



HAL
open science

Experimental Phase Function and Degree of Linear Polarization Curves of Millimeter- sized Cosmic Dust Analogs

Olga Muñoz, Fernando Moreno, J.C. Gómez-Martín, Fernando Vargas-Martin, Daniel Guirado, J. L. Ramos, I. Bustamante, Ivano Bertini, E. Frattin, J. Markannen, et al.

► **To cite this version:**

Olga Muñoz, Fernando Moreno, J.C. Gómez-Martín, Fernando Vargas-Martin, Daniel Guirado, et al.. Experimental Phase Function and Degree of Linear Polarization Curves of Millimeter- sized Cosmic Dust Analogs. *The Astrophysical Journal Supplement*, 2020, 247 (March), pp.19. 10.3847/1538-4365/ab6851 . insu-02434855

HAL Id: insu-02434855

<https://insu.hal.science/insu-02434855v1>

Submitted on 25 Feb 2020

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



Experimental Phase Function and Degree of Linear Polarization Curves of Millimeter-sized Cosmic Dust Analogs

O. Muñoz¹, F. Moreno¹, J. C. Gómez-Martín¹, F. Vargas-Martín², D. Guirado¹, J. L. Ramos¹, I. Bustamante¹, I. Bertini³, E. Frattin³, J. Markannen⁴, C. Tubiana⁴, M. Fulle⁵, C. Güttler⁴, H. Sierks⁴, A. Rotundi⁶, V. Della Corte⁶, S. Ivanovski⁶, V. V. Zakharov^{6,7}, D. Bockelée-Morvan⁷, J. Blum⁸, S. Merouane⁴, A. C. Levasseur-Regourd⁹, L. Kolokolova¹⁰, T. Jardiel¹¹, and A. C. Caballero¹¹

¹Instituto de Astrofísica de Andalucía, CSIC, Glorieta de la Astronomía s/n, E-18008 Granada, Spain

²Department of Electromagnetism and Electronics, University of Murcia, E-30100 Murcia, Spain

³Department of Physics and Astronomy “G. Galilei,” University of Padova, Vicolo dell’Osservatorio 3, I-35122 Padova, Italy

⁴Max-Planck-Institut für Sonnensystemforschung, Justus-von-Liebig-Weg, 3, D-37077 Göttingen, Germany

⁵Osservatorio Astronomico, Via Tiepolo 11, I-34143 Trieste, Italy

⁶INAF-Istituto di Astrofisica e Planetologia Spaziali, Via Fosso del Cavaliere, 100, I-00133 Rome, Italy

⁷LESIA, Observatoire de Paris, Université PSL, CNRS, Sorbonne Université, Université de Paris, 5 place Jules Janssen, F-92195 Meudon, France

⁸Institut für Geophysik und extraterrestrische Physik, Technische Universität Braunschweig, Mendelssohnstr. 3, D-38106 Braunschweig, Germany

⁹CNRS, LATMOS, Sorbonne Université 4, place Jussie F-75252 Paris Cedex 05, France

¹⁰Department of Astronomy, University of Maryland, College Park, MD 20742-2421, USA

¹¹Instituto de Cerámica y Vidrio, CSIC, C/Kelsen 5, Campus Cantoblanco, E-28049 Madrid, Spain

Received 2019 November 13; revised 2019 December 19; accepted 2020 January 5; published 2020 February 24

Abstract

We present laboratory measurements of the phase functions and degree of linear polarization (DLP) curves of a selection of millimeter-sized cosmic dust analog particles. The set includes particles with similar sizes but diverse internal structure (compact and porous) and absorbing properties. The measured phase functions are found to be in all cases very different from those of micron-sized particles. They show a monotonic decrease with increasing phase angle from the back- to the side-scattering region, reaching a minimum at large phase angles before a steep increase of the forward peak. This is in stark contrast to the phase functions of micron-sized particles, which are rather flat at low and intermediate phase angles. The maximum of the DLP for millimeter-sized compact particles is shifted toward larger phase angles ($\sim 130^\circ$) compared to that of micron-sized particles ($\sim 90^\circ$). Porosity plays an important role in the measured DLP curves: the maximum significantly decreases for increasing porosity as a result of multiple scattering within the particle. Large porous particles with highly absorbing inclusions can reproduce both the OSIRIS/Rosetta phase functions and ground-based DLP observations of comet 67P/Churyumov–Gerasimenko.

Unified Astronomy Thesaurus concepts: [Circumstellar dust \(236\)](#); [Polarimetry \(1278\)](#); [Circumstellar disks \(235\)](#); [Debris disks \(363\)](#); [Comets \(280\)](#); [Experimental techniques \(2078\)](#); [Protoplanetary disks \(1300\)](#)

1. Introduction

The angular dependence of the brightness and degree of linear polarization (DLP) of stellar light scattered by cosmic dust clouds results primarily from the size, shape, and composition of the dust. Therefore, these physical properties may be retrieved from the analysis of photopolarimetric observations of the light scattered by clouds in different environments, such as circumstellar regions around young and evolved stars (Canovas et al. 2015; Milli et al. 2017; Ren et al. 2019), or planetary (McLean et al. 2017) and cometary atmospheres (Bertini et al. 2017; Rosenbush et al. 2017).

Computational characterization of irregular cosmic dust particles from the observed scattered light remains an extremely difficult task owing to their complicated morphology. Computations usually rely on simplified model particles and are constrained to limited size ranges (see, e.g., Min et al. 2003; Moreno et al. 2007; Merikallio et al. 2015; Pohl et al. 2016; Zubko et al. 2016; Escobar-Cerezo et al. 2017; Kolokolova et al. 2018). Thus, experimental scattering patterns

of cosmic dust analogs of representative sizes, shapes, and compositions are a highly valuable alternative for interpreting astronomical observations.

Over the past 10 yr the IAA Cosmic Dust Laboratory (CoDuLab; Muñoz et al. 2010, 2011) has produced an important number of high-quality experimental phase functions and DLPs for clouds of randomly oriented cosmic dust analogs with radii ranging from submicron to up to $100 \mu\text{m}$. The data are available in digital form in the Amsterdam–Granada light scattering database (www.iaa.es/scattering; Muñoz et al. 2012). However, the millimeter size range is still poorly studied. Dense clouds of millimeter-sized particles have been inferred in the so-called dust traps in the outer regions of young protoplanetary disks (van der Marel 2013; Casassus et al. 2015; Canovas et al. 2016; Walsh et al. 2016). It is in these regions where the initial phases of planet formation are believed to take place (see, e.g., Pinilla et al. 2012; Testi et al. 2014). The millimeter-sized regime seems to be of particular importance in protoplanetary disks, because it marks the end of the very efficient hit-and-stick regime (Zsom et al. 2010; Lorek et al. 2018).

Dust particles in the millimeter-sized range have also been detected in comet 67P/Churyumov–Gerasimenko (hereafter 67P), target of the European Space Agency *Rosetta* mission.

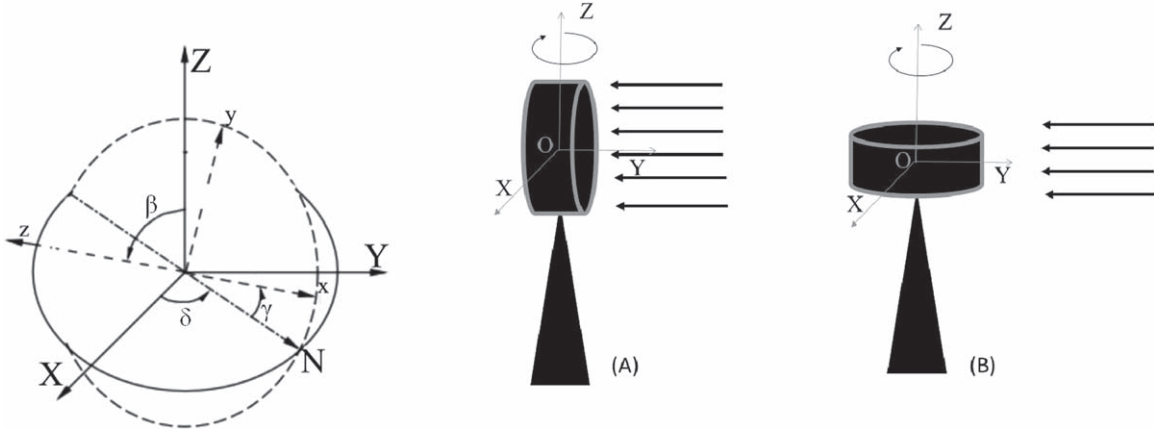


Figure 2. Left panel: laboratory, XYZ, and auxiliary, xyz, reference frames. Right panel: (A) particle in its initial position on the holder; (B) particle after a rotation of $\beta = 90^\circ$. $Oxyz$ defines the laboratory reference frame. In both cases each orientation of the particle corresponds to a rotation around Z.

orientation, p , of the particle under study. The measurements cover the scattering angle range from 10° to 170° . In general, F^p contains 16 nonvanishing elements (see, e.g., Hovenier et al. 2004):

$$F^p = \begin{pmatrix} F_{11}^p & F_{12}^p & F_{13}^p & F_{14}^p \\ F_{21}^p & F_{22}^p & F_{23}^p & F_{24}^p \\ F_{31}^p & F_{32}^p & F_{33}^p & F_{34}^p \\ F_{41}^p & F_{42}^p & F_{43}^p & F_{44}^p \end{pmatrix}. \quad (1)$$

The elements of F^p are dimensionless and depend on the physical properties of the particle (shape, porosity, size, and refractive index) and the direction of scattering, i.e., the direction from the particle to the detector. The direction of scattering is defined by the scattering angle, θ , the angle between the directions of propagation of the incident and the scattered beams with $0 \leq \theta \leq \pi$, and an azimuth angle, ϕ , that ranges from 0 to 2π . The scattering angle is related to the phase angle, α , as $\alpha = 180^\circ - \theta$.

In the case of a particle in random orientation, all scattering planes are equivalent. Thus, the scattering direction is fully described by the scattering angle θ . Further, for a homogeneous sphere the scattering matrix has only four independent elements that are not equal to zero. In that case $F_{xy}^p = F_{yx}^p$ and the scattering matrix, F , takes the form

$$F = \begin{pmatrix} F_{11} & F_{12} & 0 & 0 \\ F_{12} & F_{11} & 0 & 0 \\ 0 & 0 & F_{33} & F_{34} \\ 0 & 0 & -F_{34} & F_{33} \end{pmatrix}. \quad (2)$$

For unpolarized incident light the first element of the scattering matrix, $F_{11}(\theta)$, is proportional to the flux of the scattered light and is called the phase function. The $-(F_{12}(\theta)/F_{11}(\theta))$ ratio is, for incident unpolarized light, equal to the DLP.

In this work we only present measurements of $F_{11}(\theta)$ and $-(F_{12}(\theta)/F_{11}(\theta))$ curves of our cosmic dust analogs. The measurement procedure with particles in random orientation conditions is as follows: The detector is moved along the ring in steps of 1° or 5° , covering the phase angle range from 10° to 170° . For each data point at a given phase angle, 800 measurements are conducted in about 1 s. Thus, one data point is an average of 800 distinct measurements. The error of

one data point is the standard deviation of the series of 800 measurements. During the measurements, the particle is located on the rotating conical holder as shown in the right panel of Figure 2. To simulate random orientation, the $F_{xy}(\theta)$ is the result of averaging over 54 $F_{xy}^p(\theta)$, corresponding to 54 different orientations. First, the particle is located with its longest axis aligned with the holder (Figure 2, (A)). Starting with a given orientation, the $F_{11}^p(\theta)$ and $-(F_{12}(\theta)/F_{11}(\theta))^p$ are measured after each of 36 successive rotations in steps of 10° around the vertical axis (Z). Second, the position of the particle is rotated 90° toward the direction of the laser beam (Figure 2, (B)). Again, starting from that position, the scattering pattern of the particle is measured in each of 18 successive rotations in steps of 20° around the Z-axis. According to Mischenko & Yurkin (2017), a rigorous 3D orientation average could be obtained by a sufficient number of Euler rotations (Figure 2, left panel): (i) rotation around the vertical axis (δ), (ii) rotation around the x-axis (β), and (iii) rotation around the axis perpendicular to the base of the particle (γ), with δ and γ uniformly distributed, while β ought to follow a distribution proportional to $\sin(\beta)$. Such a procedure would involve a mechanical holder with two degrees of freedom, which would interfere with the intrinsic scattering pattern of the grain much more than the vertical stand we use in our experimental setup. Moreover, the realization of so many measurements would take up an inordinate time of experimental work. Instead, our procedure is a simplified implementation of the rigorous recipe in the particular case of only one value of $\beta = 90^\circ$. As β must follow a $\sin(\beta)$ distribution (Mischenko & Yurkin 2017), this is the most convenient single rotation around the laser direction in order to optimize the average. Strictly speaking, a complete 3D random orientation average was not properly calculated, but our experimental procedure is a practical optimal compromise between a rigorous calculation and a feasible experimental practice.

3. Test Measurements

The performance of the new optical train and holder is tested by comparing the measured phase function, $F_{11}(\alpha)$, and DLP, $-(F_{12}(\alpha)/F_{11}(\alpha))$, of a calibration sphere to results of Lorenz-Mie calculations for the corresponding size and refractive index. Physical properties of the N-BK7 glass spheres (Edmund Optics) are presented in Table 1. The size of the

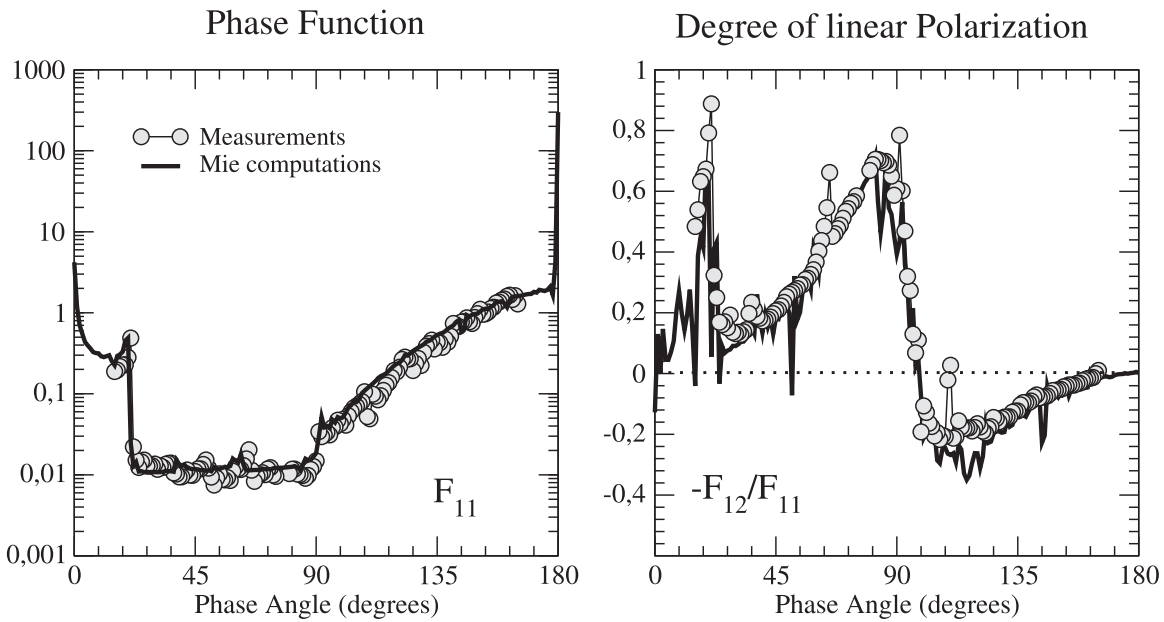


Figure 3. Comparison of measured (gray symbols) and computed (black lines) F_{11} and $-F_{12}/F_{11}$ curves for the N-BK7 calibration sphere. All F_{11} curves are normalized to unity at 150° .

Table 1
Properties of the Calibration Spheres and Cosmic Dust Particles

Composition	Diameter (mm)	$m = n+ki$ (520 nm)	Reference
N-BK7	5.0	$n = 1.5168, k = 9 \times 10^{-9}$	Edmund Optics Catalog
Charcoal	4.3 ^a	$n = [1.8-2.3], k = [0.5-0.9]$	Duley (1984)
Quartzite	3.2 ^a	$n = 1.58, k = 2 \times 10^{-5}$	Dorschner et al. (1995)
MgFeAlSi	5.45 ^a	$n = [1.6-1.7], k = [0.002-0.03]$	Jäger et al. (1994)
Cotton	5.0 ^a	...	

Note.

^a Diameter of the volume-equivalent sphere.

calibration sphere has been chosen similar to that of our particles of interest.

In Figure 3, we present the measured and calculated phase functions and DLP curves for the N-BK7 calibration sphere. The measured and calculated $F_{11}(\alpha)$ are normalized to 1 at 150° . During the test measurements, the detector is moved along the ring in steps of 1° . The plotted values corresponding to Lorenz–Mie calculations are averaged over $\pm 0.25^\circ$ according to the angular resolution of the experimental setup. As shown in Figure 3, the measured phase function and DLP as functions of the phase angle agree with the Lorenz–Mie computations over the entire angle range. Small differences might be caused by small inhomogeneities in the calibration sphere. Moreover, the measurements are strongly dependent on the exact position of the calibration sphere at the center of the measuring ring.

4. Sample Description

In this work we study three millimeter-sized compact particles consisting of charcoal (vegetable origin), Mg–Fe aluminosilicate (MgFeAlSi), and quartzite, respectively. Further, we study two highly porous particles consisting of a white cotton ball and a white cotton ball with charcoal submicron inclusions. In Figure 4 we present optical images of

the three compact dust particles. The physical properties of all studied particles are summarized in Table 1.

The charcoal particle has been artificially caved out of a piece of vegetable charcoal. First, the charcoal is cut rough to a flake-like shape. Second, the rough flake is gently sanded to produce macroscopically smooth surfaces with rounded edges (Figure 4(a)). By softening the particle shape, we can focus our study on the effect of absorption on the measured scattering matrix elements. In spite of the sanding process, at microscopic scale we can still distinguish the tubular wall cell structure (Figure 5) that evolves into a porous mosaic texture as we approach the particle edges (Figure 6). Charcoal is a highly absorbing material. Based on literature values (Duley 1984; Papoular et al. 1993; Stagg & Charalampopoulos 1993), we can assume that at visible wavelengths the real part of the refractive index lies between 1.8 and 2.3, while the imaginary part lies in the range of 0.5–0.9.

The Mg–Fe aluminosilicate (MgFeAlSi) particle is a natural stone that presents an ellipsoidal shape with surface roughness (Figure 4(b)). As shown in the scanning electron microscope (SEM) images (Figure 7), surface structures are of the order of a few micrometers. According to the experimental study presented by Mutschke et al. (1998), the UV/VIS/IR spectra of Mg–Fe aluminosilicate are determined by the iron ions, with no finding of any significant effect on the aluminum

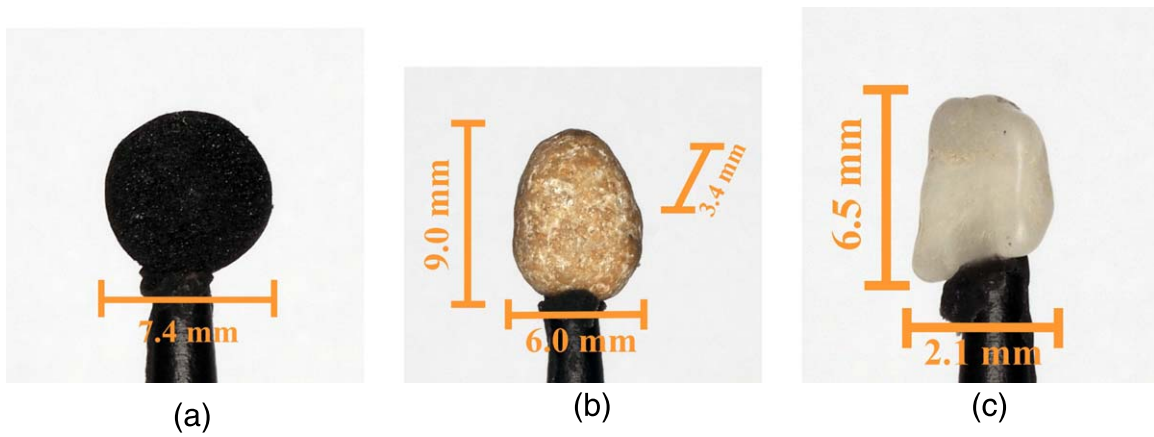


Figure 4. Optical images of (a) charcoal, (b) MgFeAlSi, and (c) quartzite particles.

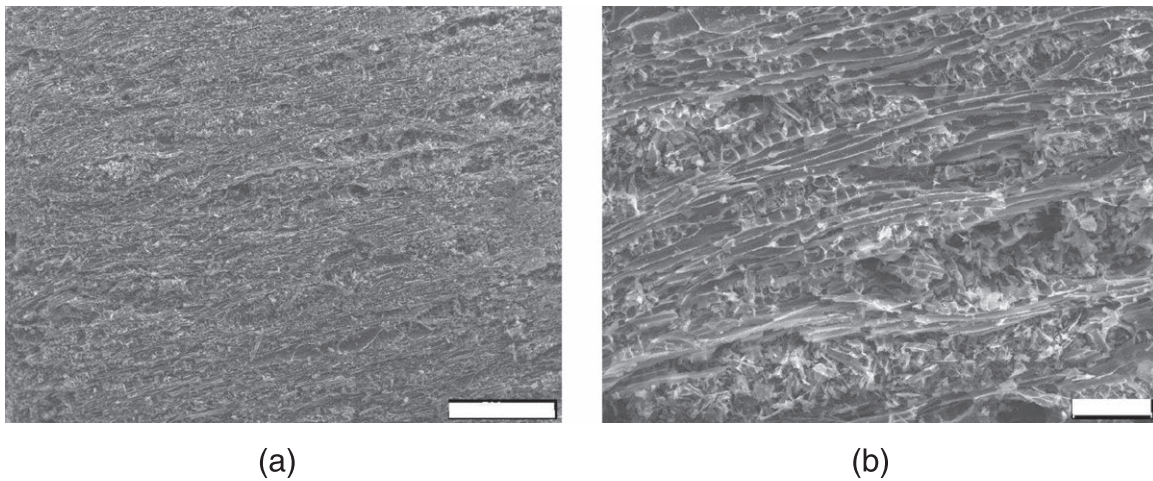


Figure 5. SEM images of the charcoal particle, central region. White bars denote (a) 500 μm and (b) 100 μm .

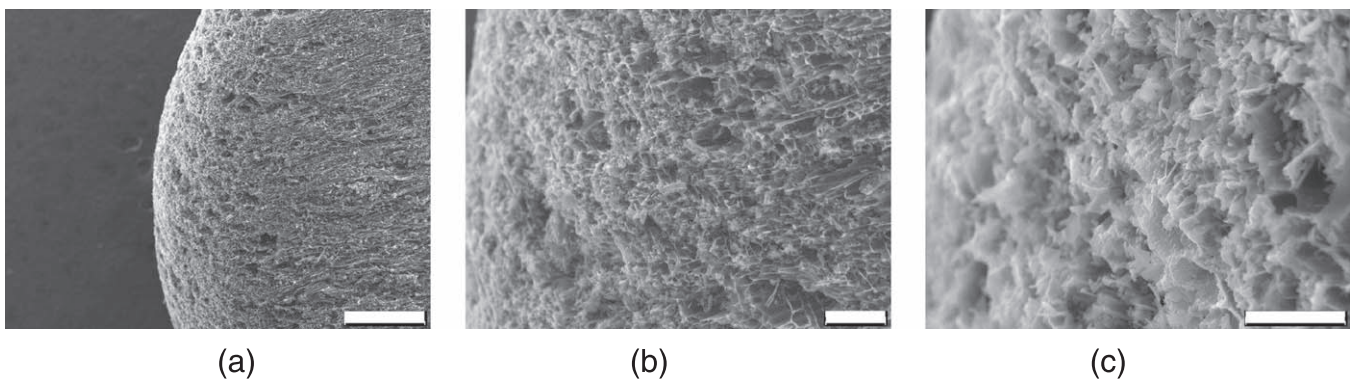


Figure 6. SEM images of the charcoal particle, border region. White bars denote (a) 500 μm , (b) 100 μm , and (c) 50 μm .

content. Based on the data presented by Mutschke et al. (1998) and Jäger et al. (1994), we estimate the refractive index of the MgFeAlSi at 520 nm to be in the range $n = [1.6-1.7]$, $k = [0.002-0.03]$. Therefore, it can be taken as a good representative example for moderate absorbing particles.

The quartzite particle shows a rectangular-prism shape with naturally polished surfaces (Figure 4(c)). In Figure 8, we present SEM images for the quartzite particle. At microscopic scale we can hardly distinguish any surface roughness. Quartzite is a low absorbing material with a nearly zero imaginary part of the refractive index at visible wavelengths.

As in the case of the charcoal chunk, the lack of surface roughness allows us to focus on the effect of absorption on the measured scattering matrix elements.

The three particles described above present a compact internal structure. To study the effect of porosity on the measured scattering matrix elements, we also study the scattering pattern of a millimeter-sized cotton ball. Further, to study the effect of absorption on the measured scattering matrix elements, the white cotton ball has been doped with submicron-sized charcoal inclusions. In Figure 9, we present SEM images of the highly porous cotton ball. Keeping in mind that our porous particle

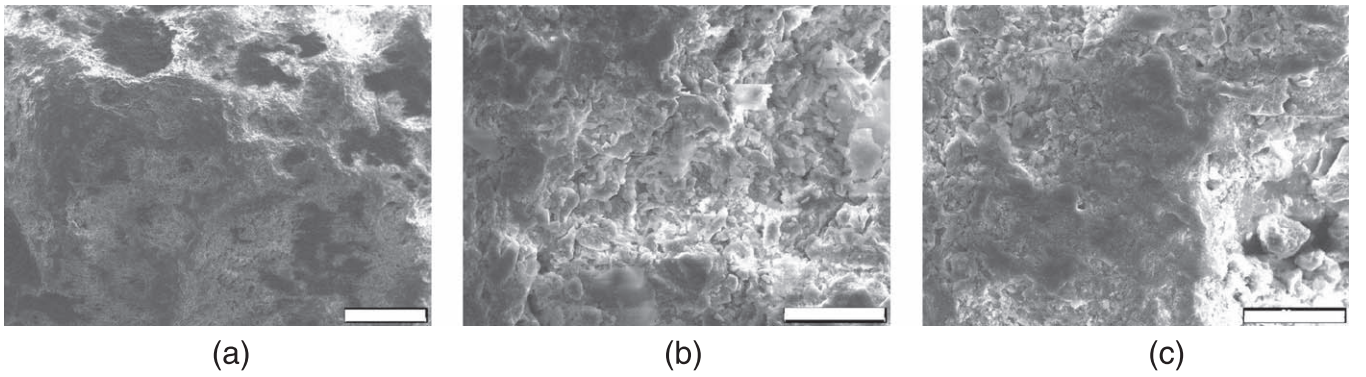


Figure 7. SEM images of the MgFeAlSi grain. White bars denote (a) 500 μm and (b, c) 50 μm .

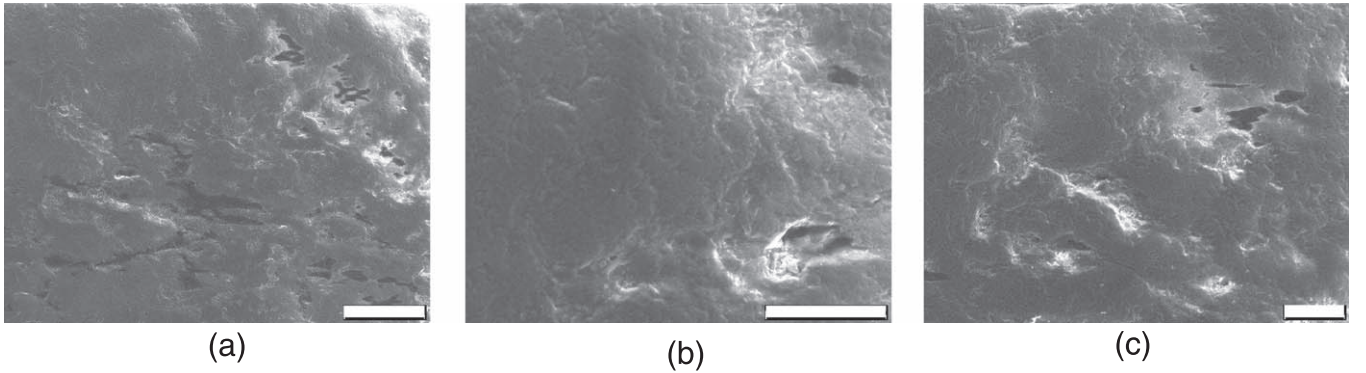


Figure 8. SEM images of the quartzite grain. White bars denote (a) 500 μm and (b, c) 100 μm .

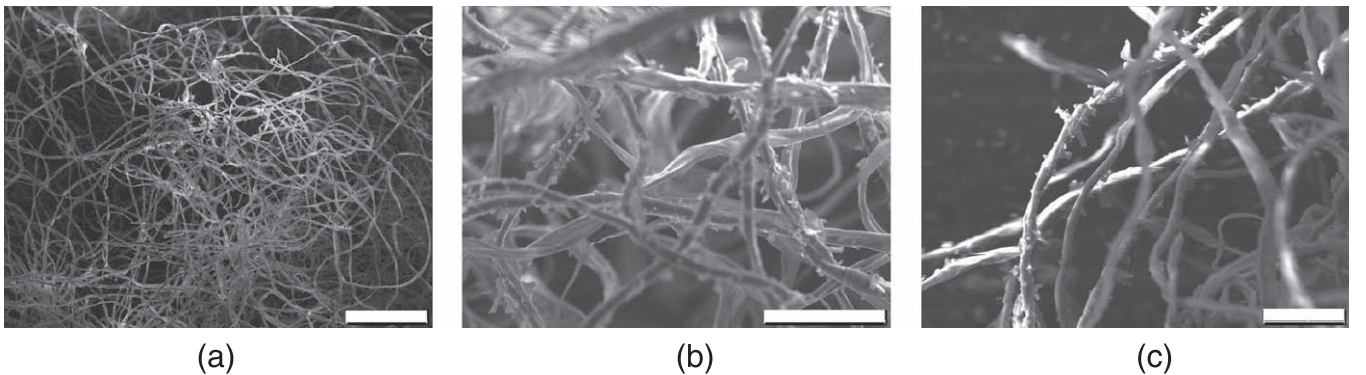


Figure 9. SEM images of the dirty cotton ball grain. White bars denote (a) 500 μm and (b, c) 100 μm . Small particles covering the cotton fibers correspond to the charcoal inclusions.

cannot be strictly considered as a cosmic dust analog, it is fully relevant and useful to study how porosity may affect the measured scattering matrix elements. Large porous particles seem to be a good optical model for, e.g., the dust orbiting Fomalhaut (Acke et al. 2012). Large particles are needed for reproducing the observed phase function at side- and back-scattering regions in such environments (Min et al. 2010). In addition, they should present a porous structure to explain the far-infrared images.

In summary, we have selected samples corresponding to the two extreme cases as far as internal structure of the particles is concerned, i.e., compact particles (charcoal, Mg–Fe aluminosilicate, and quartzite) with different absorbing properties and a highly porous particle (cotton ball) with and without sub-micron-sized charcoal inclusions. In this way we can study not only the effect of absorption but also that of porosity on the measured phase functions and DLP of millimeter-sized

particles. All particles present similar sizes to the N-BK7 sphere used to test the experimental apparatus. In this way we ensure a homogeneous illumination over the entire particle.

5. Measurements

In Figure 10 we present the measured phase function, $F_{11}(\theta)$, and DLP ($-F_{12}(\theta)/F_{11}(\theta)$) curves for the charcoal, Mg–Fe aluminosilicate, and quartzite particles in random orientation. As explained in Section 2, to simulate random orientation, the plotted F_{11} and $-F_{12}/F_{11}$ curves are results of averaging F_{11}^p and $-(F_{12})^p$ over 54 different orientations. In the context of single irregular particle measurements, each orientation would be equivalent to a different particle shape. It is known that any particle shape produces a unique, shape-specific scattering pattern (e.g., Mishchenko et al. 1997), whereas experimental measurements with samples consisting of natural dust particles

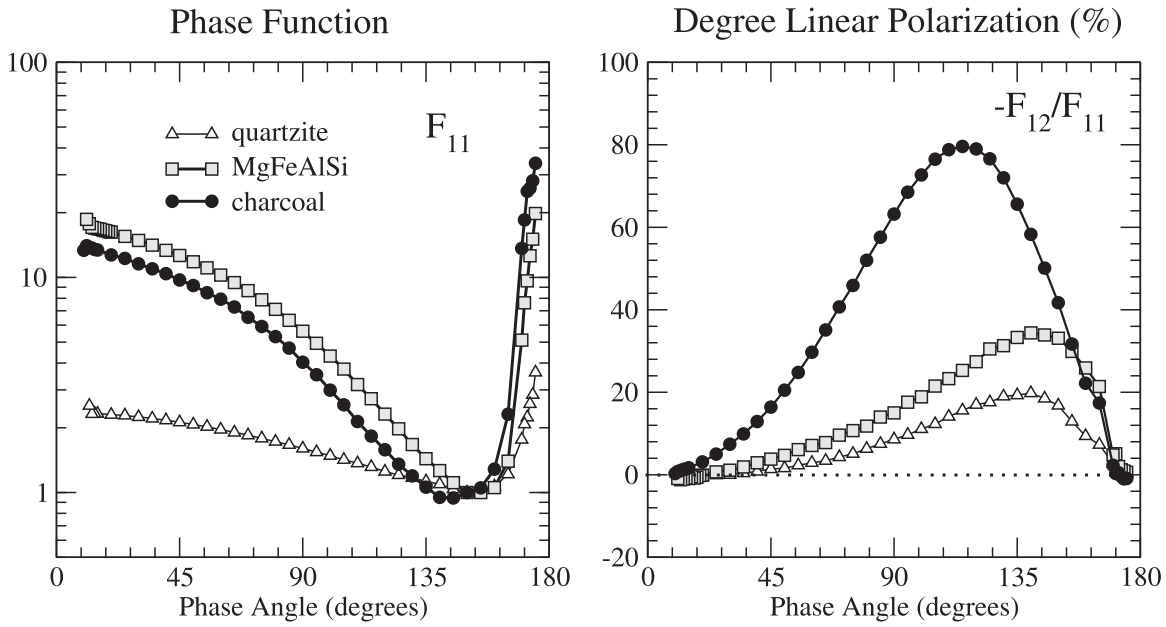


Figure 10. Experimental phase functions ($F_{11}(\theta)$) and DLP ($-F_{12}(\theta)/F_{11}(\theta)$) curves at 520 nm for charcoal (filled circles), MgFeAlSi (filled squares), and quartzite (triangles). All F_{11} curves are normalized to unity at 150°.

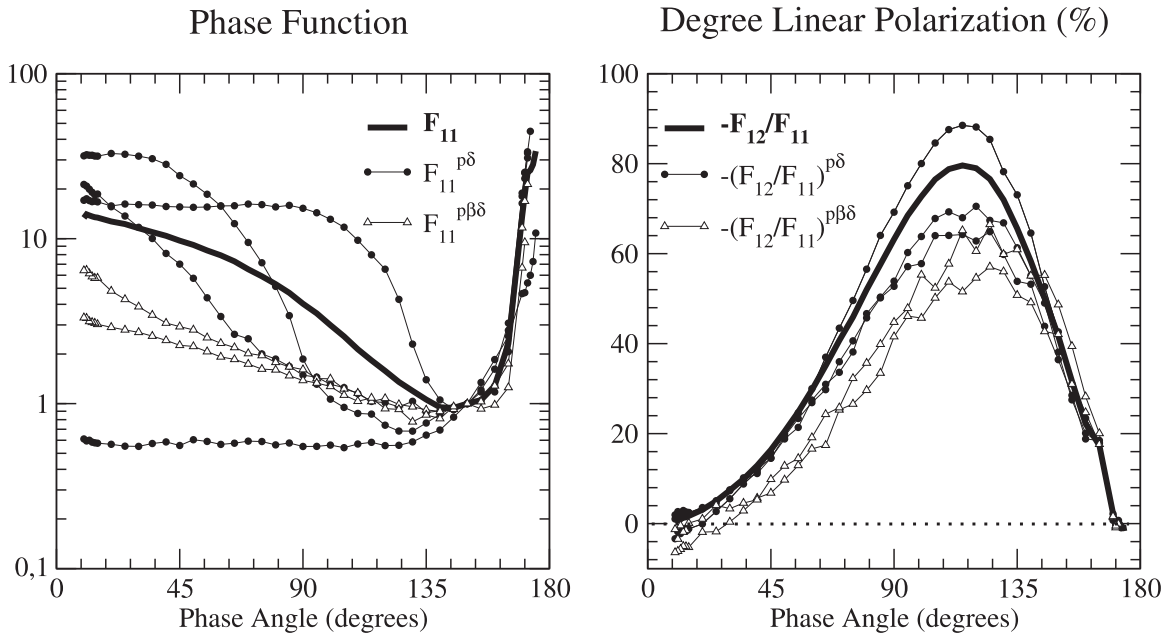


Figure 11. Measured phase function, F_{11}^p , and DLP curves, $-(F_{12}/F_{11})^p$, for different orientations (p) of the charcoal particle around δ (small filled circles). Small open triangles correspond to different orientations (p) of the charcoal particle around δ after a rotation of the particle on the holder $\beta = 90^\circ$. The measured curves are presented with their error bars. In cases in which no error bars are shown, they are smaller than the symbol. Corresponding averaged F_{11} and $-(F_{12}/F_{11})$ are represented with thick solid lines. The averaged values are based on all 54 measured orientations. All F_{11} curves are normalized to unity at 150°.

in random orientation show smooth featureless patterns (e.g., Weiss-Wrana 1983; West et al. 1997, or any of the measurements presented in the Amsterdam–Granada light-scattering database, www.iaa.es/scattering). That is also the case for the measurements presented in this work. As an example, Figure 11 illustrates the effect of rotation on the measured phase function and DLP curves for the charcoal particle. Measured F_{11}^p and $-(F_{12}/F_{11})^p$ curves corresponding to a set of selected orientations for the charcoal grain are presented together with the averaged values based on the 54 measured orientations. For simplicity, we only show measurements corresponding to six orientations. The F_{11}^p and

$-(F_{12}/F_{11})^p$ curves are presented with their error bars. In cases in which no error bars are shown, they are smaller than the symbol. Figure 11 shows the high dispersion of results for each of the individual orientations.

Figure 12 shows the measured F_{11}^p and $-(F_{12}/F_{11})^p$ curves for two millimeter-sized porous balls in a fixed position. From this point the cotton ball doped with charcoal inclusions is referred to as dirty. Both balls present a diameter of approximately 5 mm. The effect of flattening the dirty ball into an ellipsoidal-like shape is presented in Figure 13. In this case, the porous ellipsoidal particle has been placed with its largest projected surface facing the laser beam. From this initial

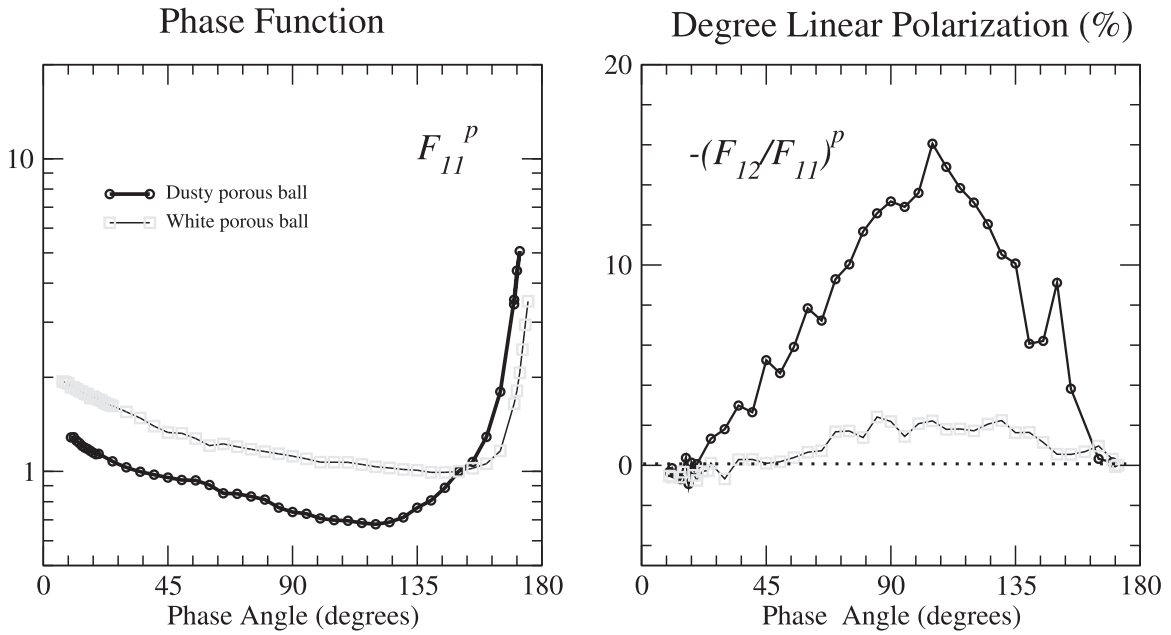


Figure 12. Measured phase function, F_{11}^p , and DLP (in percentage) curves, $-(F_{12}/F_{11})^p$, for white (gray symbols) and dirty (black symbols) highly porous balls in a fixed position. The dirty ball has been doped with submicron charcoal particles. The measured curves are presented with their error bars. In cases in which no error bars are shown, they are smaller than the symbol. The F_{11} curves are normalized to unity at 150° .

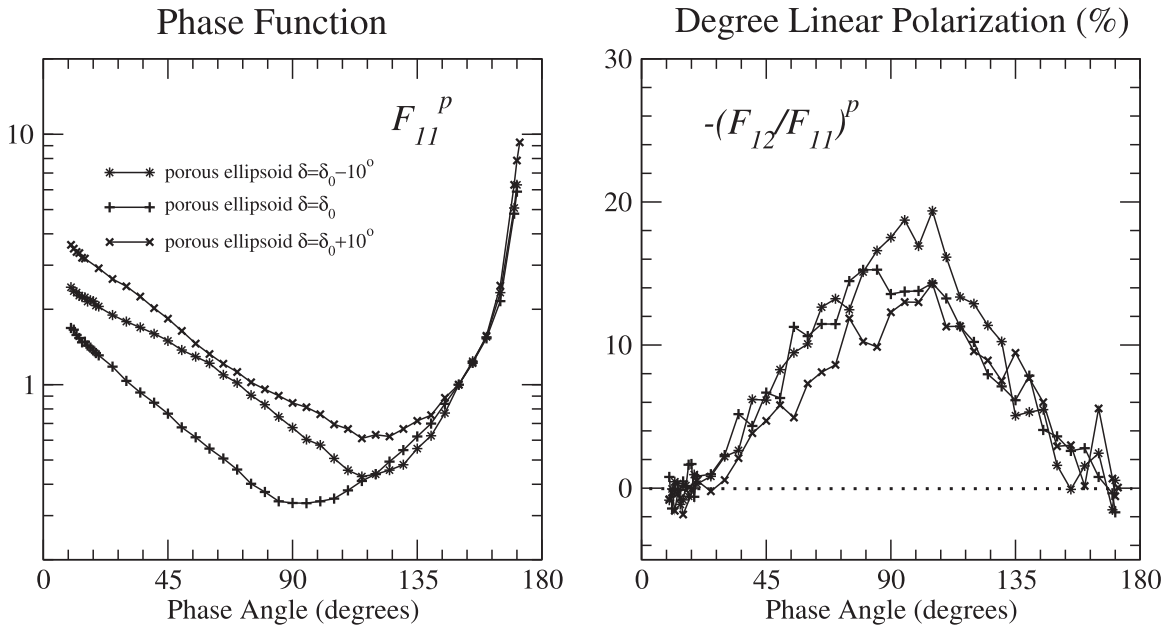


Figure 13. Measured phase function, F_{11}^p , and DLP (in percentage) curves, $-(F_{12}/F_{11})^p$, for a dirty highly porous ellipsoidal particle at three different orientations, p . The measured curves are presented with their error bars. In cases in which no error bars are shown, they are smaller than the symbol. The F_{11} curves are normalized to unity at 150° .

position (δ_0) the holder is rotated to $\delta_0 + 10^\circ$ and $\delta_0 - 10^\circ$. The displacement of the minimum of the phase function toward larger phase angles for the cases $\delta_0 + 10^\circ$ and $\delta_0 - 10^\circ$ with respect to the δ_0 position is remarkable, as discussed in Section 7.

6. Discussion

As shown in the left panels of Figures 10 and 12, the measured phase functions of both compact and porous millimeter-sized particles show two well-defined regions: strong forward lobes in the 150° to $\sim 170^\circ$ phase angle range

and an increase with decreasing phase angle from $\sim 140^\circ$ – 130° to 10° . For the size of our dust particles and distance to the detector, the angular width of the diffraction peaks is approximately $\pm 0.8^\circ$ around the exact forward direction, which is outside the accessible range in our experiment. It is interesting to note that the slope of the phase function in the 150° – 10° angle range is larger for the two absorbing millimeter-sized compact particles with soft or moderate surface roughness, i.e., charcoal and MgFeAlSi particles. The behavior of the low absorbing millimeter-sized quartzite particle is similar to that found in Muñoz et al. (2017) for millimeter-sized quartz and enstatite particles with similar

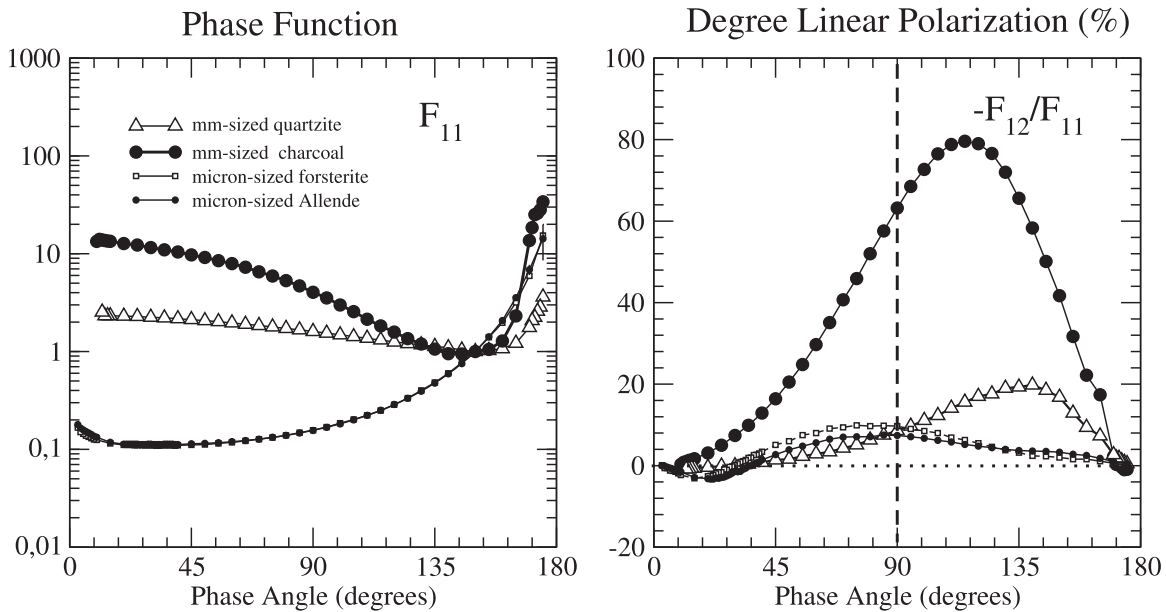


Figure 14. Measured phase functions, F_{11} , and DLP (in percentage) curves for the low absorbing millimeter-sized (quartzite) particles (open triangles), highly absorbing millimeter-sized (charcoal) particles (black circles), and two micron-sized samples, forsterite (small open squares) and the Allende meteorite (small black circles). The measured curves are presented with their error bars. In cases in which no error bars are shown, they are smaller than the symbol. All F_{11} curves are normalized to unity at 150° . All measurements are performed at 520 nm.

refractive indices. However, in Muñoz et al. (2017) the slope of the $F_{11}(\theta)$ of the Etna particle (moderately absorbing) is significantly smaller than those of the charcoal and FeMgAlSi particles. We must note that the Etna particle presents the typical vesicular structure of volcanic particles. Thus, the incident light is multiple scattered on the crater surface, decreasing the reflected component of the scattered light.

The behavior of the phase function at side- and back-scattering regions is typical of particles significantly larger than the wavelength of the incident light (Muñoz et al. 2017). In contrast, the phase functions of clouds of micron-sized (compact and porous) particles in random orientation present a nearly flat dependence with the phase angle at side- and backward-scattering regions (Muñoz et al. 2012). Illustrative examples are shown in the left panel of Figure 14: Allende and forsterite samples consisting of compact particles (Frattin et al. 2019). The Allende sample corresponds to a ground piece of the Allende meteorite, a carbonaceous chondrite, class CV, type III. Its refractive index at the measured wavelength, 520 nm, is estimated to be of the order of $m \approx 1.7 + i0.02$ (Zubko et al. 2015), which is reasonably close to the refractive index of the MgFeAlSi particle (Table 1). The effective radius, r_{eff} , and variance, v_{eff} (as defined by Hansen & Travis 1974), of the samples used by Frattin et al. (2019) are equal to 2.44 and 3.42 μm , respectively. The forsterite sample presents a similar size distribution ($r_{\text{eff}} = 3.06 \mu\text{m}$, $v_{\text{eff}} = 1.04$) but different absorbing properties. The refractive index of forsterite is $m = 1.65 + 0.0005i$ (Dorschner et al. 1995), i.e., it is a low absorbing material. In both cases the measured phase functions show strong forward peaks, a decrease at side-phase angles showing a nearly flat dependence in the phase angle range from 3° to 90° . Similar characteristics are observed for clouds of randomly oriented micron-sized porous particles (Volten et al. 2007).

In Figure 15, the measured phase functions of the white and dirty cotton balls are plotted together with the experimental phase functions for two samples consisting of micron-sized

fluffy magnesiosilica aggregates. The latter were synthesized in a condensation flow apparatus (CFL) with the purpose of mimicking the formation of circumstellar dust (Volten et al. 2007). The experimental $F_{11}(\theta)$ curves for the two samples consisting of micron-sized porous particles show a flat dependence with the phase angle in the backward hemisphere. By contrast, the $F_{11}(\theta)$ curves of millimeter-sized porous particles increase with decreasing phase angle in the side- and back-scattering regions. Therefore, brightness observations of the light scattered by cosmic dust clouds covering a broad angle range could be a good diagnostic tool for discriminating the dominant size of the particles populating the cloud.

The measured DLP curves of large compact particles (Figure 10, right panel) show the typical bell shape for irregular particles. The maximum of the DLP curves, DLP_{max} , is strongly dependent on the value of the imaginary part of the refractive index, showing significantly higher values for the highly absorbing charcoal particle ($\text{DLP}_{\text{max}} \approx 80\%$) than for the low absorbing quartzite particle ($\text{DLP}_{\text{max}} \approx 20\%$). The DLP_{max} for the moderately absorbing MgFeAlSi particle is located within the range of the quartzite and charcoal measurements. The maxima are placed in the 115° – 140° phase angle range, i.e., it is shifted toward larger phase angles than in the case of clouds of micron-sized compact particles (Muñoz & Hovenier 2015). In the right panel of Figure 14, the measured DLP(θ) for millimeter-sized particles is compared to those measured for the two aforementioned micron-sized cosmic dust analogs (Frattin et al. 2019). In the latter the maximum DLP is located in the 75° – 85° phase angle range. The shift of the position of the DLP_{max} with size for compact particles is consistent with previous computations of the scattering matrix for Gaussian random spheres covering sizes from the Rayleigh to the geometric optic regimes (Liu et al. 2015). Therefore, the position of the DLP_{max} could also be a good diagnostic tool for discriminating whether the compact dust particles belong to the resonance or geometric optics regimes as far as their sizes are concerned. Significant differences are found in the case of

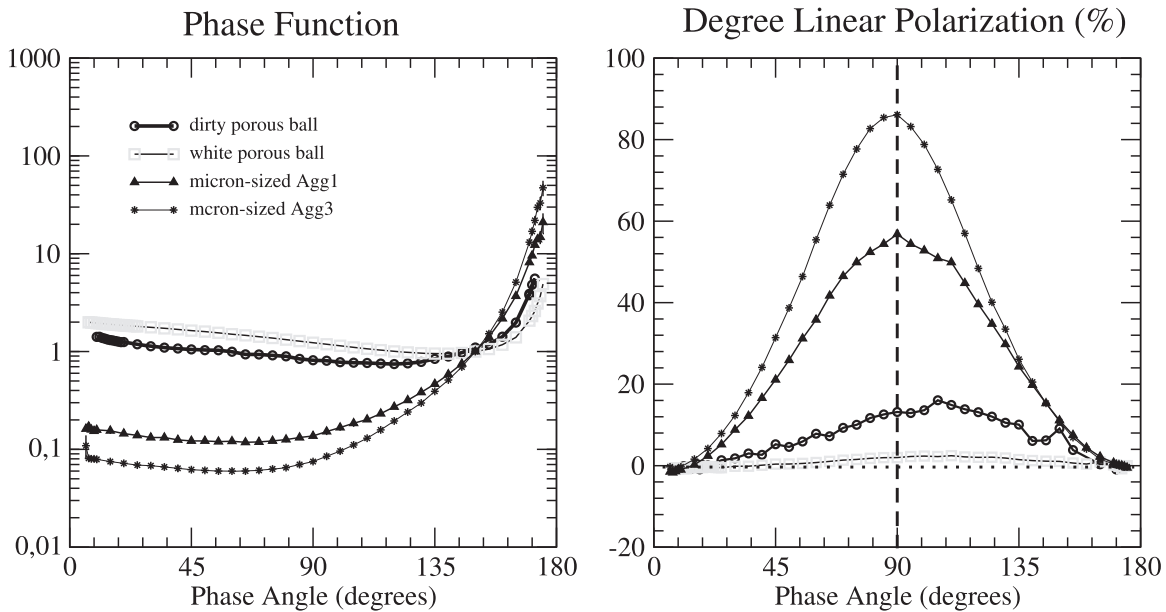


Figure 15. Measured phase functions, F_{11} , and DLP (in percentage) curves for the millimeter-sized white (open gray squares) and dirty (large black squares) cotton balls and dark-brown magnesiosilica (filled small triangles) and light-brown magnesiosilica (small asterisks) fluffy aggregate samples. All F_{11} curves are normalized to unity at 150° . The measured curves are presented with their error bars. In cases in which no error bars are shown, they are smaller than the symbol. The measurements for the cotton balls and aggregates are performed at 520 and 632.8 nm, respectively.

highly porous particles. As shown in Figures 12 and 15, the DLP_{\max} for the large porous particles ranges from 2.4% for the white cotton ball to 16% for the dirty ball. The maximum DLP value is obtained in the 85° – 105° phase angle range. Light scattered many times within the porous white cotton ball becomes largely unpolarized (see, e.g., Mishchenko et al. 2006). However, adding highly absorbing submicron charcoal inclusions to the low absorbing porous cotton ball increases the DLP_{\max} up to 16%. The effect of internal inhomogeneities on the scattering behavior of large cosmic dust particles by means of model simulations has been previously studied by Escobar-Cerezo et al. (2017). Computational results presented by those authors also indicate that adding highly absorbing inclusions on a weakly absorbing host particle produces an increase of the DLP_{\max} . In contrast, the light scattered by micron-sized fluffy aggregates consisting of nanometer-sized grains becomes highly polarized with DLP_{\max} as high as 57% and 86%, respectively, labeled as Agg1 and Agg3 in Figure 15. For both samples DLP_{\max} is located at 90° . In those cases, the sizes of the individual nanometer grains forming the aggregates determine the $-F_{12}(\theta)/F_{11}(\theta)$. In general, the smaller the size of the grains, the higher the maximum of the DLP (see, e.g., West & Smith 1991; Hadamcik et al. 2006).

Another interesting feature is that the DLP curves tend toward negative values near the back-scattering region, i.e., small phase angles. Figure 16 shows the DLP curves of the three compact millimeter-sized particles in the backward hemisphere. The quartzite and MgFeAlSi particles show a shallow NPB at the backward direction. The inversion angle (α_0), i.e., the angle at which the DLP changes its sign, seems to be dependent on the composition of the particle. The higher the imaginary part of the refractive index, the smaller the inversion angle. Indeed, the highly absorbing charcoal particle does not show any negative branch at the measured phase angle range, although it seems to tend toward negative values at smaller phase angles. Interestingly, as shown in Figure 11, the DLP for the charcoal particle tends toward negative values at the

backward direction for some orientations. That is the case when the charcoal particle is oriented with its shortest axis aligned with the holder, so that the edges of the particle are facing the beam, i.e., the laser beam is illuminating the micron-sized porous mosaic structure (Figure 2, (B)). For comparison, in Figure 16 we also present the experimental DLP for the two cosmic dust analogs consisting of micron-sized particles. The measured NPB for both samples is deeper than for the millimeter-sized particles. A similar shallowing effect was found by Shkuratov et al. (2006) when comparing experimental DLP curves of micron-sized particles in air and of particulate surfaces composed of the same particles. In addition, the tendency of the position of the inversion angle seems to be reversed as compared to the millimeter-sized particles, i.e., the DLP for the Allende meteorite sample becomes negative at larger phase angles than for the low absorbing forsterite sample. In Table 2 we present the measured main parameters of the DLP curves in the region of minimum polarization (DLP_{\min} , α_{\min}), inversion (α_0 , h), where h is the slope of the positive branch between α_{\max} and α_0 , and maximum polarization (DLP_{\max} , α_{\max}).

The exact mechanism producing the negative branch of the DLP is still not clear, but it seems to be related to constructive interference of light multiple scattered by particle surfaces in the so-called coherent back-scattering mechanism (CBM; Shkuratov 1989; Muinonen 1990). Due to the lack of surface roughness of the quartzite particle, constructive interaction of fields generated by the internal structure of the particle and refracted back could be responsible for the measured negative branch. In the case of the charcoal particle the refracted component is absorbed within the particle and does not contribute to the polarized light in the backward direction. When the charcoal particle is oriented on the holder with its largest surface parallel to the incident beam, the CBM produced by the porous mosaic surface structure could be responsible for the measured negative branch. For clouds of particles in single scattering conditions, an interference effect

Table 2

Measured Main Parameters of the DLP(α) Curves in the Region of Minimum Polarization (DLP_{min}, α_{\min}), Inversion (α_0 , h), where h Is the Slope of the Polarization Curves Computed between α_{\max} and α_0 , and Maximum Polarization (DLP_{max}, α_{\max}), Corresponding to the Samples Presented in Figures 14 and 15

Sample	Size	Color	DLP _{min}	α_{\min}	α_0	h (%/deg)	DLP _{max}	α_{\max}	
Compact	<i>Allende</i>	$r_{\text{eff}} = 2.44 \mu\text{m}$	dark gray	-3.3%	22°	36°	0.15	7.5%	85°
	<i>Forsterite</i>	$r_{\text{eff}} = 3.06 \mu\text{m}$	white	-3.1%	15°	30°	0.22	9.9%	75°
	Charcoal	$d = 4.3 \text{ mm}^{\text{a}}$	black	10°	0.76	79.6%	115°
	MgFeAlSi	$d = 5.45 \text{ mm}^{\text{a}}$	reddish	-0.9%	15°	20°	0.29	34.4%	140°
	Quartzite	$d = 3.2 \text{ mm}^{\text{a}}$	white	-0.8%	12°	30°	0.18	19.8%	140°
Porous	<i>Agg1</i>	$r \simeq 0.65 \mu\text{m}^{\text{b}}$	dark brown	-1.7%	7°	10°	0.71	56.8%	90°
	<i>Agg3</i>	$r \simeq 0.65 \mu\text{m}^{\text{b}}$	light brown	-1.3 %	7°	10°	1.08	86.1%	90°
	White ball	$d \simeq 5.0 \text{ mm}^{\text{a}}$	white	-0.6%	11°	30°	0.04	2.4%	85°
	Dirty ball	$d \simeq 5.0 \text{ mm}^{\text{a}}$	gray	-0.7%	14°	20°	0.19	16.0%	105°

Notes. Italic and boldface types correspond to micron-sized and millimeter-sized samples, respectively.

^a Diameter of the volume-equivalent sphere.

^b Aggregate/cluster size.

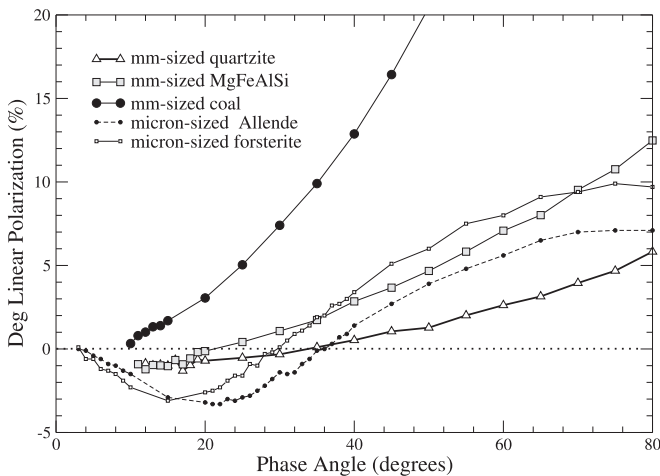


Figure 16. Measured negative polarization branches (in percentage), for the millimeter-sized compact particles and two micron-sized samples.

of forward- and backward-propagating internal waves within the particles could be responsible for the appearance of an NPB (Muinonen et al. 2015). Recent laboratory measurements indicate that particles smaller than $1 \mu\text{m}$ are responsible for the NPB of a cloud of poly-disperse micron-sized lunar dust analog particles (Escobar-Cerezo et al. 2018). In that work, it was shown that removing particles smaller than $1 \mu\text{m}$ from the bulk sample results in the decrease (in absolute values) of the NPB.

7. Comparison with Observations of Comet 67P/Churyumov–Gerasimenko

The analysis of the *Rosetta* data set has exposed challenging contradictions between the properties of cometary dust as retrieved from ground-based and from in situ observations. On the one hand, the OSIRIS camera system on board the *Rosetta* spacecraft provided unique observations of the intensity of the light scattered by dust within 67P coma (Bertini et al. 2017). The observed phase functions show a peculiar U shape with a minimum at a phase angle around 100° . Similar behavior has been observed at various heliocentric and nucleocentric distances. As shown in Figures 14 and 15, neither compact nor aggregate micron-sized particles reproduce the strong increase

of the OSIRIS phase functions with decreasing phase angle in the backward hemisphere. In contrast, the phase functions of the millimeter-sized cosmic dust analogs in random orientation show a strong increase in the backward hemisphere, but the minimum is not located at 100° as is the case for the OSIRIS phase functions. However, we obtain a very good match with the measured phase functions of millimeter-sized particles in a particular fixed orientation, when the largest cross section of the particles is perpendicular to the incident beam, i.e., when an oblate-shaped particle is located on the holder with its largest surface facing the laser beam (Figure 13, case $\delta = \delta_0$).

On the other hand, ground-based observations of the DLP of 67P show an NPB at small phase angles and a maximum observed DLP of $\sim 8\%$ at a phase angle of 33° obtained after the 2015 perihelion (Myers & Nordsieck 1984; Chernova et al. 1993; Hadamcik et al. 2017; Rosenbush et al. 2017). As mentioned, the observations are limited to phase angles smaller than $\sim 35^\circ$. This polarization behavior is common to many different comets (see, e.g., the Database of Comet Polarimetry AR-C-COMPIL-5-DB-COMET-POLARIMETRY-V1.0, NASA Planetary Data System; Kiselev et al. 2005). For all observed comets the maximum DLP ranges from 10% to 30% in the phase angle range between 90° and 100° . The right panel of Figure 14 suggests that micron-sized compact particles may dominate the polarization observations of 67P. However, as explained above, micron-sized particles cannot reproduce the U-shaped OSIRIS phase functions.

As shown in Figure 13, large porous oblate-shaped particles with highly absorbing submicron inclusions could reproduce both the U-shaped OSIRIS phase functions and the observed DLP. As shown in Figure 13 (left panel), the position of the minimum of the phase function is dependent on the shape and orientation of the particle. By flattening the dirty cotton ball into a spheroidal-like shape, the slope of the phase function in the backward hemisphere is increased (Figure 13, left panel). Ellipsoidal/spheroidal model particles are also needed to reproduce the motion of the rotating 67P dust particles as inferred from the OSIRIS (Fulle et al. 2015b) and GIADA (Ivanovski et al. 2017a, 2017b) observations. Further, by locating the spheroidal porous particle with its largest projected surface area facing the beam, the minimum is shifted toward smaller phase angles (90° – 100°) as is the case for 67P OSIRIS phase functions. In Figure 17 we compare the observed phase functions (left panel) and DLP (right panel) for comet 67P with

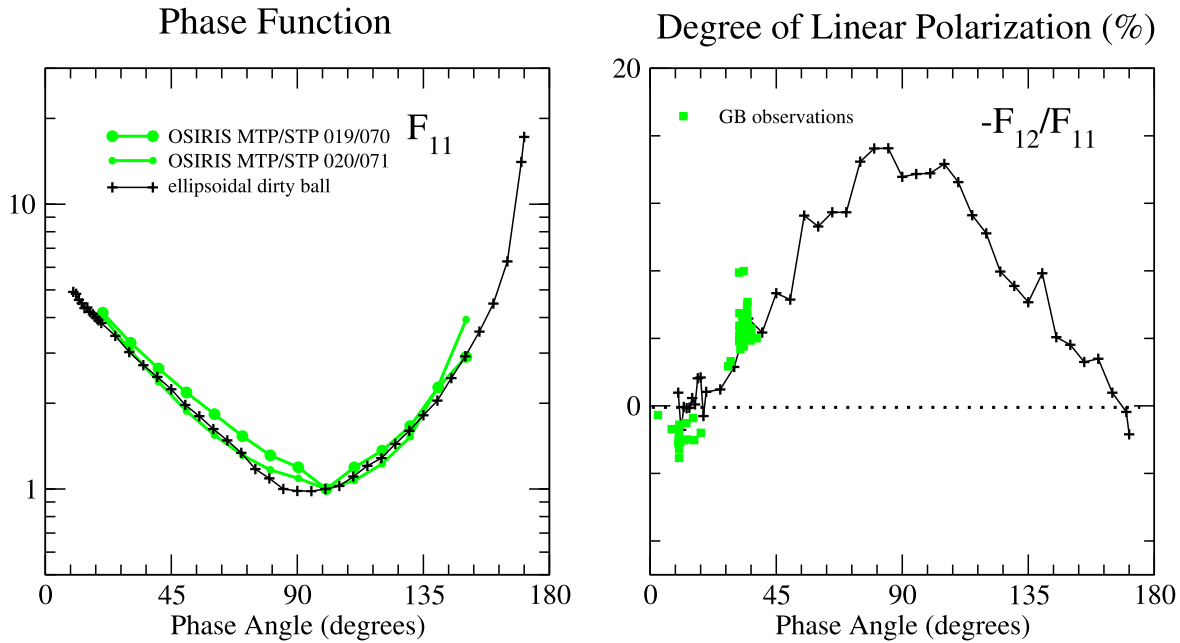


Figure 17. Green symbols correspond to the OSIRIS phase functions from Bertini et al. (2017) (left panel) and observed DLP for 67P from Rosenbush et al. (2017) and references therein (right panel). The observations are presented together with the measured phase functions and DLP for the flattened dirty cotton ball at a fixed orientation (δ_0). All F_{11} curves are normalized to unity at $\theta = 100^\circ$.

the measurements for the flattened dirty cotton ball oriented with its maximum projected surface facing the laser beam. This finding is in agreement with the results of a systematic computational study for a broad range of sizes, structure, and aspect ratios (Moreno et al. 2018). In that work, the *Rosetta*/OSIRIS phase function is reproduced using a model of particle shape distribution with a wide variety of axis ratios of large, absorbing, and moderately porous particles, in fixed orientation with respect to the solar direction. Markkanen et al. (2018) could reproduce the OSIRIS phase function using large aggregates consisting of micron-sized silicate grains with submicron organic inclusions. In the latter the dust particles are assumed to be in random orientation. It is interesting to note that the measured DLP (Figure 13, right panel) is weakly affected by the orientation of the particle.

8. Summary and Conclusions

We present the experimental phase function and DLP curves for three compact millimeter-sized cosmic dust analogs. The measurements are performed at 520 nm, covering the phase angle (α) range from 10° to 170° . The reliability of the experimental apparatus has been tested by comparing the measured phase function and DLP of a calibration sphere with Lorenz–Mie computations for the corresponding size and refractive index.

All measured phase functions show narrow forward lobes and a monotonic increase with decreasing phase angle at side- and back-scattering regions, which is characteristic of particles much larger than the wavelength of the incident light. The slope of the phase function in the backward hemisphere is larger for the two absorbing particles with smooth surfaces.

The measured DLP curves present a bell shape with a maximum (DLP_{\max}) in the 115° – 140° phase angle range, i.e., the position of the DLP_{\max} is shifted toward larger phase angles than in the case of dust particles in the micron size range (DLP_{\max} at $\alpha \sim 75^\circ$ – 85°). Therefore, the position of the DLP_{\max} might be a good indication

for the size regime (resonance or geometric optics) of the scattering particles. The DLP_{\max} ranges from 20% for the low absorbing quartzite particle to 80% for the high absorbing charcoal particle.










In addition, we have investigated the effect of porosity on the measured scattering matrix elements by performing measurements with a highly porous white cotton ball similar in size to the cosmic dust analogs. In a second step we have carried out measurements with a white cotton ball doped with submicron charcoal inclusions. The measured phase function for $\alpha < 150^\circ$ shows an increase with decreasing phase angle, in a similar way to the large compact particles. The DLP_{\max} of the porous particles is significantly decreased owing to light multiple scattered within the particle. The DLP_{\max} is increased by adding absorbing inclusions to the porous ball.

According to our measurements, the OSIRIS/*Rosetta* phase functions and ground-based observations of the DLP of 67P are compatible with large porous low absorbing particles with absorbing submicron inclusions. To reproduce the minimum of the OSIRIS phase functions at $\alpha \sim 100^\circ$, the porous particle must have an oblate-like shape and must be located with its largest projected surface area facing the laser beam as suggested by previous computations (Moreno et al. 2018). Nonspherical oblate particles are also required for reproducing the rotational dust frequency as derived from the OSIRIS (Fulle et al. 2015a) and GIADA (Ivanovski et al. 2017a) instruments on board *Rosetta*. Further, our 67P dust particle experimental model is in agreement with the in situ observations of the COSIMA mass spectrometer on board *Rosetta*. The dust particles collected by COSIMA consist of large porous nonspherical aggregates (Langevin et al. 2016) composed of 55% in mass of minerals and 45% in mass of organics (Bardyn et al. 2017).

The experimental phase function and DLP curves are freely available in digital form in the Amsterdam–Granada light-scattering database (www.iaa.es/scattering) under request of citation of Muñoz et al. (2012) and this paper.

We are indebted to Rocío Márquez from the Scientific Instrumentation Center of the University of Granada for providing the SEM images. This work has been partially funded by the Spanish Plan Nacional de Astronomía y Astrofísica LEONIDAS project RTI2018-095330-B-100 and the *Centro de Excelencia Severo Ochoa Program* under grant SEV-2017-0709.

ORCID iDs

O. Muñoz  <https://orcid.org/0000-0002-5138-3932>
 F. Moreno  <https://orcid.org/0000-0003-0670-356X>
 J. C. Gómez-Martín  <https://orcid.org/0000-0001-7972-085X>
 J. Markkanen  <https://orcid.org/0000-0001-5989-3630>
 M. Fulle  <https://orcid.org/0000-0001-8435-5287>
 A. Rotundi  <https://orcid.org/0000-0001-5467-157X>
 S. Ivanovski  <https://orcid.org/0000-0002-8068-7695>
 J. Blum  <https://orcid.org/0000-0003-1531-737X>
 S. Merouane  <https://orcid.org/0000-0002-7746-2380>

References

- Acke, B., Min, M., Dominik, C., et al. 2012, *A&A*, **540**, A125
 Bardyn, A., Baklouti, D., Cottin, H., et al. 2017, *MNRAS*, **469**, S712
 Bertini, I., La Forgia, F., Tubiana, C., et al. 2017, *MNRAS*, **469**, S404
 Blum, J., Gundlach, B., Krause, M. M., et al. 2017, *MNRAS*, **469**, S755
 Bockelée-Morvan, D., Leyrat, C., Erard, S., et al. 2019, *A&A*, **630**, A22
 Bockelée-Morvan, D., Rinaldi, G., Erard, S., et al. 2017a, *MNRAS*, **469**, S443
 Bockelée-Morvan, D., Rinaldi, G., Erard, S., et al. 2017b, *MNRAS*, **469**, S842
 Canovas, H., Cáceres, C., Schreiber, M. R., et al. 2016, *MNRAS*, **458**, L29
 Canovas, H., Menard, F., de Boer, J., et al. 2015, *A&A*, **582**, L7
 Casassus, S., Wright, C. M., Sebastian, M., et al. 2015, *ApJ*, **812**, 126
 Chernova, E. P., Kiselev, N. N., & Jockers, K. 1993, *Icar*, **103**, 144
 Della Corte, V., Rotundi, A., Accolla, M., et al. 2014, *JAI*, **3**, 1350011
 Della Corte, V., Rotundi, A., Zakharov, V., et al. 2019, *A&A*, **630**, A25
 Dorschner, J., Begemann, B., Henning, Th., et al. 1995, *A&A*, **300**, 503
 Duley, W. W. 1984, *ApJ*, **287**, 694
 Escobar-Cerezo, J., Muñoz, O., Moreno, F., et al. 2018, *ApJSS*, **235**, 9p
 Escobar-Cerezo, J., Palmer, C., Muñoz, O., et al. 2017, *ApJ*, **838**, 74
 Filacchione, G., Ammannito, E., Coradini, A., et al. 2006, *RSci*, **77**, 103106
 Frattin, E., Muñoz, O., Moreno, F., et al. 2019, *MNRAS*, **484**, 2198
 Fulle, M., Della Corte, V., Rotundi, A., et al. 2015a, *ApJL*, **802**, L12
 Fulle, M., Ivanovski, S. L., Bertini, I., et al. 2015b, *A&A*, **583**, A14
 Fulle, M., Marzari, F., Della Corte, V., et al. 2016, *ApJ*, **821**, 19
 Hadamcik, E., Levasseur-Regourd, A. C., Hines, D. C., et al. 2017, *MNRAS*, **462**, S507
 Hadamcik, E., Renard, J. B., Levasseur-Regourd, A. C., et al. 2006, *JQSRT*, **79-80**, 679
 Hansen, J. E., & Travis, L. D. 1974, *SSRv*, **16**, 527
 Hovenier, J. W., van der Mee, C. V. M., & Domke, H. 2004, *ASSL*, **318**
 Ivanovski, S. L., Della Corte, V., Crifo, J.-F., et al. 2017a, *Icar*, **282**, 333
 Ivanovski, S. L., Della Corte, V., Rotundi, A., et al. 2017b, *MNRAS*, **469**, S774
 Jäger, C., Mutschke, H., Begemann, B., et al. 1994, *A&A*, **292**, 641
 Kiselev, N., Rosenbush, V., Jockers, K., et al. 2005, *EM&P*, **97**, 365
 Kolokolova, L., Das, H. S., Dubovik, O., et al. 2015, *P&SS*, **116**, 30
 Kolokolova, L., & Kimura, I. 2010, *EP&S*, **62**, 17
 Kolokolova, L., Nagdimunoz, L., & Mackowski, D. 2018, *JQSRT*, **204**, 138
 Langevin, Y., Hilchenbach, M., Ligier, N., et al. 2016, *Icar*, **271**, 76
 Lasue, J., Levasseur-Regourd, A. C., Hadamcik, E., et al. 2009, *Icar*, **199**, 129
 Levasseur-Regourd, A. C., Renard, J.-B., Hadamcik, E., et al. 2019, *A&A*, **630**, A20
 Liu, J., Yang, P., & Muinonen, K. 2015, *JQSRT*, **161**, 136
 Lorek, S., Lacerda, P., & Blum, J. 2018, *A&A*, **611**, 18
 Mannel, T., Bentley, M. S., Boakes, P., et al. 2017, EPSC Abstracts, **11**, EPSC2017-258
 Markkanen, J., & Agarwal, J. 2019, *A&A*, **631**, A164
 Markkanen, J., Agarwal, J., Väisänen, T., et al. 2018, *ApJL*, **868**, L16
 McLean, W., Stam, D. M., Bagnulo, S., et al. 2017, *A&A*, **601**, 20
 Merikallio, S., Muñoz, O., Sundström, A.-M., et al. 2015, *JGRD*, **120**, 4102
 Milli, J., Vigan, A., Mouillet, D., et al. 2017, *A&A*, **599**, A108
 Min, M., Hovenier, J. W., & de Koter, A. 2003, *A&A*, **404**, 35
 Min, M., Kama, M., Dominik, C., & Waters, L. B. F. M. 2010, *A&A*, **509**, L6
 Mischenko, M. I., & Yurkin, M. A. 2017, *OptL*, **42**, 494
 Mishchenko, M. I., Travis, L. D., Kahn, R. A., et al. 1997, *JGR*, **102**, 16831
 Mishchenko, M. I., Travis, L. D., & Lacis, A. A. (ed.) 2006, Multiple Scattering of Light by Particles (Cambridge: Cambridge Univ. Press)
 Moreno, F., Guirado, D., Muñoz, O., et al. 2018, *AJ*, **156**, 237
 Moreno, F., Muñoz, O., Guirado, D., et al. 2007, *JQSRT*, **106**, 348
 Moreno, F., Muñoz, O., Gutiérrez, P., et al. 2017, *MNRAS*, **469**, 186
 Moreno, F., Snodgrass, C., Hainaut, O., et al. 2016, *A&A*, **587**, A155
 Muinonen, K. 1990, PhD thesis, Univ. Helsinki
 Muinonen, K., Penttilä, A., & Videen, G. 2015, in Polarimetry of Stars and Planetary Systems, ed. L. Kolokolova, A. C. Levasseur-Regourd, & J. Hough (Cambridge: Cambridge Univ. Press)
 Muñoz, O., & Hovenier, J. W. 2015, in Polarimetry of Stars and Planetary Systems, ed. L. Kolokolova, A. C. Levasseur-Regourd, & J. Hough (Cambridge: Cambridge Univ. Press)
 Muñoz, O., Moreno, F., Guirado, D., et al. 2010, *JQSRT*, **111**, 187
 Muñoz, O., Moreno, F., Guirado, D., et al. 2011, *JQSRT*, **113**, 565
 Muñoz, O., Moreno, F., Guirado, D., et al. 2012, *JQSRT*, **113**, 565
 Muñoz, O., Moreno, F., Vargas-Martín, F., et al. 2017, *ApJ*, **846**, 8
 Muñoz, O., Volten, H., Hovenier, J. W., et al. 2007, *JGR*, **112**, D13215
 Mutschke, H., Begemann, B., Dorschner, J., et al. 1998, *A&A*, **333**, 188
 Myers, R. V., & Nordsieck, K. H. 1984, *Icar*, **58**, 431
 Ott, T., Drolshagen, E., Koschny, D., et al. 2017, *MNRAS*, **469**, S276
 Papoular, R., Breton, J., Gensterblum, G., et al. 1993, *A&A*, **270**, L5
 Pinilla, P., Birnstiel, T., Ricci, L., et al. 2012, *A&A*, **538**, A114
 Pohl, A., Kataoka, A., Pinilla, P., et al. 2016, *A&A*, **593**, A12
 Ren, B., Choquet, E., Perrin, M. D., et al. 2019, *ApJ*, **882**, 64
 Riedler, W., Torkar, K., Jesezenszky, H., et al. 2007, *SSRv*, **128**, 869
 Rosenbush, V., Ivanova, O. V., Kiselev, N. N., et al. 2017, *MNRAS*, **469**, S475
 Rotundi, A., Sierks, H., Della Corte, V., et al. 2015, *Sci*, **347**, aaa3905
 Shkuratov, Y., Bondarenko, S., Ovcharenko, A., et al. 2006, *JQSRT*, **100**, 340
 Shkuratov, Yu. G. 1989, *AVest*, **23**, 176
 Stagg, B. J., & Charalampopoulos, T. T. 1993, *CoFl*, **94**, 381
 Testi, L., Birnstiel, T., Ricci, L., et al. 2014, in Protostars and Planets VI, ed. H. Beuther et al. (Tucson, AZ: Univ. Arizona Press), 339
 van de Hulst, H. C. 1957, *Light Scattering by Small Particles* (New York: Wiley)
 van der Marel, N., van Dishoeck, E. F., Bruderer, S., et al. 2013, *Sci*, **340**, 1199
 Volten, H., Muñoz, O., Brucato, J. R., et al. 2006, *JQSRT*, **100**, 429
 Volten, H., Muñoz, O., Hovenier, J. W., et al. 2007, *A&A*, **470**, 377
 Walsh, C., Juhasz, A., Meeus, G., et al. 2016, *ApJ*, **831**, 200
 Weiss-Wrana, K. 1983, *A&A*, **126**, 240
 West, R. A., Doose, L. R., Eibl, A. M., et al. 1997, *JGR*, **102**, 16871
 West, R. A., & Smith, P. H. 1991, *Icar*, **90**, 330
 Xing, Z., & Hanner, M. S. 1997, *A&A*, **324**, 805
 Zsom, A., Ormel, C. W., Güttler, C., et al. 2010, *A&A*, **512**, A57
 Zubko, E., Muinonen, K., Shkuratov, Y., et al. 2013, *MNRAS*, **430**, 1118
 Zubko, E., Videen, G., Hines, D. C., et al. 2016, *P&SS*, **123**, 63
 Zubko, E., Videen, G., & Shkuratov, Yu. 2015, *JQSRT*, **151**, 38