details about the experimental setup 171 and sampling method are given in Nsiret al. (2012).

172

173 **3. Numerical model**

174 **3.1. Geometry of the network**

175 A 3D network model based on spherical porebodies and cylindrical porethroats was developed to simulate drainage processes in a saturated porous medium. The pore space is 176 177 represented by a cubic lattice with porebodies corresponding to the vertices of the lattice and 178 porethroats connecting the porebodies. The connectivity or coordination number in the network 179 (the number of throats connected to a given pore in the network) is set equal to 6. The pore 180 body and pore throat radii were drawn at random using a probability frequency distribution 181 given by a special case of the Weibull distribution (Weibull, 1951). We used this type of 182 distribution because it is easy to implement, and its model parameters may adequately represent 183 a given pore size distribution. Compared to other models, such as normal, lognormal or bimodal 184 distribution, the probability of finding smaller pore bodies in the network is higher. In the 185 modelling approach, specified values of the minimum, mean and maximum radii (r_{min}, r_{mean}, 186 and r_{max}, respectively) are needed to achieve the pore size distribution. The probability 187 distribution used is as follows:

188
$$g(x) = \begin{cases} \frac{x}{x_2^2} \exp(-\frac{x^2}{x_2^2}) & \text{for } x \le x_3 \\ 0 & \text{for } x \succ x_3 \end{cases}$$
(1)

where the radius is r, $x = r - r_{min}$, $x_2 = r_{mean} - r_{min}$, and $x_3 = r_{max} - r_{min}$. Both porebody and porethroat radius distributions are of this type, although with different parameters: r_{min} , r_{mean} and r_{max} . For a throat connecting pores *i* and *j*, the throat length is defined as $L_{ij} = L - (r_{pore,i} + r_{pore,j})$, where Lis the distance between the centres of two adjacent pore bodies. L is considered constant in the chosen network. The values of r_{min} , r_{mean} , and r_{max} specified for both pore body and pore throat and thus for the node spacing L are hereafter considered as the geometric parameters of the network model.

3.2. Governing flow equations

197 When solving the transient flow field, the network model takes into account capillary 198 variations in space, the local viscous pressure field, and gravity. The location of fluid-fluid 199 interfaces is restricted to the connection between the pore body and pore throat. The Washburn 200 equation (Washburn, 1921) is used to quantify the flow rate in a pore throat, which is connected 201 to a pore body separated by a water-DNAPL interface. The main assumptions are as follows: 202 (i) fluids used are Newtonian, incompressible, and immiscible; (ii) flow is laminar; and (iii) 203 local capillary pressure in a pore body is negligible, resulting in only one mean pressure within 204 a pore body independent of the phase saturation of that pore body. The mass balance equation 205 for each fluid phase α , wetting (water, $\alpha = w$) and non-wetting (DNAPL or air, $\alpha = nw$), in a pore 206 bodyiisas follows:

207
$$V_i \frac{\partial S_i^{\alpha}}{\partial t} + \sum_j Q_{ij}^{\alpha} = Q_i^{\alpha, inlet}$$
 (2)

where $V_i[L^3]$ represents the volume of pore bodyi, $S_i^{\alpha}[-]$ represents local saturation (percent of V_i filled with fluid α), $Q_{ij^{\alpha}}[L^3T^{-1}]$ is the phase flow rate through a pore throat connecting pore bodyiand pore body j. $Q_i^{\alpha,inlet}[L^3T^{-1}]$ is the external phase flow rate into pore i, which is zero, unless the pore is located at the flow boundary. The sum runs over all neighbouring pores of pore bodyi.

Summation of Eq. (2) over the two phases gives the following equation for each porebody i:

215
$$\sum_{j} (Q_{ij}^{w} + Q_{ij}^{nw}) = \sum_{j} Q_{ij} = Q_{i}^{nw,inlet}$$
 (3)

The expression used for the phase flow rate Q_{ij}, depends on the fluid present in the pore throat connecting pores i and j, and on the presence of a meniscus at the boundaries between a pore body and a pore throat.

If no meniscus is present at the pore throat entry, the flow rate Q_{ij} through the pore throat
is given by Poiseuille'slaw, as follows:

221
$$Q_{ij} = \frac{\pi r_{ij}^{4}}{8L_{ij}\mu_{\alpha}} (P_{i} - P_{j} - (z_{i} - z_{j})\rho_{\alpha}g)$$
(4)

where $\mu_{\alpha}[ML^{-1}T^{-1}]$ and $\rho_{\alpha}[ML^{-3}]$ are thedynamic viscosity and the density of the phase fluid present in the pore throat, respectively;r_{ij} and L_{ij} are the radius and the length of the pore throat, respectively;P_i and P_j are the fluid pressures in pores i and j; and z_i and z_j are the height of the vertices at the centre of pore bodiesi and j. The first term of the right-hand side of Eq. (4), $\pi r_{ij}^{4}/(8 L_{ij}\mu_{\alpha})$, represents the flow conductance in the pore throat.

If a meniscus is present at the pore throat entry, the flow rate Qij through the pore throatis expressed by the Washburn equation (Washburn, 1921), as follows:

229
$$Q_{ij} = H \langle P_i - P_j - (z_i - z_j) \overline{\rho}g - P_c(r_{ij}) \rangle \frac{\pi r_{ij}^4}{8L_{ij}\mu} (P_i - P_j - (z_i - z_j) \overline{\rho}g)$$
(5)

where $P_c(r_{ij})$ [ML⁻¹T⁻²] denotes the threshold capillary pressure that must be exceeded for the DNAPL to enter the pore throat connecting pore bodiesi and j. This threshold pressure is given by the Young-Laplace equation, as follows:

233
$$P_{c}(r_{ij}) = \frac{2\sigma \cos\theta}{r_{ij}}$$
(6)

where θ is the contact angle (assumed to be zero in this work). H <X> is a Heaviside function that stands for the displacement condition of the interface in a pore throat. The throat can be blocked by capillarity if the capillary entry pressure (P_c(r_{ij})) has not yet been reached. The Heaviside function is defined as follows:

238
$$H\langle X \rangle = \begin{cases} 1 & \text{for } X \succ 0 \\ 0 & \text{for } X \le 0 \end{cases}$$
 (7)

If a meniscus is present at the boundary between a pore body and a pore throat, the identity of the fluid flowing through the pore throat (DNAPL or water, or capillary-blocked) can only be determined after computation of the pressure field in the network. Therefore, an effective viscosity and an effective density are used for the displacing fluid in Eq. (5) and are defined by

the following:

244
$$\overline{\mu} = \mu_{nw} S_{ij}^{nw} + (1 - S_{ij}^{nw}) \mu_{w}$$

$$\overline{\rho} = \rho_{nw} S_{ij}^{nw} + (1 - S_{ij}^{nw}) \rho_{ij}^{w}$$

$$S_{ij}^{nw} = (S_{i}^{nw} + S_{j}^{nw})/2$$
(8)

where S_{ij}^{nw} [-] is the average phase saturation between pore bodiesi and j. As the average phase saturation evolves as a function of time, it indirectly accounts for the interface movement inside a pore throat.

Introducing the appropriate expression of flow rate Q_{ij} in Eq. (3) leads to a set of algebraic equations with the pore body pressures as unknowns. This set of equations is written in matrix form, as follows:

$$251 \quad \mathbf{A} \times \mathbf{B} = \mathbf{P} \tag{9}$$

where A is the conductance matrix with elements that depend on the connections between different throats, Pdenotes the pressure vector, and the Bvector contains the pressure and the flow rate at the boundaries, the buoyancy terms, and the capillary pressure if a meniscus is present in the pore throat.

256 **3.3. Numerical solution procedure**

The governing equations presented in the previous section are solved for fluid pressure P and wetting fluid saturation S_w using an IMPES (IMplicit Pressure-Explicit Saturation) modelling approach. The flow chart describing the different steps of the pore-scale network model is shown in Figure 1.

Equation (7) is solved implicitly for P, assuming that S_w and throat conductances $\pi r_{ij}^4/(8$ L_{ij} μ_{α}) are known from the previous time step. The calculated pressure field is then used to quantify fluid flow rates through the pore throats. The ratio of free volume in a pore body i (not invaded by displacing fluid) to the sum of flow rates in all pore throats connected to pore body i and containing a moving interface gives the filling time needed for that pore body i to be 266 invaded. The minimum value of the calculated filling times (hereafter called T_{min}) is then used 267 to update the local saturation in each pore body as follows:

$$S_{i}^{t+1} = S_{i}^{t} + \frac{Q_{i} \times T_{min}}{V_{i}}$$
(10)

where S_i^t [-] and S_i^{t+1} [-] denote the saturation at the previous time (t) and calculated at the new time (t+1), respectively; and Q_i [L³T⁻¹] represents the sum of flow rates in all pore throats connected to pore body i and containing a moving interface.

During one time step, only one pore body reaches the full non-wetting phase saturation. This pore body generates additional interfaces at all connecting pore throats that are filled with the wetting fluid. Newly created interfaces are tested for stability, and appropriate expressions for flow rate Q_{ij} are then identified. This modifies the conductance matrix at each time step. The field pressure is computed, and the procedure for updating the saturation in pore bodies is repeated. This provides a transient response for the pressure and saturation fields.

278 To solve the set of equations (9), a Preconditioned Conjugate Gradient Method (PCGM) 279 algorithm is used. The simulations are conducted on a Linux-computer with 3956 MB RAM 280 and a Celeron processor running at 1998 MHz. One iteration on the chosen lattice network 281 (20×20×200) took approximately 90 seconds and required a memory space of approximately 4 282 MB. The corresponding Central Processing Unit (CPU) time was approximately twenty days 283 for the chosen lattice size. As the Fortran code was not parallelised and the free memory offered 284 by the used computer was limited, simulations could not be launched when a lattice size larger 285 than $20 \times 20 \times 200$ was used.

The time-stepping process is repeated until a stopping condition is reached. This condition allows the choosing of the stage at which the simulation should be achieved: after attaining a fixed saturation value at a given cross-section, after reaching a breakthrough of the invading fluid phase, after having performed a defined number of steps, or after the injectingof a predefined total volume of the invading fluid phase.

3.4. Model parameters and numerical implementation

292 To obtain a reliable simulation of laboratory experiments, the characteristic parameters 293 of size distributions for both pore bodies and pore throats (rmin, rmean and rmax) werecomputed 294 based on the grain-size distribution (GSD) of the real porous medium. Themodelling concept is 295 based on the geometric properties of packing spheres (Dodds, 1980), which are combined with 296 a probability approach proposed by Rouault and Assouline (1998). The input data for sphere 297 packing are in the form of a discrete particle-size distribution derived from the (GSD) of the 298 sand used in the experiment (Nsir and Schäfer, 2010). The obtained results consist of one pore 299 body-sized distribution curve and four pore throat-sized distribution curves. Assuming that the 300 generated pore body sizes and pore throat sizes are normally distributed, which is generally 301 assumed for a large sampling number, assessment of the mean value and the standard deviation 302 (sd) of corresponding curves allows the computation of various ranges of pore body radii and 303 pore throat radii in terms of rmin, rmean and rmax. More details of the applied method are given in 304 the work of Nsir and Schäfer (2010).

305 The geometric parameters for the pore body radii and pore throat radii considered in the 306 numerical simulations are shown in Table 1. The grid length should be slightly two times greater 307 than the maximum radius of pores (r_{max}=0.054 mm). For this reason, the distance between the 308 centres of two adjacent pore bodies (L) was fixed to 0.14 mm. The chosen values gave the best 309 fit for the measured macroscopic properties of the medium sand used in the experiment. The equivalent intrinsic permeability and porosity are 8.6×10^{-11} m² and 47%, versus the measured 310 values of 9×10⁻¹¹ m² and 40%, respectively (Nsir and Schäfer, 2010). By fixing the maximum 311 312 radii (r_{max}) and the minimum radii (r_{min}) of the size distribution as one time, two times and three 313 times the standard deviation (sd)away the mean radius (r_{mean}), threesize distributions with 314 different shapeswere considered for a given lattice size (see Table 1).

To simulate the entire laboratory column (68 cm long, 10 cm internal diameter), an equivalent network with 714×714×4858 nodes in the [X,Y,Z] directions, corresponding to 2,476,588,968 pore elements is required. Simulations with such lattice size are highly CPU intensive and RAM consuming and were, consequently, not manageable by our computational resources. To face this difficulty, we decided to reduce the size of the network in order to match the maximum height and width of the column.

321 An equivalent network of 7×7×4858 pore bodies was initially chosen to simulate drainage 322 experiments. This spatial discretisation has the advantage of reproducing the total height of the 323 physical model and, consequently, gravity effects, even when only a small fraction of the 324 column section is used (1 square millimetre). This might favour the formation of very few 325 fingers that might occupy most of the cross-section of the model. As they move downward, the 326 number of pore bodies to invade before reaching the bottom might increase the drainage of the 327 porous medium. Consequently, an overestimation of the saturation of the invading fluid can be 328 induced by a coarse pore discretisation in the transverse direction. Using the correct shape of 329 the cross-section is thus as important as the real column height.

330 To account for a sufficiently large section of the medium that is manageable by our proper 331 computational resources, additional simulations considering networks with more nodes along 332 the two directions of the horizontal section (20×20 , rather than 7×7) but with minimum nodes 333 in the direction of flow (200, instead of 4858) have also been undertaken. To conserve 334 representation of the total physical height, the node-spacing was increased (3.4 mm, instead of 335 0.14 mm). Increasing the node spacing does not impact the macroscopic properties of the 336 equivalent network as already discussed in the previous work of Nsirand Schäfer (2010). Furthermore, the corresponding network may be assimilated in this case to a package of 337

cylindrical tubes joining at junctions with volume, which remains the physical representativeof reality.

340 To reproduce the conditions of the performed drainage experiment, the network model was initially water-saturated and a constant flow rate of 29.6×10⁻⁴ mL/min of DNAPL was 341 342 applied at the inlet section of the model. As the simulated cross-section of the network was 343 significantly smaller than the real cross-section of the experimental soil column, the simulated 344 injection rate was reduced to the experimental injection rate by the ratio of the cross-sectional 345 area of the model to that of the column. At the outlet section of the model, the observed water 346 head was specified as a constant pressure boundary. The simulation was stopped when the time 347 needed to inject the DNAPL volume considered in the experiment was reached.

348

349 4. Results and discussion

350 4.1 Water retention curve modelling

351 The relationship between the amount of water, typically quantified by the degree of 352 saturation (S) or volumetric water content (θ), and pore-water potential, typically quantified by 353 matric potential or capillary pressure (Pc), is referred to as the water retention curve(WRC) of 354 soils. A key attribute of the developed model is its capability to compute fluid pore-scale 355 saturation as a function of capillary pressure applied to a given lattice, which allows modelling 356 the WRC of a porous medium.Comparison of the numerically calculated WRC with the 357 experimentally obtained oneallows for verification if the predicted pore space parameters match the 358 features of WRC observed ina column experiment.

The experimental data used for verification were obtained independently in a multistep outflow experiment (Cotel, 2008). To reproduce the functional relationship between capillary pressure and water saturation, a displacement simulation was performed using a series of sequential capillary pressure steps. The water saturation of the porous medium was computed at the end of each displacement step. For each prescribed capillary pressure, the dynamics of the desaturation of the medium is quantified by the track of the generated interfaces in the pore network. This rule was applied iteratively until all the air/water interfaces remained trest under the given capillary pressure level, and the invasion of water-filled pores by air is stopped. At this stage, the whole network is under hydrostatic conditions and the corresponding water saturation can thus becomputed. Then, the applied capillary pressure is again increased. The simulation is stopped when the air/water front reached the outlet face of the network.

The simulations were conducted on a network of 20×20×200 nodes because it has lower CPU consumption and presents a larger cross section than the 7×7×4858 lattice. Furthermore, matching a fine vertical discretisation of the column is not absolutely necessary to model the macroscopic capillary pressure as a function of the water saturation. According to the experimental data, the first capillary pressure applied to the network boundary was fixed to 100 Pa. The network was then drained stepwise by systematically incrementing the prescribed capillary pressure by a value of 100 Pa at each displacement step.

377 The simulated WRC for different pore throat size distributions compared to the measured 378 one are given in Figure 2. The agreement in the sloping of the curves shows saturation changes 379 in a similar fashion for a given change in pressure. The model seems to be able to adequately 380 predict the observed capillary pressure-saturation relationship up to a capillary pressure of 381 approximately $0.2 \times 10^{+4}$ Pa (equivalent to 0.2 m water head). The model predicts slightly higher 382 water saturations than those measured in the experiment. However, it clearly deviates from the 383 experimental data set for high capillary pressures corresponding to water saturations lower than 384 0.2. The mobilisation of the wetting phase in the simulated network appears significantly higher 385 than that observed in the experiment in this condition. This may be due to limitations of the 386 numerical model when a network section of only (20×20) pores in a horizontal transect is used. 387 In fact, neglecting the spatial pore size correlations or connectivity may lead to inaccurate

388 predictions of water retention at very low water saturation. In addition, the simulated fluid 389 displacement is considered frontal. Thus, entrapment of the wetting phase due to snap off is not 390 considered in the numerical model. This means that water cannot be trapped as the menisci 391 advance into a pore throat and there is no residual wetting phase left behind.

392 The misfit between the measured WRC and modelled one may also reflect limitations 393 inherent in the experimental results within this range, where water retention mechanisms other 394 than capillarity may dominate. Several studies on the WRC of soils led us to believe that the 395 water retention characteristic is not only closely related to the pore size distribution but also to 396 the solid pore interfaces (Rossi and Nimmo, 1994; Fayer and Simmons, 1995; Webb, 2000; 397 Tuller and Or, 2005; Khlosi et al. 2006; Silva et al. 2007). The experimental setup used in the 398 laboratory experiment does not provide a highly accurate description of the WRC in the very 399 dry range of the sand. On the other hand, using a wider distribution of the pore throat size gives 400 a much better match with the measured one (Figure 2). This is clearly due to the generation of 401 a few additional thinner pore throats when doubling or tripling the width of the distribution. 402 The penetration of the non-wetting phase into the pore bodies is thus reduced, and more residual 403 water phase is left behind. The characteristics of the pore throat distribution used in the network, 404 such as the mean radius and standard deviation, seem to be a key factor to minimise the difference between experimentally observed WRC and numerically modelled WRC. 405 406 Optimizing the distribution parameters in this way is similar to optimising fitting parameters in 407 commonly adopted WRC models (Brooks and Corey, 1964; Van Genuchten, 1980). However, 408 the link between modelling parameters and physical properties of the soil is here more explicit. 409 Despite this improvement, the shape of the network, i.e. the number of pores simulated in the 410 horizontal transect on the WRC, remains the principal cause of the misfit between the observed 411 and the modelled WRC.

Using a 2D network on a X-Z plane allowed us to study the impact of the network shape on the numerical results and to compare them to the experimental results, as we are now able to double or quadruple the number of pores of the network along the cross-section. Such a choice was not possible with a 3D network, as the computational resources do not permit running simulations with a large lattice size. Here, we studied the effect of the shape of the network on the WRC.

418 Simulated water retention curves with networks of 50×50, 75×75, and 100×100 height by 419 width, but with the same pore throat size (1 sd), are compared with the experimental curve 420 (Figure 3). Numerical results show now a good agreement with the measured curves, especially 421 in the region of pendular water (S<0.2). Compared to the 3D simulation (with a small cross 422 section of 20×20), the simulated (100×100 based) water retention curve (WRC) fits the 423 measured WRC quite well at low water saturation but not at high wetting saturation $(0.2 \le \le 1)$. 424 This indicates that the larger the horizontal transect is, the higher the trapped water will be. On 425 the other hand, reducing the vertical discretisation of the pore network will lead to an 426 underestimation of the quantity of capillary and funicular water. The behaviour of the pore 427 network is thus shape dependant (function of the number of pores modelled in the cross-428 section), as well as size dependant (number of pores modelled along the height). Based on these 429 results, the discrete network model should have enough nodes in all three directions to obtain 430 accurate matching of the experimental WRC.

431

432 **4.2. Modelling of a laboratory experiment on DNAPL/water drainage**

433 **4.2.1.** Displacement behaviour of the water/DNAPL front for a low injection rate

434 The simulations were conducted on a network of $20 \times 20 \times 200$ nodes in the [X,Y,Z] 435 directions. This lattice size was preferred to the $7 \times 7 \times 4858$ lattice size because the modelled

436 cross-section is larger, and as shown in section 4.1, the emergent network behaviour is shape437 dependent.

438 TheDNAPL arrival times computed at individual pore bodies of a control sectionas 439 defined in the experiment setup (Nsiret al. 2012) have been compared to the measured arrival 440 times for both vertical-upward and vertical-downward flow modes (Figure 4). The 441 corresponding curves were plotted as a function of DNAPLarrival time, normalized by the 442 average arrival time for both the experiments and numerical simulations. As shown in Figure 4, 443 the simulations exhibited behaviours similar to those observed experimentally. In fact, the 444 dimensionless DNAPLarrival timescalculated by the developed modelfor both flow modesare 445 in good agreement with those obtained in the experiments. The calculated standard deviations 446 are also rather close to the measured values. In fact, the standard deviation values were 14 sec 447 and 75 sec, compared to 9 sec and 70 sec measured in the experiments, for the case of vertical-448 upward displacement and vertical-downward displacement, respectively. Thus, the model 449 isable to adequately reproduce even the observed displacement instabilities caused by the 450 negative contribution of gravity.

451 In the case of upward displacement, the gravitational component is added to the total 452 potential driving flow and creates an increase in the global inlet pressure. Consequently, the 453 fraction of accessible pores increases and a compact pattern of the invading fluid is established, 454 resulting in a nearly uniform distribution of DNAPL in a porous medium transect. In contrast, 455 because of the negative effect of the gravity forces, the water/DNAPL interface is no longer 456 uniformly distributed over the cross-section in the case of downward displacement and many 457 pore throats become blocked by capillary effects. The number of active invasion paths is 458 therefore lower in this situation, and many vertically oriented fingers may develop in the pore 459 network.

460 **4.2.2. DNAPL saturation**

461 The final average DNAPLsaturations calculated over the entire network are quite 462 different for upward and downward displacements, confirming that density contrast plays a 463 significant role in the migration of a DNAPL in a porous medium, particularly at low DNAPL 464 injection rates. According to the numerical simulations, we determined an average DNAPL 465 saturation of approximately 72% in the case of upward displacement but only 41% for 466 downward displacement. These values are in the same order of magnitude of those obtained in 467 the experiments as an average DNAPL saturation of 66% and 33% was obtained for upward and 468 downward displacement, respectively. This difference is mainly due to the stable growth of the 469 water/DNAPL front during upward displacement, whereasthe downward displacement is 470 characterized by flow instabilities that were obviously reproduced quite well with the developed 471 model.

472 Figure 5 illustrates a 3D representation of the calculated DNAPL saturation along a 1.5-473 cm length of the equivalent network of the medium sand used in the experiment. The numerical 474 results correspond to an unstable downward displacement. The 3D view of saturation field 475 clearly illustrates the formation of gravity-enhanced fingering in the simulated porous medium. 476 In this condition, only a small amount of displaced fluid (water) comes in contact with the 477 DNAPL and due to the destabilizing effect of gravity, the displacing fluid quickly invades the 478 larger throats and blocks narrow throats where water remains entrapped. Consequently, the 479 advancing DNAPL/water front exhibits several fingers that elongate downwards while 480 advancing through the network.

Based on the DNAPL saturation field computed in the network at a given time, a volumeaveraged DNAPL saturation can be computed over a representative volume of the medium. The resulting macroscopic profiles of volume-averaged DNAPL saturation, as a function of depth for both upward and downward displacement, were then compared to those obtained in the experiment (Figure 6). Similarto the experimental observations, the front behaviourof predicted 486 DNAPL saturations appears to be abrupt in the case of upward displacement and presents 487 remarkable fluctuations in the case of downward displacement. The numerical results confirm 488 the experimental observations that the water-DNAPL displacement occurs uniformly when 489 DNAPL is injected from the bottom. However, a heterogeneous cross-section distribution of 490 DNAPL is obtained when the displacing fluid is injected from the top of the column due to both 491 gravity effects and an unfavourable viscosity ratio. The numerical results confirm the 492 experimental findings. However, the calculated DNAPL saturations are higher than the 493 measured values for both displacement modes (upward and downward), especially when a 494 narrow pore throat size distribution is used (1 sd). Significant differences appear, particularly 495 in the region close to the network inlet. For example, at a depth between 10 and 20 cm, differences in saturation may reach 40% in the case of stable water displacement. Apparently, 496 497 the simulated number of active and invading fluid paths seems to be relatively higher than the 498 experimental values. Discrepancies to the measurement are reduced and a better fit is obtained, 499 particularly in the case of downward displacement, when a wider pore throat size distribution 500 is used (case where r_{max} - r_{mean} = 2 sd). In this case, much higher capillary pressure in the pore 501 throatis generated and the possibility to overcome it is significantly reduced. This might 502 equilibrate interplay between viscous forces, enhancing the full drainage of water, and capillary 503 forces that are acting to retain displaced fluid. Consequently, the displacement of water by the 504 DNAPL is now better represented by the model leading to simulated DNAPL saturations that 505 are closer to the measured ones.

As previously mentioned when modelling WRC (see section 4.1), the relatively higher residual saturations of the invading fluid predicted by the numerical model can also be attributed to the chosen small cross-section of the model. The simulated cross-section of the equivalent network is represented by a small number of nodes (20×20) and remainssmall compared to the reality, which may have limited development of fingering patterns during DNAPL 511 displacement. Using a larger section of network may be more appropriate to model the real 512 porous medium, butlarger networks suffer from prohibitive computation times even with 513 powerful computers. To show the effect of the cross-section shape on the emergence of DNAPL 514 displacementbehaviour, we have undertaken a series of additional simulations with a short 515 reduced height (100 nodes) and three sizes of the cross-section, 6×6, 12×12, and 24×24. Using 516 a much larger cross-sectional size (> 24×24) was not manageable with our proper computational 517 resources. Figure 7 shows the DNAPL saturation field and vertical section-averaged DNAPL 518 profile calculated after 8 sec of injection for each of the three cross-sections. The larger the 519 cross-section is, the more advanced the DNAPL fingers are and the less DNAPL saturated the 520 pores are at the inlet section. This clearly underscores the need to increase the cross-section by 521 at least 5 times more nodes in each direction to obtain an improved fit of the experimental 522 results.

523 **4.2.3**.

4.2.3. DNAPL pressure at the inlet section

524 Although the DNAPL saturation describes the distribution of displacement fluids in the 525 porous medium, it is the pressure build-up that significantly determines the displacement of one 526 fluid by another. Thus, to better understand the interplay between global pressure behaviour 527 and the displacement condition (stable or unstable), the variation of the inlet DNAPL pressure 528 as a function of time was predicted by the model and compared to the measurements for the 529 cases of upward displacement and downward displacement, respectively (Figure 8). According 530 to the measured data, the boundary pressure (applied to the outlet section of the experimental 531 system), which was taken into account in the simulation for both upward and downward 532 displacement, corresponded to a water height of 18 cm and 86 cm, respectively. As observed 533 in the experiments, the pressure increased with time in the case of vertical upward displacement, 534 whereas it decreased in the case of downward displacement.

535 In the situation where DNAPL is injected at the bottom of the network, the water/DNAPL 536 interface is stabilized by the gravity effect and the potentially destabilizing influence of the 537 viscosity ratio was not significant. The pressure increase is therefore caused by the high density 538 of the invading fluid, which overrides the decrease in viscous pressure drop during the 539 displacement of the less viscous DNAPL. Although the time-dependent increase in DNAPL 540 pressure was well reproduced by the numerical simulations, the calculated pressure increase 541 seems to be slightly lower than that observed in the experiment. This can be explained by the 542 chosen arrangement of throat sizes in the network model. Certain narrow throats that may exist 543 in the real porous medium were not captured in the network and may require a higher 544 displacement pressure o be invaded by the displacing fluid.

In the case of downward DNAPL displacement, the interplay between hydrostatic 545 546 pressure and viscous pressure changes leads to an overall decrease of the inlet DNAPL pressure. 547 Thesudden increase of pressure illustrated in Figure 8b corresponds to the breakthrough of the 548 invading fluid at the outlet section. Here, gravity forces are destabilizing and dominate the 549 movement, resulting in typical DNAPL fingers in the displaced fluid. The number of active 550 invasion paths is therefore lower and the flow section of DNAPL is reduced. The contribution 551 of viscous pressure is also limited and is dominated by the contribution of the higher density of 552 the invading fluid. The combination of all these effects results in decreased inlet pressure. The 553 observed decrease of inlet pressure is correctly reproduced by the numerical model, and the rate 554 at which it decreases seems to be relatively higher than that of the measured one. In addition, 555 the computed breakthrough time is earlier compared to that observed in the laboratory 556 experiment. This can be explained by the number of active invasion paths, which may be lower 557 in the network model than in the real porous medium. The leading fingers as simulated in the 558 model (see Figure 5) are essentially moving straight, pertaining to a zero tortuosity. The

559 development of such "no wiggle" fingers decreases the number of pore bodies to invade before 560 reaching the bottom, accelerating the simulated breakthrough.

561

4.2.4. Influence of the DNAPL injection rate on gravity fingering

562 The DNAPL injection rate is one of the key factors in drainage processes, and it controls 563 the balance between buoyancy, viscous forces, and capillary forces. It has been previously 564 shown (see section 4.2.2) that under a low injection rate, the vertical-downward displacement 565 of water by DNAPL gives rise to several fingers. The invasion of the saturated porous medium 566 is only partial, and the resulting distribution of the DNAPL is thus inhomogeneous. Nsiret al. 567 (2012) showed in previous experimental work that increasing the flow injection rate 568 significantly stabilizes the displacement and may entirely suppress the fingering process during 569 immiscible downward displacement. This scenario was also simulated by the developed model 570 to test its capacity to reproduce such phenomena.

571 Figure 9shows the comparison of the simulated dimensionless arrival times of the 572 water/DNAPL front with the measured values. The statistical data of both distributions are 573 similar. The calculated standard deviation was very close to the measured value (24 secagainst 574 20sec measured in the experiment) and much lower than that computed at the low injection rate 575 condition (75 sec). Likewise, the mean arrival time was approximately 489 sec, which is 576 compared to the observed time of approximately 512 sec. Thus, although gravity fingering is 577 considered to be a highly dynamic process, the numerical results also showthat increasing the 578 flow rate alters its destabilizing effect and leads consequently to the stabilization of the 579 water/DNAPLfront. At a low injection rate, DNAPL moves through a pathway of larger pore 580 bodies and pore throats with the lowest capillary entry pressure because the viscous forces are 581 not significant and do not disrupt the dynamic filling of pore bodies and pore throats. This leads 582 to a ramified invasion and to a preferential path growth in the saturated porous medium. As the 583 flow rate increases, viscous forces become more significant, more meniscibecome mobile, and 584 consequently, even fine pore throats may be as overcome as larger ones because of the 585 significant pressure gradient. As a result, a compact pattern of the invading fluid occurs during 586 displacement.

587 Figure 10 illustrates the macroscopic profile of the volume-averaged DNAPL saturation 588 as a function of depth, calculated when the injection rate of DNAPL was doubled and compared 589 to the measured one. Here, the DNAPL saturations are higher and their spatial distribution is 590 clearly more homogenous compared to those calculated under low injection rate. Such 591 macroscopic behaviouris in good agreement with the experimental observations. However, the 592 simulation results slightly overestimate the monitored DNAPL saturation. Discrepancies are 593 significantly reduced when a wider pore throat size distribution is used in the simulation. The 594 arguments previously detailed in the case of the low injection rate (see section 4.2.2) may also 595 explain the small misfit between measured and calculated average DNAPL saturations. In 596 addition, increasing the size of the network cross-section may improve the fit of the numerical 597 results with the experiment.

598

599 **5.** Conclusions

600 The study presents detailed comparisons between numerical simulations of drainage processes (displacement of water by air, water by DNAPL) and corresponding physical 601 602 experiments at the scale of a few tens of centimetres. The goodness of fit between the developed 603 pore-scale network model and the experiment seems to be a function of the grid characteristics 604 and modelling domain dimensions. A major feature of the model is its capacity to reasonably 605 well reproduce the redistribution of the fluid phases in the pore space for a given pressure 606 change, a modification of the applied displacement condition (stable/unstable) or for a rate 607 injection increase. In fact, the predicted water retention curve matched well globally with that 608 obtained in the experiment, especially within the region of higherwater saturation $(0.2 \le \le \le 1)$.

609 The predicted distribution of arrival times of the water/DNAPL front computed at a given cross-610 section are in good agreement with the experimental data obtained for a given displacement 611 scenario. The slightly higher DNAPL saturations predicted by the numerical model are 612 essentially attributed to the chosen small cross-section of the equivalent network. In the actual 613 version of the model, the lattice sizes are limited by the computation time and space memory 614 and remain too far to adequately well represent the whole cross-section of the real porous 615 medium. Thus, a network model with enough nodesfor the cross-section allowsdistinct 616 behaviourof immiscible displacement, such as DNAPL gravity-driving fingering to emerge 617 sufficiently from the interactions of the various pores and throats that constitute the network 618 and the various forces taken in account in the model. This may reduce the differences between 619 experimentally determined saturations and modelled saturations. In this context, further 620 developments of the numerical code, such as implementation of an iterative and more powerful 621 solver, should be undertaken to reduce and optimize the CPU time. Complementary studies are 622 also necessary to test additional features of the pore-space geometry of the porous medium. The 623 model can also be extended to simulate the imbibition process and promote application of the 624 model to reproduce the experimentally obtained residual DNAPL saturations.

625

626 Acknowledgements

Financial support for this research was received from the French Agency for Research
(AgenceNationale de la Recherche), through the Labex Voltaire ANR-10-LABX-100-01. The
authors benefited also from the use of the cluster at the Centre de CalculScientifiqueen region
Centre (CCSC) in France. Laurent Catherine is acknowledged for his technical assistance.
Furthermore, theauthorswouldlike to thanktheRegionAlsace, the GDR «Hydrodynamique et
Transfertsdans les HydrosystèmesSouterrains » (INSU-CNRS), and theConseilScientifique de
l'Université de Strasbourgfortheirfinancialsupport.

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797 Table 1: Minimum, mean, and maximum radii of pore bodies and pore throats derived from

the sphere-packing model.

	minimum (r _{min})		0.042	
Pore-body radius [mm]	mean(r _{mean})		0.048	
	maximum (r _{max})		0.054	
		r _{max} -r _{mean} =sd	r _{max} -r _{mean} =2 sd	r _{max} -r _{mean} =3 sd
	minimum (r _{min})	0.026	0.022	0.018
Pore-throat radius [mm]	$mean\left(r_{mean} \right)$	0.030	0.030	0.030
	$maximum \left(r_{max} \right)$	0.034	0.038	0.042

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801 Figure captions

Fig. 1: Flow chart of the pore-scale network model. The time-stepping process is repeated until
a stopping condition is (dynamically) reached, or when equilibrium state is achieved, i.e., all
the interfaces are blocked.

Fig. 2: Experimental and modelled WRC of the quartz sand used in the laboratory experiments.

806 Simulations with a 3D lattice network $(20 \times 20 \times 200)$ and 3 different pore throat radii 807 distributions. The capillary pressure value is expressed as equivalent water head (m H₂O).

808 Fig. 3: Experimental and modelled WRC of the quartz sand used in the laboratory experiments.

Simulations with a 2D lattice network with 3 different sizes $(50 \times 50, 75 \times 75, \text{ and } 100 \times 100)$ and

810 a given pore-throat radii distribution (r_{max} - r_{mean} =1sd). The capillary pressure value is expressed

- 811 as equivalent water head (m H₂O).
- 812 Fig. 4: Measured and simulated dimensionless arrival times of the water/DNAPL front using a

813 3D lattice network (7×7×4858) in both vertical-upward flow mode and downward flow mode:

- 814 The case of drainage of water-saturated medium sand at low DNAPL injection flow rate
- 815 (Q= 29.6×10^{-4} mL/min). t_{mean} is the average arrival time of the DNAPL front.
- 816 Fig. 5: The 3D view of the simulated DNAPL saturation field for vertical-downward drainage
- 817 of saturated medium-sized sand at low DNAPL injection flow rate using a 3D lattice network

818 $(7 \times 7 \times 4858 \text{ nodes})$: (a) near the inlet, between z=0 cm and z=-1.5 cm; (b) in the middle of the 819 soil column, between z= -34 cm and z=-35.5 cm; and (c) near the outlet, between z= -66.5 cm 820 and z=-68 cm.

Fig. 6: Measured and simulated saturation as a function of depth at the end of the experiment using a 3D lattice network (20×20×200) with 3 different pore throat radius distributions: (a) in the case of vertical-upward drainage of water-saturated medium sand at low DNAPL injection flow rate and (b)in the case of vertical-downward drainage of water-saturated medium sand at low DNAPL injection flow rate.

Fig. 7: Effect of the size of the cross-section (6×6 , 12×12 , and 24×24) on the simulated DNAPL saturation field and cross-section averaged DNAPL saturation profile: in the case of verticaldownward drainage of saturated medium-sized sand at low DNAPL injection flow rate (Q= 29.6×10^{-4} mL/min), after 8 sec of DNAPL injection.

Fig. 8: Measured and simulated inlet DNAPL pressure as a function of time using a 3D network (7×7×4858): (a) in the case of vertical-upward drainage of water-saturated medium sand at low DNAPL injection flow rate and (b) in the case of vertical-downward drainage of water-saturated medium sand at low DNAPL injection flow rate (Q= 29.6×10^{-4} mL/min).

Fig. 9: Measured and simulated dimensionless arrival times of the water/DNAPL front in medium sand. The case of vertical-downward drainage of water-saturated medium sand at high DNAPL injection flow rate ($Q=59.2 \times 10^{-4}$ mL/min).t_{mean} is the average arrival time of the DNAPL front

Fig. 10: Measured and predicted DNAPL saturation as a function of depth at the end of the experiment using a 3D lattice network ($20 \times 20 \times 200$) with 3 different pore throat radius distributions. The case of vertical-downward drainage of water-saturated medium sand at high DNAPL injection flow rate (Q=59.2×10⁻⁴ mL/min).

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