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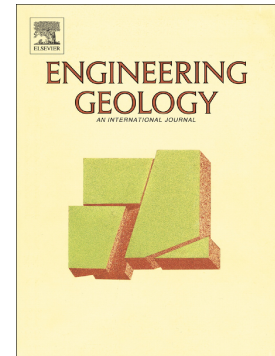


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Journal Pre-proof

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Which fractures are imaged with Ground Penetrating Radar? Results from an experiment in the Äspö Hardrock Laboratory, Sweden

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Abstract

Identifying fractures in the subsurface is crucial for many geomechanical and hydrogeological applications. Here, we assess the ability of the Ground Penetrating Radar (GPR) method to image open fractures with sub-mm apertures in the context of future deep disposal of radioactive waste. GPR experiments were conducted in a tunnel located 410 m below sea level within the Äspö Hard Rock Laboratory (Sweden) using 3-D surface-based acquisitions (3.4 m x 19 m) with 160 MHz, 450 MHz and 750 MHz antennas. The nature of 17 identified GPR reflections was analyzed by means of three new boreholes (BH1-BH3; 9-9.5 m deep). Out of 21 injection and outflow tests in packed-off 1-m sections, only five provided responses above the detection threshold with the maximum transmissivity reaching $7.0 \times 10^{-10} \text{ m}^2/\text{s}$. Most GPR reflections are situated in these permeable regions and their characteristics agree well with core and Optical Telemetry data. A 3-D statistical fracture model deduced from fracture traces on neighboring tunnel walls show that the GPR data mainly identify fractures with dips between 0 and 25° . Since the GPR data are mostly sensitive to open fractures, we deduce that the surface GPR method can identify 80% of open sub-horizontal fractures. We also find that the scaling of GPR fractures in the range of 1-10 m² agrees well with the statistical model distribution indicating that fracture lengths are preserved by the GPR imaging (no measurement bias). Our results suggest that surface-GPR carries the resolution needed to identify the most permeable sub-horizontal fractures even in very low-permeability formations, thereby, suggesting that surface-GPR could play an important role in geotechnical workflows, for instance, for industrial-scale siting of waste canisters below tunnel floors in nuclear waste repositories.

Key words: Ground Penetrating Radar, surface-based method, fracture, core log, tunnel, statistical fracture model, nuclear waste disposal

1. Introduction

In hard rock systems, fractures are the main conduit for flow (Becker & Shapiro, 2000), for contaminant transport (Selroos et al., 2002), and they play a critical role in determining the mechanical properties of rocks (Davy et al., 2018a). Hydrogeological and geomechanical applications require, henceforth, an appropriate characterization of the fracture network and of its hydrological and mechanical properties (Davy et al., 2018a). Traditionally, this information is mostly derived from a statistical analysis of 2-D fracture traces mapped in tunnel walls and surface outcrops, or from 1-D fracture intercepts along boreholes. Such statistical approaches have drawbacks: 1) the 3-D fracture models do not rely on actual 3-D observations, which requires crude assumptions on some fracture properties (e.g., fracture shapes) (Davy et al., 2018b); 2) some scales are hardly measured because of the limited size of outcrops, tunnel walls, or borehole diameter; 3) models that aim at making predictions are generally better constrained by conditioning to location-specific deterministic information than by global statistics only (Andersson & Dverstorp, 1987). This is why imaging fractures at different scales, especially with non-invasive methods, is of high importance for hydrogeological and geomechanical applications (e.g. mine and tunnel stability, detection of flow paths, contaminant transport).

A particular application, which partly motivates this study, is the detection of potential pathways (at the 10 m scale) from defective canisters for nuclear waste with non-invasive (i.e., without drilling) surface methods. This is required to identify locations that are unsuitable for storing nuclear waste in canisters emplaced under the tunnel floor, as envisioned for the storage of nuclear waste in Finland and Sweden. In the very low-permeability formations that are of interest for the nuclear waste repositories of Sweden or Finland, transport of potentially released radionuclides take place through fractures with sub-millimetric apertures that are very difficult to detect remotely. This excludes many geophysical methods such as seismic reflection/refraction, electrical resistivity and nuclear magnetic resonance for this task. If one adds both the constraint of being surface-based and being

able to detect meter-scale individual fractures remotely, the only suitable method is ground penetrating radar (GPR) (Day-Lewis et al., 2017).

There is a rich literature describing how GPR data were used to detect permeable fractures in various hydrogeological (Becker & Tsoflias, 2010; Day-Lewis et al., 2003; Dorn et al., 2011a; Dorn et al., 2011b; Dorn et al., 2012; Shakas et al., 2016; Tsoflias et al., 2001), geotechnical (Davis & Annan, 1989; Grasmueck et al., 2005; Grégoire & Halleux, 2002; Seol et al., 2001) and nuclear waste-related (Baek et al., 2017; Döse & Carlsten, 2017; Olsson et al., 1992; Serzu et al., 2004) applications. Notably, the GPR reflections caused by fracture planes are enhanced when the fractures are fluid-filled or have large apertures (Grasmueck, 1996; Hollender & Tiliard, 1998; Hollender et al., 1999; Jeannin et al., 2006; Markovaara-Koivisto et al., 2014; Shakas & Linde, 2017; Tsoflias & Becker, 2008; Tsoflias & Hoch, 2006). Electromagnetic (EM) waves with wavelengths on the m-scale respond to fractures with sub-millimetric aperture because of the strong contrast in electrical properties between the fracture filling and the surrounding rock matrix and because of multiple internal reflections between the fracture walls generating wavelet interferences (the thin-bed response) (Bradford & Deeds, 2006; Deparis & Garambois, 2008; Grégoire & Hollender, 2004; Sassen & Everett, 2009; Shakas & Linde, 2015). At repository depth (~400-600 m below sea level), the fracture aperture can be very small and it is not yet clear whether observed GPR reflections in such an environment are primarily related to water-filled fractures and not to other geological interfaces (e.g., dike intrusion, geological contacts, material-filled fractures). It is also not clear which percentage of open fractures are imaged as a function of their sizes and orientations.

In this contribution, we present a 3-D GPR imaging experiment performed at 410 m depth in the Äspö Hard Rock Laboratory, Sweden (Figure 1a). The GPR data have been migrated to form a 3-D network of reflectors, hereafter, named GPR fractures. After the GPR experiment, three 9-m deep boreholes were drilled in the zone (Figure 1b), mapped with televiwer logging, and hydraulically tested to ground-truth the GPR results.

Our main aims are to address the following questions:

1. Do GPR reflections observed in deep low-permeability granitic formations correspond to open transmissive fractures only or also to other types of geological discontinuities?
2. What is the detection accuracy of the GPR fractures in terms of fracture sizes and orientations?

The first point has been addressed by a careful GPR experiment performed in a 410-m deep tunnel by picking the main reflectors and verifying the nature of reflectors from a subsequent drilling of three boreholes analyzed by core logging and hydraulic tests. The second point has been addressed by comparing the statistics of GPR fractures with the 3-D fracture statistics derived from outcrop and borehole mapping.

2. Test Site

The Äspö Hard Rock Laboratory (HRL) is an underground research facility below the island of Äspö located approximately 300 km south of Stockholm on the peninsula of Simpevarp surrounded by the Baltic Sea (Figure 1a). It was constructed in 1986 (Cosma et al., 2001) by the Swedish Nuclear Fuel and Waste Management Company (SKB) as a R&D site to develop new methodologies and technologies to build the know-how needed to construct a hard rock repository for nuclear waste. It contains a main tunnel of 3.6 km length and several side-tunnels extending from the surface down to 450 m depth (Figure 1a) (SKB, 2016). The geology is mainly composed of fractured granitic rocks that are more than 1.7 billion years old (Cosma et al., 2001).

The GPR investigation focuses on the secondary TAS04 tunnel, which was excavated at a depth of 410 m by the drill-and-blast method (Ericsson et al., 2015; Ericsson et al., 2018). The tunnel is 36 m long, 4.2 m wide and 5.3 m high. Its geology is composed by three main rock types: fine-grained granite, Äspö diorite and Ävrö granodiorite, with some pegmatite veins (Figure 1b) (Ericsson et al., 2015; Ericsson et al., 2018). Geotechnical (check of drilling and charging), geological (fracture

mapping), geophysical (surface GPR) and hydrogeological (42 borehole drillings of 2 m depth and hydraulic tests) investigations were used to characterize superficial fractures induced by the blasting. It was found that the excavation-damage zone (EDZ) was 0.5 m thick (Ericsson et al., 2015; Ericsson et al., 2018). The EDZ was removed by cutting and sawing the tunnel floor with a diamond wire along 20 m of the tunnel length; it is in the resulting very flat area that our GPR measurements were performed (Figure 1b).

In addition to the TAS04 tunnel, three surrounding tunnels at the same depth are used to derive the 3-D statistical fracture model. The TAS05 and TASN tunnels are parallel to the TAS04 and are 17 m and 52 m long, 4.5 m and 4.2 m wide and 4.5 m and 3.7 m high, respectively. The TASP tunnel is perpendicular to the others and is 57 m long, 7 m wide and 4.1 m high.

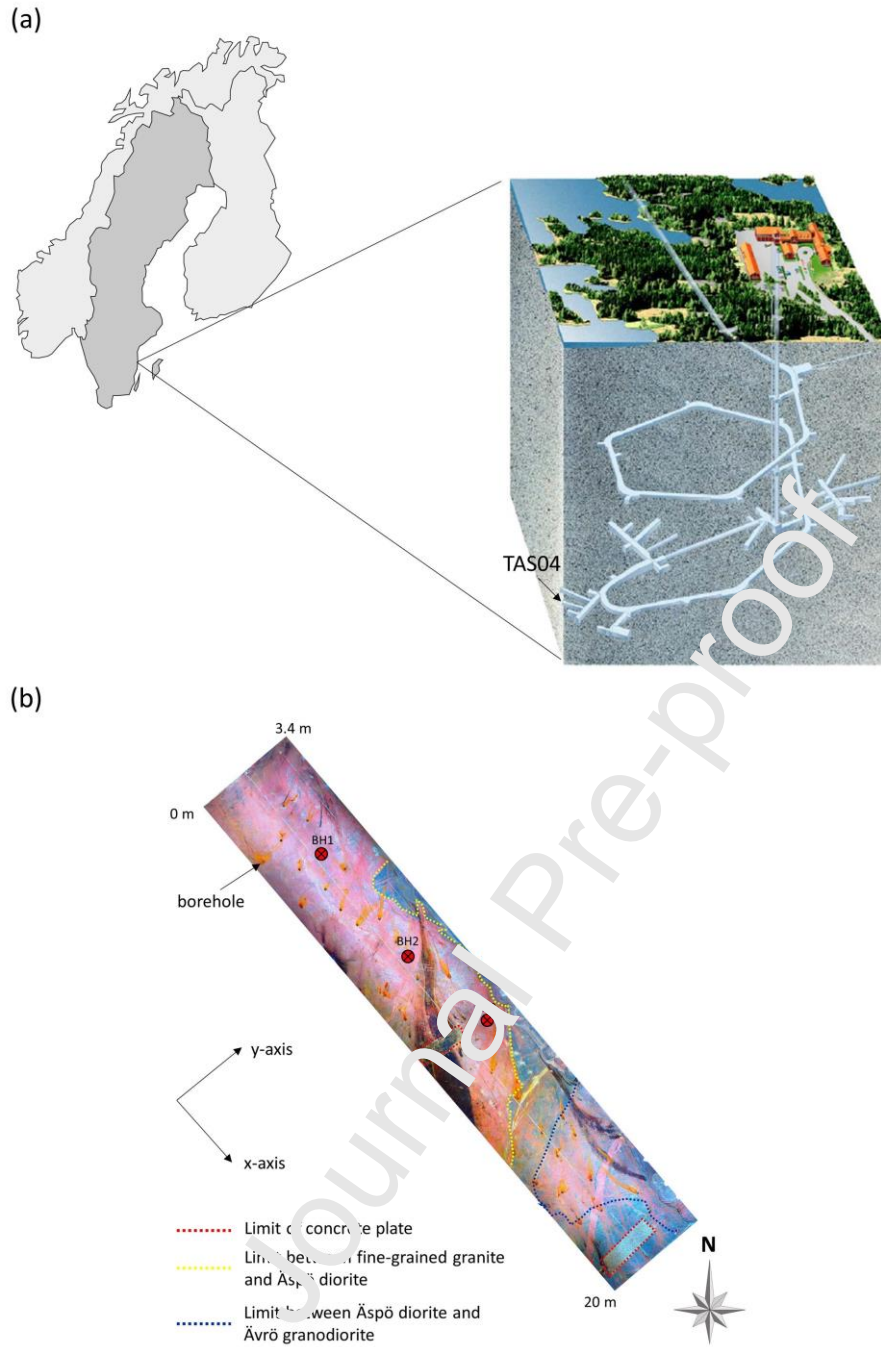


Figure 1: (a) Illustration of the Äspö Hard Rock Laboratory in the Simpevarp peninsula, Sweden. The study tunnel (TAS04) is situated at a depth of 410 m. Figure modified from SKB (2016), courtesy of SKB, Illustrator: Jan Rojmar. (b) Orthophotography of the tunnel floor showing the geological limit between fine-grained granite (to the left), Äspö diorite and Ävrö granodiorite (to the right) indicated by yellow and blue dashed lines, shallow pre-existing boreholes represented by black dots with oxidation (orange traces) and concrete plates delimited by red dashed lines. The three new boreholes (BH1, BH2 and BH3 indicated by red circles with crosses) were drilled in the granitic formation with locations chosen based on the GPR results. (Figure size: 2 column fitting; Colors: yes)

3. GPR experiment methodology

3.1. GPR survey

The GPR data from the TAS04 tunnel were acquired in the period of November 6-10, 2017, using the MALÅ GroundExplorer (GX) HDR-serie (High Dynamic Range), equipped with skid plate and wheel. 160, 450 and 750 MHz antennas were used to achieve different investigation depths and image resolutions. The acquisition parameters are given in Table 1. The shielded transmitter and receiver antennas, separated by a fixed separation in a so-called common-offset configuration (Annan, 2003), were pulled along the cleaned and flat tunnel floor (Figure 2). The GPR profiles were acquired with 2.34 cm measurement spacing and a line separation of 0.05 m for the 450 and 750 MHz surveys and 0.10 m for the 160 MHz survey. The profiles were oriented along the tunnel length (x-direction) using multiple orthogonal measurement tapes to ensure straight and parallel measurement lines. The resulting acquisition area was 3.4 m × 19 m. Measurements with a total station using fixed geodetic points in the tunnel were used to convert the acquisition geometry into the local Äspö coordinate system (Äspö96).

Table 1: Experimental parameters used for the GPR acquisitions in common-offset mode. (Table size: 2 column fitting)

Parameters	Frequencies (MHz)		
	160	450	750
Antenna separation (m)	0.33	0.18	0.14
Measurement spacing (m)	0.02355	0.02355	0.02355
Profile separation (m)	0.10	0.05	0.05
Number of profiles	34	69	69
Investigation depth (m)	0 to 10	0 to 8	0 to 5

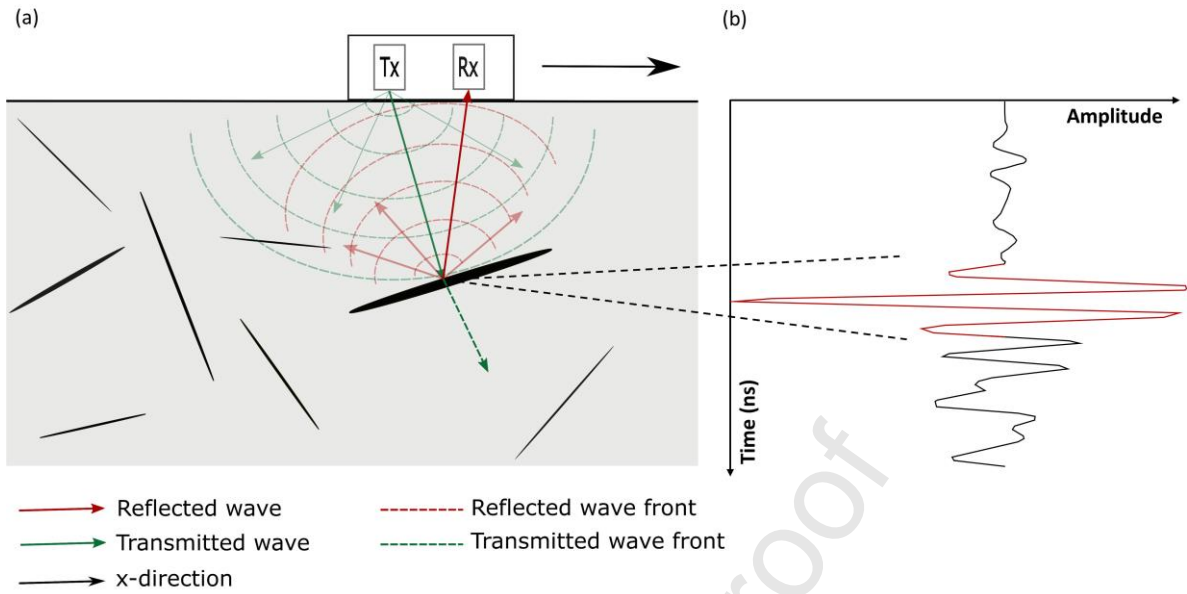


Figure 2: (a) The common-offset GPR configuration: the transmitter (Tx) and receiver (Rx) antennas are placed in a shielded box. The surface GPR is pulled along the tunnel floor (x-direction). The transmitter antenna sends an electromagnetic pulse into the subsurface and the receiver antenna records the returning signal amplitudes over time as shown schematically in (b). (Figure size: 2 column fitting; Colors: yes)

3.2. Data processing

The GPR data processing and migration workflow is depicted in Figure 3. We consciously avoid automatic gain control to enable relative comparisons of reflectivity at different locations in the investigated volume. The editing step involves removal of some limited data at the end of certain profiles to ensure a rectangular-shaped survey area. Direct Current (DC) removal used to remove offsets in the data is achieved by subtracting the mean of the last 33% of the GPR traces. Time zero corrections are made to ensure that the actual source initiation time is treated as zero. For each trace, this is achieved by shifting the time vector such that the time when the signal magnitude is first above the noise-level corresponds to the time it takes for the speed of light in a vacuum to travel the distance between the source and receiver. Irregularity removal refers to traces that are adversely affected by the many (42) shallow boreholes (0-1 m depth) and two concrete plates. To avoid the migration of these data that largely respond to non-geologic features, we automatically detected (5-6% of the data) and removed these traces by identifying irregularities in the magnitudes of their direct waves. Median trace removal along each line was performed to not only remove the direct

wave, but also significant ringing in the data. Time-gain with a different exponent for each frequency (2.5 for 160 MHz, 2.5 for 450 MHz and 2.0 for 750 MHz data) was applied to correct for geometric spreading and attenuation of later-arriving signals. Finally, singular value decomposition (SVD) was used to remove the first 3 to 5 singular values to further suppress ringing effects.

Migration was needed to collapse the many diffractors in the data and to properly locate the reflections at depth. For this, we used 3-D depth Kirchhoff migration (Margrave & Lamoureux, 2019) as implemented in the CREWES Matlab toolbox (CREWES, 1988) with a constant velocity of 0.130 m/ns as determined by diffraction analysis and visual inspection of migration results.

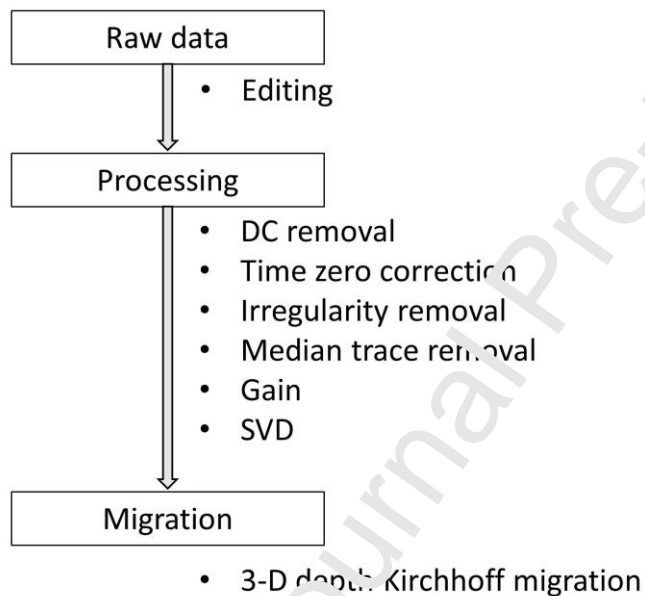


Figure 3: Flow chart describing how the raw data are edited and processed before migration. (Figure size: 1 column fitting; Colors: no)

4. Results

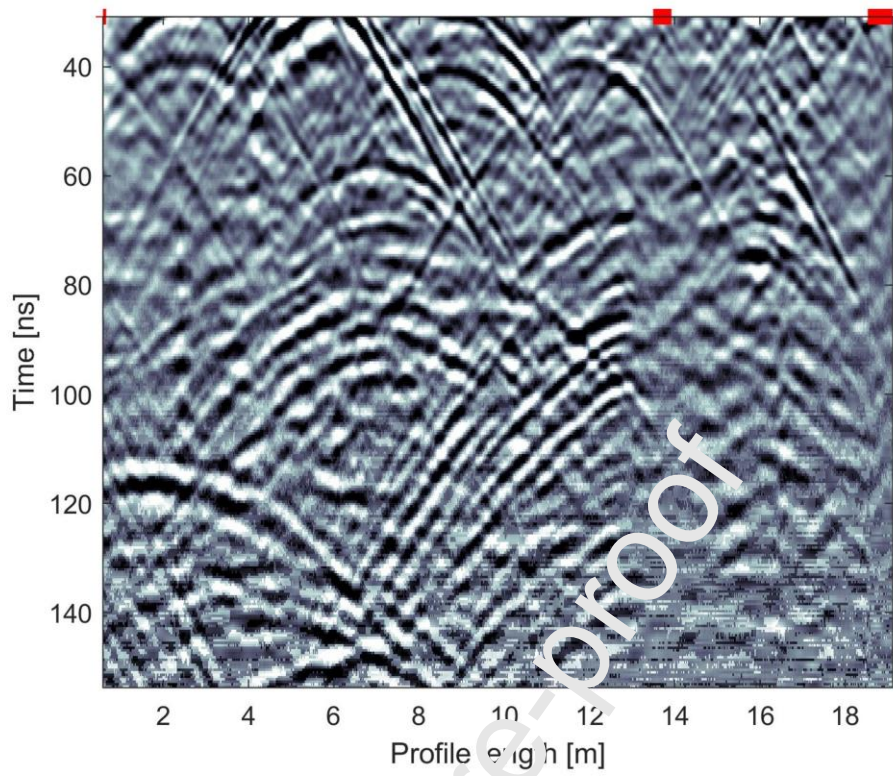
The 3-D GPR results are exemplified by processed profiles of 160 MHz (Figure 4), 450 MHz (Figure 5) and 750 MHz (Figure 6) data and corresponding 3-D migration results along a 2-D section located approximately in the middle of the tunnel. As expected, the 750 MHz data have the highest resolution and the lowest investigation depth, while the 160 MHz data have the lowest resolution and the highest investigation depth. The 450 MHz is the most suitable frequency for identifying each individual feature from 0 to 8 m depth. To a first order, the vertical and horizontal resolution enabling separation of features in migrated images are $\lambda/4$, where λ is the wavelength (Annan, 2003; Grasmueck, 2005; Jol, 2008; Reynolds, 1997). Since the average wave speed is 0.13 m/ns, the vertical and horizontal resolutions are 0.2 m for 160 MHz, 0.06 m for 450 MHz and 0.04 m for 750 MHz.

The unmigrated data (Figure 4a, Figure 5a, Figure 6a) show diffractions manifested by characteristic hyperbolas. The shallow diffractions are mainly caused by the shallow boreholes (42), while deeper diffractions may be related to fracture wall irregularities, fracture intersections or geological heterogeneities (Grasmueck et al., 2015; Grasmueck et al., 2013; Grasmueck et al., 2005). On depth slices, these diffractions appear as concentric circles, whose radii are increasing with depth (Figure 7a).

To remove the diffractions and locate the reflections in space, we used 3-D Kirchhoff migration with a constant velocity of 0.13 m/ns. After migration, the energy contained in the hyperbola tails is ideally gathered into a unique point corresponding to the initial diffraction point (Figure 7b). After migration, sub-horizontal reflections that might correspond to fractures are visible on vertical 2-D GPR slices with alternating positive and negative amplitudes aligned in sub-horizontal patterns (Figure 4b, Figure 5b, Figure 6b). This alternation is a consequence of the finite-length source wavelet used by the GPR antennas. Sub-vertical features that might correspond to fractures appear as bright spots plunging with depth that are clearly visible in the horizontal GPR depth slices (Figure 7b, c).

To visualize the GPR results in three dimensions, we imported 2-D processed and migrated data slices into the software Paradigm GOCAD™ (Figure 8) using Äspö coordinates. By comparing unmigrated (Figure 4a, Figure 5a, Figure 6a) and migrated (Figure 4b, Figure 5b, Figure 6b) data for the three frequencies, we created a simplified fracture network model (Figure 8). This manual procedure of identifying GPR fractures is somewhat subjective. Large sub-horizontal GPR structures were picked on each vertical 2-D slice at the interface between the background signal and the signal corresponding to the reflection of the structure represented by positive (intense white) or negative (intense black) amplitudes. Sub-vertical fractures were identified on horizontal depth slices by picking their horizontal edge traces (Figure 7c). The set of the trace picks was used to construct the fracture surface using the convex hull plane that connects the picks, with no assumption on fracture form in order to avoid over- or underestimation of the data. We identified a total of 21 reflections that might correspond to fractures with dimensions of 1 to 4 m. This work was focused on the first 15 m of the GPR block along the axis of the tunnel, in order to be within the same fine-grained granitic environment (Figure 8).

(a)



(b)

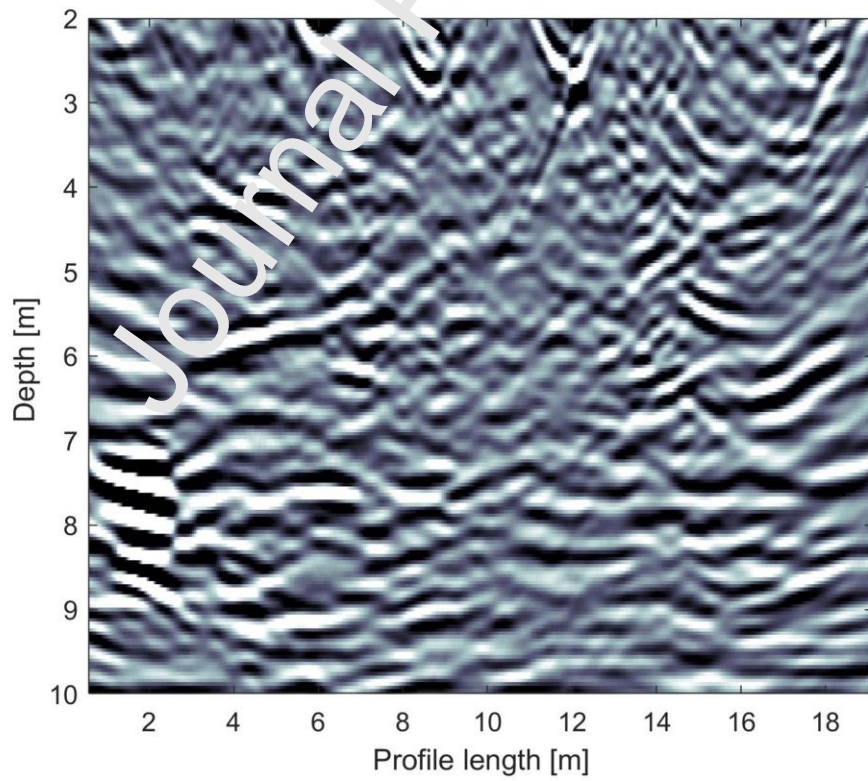
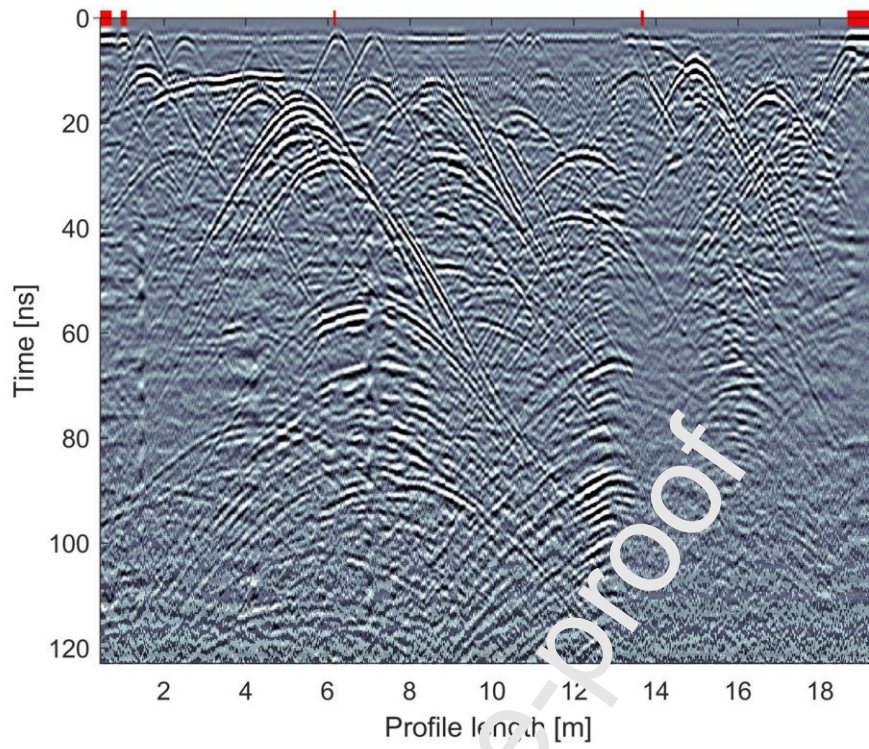


Figure 4: (a) Processed 2-D GPR slice acquired with 160 MHz antennas at $y = 2.25$ m. Red plus signs correspond to shallow boreholes and concrete plate irregularities; the corresponding traces are removed before migration. (b) Migrated data based on 3-D Kirchhoff migration with a constant velocity of 0.13 m/ns. The time and depth intervals are chosen based on the associated resolution and depth of penetration. (Figure size: 2 column fitting; Colors: yes)

(a)



(b)

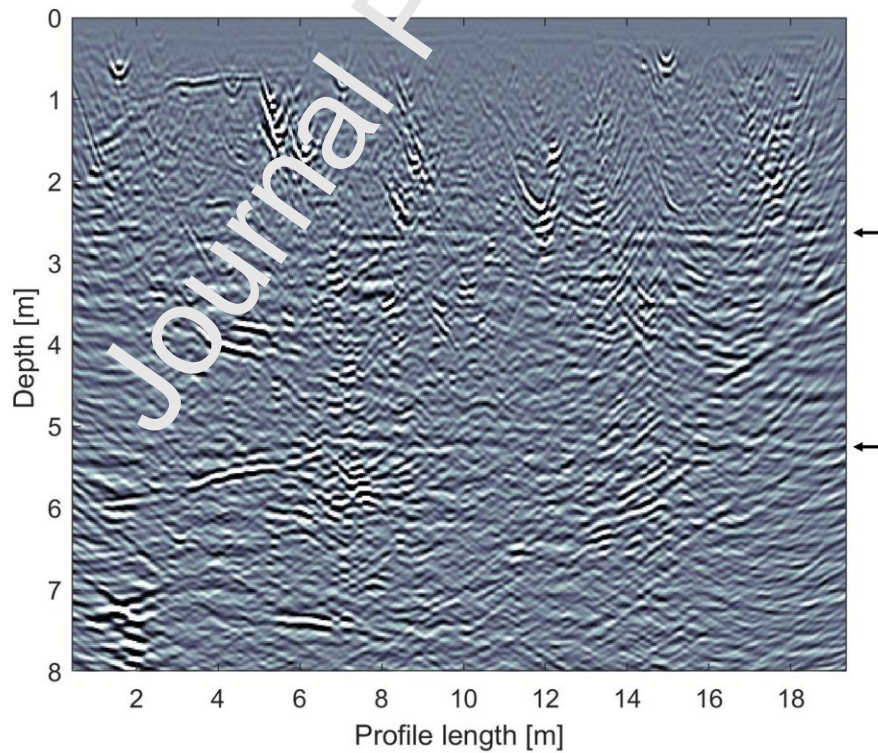


Figure 5: (a) Processed 2-D GPR slice acquired with 450 MHz antennas at $y = 2.28$ m. Red plus signs correspond to shallow boreholes and concrete plate irregularities; the corresponding traces are removed before migration. (b) Migrated data based on 3-D Kirchhoff migration with a constant velocity of 0.13 m/ns. The depth interval is chosen based on the associated resolution and depth of penetration. The large horizontal features at depths of 2.5 and 5.1 m (indicated by black horizontal arrows) are attributed to reflections at the tunnel roof and corresponding multiples. (Figure size: 2 column fitting; Colors: yes)

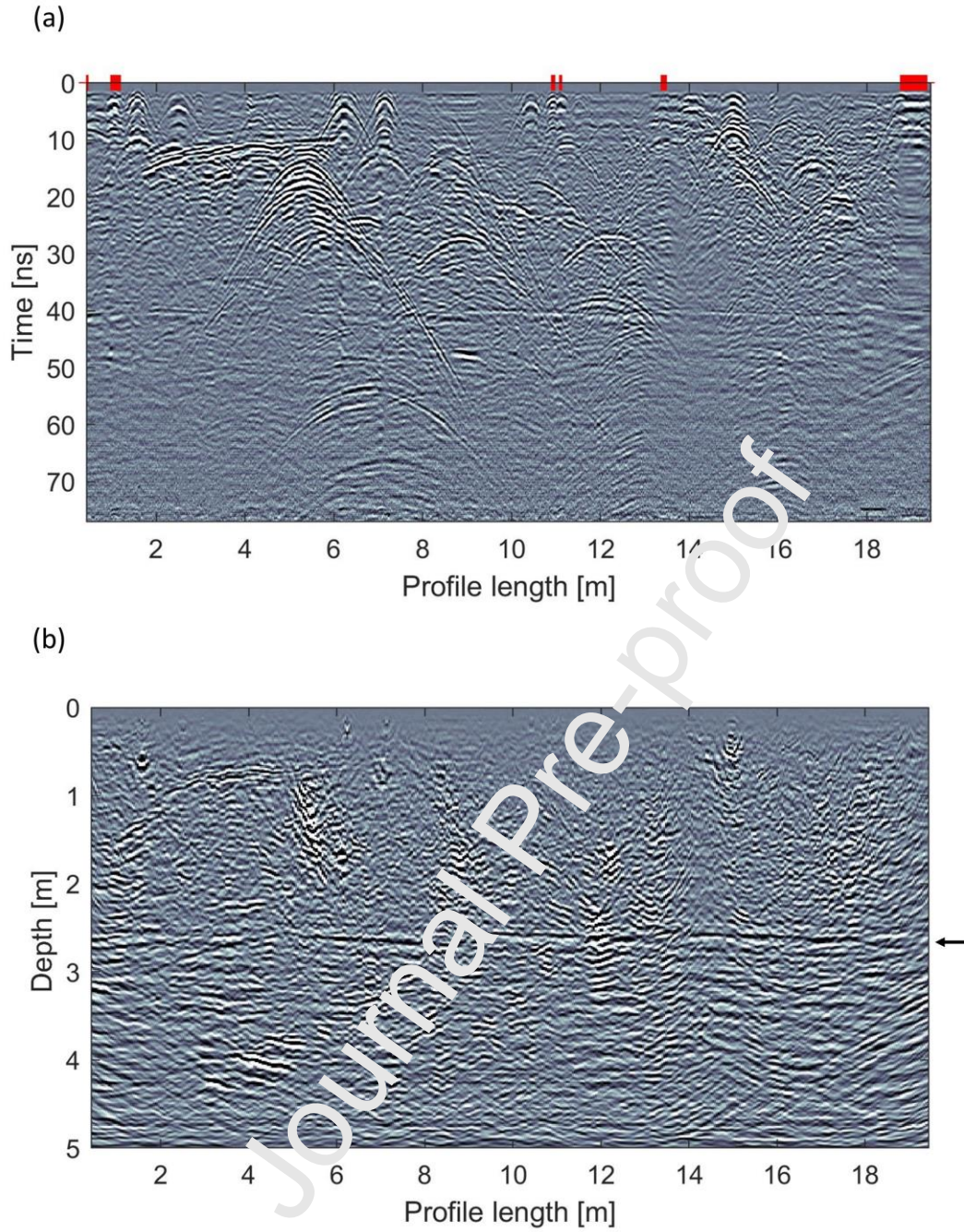


Figure 6: (a) Processed 2-D GPR slice acquired with 750 MHz antenna at $y = 2.28$ m. Red plus signs correspond to shallow boreholes and concrete plate irregularities; the corresponding traces are removed before migration. (b) Migrated data based on 3-D Kirchhoff migration with a constant velocity of 0.13 m/ns. The depth interval is chosen based on the associated resolution and depth of penetration. The large horizontal feature at a depth of 2.5 m (indicated by a black horizontal arrow) is attributed to reflections at the tunnel roof. (Figure size: 2 column fitting; Colors: yes)

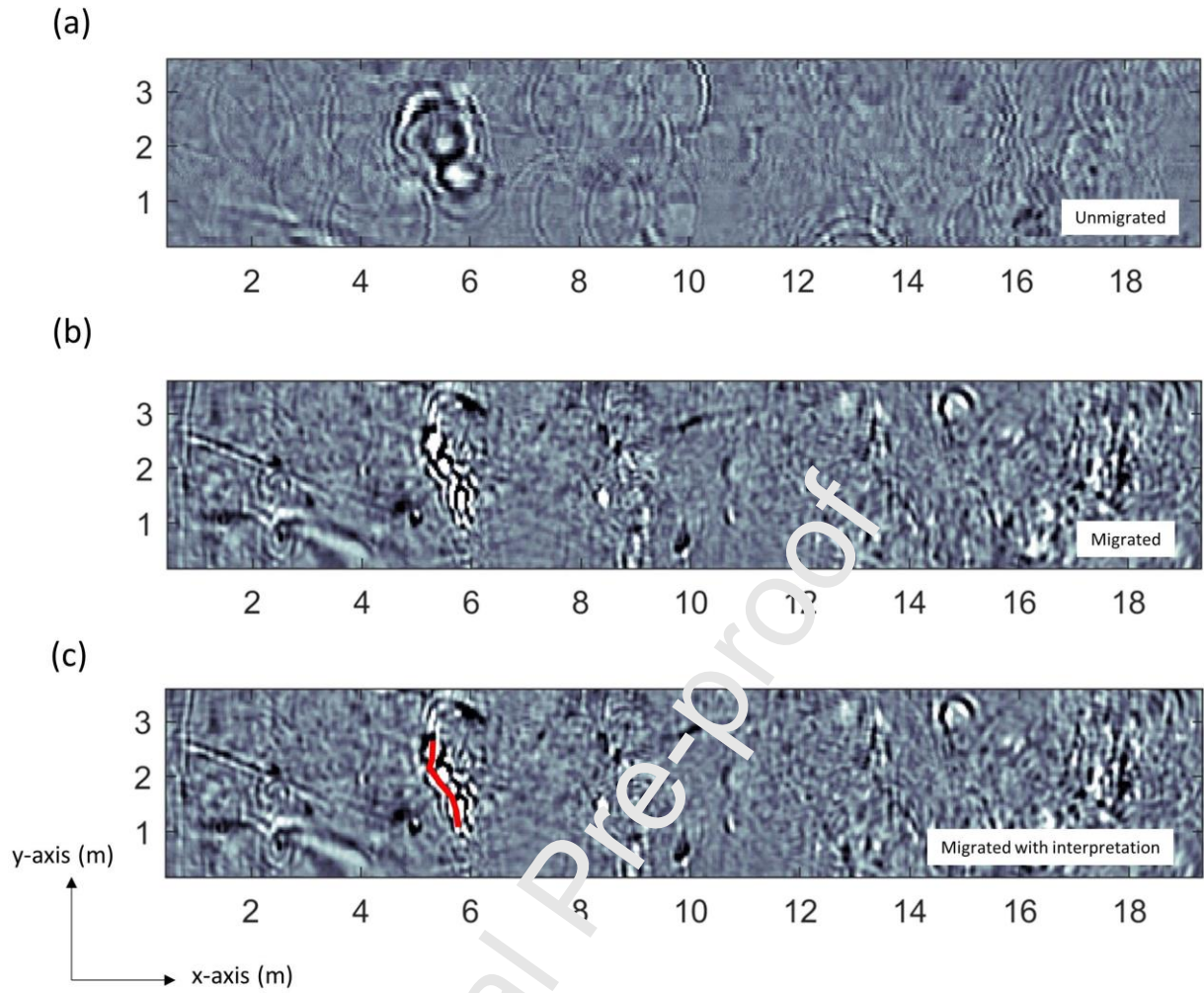


Figure 7: Depth slices obtained from 450 MHz data at 1.32 m depth illustrating diffractions that are likely due to sub-vertical fractures. (a) Unmigrated processed data to which the diffractions are represented by circular shapes. (b) Migrated data in which the diffractions collapse and (c) the corresponding sub-vertical features can be identified manually. (Figure size: 2 column fitting; Colors: yes)

5. Verification of GPR fractures with borehole data

Based on our simplified GPR fracture model, we sited three boreholes of 9.0 to 9.5 m depth with a diameter of 0.076 m: BH1 (K04018G02) in a region with multiple sub-horizontal reflections that we expected would correspond to an overall more transmissive region, BH2 (K04022G02) in a region of prominent sub-vertical reflections and diffractions with an expected significant transmissivity and BH3 (K04026G02) in a region with few GPR reflections suggesting that it would contain fewer open fractures and be less permeable than BH1 and BH2 (Figure 8). Because of technical constraints, the boreholes had to be separated by at least 3 m and located at a certain distance away from the 42 shallow pre-existing boreholes and concrete plates. The final locations of the boreholes are seen in Figure 1b.

After drilling, BH1 was sealed and its pressure was monitored during the drilling of BH2 and BH3. The same procedure was followed for BH2 during the drilling of BH3. This provides useful information about the hydraulic connections between boreholes. All boreholes were cored and imaged with a televiewer in order to map intersecting fractures. The orientation and openness of the intersecting fractures were subsequently determined from these data.

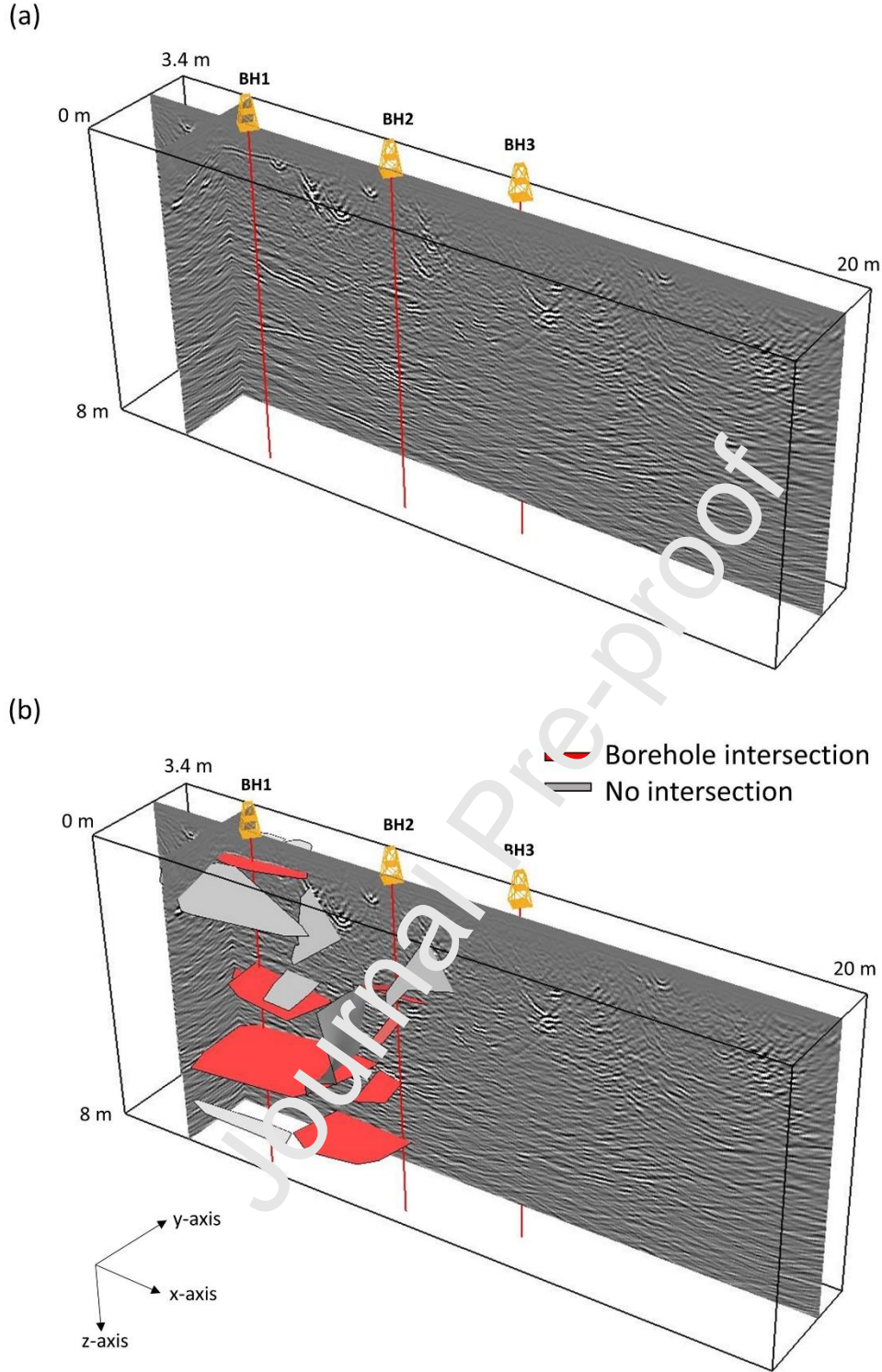


Figure 8: Fence diagrams displaying the migrated 450 MHz data. (a) The migrated GPR data based on which three boreholes (BH1, BH2 and BH3) were drilled. The basis for the borehole design is illustrated in (b) where GPR reflections corresponding to expected fractures are displayed. The strong reflections were manually picked at the interface between the background signal and the signal corresponding to the reflection of the structure. The fracture planes were constructed by the convex hull method and the fractures intersecting the boreholes are represented in red. Reflections are only interpreted in the region of fine-grained granite (first 15 m). (Figure size: 2 column fitting; Colors: yes)

5.1. Connectivity between boreholes

During the drilling of BH2, the pressure in BH1 showed two periods of net decreases (Figure 9a) corresponding to the boring of sections from 3.2 to 3.5 m depth and from 7.1 to 7.5 m depth. This suggests that BH1 is at least connected to fractures at these two section depths in BH2. During the drilling of BH3, pressure in BH1 (not shown) and BH2 (Figure 9b) showed similar behavior with three distinct decreases corresponding to the boring of BH3 in the sections from 1.9 to 2.9 m, 4.9 to 5.2 m and 6.4 to 6.9 m depth, respectively. Due to the vicinity to BH3, the pressure drop in BH2 is three times higher than in BH1. Finally, the stationary pressure (1850 kPa in BH1, 2050 kPa in BH2 and 2150 kPa in BH3) in each packed-off borehole indicates a strong hydraulic gradient from BH3 towards BH1.

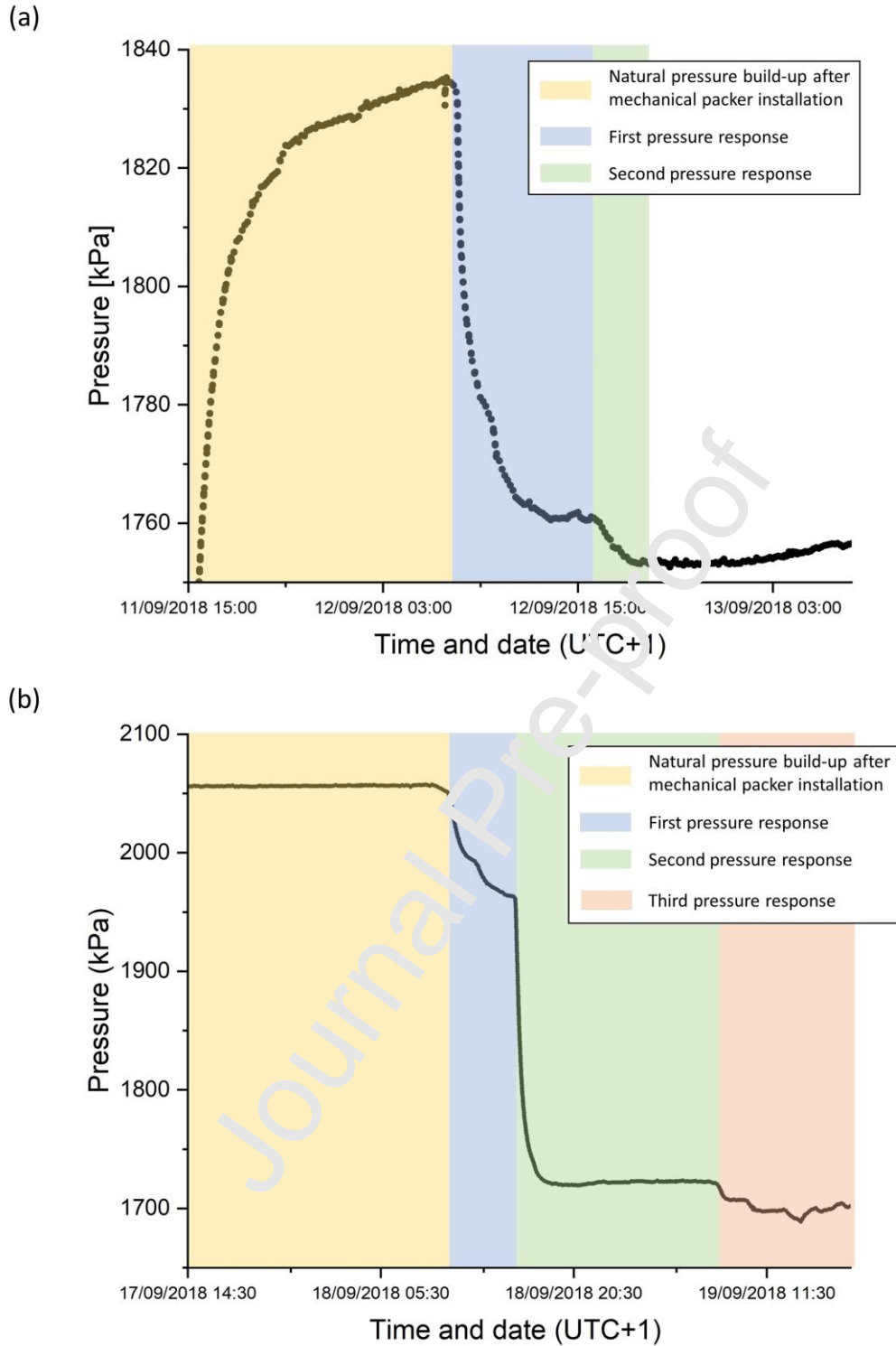


Figure 9: Pressure responses observed in observation boreholes while drilling new boreholes. Pressure response in (a) BH1 during the drilling of BH2 and (b) BH2 during the drilling of BH3. The first part of the curves (yellow) represents pressure rise due to the installation of a mechanical packer in drilled borehole at 1 m depth. The initiations of pressure drops (blue, green and orange) correspond to drilling of borehole sections (3.2-3.5 m and 7.1-7.5 m in BH2 and 1.9-2.2, 4.9-5.2 m and 6.4 m in BH3). A subsequent smaller pressure decrease is also observed in BH2 (blue part) corresponding to the drilling between 2.7 and 2.9 m in BH3. (Figure size: 2 column fitting; Colors: yes)

5.2. Hydraulic tests

The hydraulic properties of the fractured rock were estimated from injection and outflow tests in 1-m packed-off sections from 1 to 8 m depth (Andersson & Ragvald, 2019) by means of a High pressure Water Injection Controller (HWIC) equipment (Hjerne et al., 2013) that automatically measures the injection or outflow with a constant imposed pressure. Most of the tests (Table 2) were performed with outflowing conditions due to the very high ambient borehole pressure (approximately 2000 kPa). In some sections, the pressure could not return to its initial state quickly enough after an outflow test and injection tests were performed.

Of the 21 1-m sections being tested, only 5 sections (3 for BH 1, 1 for BH2 and 1 for BH3) provided a flow rate above the measuring limit of the flowmeter (2 ml/min.). Hydraulic transmissivities of the 1-m sections were then estimated by Andersson and Ragvald (2019) using Moye's formula (Moye, 1967) assuming that steady-state was reached at the end of each test:

$$T_M = Q_p \cdot \rho_w \cdot g \cdot C_M / \Delta P_p, \quad (1)$$

$$C_M = (1 + \ln(L_W / 2r_w)) / 2\pi, \quad (2)$$

where T_M is the hydraulic transmissivity (m^2/s); Q_p is the flow rate at the end of the flow duration (m^3/s); ρ_w is the water density (kg/m^3); g is the acceleration of gravity (m/s^2); C_M is the geometrical shape factor; ΔP_p is the injection/outflow pressure differences; L_W is the measurement section length and r_w is the borehole radius (m). Based on the results (Table 2), the rock is found to have a very low transmissivity with the five 1-m sections above the detection limit having transmissivities ranging between $2.2\text{-}7.0 \times 10^{-10} \text{ m}^2/\text{s}$.

The boreholes with the transmissive zones highlighted are plotted together with crossing migrated 450 MHz GPR slices in Figure 10. Strong and large sub-horizontal reflections traversing the boreholes are highlighted. Four such reflections are identified near BH1 with three of them being situated in the

transmissive zone. Along BH2, six strong (but not very large) reflectors are identified with two being situated in the transmissive zone. No strong reflectors are identified along BH3.

Table 2: Results of hydraulic tests in 1-m packed-off sections for each borehole (BH1 to BH3) using High pressure Water Injection Controller (HWIC) equipment (Hjerne et al., 2013). Pressure measured in each 1-m test section shows the variation due to the hydraulic disturbance: injection tests give positive pressures and outflow tests give negative pressures. Hydraulic transmissivity was calculated from Moya's formula (Moya, 1967). (2 column fitting)

Borehole ID	Test section (m)	Pressure (kPa)	Flow rate (L/min)	Hydraulic transmissivity (m ² /s)
BH1	1-2	200	< detection limit	
	2-3	510	< detection limit	
	3-4	-1427	-0.0033	2.2E-10
	4-5	-1086	-0.0073	6.3E-10
	5-6	-1080	-0.0065	5.6E-10
	6-7	-1449	< detection limit	
	7-8	-1376	< detection limit	
BH2	1-2	655	< detection limit	
	2-3	-1875	< detection limit	
	3-4	-1509	-0.0038	2.2E-10
	4-5	400	< detection limit	
	5-6	-1979	< detection limit	
	6-7	-1600	< detection limit	
	7-8	-1979	< detection limit	
BH3	1-2	175	< detection limit	
	2-3	-833	< detection limit	
	3-4	191	< detection limit	
	4-5	-1300	-0.0097	7.0E-10
	5-6	-1600	< detection limit	
	6-7	-1659	< detection limit	
	7-8	-1300	< detection limit	

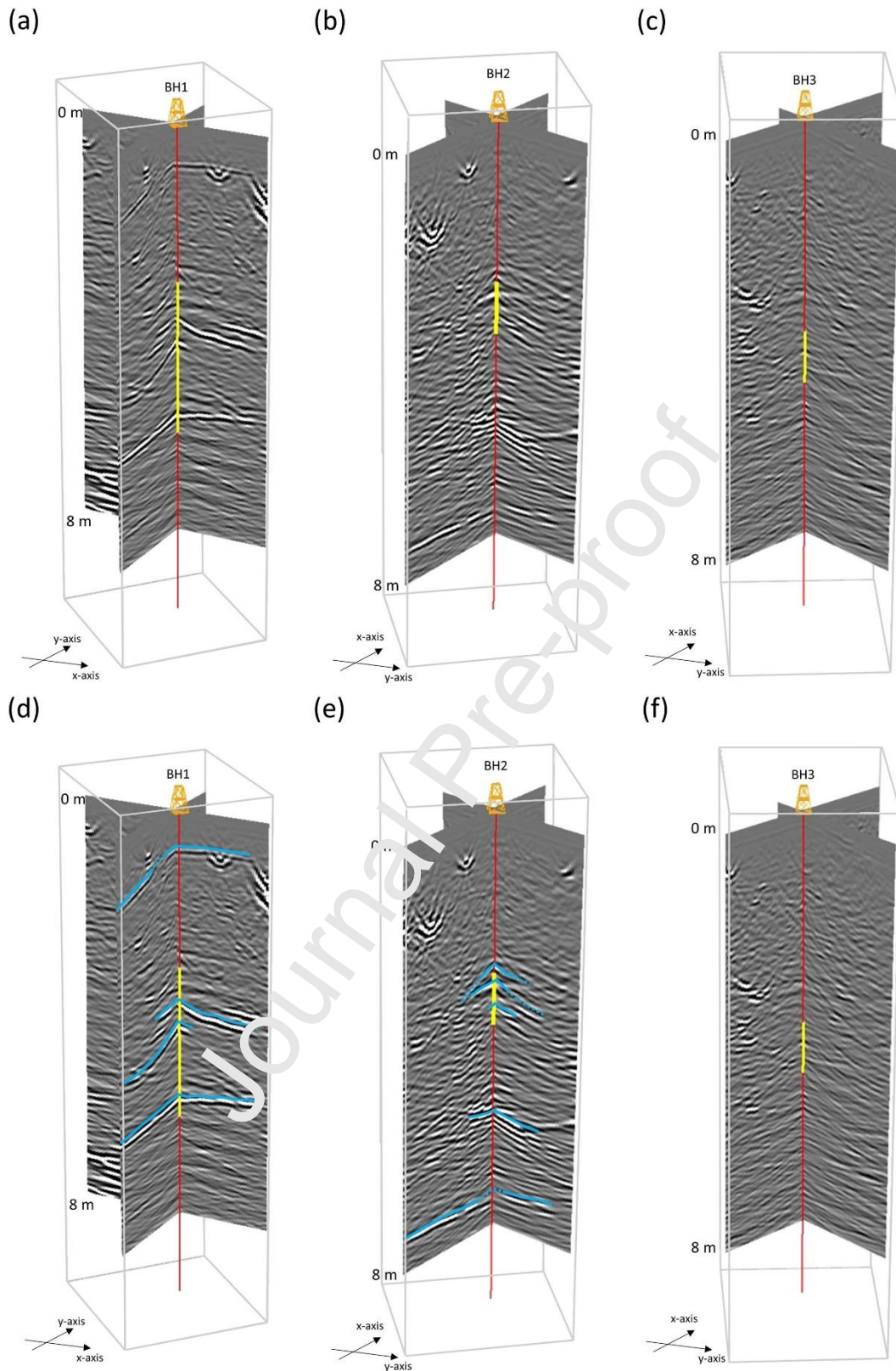


Figure 10: Fence diagrams displaying migrated data (450 MHz) crossing each borehole (BH1, BH2 and BH3). The yellow vertical line segments indicate transmissive 1-m sections as determined by water injection tests, while the red sections induce less flow than the detection limit of 2 mL/min. Transmissive 1-m sections are located between 3 and 6 meters depth in BH1, between 3 and 4 m of depth in BH2 and between 4 and 5 m depth in BH3. Uninterpreted GPR sections along BH1 (a), BH2 (b) and BH3 (c) and interpreted GPR sections where strong reflections are represented in full blue lines, while blue dashed lines correspond to the potential extensions of the reflectors along BH1 (d), BH2 (e) and BH3 (f). (Figure size: 2 column fitting; Colors: yes)

5.3. Fracture mapping

Fracture characteristics (e.g., position, depth, strike, dip, filling mineralogy, open/sealed information) were obtained by Optical Televiewer (OPTV) and core logging (Andersson & Ragvald, 2019). With the position and orientation information, we could implement the fractures into our database, describing the fractures as disks centered on the boreholes. This enables a detailed assessment of the agreement between the GPR reflections and the fractures seen in the core logging (Figure 11, Figure 12, Figure 13).

We present the fracture positions in terms of depth, orientation (strike and dip) and opening (sealed or open) using tadpole plots (Figure 11a, Figure 12a and Figure 13a). This interpretation is based on televiewer and core inspection in the laboratory. Each borehole is represented by a cylinder divided into 1-m sections used for hydraulic measurements with indication of GPR reflections crossing the borehole and the sections with recorded outflow, above the measurements limit (Figure 11b, Figure 12b and Figure 13b). Fence diagrams are used to highlight strong GPR reflections along the boreholes and to compare them with fractures seen on cores (Figure 11c,d, Figure 12c,d and Figure 13c). To do so, we superimposed fractures from core log data on the GPR sections crossing the borehole, and observed the match based on fracture depth, strike and dip. We assume that a GPR fracture matches a fracture intersection trace if their depth and dip do not exceed a deviation of 0.3 m and 15° , respectively (Table 3). The strike is also used to assess the fracture matching, but its uncertainty is particularly high for sub-horizontal fractures. Consequently, we used a maximum strike deviation of 60° . The corresponding fracture intercepts are well seen in the OPTV images (Figure 11e,f, Figure 12e,f and Figure 13d).

Along BH1 (Figure 11), we observed four strong reflections that match very well with four fractures seen on cores. The maximum disagreement in terms of fracture depth, dip and strike are 0.1 m, 6° and 54° , respectively (Table 3). The fractures have all been interpreted as open and three of them are located in the transmissive region (above the flow measurement threshold) while the remaining

fracture is located in the 0 to 1 m interval where no hydraulic tests were made. We note that this corresponds to a rather ideal case for GPR data, as the identified transmissive fractures all have low dips for which the GPR reflections are the strongest.

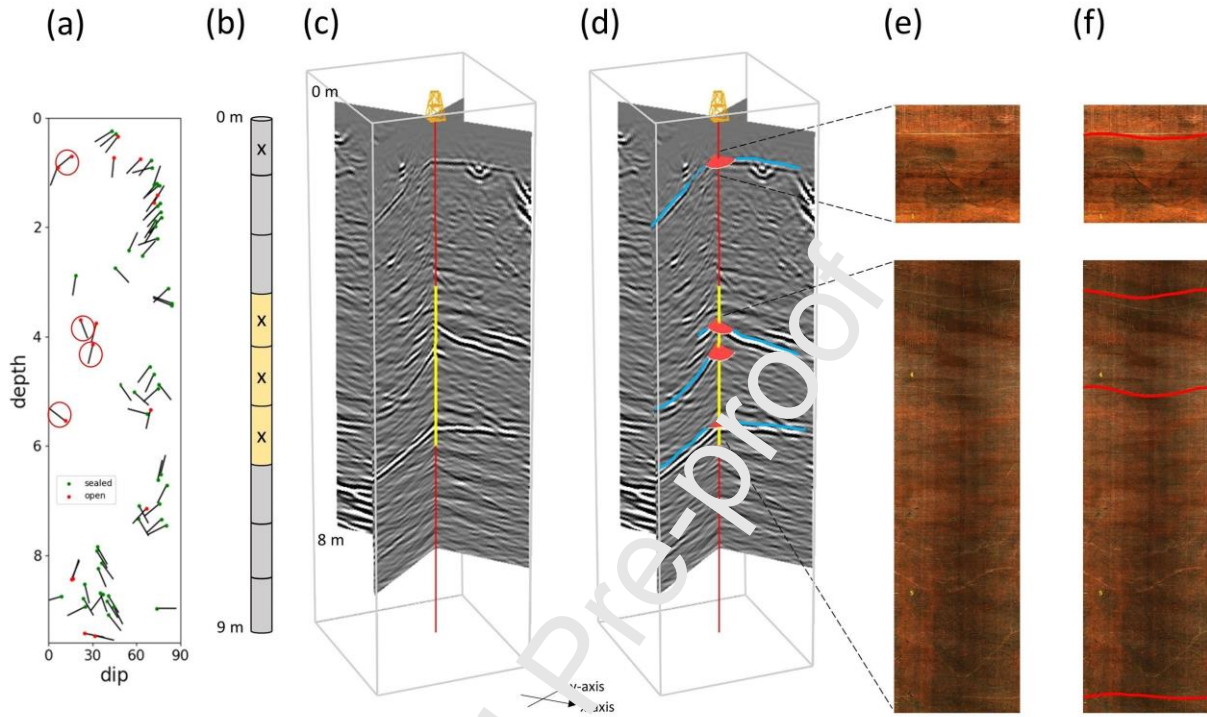


Figure 11: Comparison of core log, hydraulic and GPR data for BH1. (a) Tadpole plot representing the fracture characteristics (depth, orientation and aperture) along the borehole. The circle symbols show the fracture localization in term of depth (y-axis) according to their dip (x-axis). The red and green colors correspond to the open and sealed fractures. The ended black tails represent the direction of the dip, with North (0° and 360°), East (90°), South (180°) and West (270°) being up, right, down and left respectively. The fractures matching by the depth, dip and/or strike with GPR reflectors are encircled in red. (b) Borehole representation with transmissive sections (yellow) and strong reflections (cross in the middle of the sections). Fence diagrams display migrated GPR data (450 MHz) crossing BH1 (c) before and (d) after interpretation. The identified transmissive zones are represented in yellow and fractures logged along the borehole and matching (by depth, strike and/or dip) with strong GPR reflections (blue lines) are symbolized by red disks (open fracture) centered on the borehole. (e) Uninterpreted and (f) interpreted Optical Televiwer images showing the fracture traces on borehole walls. Fractures matching with GPR reflectors are underlined in red lines. Yellow depth scale corresponds to the depth recorded by the Televiwer. (Figure size: 2 column fitting; Colors: yes)

Along BH2 (Figure 12), five reflections have been identified (Figure 10) that are generally less strong than those crossing BH1. Since the fractures observed in this borehole are mostly composed by sub-vertical fractures (75%), the surface GPR data contain multiple diffractions (Figure 5) that clutter the resulting migrated images and make the match with any sub-horizontal fractures non-trivial. This superposition of energy is particularly present in the area situated between 2.8 and 3.8 m. The two first reflections seem to match with two sets of closely separated sub-horizontal fractures that are

interpreted as open. Each set is composed by two fractures separated by 0.1 m. The first set is well correlated in terms of depth, dip and strike with the first reflector. The second set is well correlated in terms of depth and strike with the second reflector while the dip is above the threshold. The third reflection matches well in terms of depth, dip and strike with a fracture at 3.7 m of depth (Table 3). These five open fractures are concentrated in the zone where flow could be measured (the first fracture is situated at 0.1 m above this measured section). The strong reflector that appears to cross the borehole at 5.7 m depth does not correspond to any borehole fractures. Such a mismatch can be explained by the fact that borehole data give punctual information while GPR gives a measure that is averaged on a roughly metric scale. This implies that the geological heterogeneity or fracture corresponding to this reflection could be next to the borehole. The last reflector, matching in terms of depth, strike and dip with an open fracture at 7.4 m, is located in the borehole section (7.13 to 7.54 m) that produced a pressure response in BH1 during the drilling of BH2. Even if its transmissivity could not be determined because of the minimum threshold, it does provide a strong GPR reflection. This suggests that this fracture is locally less permeable at the borehole location, which is also indicated by the GPR reflectivity that is significantly increased away from the borehole.

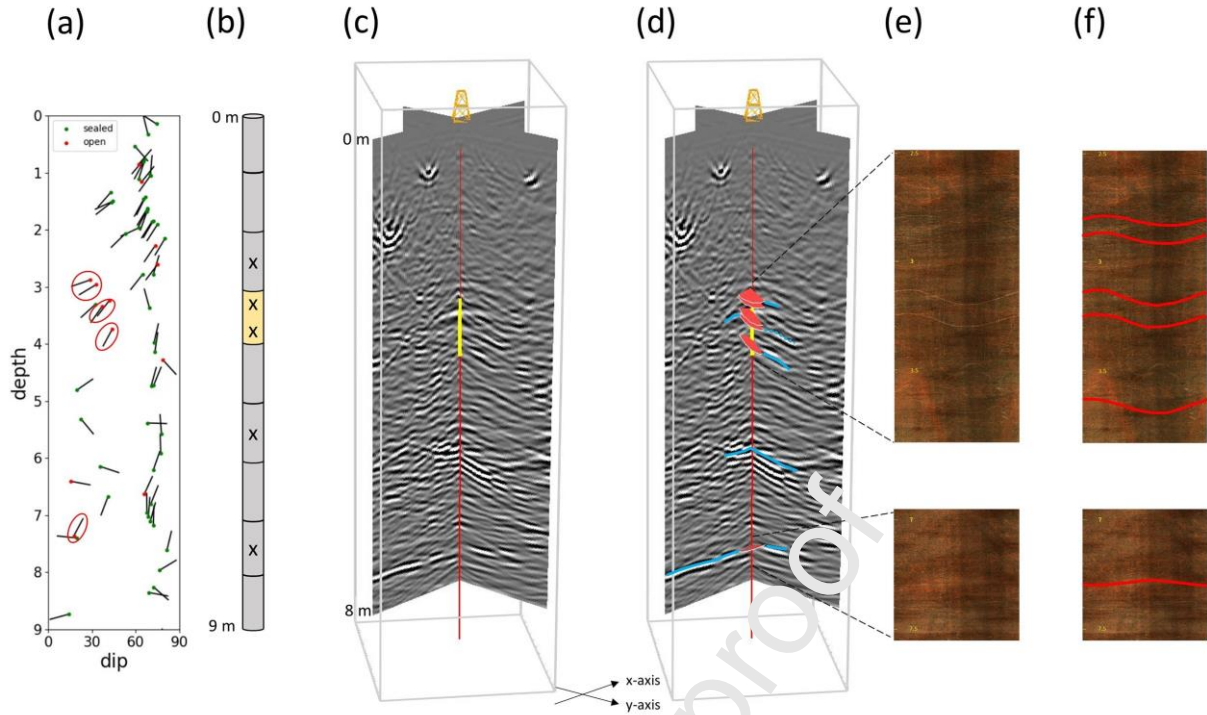


Figure 12: Comparison of core log, hydraulic and GPR data for BH2. (a) Tadpole representing the fracture characteristics (depth, orientation and aperture) along the borehole. The circles, symbols show the fracture localization in term of depth (y-axis) according to their dip (x-axis). The red and green colors correspond to the open and sealed fractures. The ended black tails represent the direction of the dip, with North (0° and 360°), East (90°), South (180°) and West (270°) being up, right, down and left respectively. The fractures matching by depth, dip and/or strike with GPR reflectors are encircled in red. (b) Borehole representation with transmissive sections (yellow) and strong reflections (cross in the middle of the sections) Fence diagrams display migrated GPR data (450 MHz) crossing BH2 (c) before and (d) after interpretation. The identified transmissive zones are represented in yellow and fractures logged along the borehole and matching (by depth, strike and/or dip) with strong GPR reflections (blue lines) are symbolized by red disks (open fracture) centered on the borehole. (e) Uninterpreted and (f) interpreted Optical Televiewer images showing the fracture traces on borehole walls. Fractures matching with GPR reflectors are underlined in red lines. Yellow depth scale corresponds to the depth recorded by the Televiewer. (Figure size: 2 column fitting, Colors: yes)

BH3 is mostly composed by sub vertical (90%) and sealed (80%) fractures that highly limit the possibility of imaging fractures with the surface GPR method. In the transmissive region, all open fractures have dips exceeding 60°. Consequently, no GPR fracture was identified (Figure 10, 13).

The match between GPR data and borehole data (pressure, hydraulic and core logging data), for BH1 and BH2, shows that fractures interpreted by GPR are mostly situated in the most transmissive hydraulic sections measured along boreholes. Most remaining GPR reflections showed correlation with depth sections being connected to other boreholes (pressure measurements) or matched with fractures from borehole (core log data). In one case, it had to be assumed that the fracture was positioned just next to the borehole. The reason that no fracture is seen by GPR along BH3, despite

that it contains the most permeable 1-m section, is explained by the significant number of sub-vertical fractures, highlighting the well-known fact that surface-based GPR is unable to image very steeply dipping fractures.

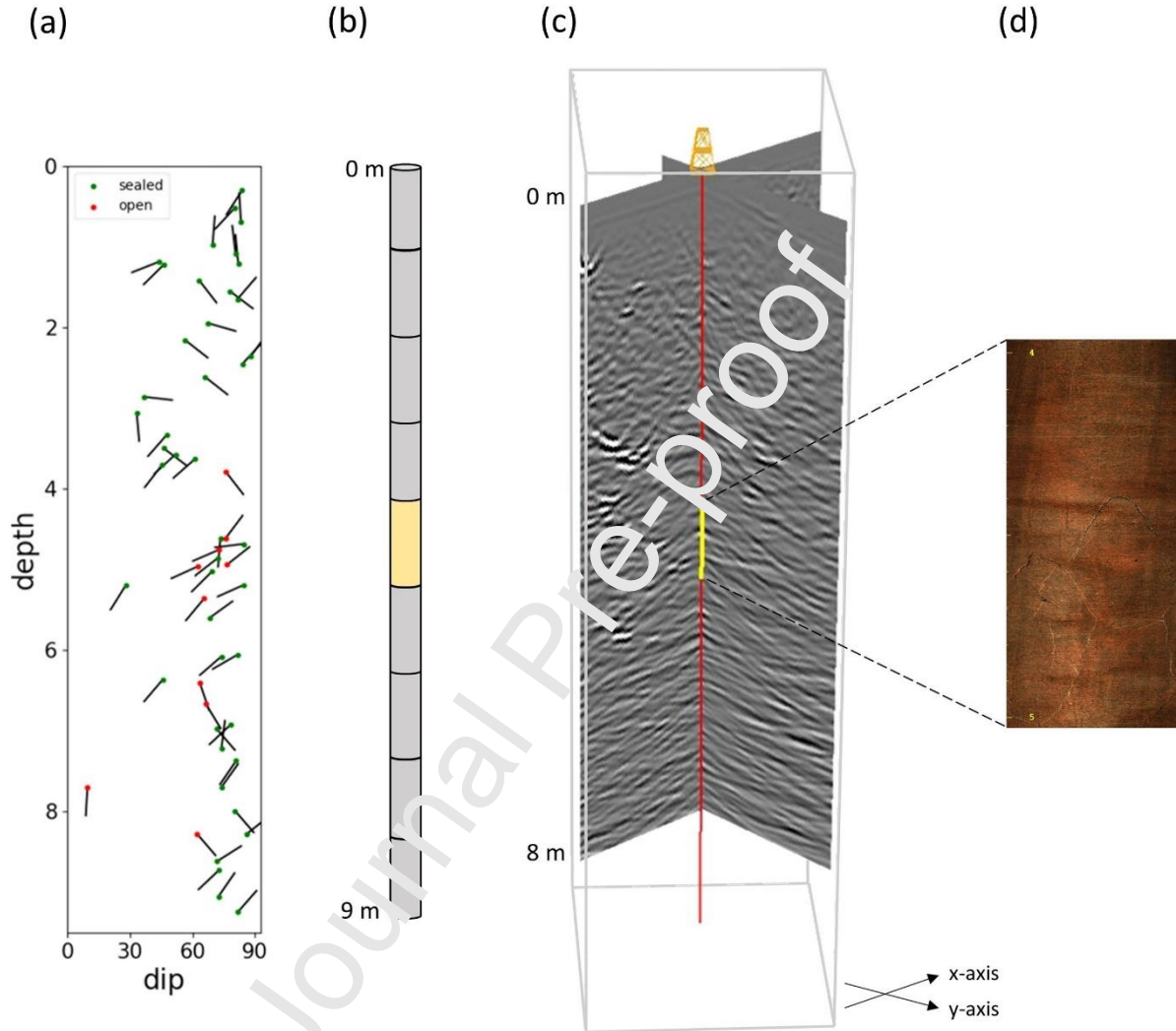


Figure 13: Comparison of core log, hydraulic and GPR data for BH3. (a) Tadpole plot representing the fracture characteristics (depth, orientation and aperture) along the borehole. The circle symbols show the fracture localization in term of depth (y-axis) according to their dip (x-axis). The red and green colors correspond to the open and sealed fractures. The ended black tails represent the direction of the dip, with North (0° and 360°), East (90°), South (180°) and West (270°) being up, right, down and left respectively. (b) Borehole representation with transmissive sections (yellow). No strong GPR reflections are listed. Fence diagrams display migrated GPR data (450 MHz) crossing BH3 (c). The identified transmissive zone is represented in yellow. No reflector is seen along the BH3 and no matching could be done. (d) Optical Televue images showing the transmissive zone composed mostly by open fractures with dips $>60^\circ$. Yellow depth scale corresponds to the depth recorded by the Televue. (Figure size: 2 column fitting; Colors: yes)

Table 3: Matching criteria based on the depth, strike and dip comparison between GPR reflectors (R) and core logged fractures (F). A maximum threshold was defined: 0.3 m for depth, 15° for dip and 60° for strike. The matching criteria is validated when the gap (calculated by subtracting values from R and F) is below the threshold (v). Any values above this threshold are rejected (x). (2 column fitting)

Borehole ID	Depth (m)			Strike (° N)			Dip (°)			Matching criteria		
	R	F	Gap	R	F	Gap	R	F	Gap	Depth	Strike	Dip
BH1	0.7	0.7	0	166	141	25	10	16	6	v	v	v
	3.7	3.7	0	123	69	54	22	22	0	v	v	v
	4.2	4.1	0.1	141	104	37	24	30	6	v	v	v
	5.6	5.5	0.1	188	218	30	8	11	3	v	v	v
BH2	2.9	2.9	0	181	161	20	27	29	2	v	v	v
		3.0	0.1		149	32		33	6	v	v	v
		3.2	0		128	11		42	36	v	v	x
	3.2	3.3	0.1	117	125	8	6	37	31	v	v	x
	3.7	3.7	0	84	119	35	30	44	14	v	v	v
	5.7	/	/	102	/	/	18	/	/	x	x	x
	7.4	7.4	0	329	298	30	11	18	7	v	v	v

6. Statistical completeness and GPR agreement

The proportion of existing fractures that are identified by GPR likely depends on the fracture size, orientation and filling content. In order to estimate this ratio, we derived the 3-D orientation and size distribution of fractures from the fracture traces observed in the surrounding tunnel walls. The following sections describe the methodology used and compare the density of GPR-observed fractures to the expected values derived from this 3-D density distribution.

6.1. Tunnel data (size and orientation distributions of fracture traces)

In addition to the tunnel (TASu4) in which the GPR experiment was carried out, we also used information from two parallel (TAS05 and TASN) and one perpendicular tunnel (TASP). A total of 3513 fracture traces have been observed on tunnel walls and stored in the SKB database together with their fracture characteristics: trace length, orientation (dip and strike), aperture, mineral filling and fracture shape. The trace length density distribution per unit surface is shown in Figure 14. It exhibits two different scaling behaviors above and below 3.6 m even after removing censoring and edge biases (Laslett, 1982), that is, fracture traces smaller than 1 m and larger than 8.6 m. The observed trend is fitted by a power law with a scaling exponent of -2 for small traces and -3 for large

ones. This two-power-law trace size distribution model is consistent with the analysis of outcrop maps in the same area (Davy et al., 2010).

The stereonet of fracture trace orientation poles (i.e., one pole per fracture) is given in Figure 15a. It shows three main orientation poles: two vertical ones trending NW and NE, and one horizontal. The comparison of the fracture trace orientation with those of the GPR fractures is described in section 6.3.

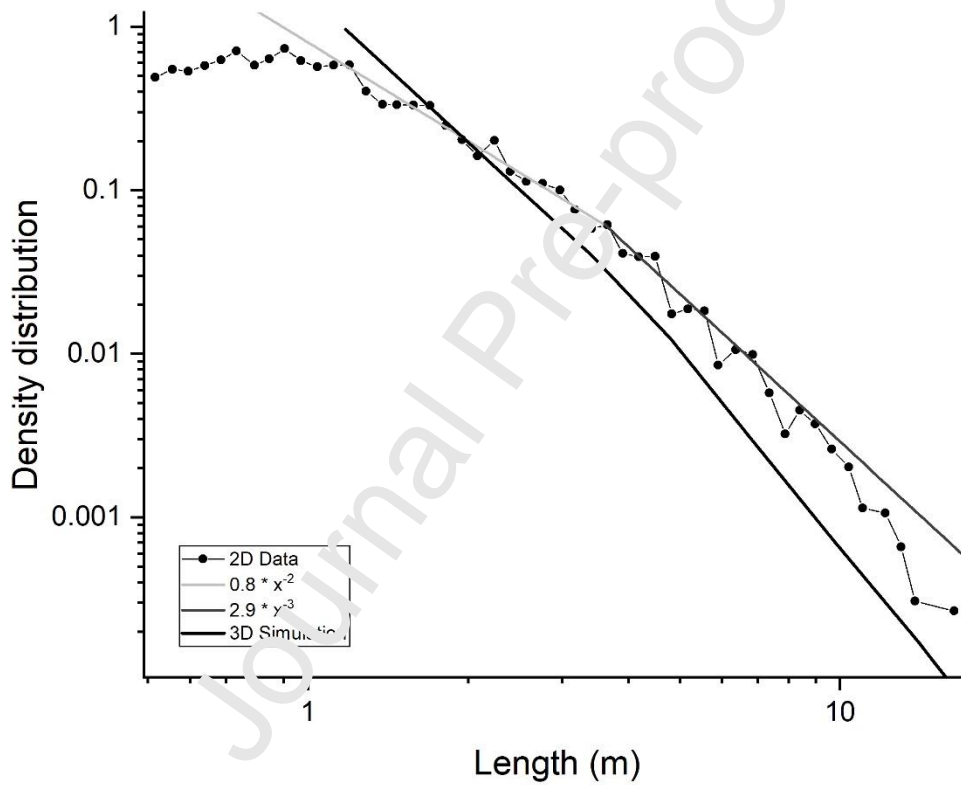
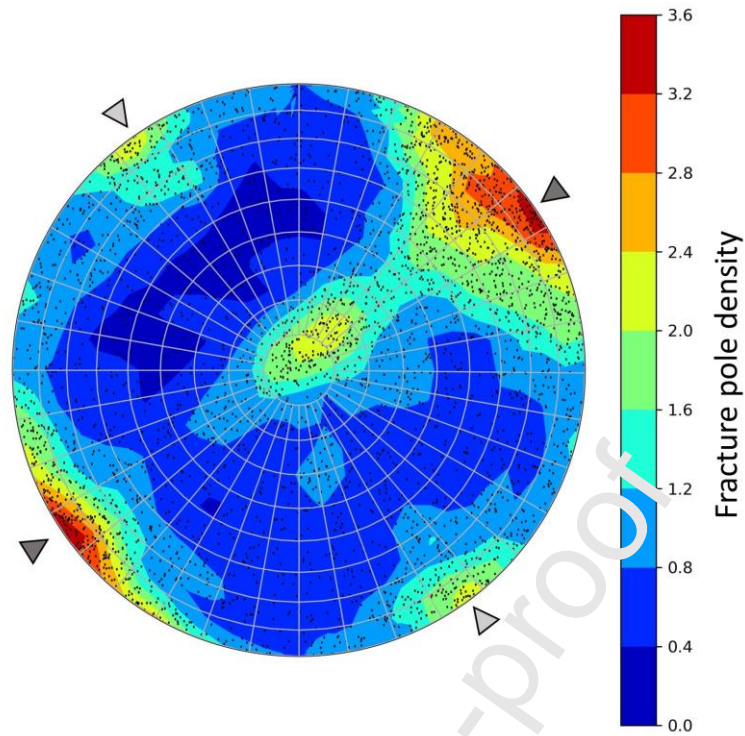


Figure 14: Trace and fracture length density distribution per unit surface and volume, respectively. The trace length distribution is represented by black dots corresponding to the number of fracture traces observed on tunnel walls normalized by tunnel surfaces (y-axis), in size ranges using logarithmic binning. The fits of the trend are represented by light and dark gray curves for fractures smaller and larger than 3.6 m, following a power law. The corresponding 3-D distribution (black curve) was calculated from stereological rules (Piggott, 1997) applied to trace data. (Figure size: 2 column fitting; Colors: no)

(a)



(b)

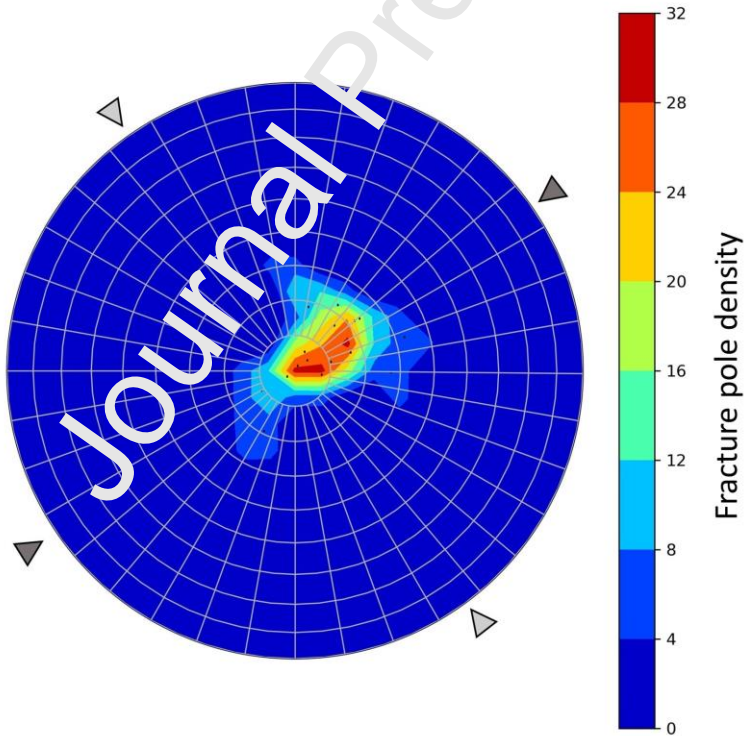


Figure 15: Stereonet representation (equal area projection) showing fracture orientation poles (black dots). The strike is indicated around the circle, with North (0° and 360°), East (90°), South (180°) and West (270°) being up, right, down and left respectively while the dip is seen from the middle (0°) to the edge of the stereonet (90°). The density color scale represents the fracture density distribution according to orientation units, explaining higher density values for GPR fracture orientations. Tunnel orientations are represented by dark (TASP) and light (TAS04, TAS05 and TASN) gray triangles. (a) Representation of the fracture trace orientation poles (3513) showing two vertical trending (NW and NE) following the tunnel directions and one horizontal (middle of stereonet), (b) fracture pole orientations imaged by GPR (17) showing a horizontal trend of the fractures. (Figure size: 2 column fitting; Colors: yes)

6.2. 3-D statistical model

The 3-D statistical model is calculated by assuming disk-shaped fractures and that the orientation distribution is similar for all fracture sizes in the target range (1-8 m). The statistical model is based on trace size distribution and orientation developed in section 6.1 and its consistency has been checked on three realizations.

The 3-D distribution parameters (density and power law exponent terms) are calculated according to the stereological rules described by Piggott (1997). These rules were initially applied for an infinite surface with fractures having uniform orientation. Nevertheless, they have been tested by several simulations for non-uniform fractures sampled on cylindrical tunnels and it shows that Piggott's rules can be applied for fractures sampled on tunnel walls (Appendix A). For a power law and assuming that fractures are disk shaped, the relation is:

$$a_{3D} = a_{2D} + 1, \quad (3)$$

$$\alpha_{3D} = \alpha_{2D} \sqrt{\pi} \frac{\Gamma\left(\frac{2+a_{2D}}{2}\right)}{\Gamma\left(\frac{3+a_{2D}}{2}\right)}, \quad (4)$$

where a_{2D} and a_{3D} are the 2-D and 3-D exponents of fracture traces and sizes, respectively, and α_{2D} and α_{3D} are the density terms in 2-D and 3-D, respectively. The calculated 3-D density parameters are $\alpha_{3D} = 1.6$ and $a_{3D} = 3$ for fracture sizes between 1 m and 4.2 m and $\alpha_{3D} = 6.8$ and $a_{3D} = 4$ for fracture lengths above 4.2 m.

The fracture orientations are calculated from the occurrence of fracture traces by applying a weighting factor equal to the angular correction of Mauldon and Mauldon (1997) for a cylindric tunnel and fracture sizes smaller than the tunnel diameter:

$$\omega(\theta) = \sqrt{\frac{2}{1 + \cos^2(\theta)}}, \quad (5)$$

where θ is the angle between the fracture pole and the tunnel direction.

We verify from direct simulations (i.e., calculating fracture traces from a 3-D fracture network generated with the size and orientation distribution deduced from equations (3), (4) and (5)) that the model is consistent with data, and consequently that:

- The cylindric-shape assumption is valid even if tunnels have more complex shapes;
- The two-power-law model is required to honor the observed trace distribution. We check that the large-scale power-law regime is distinct from the finite-size effect due to the tunnel diameter.

Considering the density and orientation characteristics, the 3-D distribution of fracture sizes is then calculated (Figure 14), which gives the number of fractures per unit area, per unit pole angle and per unit volume.

6.3. Comparison with GPR fracture distribution

The comparison with the orientation distribution deduced from fracture traces shows that the GPR fracture orientation (picked from all frequencies, corresponds to the sub-horizontal poles (dip $< 35^\circ$) of the fracture traces (Figure 15b). Since the GPR has imaged the fractures with area from 1 to 10m^2 and dip less than 35° , we compared the same fracture population in the 3-D statistical model. We first estimated the detection capacity of GPR by dividing the observed density (total surface by unit of volume per dip range) with the 3-D modeled density calculated in the section 6.2 (Figure 16a). The observed fluctuations between 0 and $20\text{--}25^\circ$ may be due to the limited number GPR fractures, but there is a clear cut-off of detection above 25° even if some GPR fractures are detected between $25\text{--}35^\circ$. On average, 5.5% of the fractures with area of $1\text{--}10\text{m}^2$ were detected by GPR. This result is a direct consequence of the geometry of the GPR antenna, where the surface-based acquisition favors the imaging of sub-horizontal fractures. This ratio rises to 42% for any type of fracture apertures (opened or sealed) when considering fractures dipping less than 25° . The ratio of open fractures in the borehole data (Table 4) is 53% for fractures dipping less than 25° . Assuming that this is also the

ratio for 1-10 m² fractures, we find that the GPR method is likely imaging 80% of the open fractures with dip <25°.

According to the GPR fracture dip cut-off, the area distribution of GPR fractures have been calculated (e.g., number of fractures per unit area and unit volume) for all fractures dipping less than 25° (Figure 16b). In a log-log plot, it appears to follow the same power-law trend as the 3-D modeled area distribution. The dashed line represents the plot of the modeled distribution area for fractures in the same dip range considering that 80% of the actual fractures are detected. A remarkable result is that it fits well the GPR data within the data uncertainties (Figure 16b). The fact that the fracture area distribution in the range 1-10 m² is similar to the 3-D area distribution modeled by extrapolating the tunnel fracture traces means that the GPR is able to image the fractures in proportion to the length distribution trend (no size selection). This is a promising result, but it does not offer a definite conclusion because of the small number of GPR fractures, and because of the uncertainty on the modeled distribution due to the assumptions used.

Table 4: Ratio of GPR detection according to fracture parameters: dip and aperture. Analysis is focused on the open fractures intersecting the boreholes (BH1 to BH5), dipping less than 25°.

Fracture parameters		Borehole fractures	GPR
Dip	Aperture	Number	Imaging probability
0-90°	open + sealed	188	5.5 %
< 25°	open + sealed	19	41.6 %
< 25°	open	10 (52.6 %)	79.1 %

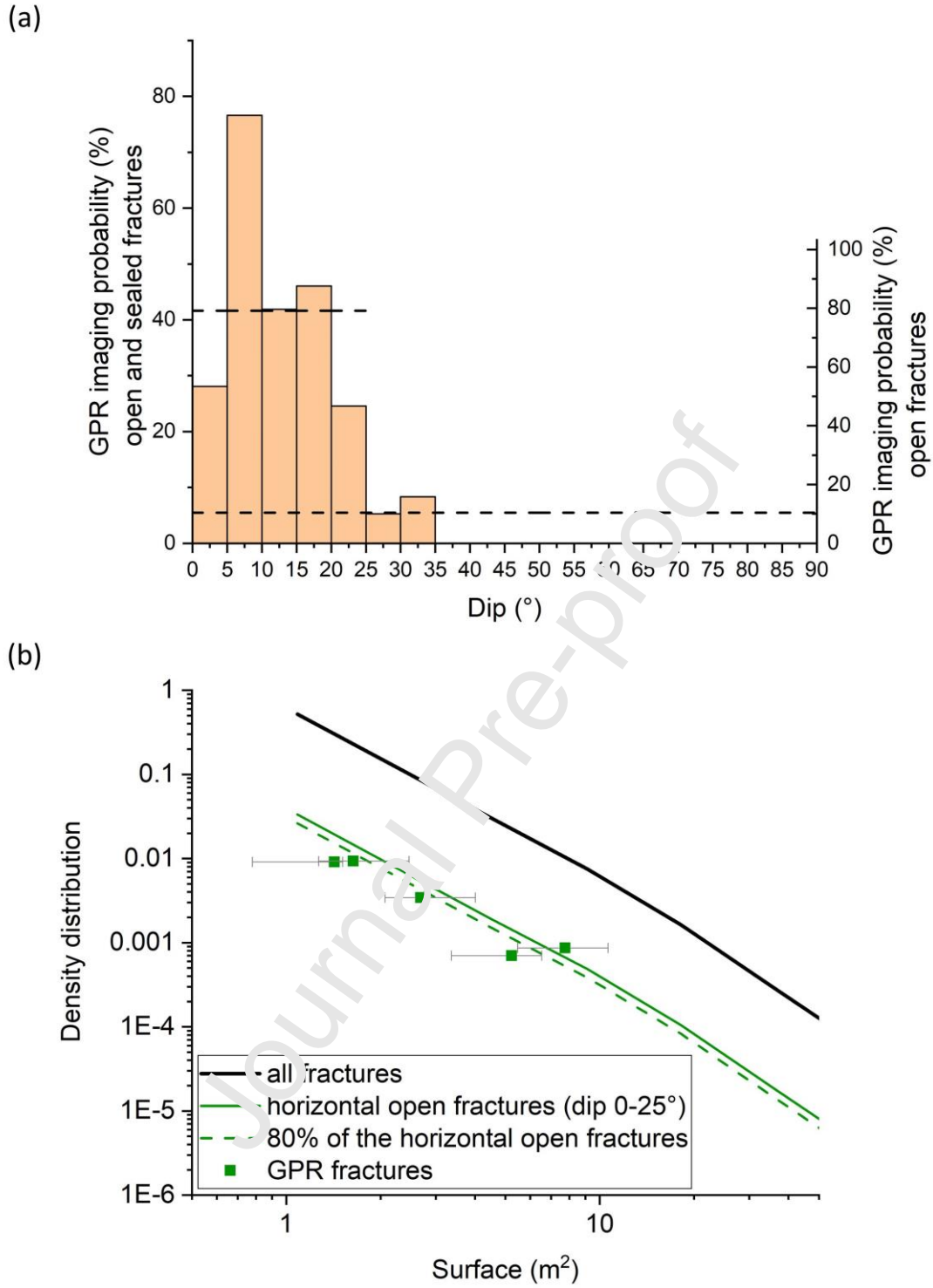


Figure 16: (a) GPR detection capacity for open and sealed (left y-axis) and open (right y-axis) fractures having an area between 1 and 10 m^2 according to the dip (x-axis). The detectability cut-offs are represented by black dashed curves (b) Comparison of the modeled 3-D density and GPR density distribution. The area distribution of GPR fractures (y-axis) included in area ranges using an overlapping logarithmic binning (x-axis). Gray bars represent the data uncertainties corresponding to bin limits. The 3-D density model deduced from fracture traces comprised in dip ranges of $[0-90^\circ]$, $[0-25^\circ]$ and $[0-25^\circ]*80\%$ are represented by black curve, green curve and dashed green curve, respectively. (Figure size: 2 column fitting; Colors: yes)

7. Conclusions and perspectives

The purpose of this work was to assess the ability of the GPR method to image fractures with sub-millimetric aperture in a very low permeable crystalline rock. To do so, we performed surface-based measurements in a tunnel situated at 410 m depth. GPR profiles were measured in a 3-D configuration (3.4 m x 19 m) using three frequencies (160, 450 and 750 MHz). A total of 17 sub-horizontal reflections were manually picked from the 3-D acquisition block, whose minimum and maximum length were 0.8 m and 5 m, respectively. To define the nature of these reflections, three boreholes (BH1-BH3; 9-9.5 m deep) were drilled. A very good correlation in terms of depth and orientation between the GPR reflections crossing BH1 and BH2 and the open transmissive fractures dipping $< 35^\circ$ located in boreholes was established. The lack of reflections along BH3 is explained by the sub-vertical orientation of the fractures crossing the borehole.

We derived a 3-D statistical fracture density model from fracture traces observed on surrounding tunnels walls. This density model predicts the expected number of fractures in the domain for given orientations and sizes, thereby, enabling comparison with the distribution of GPR fractures. The comparison is made for fracture areas in the range $1\text{-}10\text{ m}^2$, which contains most of the GPR fractures detected by 160, 450 and 750 MHz antennas. The percentage of fractures detected by GPR is:

- 5.5 % of all the observed fractures regardless of orientation or if they are open or sealed;
- 42 % of the fractures dipping less than 25° ;
- 80 % of open fractures dipping less than 25° .

In addition, the dependency with size of the GPR fracture density distribution is similar to the real fracture density distribution. Both size distributions fit perfectly if one considers the sub-network of open fractures dipping less than 25° . This result indicates that there is no size selection in the range of $1\text{-}10\text{ m}^2$ by GPR imaging (the ratio between the fracture size is conserved).

We conclude that GPR imaging can be very efficient to detect open sub-horizontal fractures with sub-millimeter aperture. The resolution of the present statistical analysis is limited to ~ 1 m, mainly because of the cut-off of fracture traces during the tunnel mapping, which constrained the comparative analysis to this minimum fracture size. The largest fractures and the fracture orientations are limited by the geometry of the acquisition setup. Further work is planned to use time-lapse GPR imaging for tracing solute transport in the fracture network similarly to Dorn et al. (2011b) and Shakas et al. (2016). The main objective of this experiment is to hydraulically characterize the fracture media and identify the potential conduit for flows.

Appendix A: Piggott stereology tested on non-uniform orientation and cylindrical outcrops

Piggott (1997) derived the stereological rules that give the 3-D size distribution of uniformly-oriented disk fractures from a power-law size distribution of fracture traces measured on an infinite plane :

$$a_{3D} = a_{2D} + 1 ,$$

$$\alpha_{3D} = \alpha_{2D} \sqrt{\pi} \frac{\Gamma\left(\frac{2+a_{2D}}{2}\right)}{\Gamma\left(\frac{1+a_{2D}}{2}\right)},$$

with a_{2D} and a_{3D} being the 2-D and 3-D exponents of fracture traces and sizes, respectively, and α_{2D} and α_{3D} being the density terms in 2-D and 3-D, respectively.

Here we test whether similar rules can be applied to a finite cylindrical tunnel. For this, we run 3-D simulations where fracture networks are generated with a power-law size distribution and non-uniform orientations, and fracture traces are identified on the wall of a cylindric tunnel. We then calculate the trace size distributions, fit them with a power law, and compare the fit with Piggott's formulae (Figure A 1). The ratio between the power-law fits and Piggott's formulae reaches 1.5, 1.2, 1.1 and 1 for a_{2D} of 2.0 (165213 fractures and 2834 fracture traces), 2.5 (1156665 fractures and 1479 fractures traces), 3.0 (924152 fractures and 1007 fracture traces) and 3.5 (786477 fractures and 791 traces) respectively. To support our analysis, we compare the fracture trace size distribution observed on tunnel walls with our statistical model generated with a double power-law size distribution and orientation bootstrapped from data (Figure A 2).

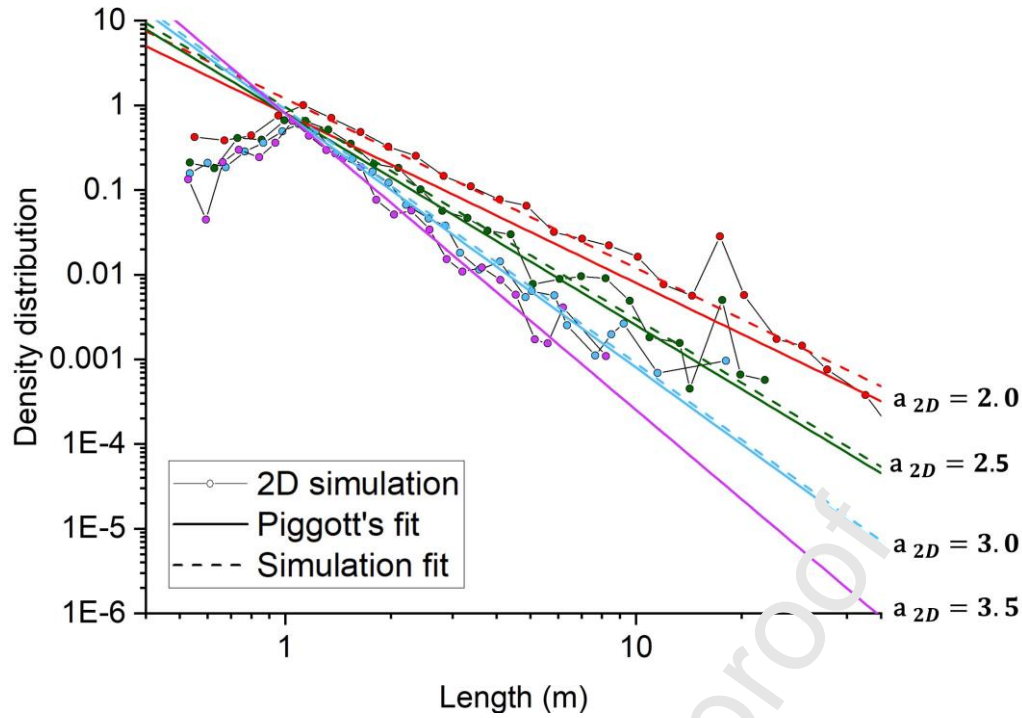


Figure A 1: Trace length density distributions (lines with circles) deduced from 3D simulations ran according to a single power-law and different exponents (a_{2D} terms). Solid lines are the expected fits calculated by stereological rules and dashed lines are the real fits. (Figure size: 2 column fitting; Colors: yes)

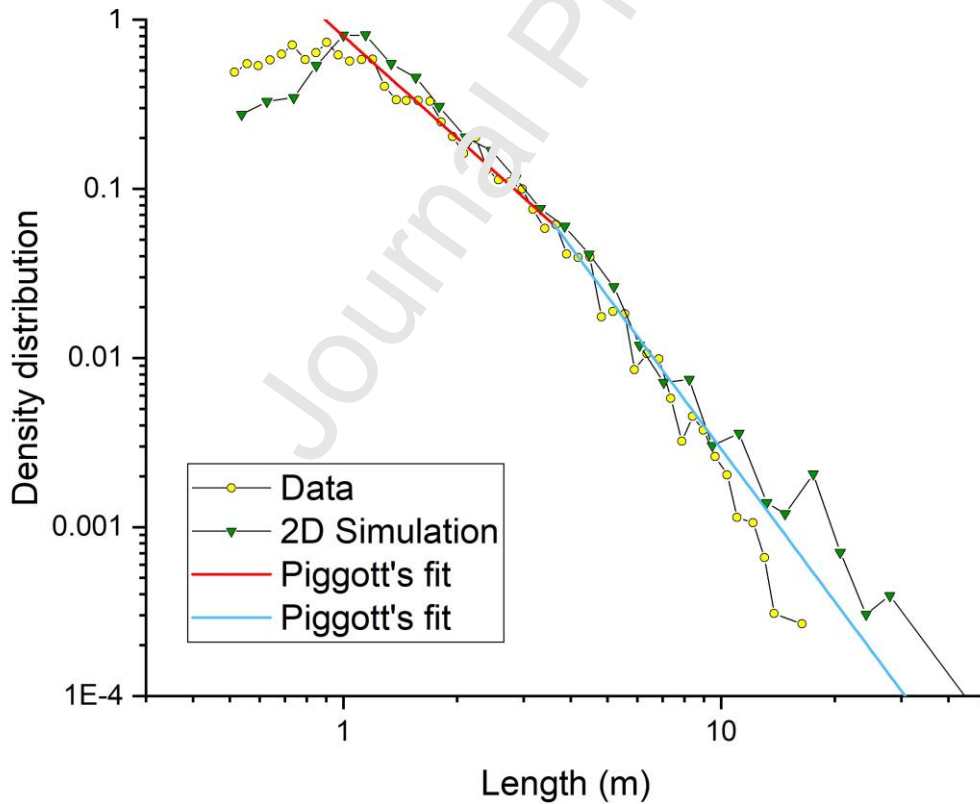


Figure A 2: Comparison of fracture trace density distribution between the data (yellow) and the statistical model (green) using Piggott's stereological rules. The red and blue curves are the fits for fractures smaller and larger than 3.6 m, respectively. (Figure size: 2 column fitting; Colors: yes)

Acknowledgements

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- Tunnel-based GPR investigation in the context of nuclear waste repositories
- GPR method detects open sub-horizontal fractures with sub-millimeter aperture
- Reflections in granite at 410 m depth originates from open fractures
- Scaling of GPR fracture density is similar to a statistical fracture model
- GPR detects 80% of open fractures with area from 1 to 10 m² dipping less than 25°

CRedit author statement

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Declaration of interests

☒ The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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