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22	Highlights
23	• Thermal conductivity and mechanical behavior of new straw composite were modeled
24	using 3D numerical homogenization.
25	• X-ray micro-tomography was used to determine volume fractions of composite
26	constituents.
27	• A particular shape of inclusion "3D-curved spherocylindrical" was adopted to
28	represent plant aggregates.
29	• The numerical homogenization method used, allowed to predict the mechanical
30	strength of the new bio-based composite.

32

# 33 Abstract

Bio-based materials have been extensively studied in recent decades. These materials based 34 on vegetable aggregates are highly heterogeneous, and their complex behaviour depends on 35 the behaviour of the constituents as well as their spatial distribution, size, and shape. 36 Classically, homogenization methods are used for the prediction of the behaviour of 37 38 heterogeneous materials because they allow to take into-account the microscopic phenomena and characteristics governing the macroscopic behaviour at a considered scale. In the case of 39 composite materials, the use of this prediction approach allows to optimize the properties 40 according to some criteria while limiting often expensive and time-consuming experimental 41 tests. This paper aims to predict the effective thermal conductivity and model the mechanical 42 behaviour of a bio-composite based on lime and cereal straw. A numerical homogenization 43 44 approach was adopted to consider the complex microstructure of these biobased materials. An experimental characterization of the composites was carried out to describe the microstructure 45 of the material (size, orientations, and shape of aggregates). X-Ray micro tomography 46 observation was performed to determine volume fraction of the different phases of the 47 biocomposite. 48

A statistical approach was also used to determine the size of the Representative Volume Element (RVE) of the studied material for different distributions of heterogeneities. Then, numerical simulations of the thermal and mechanical behavior of composite was carried out. The results show the need to take into account an interphase between the straw aggregates and the matrix as well as the effect of the vegetal aggregates on the hydration of the binder to accurately predict the effective properties of the material.

Keywords: Straw Composite, Thermal Conductivity, Mechanical Behavior, X-Ray Micro tomography, Representative Volume Element (RVE), Modeling, Numerical Homogenization,

# 57 **1 Introduction**

Bio-based materials have a growing interest in improving building thermal performance and 58 reduces the carbon emissions of the construction sector. Generally, these materials are based 59 on vegetable, renewable aggregates and organic/inorganic binders [1–7]. Numerous scientific 60 studies have been carried out on the development and the experimental characterization of 61 these composites. They showed interesting thermal, acoustic insulation capacities and 62 excellent hydric properties of these materials [8–14] combined with interesting characteristics 63 such as low energy consumption, low carbon footprint, low cost, low density and 64 biodegradability [15–19]. The properties of the bio-composites depend strongly on the 65 fraction and the morphology of the constituents, in particular the type and content of binder, 66 the distribution and the size of the aggregates [20,21]. It has also been reported in the 67 literature that the relative humidity significantly impacts the thermal conductivity of the 68 composites due to their hygroscopic nature [22–24]. 69

Several works in the literature have attempted to determine thermal and mechanical 70 71 macroscopic properties of this type of materials by taking into account their microstructure [22, 24–27]. In all these works self-consistent homogenization based on a spherical inclusion 72 73 (bicomposite or tricomposite) was used. However, the predictions of this method become medicor when the binder fraction decreases below 19% of the volume because of the 74 assumption of the matrix continuity which is not verified for this case [25]. Akkaoui et al. 75 76 2017 [28] have used self-consistent method combined with a composite-sphere like microstructure to predict the Young modulus of a wood aggregate concrete. Following these 77 authors the representation of the microstructure of wood concrete as an aggregation of solid 78 grains surrounded by a layer of binder and porosity represented by voids among these 79

aggregates seems to be a better alternative of structure description as compared to hollow spherical inclusions microstructure used by [25]. The results obtained, using this microstructure representation are in good agreement with the experimental measurements and model has been considered according to the authors as a predictive tool to optimize the elastic properties of wood aggregate concrete [28]. However, the use of such microstructure representation remains limited to the case of materials with an intergranular porosity of less than 50% which is the percolation limit of the self-consistent scheme.

In a recent study, Tran-Le et al. 2018 [29] have developed a novel analytical model approach 87 to predict effective thermal conductivity tensor of lime-hemp concrete by taking into account 88 89 the anisotropy, size, orientation of aggregates and the interface between the binder and aggregates. This approach could be seen as an extension of the Eshelby's solution to several 90 ellipsoidal inclusions. By comparing results of their model with experimental measures, they 91 concluded on the necessity of taking into account in modeling the thermal contact resistance 92 between the aggregates and the binder, in order to fit the observed values of thermal 93 conductivity. This model constitutes a suitable prediction tool of the thermal conductivity of 94 hemp concrete, but it is only valid in the dry state. 95

Couture et al. 2017 [30] also noted that the pre-compaction used during the manufacturing of 96 the materials leads to anisotropy of thermal conductivity at the macroscopic scale. The 97 authors adopted a numerical approach based on finite element calculations to model the 98 thermal conductivity of hemp concrete. The hemp aggregates were represented by cylindrical 99 inclusions aligned in the same direction and arranged randomly. However, their volume 100 fraction does not exceed 15%. The authors confirmed by the simulations carried out, the 101 102 transverse isotropic character of thermal conductivity of hemp concrete. Mom et al. 2011 [31] used an iterative homogenization approach based on finite element calculations to model the 103 thermal conductivity of hemp concrete with bar shaped particles and high porosity rates. This 104

approach made it possible to take into account the anisotropy of the material and to represent the hemp particles by plate inclusion. The authors compared the results of this model with the experimental measurements of Cerezo 2005 [25] and Nguyen et al. 2018 [32]. They concluded that the multi-scale iterative technique adopted, provides a satisfactory prediction of thermal conductivity.

The knowledge of the effective properties of other lightweight insulation materials is also a 110 topic of actual interest of foam concretes, due to their wide use in construction project. This 111 special class of porous materials with cellular microstructure have been extensively studied by 112 using periodic homogenization method. Low et al 2020 [33] studied the influence of 113 114 boundary conditions on the computation of the effective thermal conductivity of foams with a high porosity of 74%. Three types of foam geometries were used, namely, unit cell-based 115 structures, digitally generated periodic foams, and tomography-reconstructed real foams. The 116 authors have shown the importance of choosing the appropriate boundary conditions for the 117 geometries used to accurately estimate the effective thermal conductivity. Miled et al 2016 118 [34] proposed a three dimensional finite Element Method for the prediction of the effective 119 thermal conductivity of foam concretes having a porosity ranging between 0 and 0.68. They 120 have reported that the effective thermal conductivity of foam concretes can be predicted 121 122 according to their porosity by a general power law. Their results also showed no significant effect of the pores size distribution, and spatial distribution on the effective thermal 123 conductivity of foam concretes. 124

The present study aims to predict the thermal conductivity and model mechanical behavior of straw insulation composite developed in previous works by authors [2,35]. The objective is the mixtures optimization by using predictive capacity of homogenization approach in order to limit experimental tests. A numerical homogenization approach is adopted to take into account a complex microstructure more representative of the real composite, considering the

the shape, the orientation of the aggregates with high rate and also the 130 size. significant intergranular porosity. In addition to Young's modulus prediction of biobased 131 concrete, a subject very often treated in abundant research, the modeling approach proposed 132 aims at description of full nonlinear mechanical behavior of this biocomposite. In fact, the 133 mechanical strength in compression is an essential parameter to be determined for all 134 constructing materials. So, the proposed non-linear modeling should be a tool to estimate the 135 mechanical strength of straw concrete as a function of the structure and composition. Using 136 the model makes it possible to optimize the mixtures by taking into account two criteria of 137 use, a better thermal performance and a good mechanical strength for material's buildability. 138

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# Materials and characterization methods

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# 141 2.1 Materials

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Two composites were selected from previous work [35] for this investigation. The first is based on lime with a ratio of Water/Binder = 1.1 and Straw/Binder = 0.2 and the second prepared with the same Water/Binder ratio and a higher ratio of Straw/Binder = 0.4 with a binder consisting of lime and 20 % gelatin. The use of this biopolymer allows increasing of the ratio of vegetal aggregates. The description of raw materials and manufacturing procedure is detailed in the work of Ismail et al. 2020 [35]. The composites are denoted respectively C1 and C2, as indicated in Tab. 1.

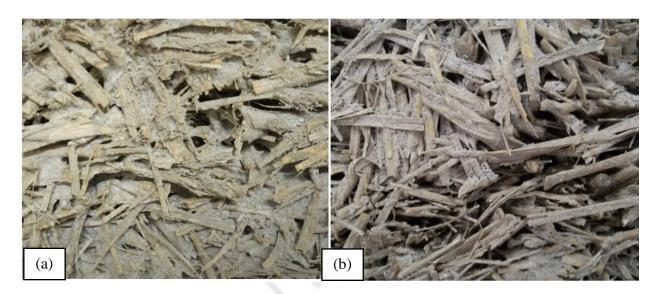
Composites	Binder	Straw/Binder (kg/kg)	Water/Binder (kg/kg)	Density (kg/m <sup>3</sup> )
C1	Lime	0.2	1.1	450
C2	Lime+20% gelatin	0.4	1.1	300

150

**Tab. 1.** Composite designation and detailed mixture proportions

Fig. 1 shows the appearance of the two composites. We can observe that in both cases, theaggregates are coated with a layer of binder and voids between them. These coated aggregates

- are connected by binder bridges. There are randomly arranged and not always straight but are
- 155 curved due to their low stiffness. We can also observe in Fig 1c the presence of the interphase
- 156 or decohesion between the straw aggregate and the matrix.
- 157
- 158





159

Fig. 1. Appearance of composites (a) C1 (with a high binder content) (b) C2 (with a low binder content) (c) microscope visualization of the straw aggregate-matrix interface

# 162 2.2 Experimental characterization

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178

163 2.2.1 X-ray micro-tomography: volume fractions of the constituents:

In order to determine the fraction of each constituent phase in composites, micro computed 164 tomography (microCT) analyses were performed at the Institut des Sciences de la Terre 165 d'Orléans (Orléans, France) on a Nanotom 180NF from Phoenix X-Ray (Fig. 2). We used an 166 accelerating voltage of 180 kV, a filament current of 170 nA, and an operating voltage of 120 167 V. During acquisition, the sample rotates 360°, allowing the instrument to take successive 168 169 images, covering all angles. Microtomography analysis was performed on representative samples of  $3 \times 3 \times 3$  cm<sup>3</sup> which resulted in a resolution of 17 um<sup>3</sup> per voxel. After the 170 analysis, the stack of 2D images is processed to construct a volume, manually extracted using 171 the software VG-Studio Max 1.2. A 3<sup>3</sup> median filter was applied to obtain homogeneous and 172 clear images. The dataset was processed by VGStudio MAX software. Fig. 3 shows an 173 example of 3D-reconstruction images obtained for the C1 composite. Tab. 2 shows the 174 volume fractions of the constituents obtained for the two composites, C1 (with a high binder 175 content) and C2 (with a low binder content). 176

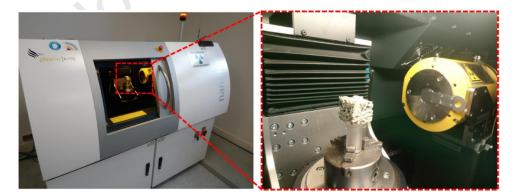
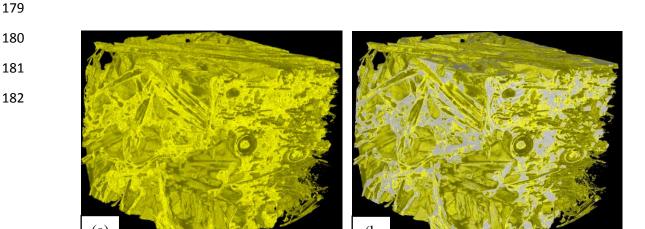


Fig. 2. Nanotom tomograph with a straw composite sample



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18	3
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18	5
18	6
18	7
18	8
18	9
19	0
19	
19	<b>Fig. 3.</b> 3D-reconstruction of a straw concrete sample (a) straw (b) combination
19	3 straw and binder (c) composite (straw+binder+porosity).
19	4
19	5
19	6
19	7
	<u>C1</u> C2

	CI	C2
Binder	33%	11%
Straw	30%	35%
Porosity (intergranular)	37%	54%
( Bronnon)	2.70	2.70

- 198
- 199

**Tab. 2**. Volume fractions of the different phases for the two composites

200 2.2.2 Thermal and mechanical characterization

To evaluate the experimental mechanical behavior of the two composites, uniaxial 201 compression tests were carried out using a compression testing machine (IGM250), equipped 202 with a load cell of 25 kN at a displacement rate of 0.5 mm/min. It should be noted that during 203 the manufacture of composites, under the effect of the self-weight of the mixture, the straw 204 aggregates tend towards stratified planes perpendicular to the compaction direction (Fig. 4). 205 For this reason, the tests were carried out in the perpendicular direction to compaction 206 (horizontal) on  $20 \times 20 \times 10$  cm<sup>3</sup> samples (Fig. 5-a) and also in the parallel direction of 207 aggregates (vertical) on  $15 \times 15 \times 10$  cm<sup>3</sup> samples (Fig. 5-b). 208

210

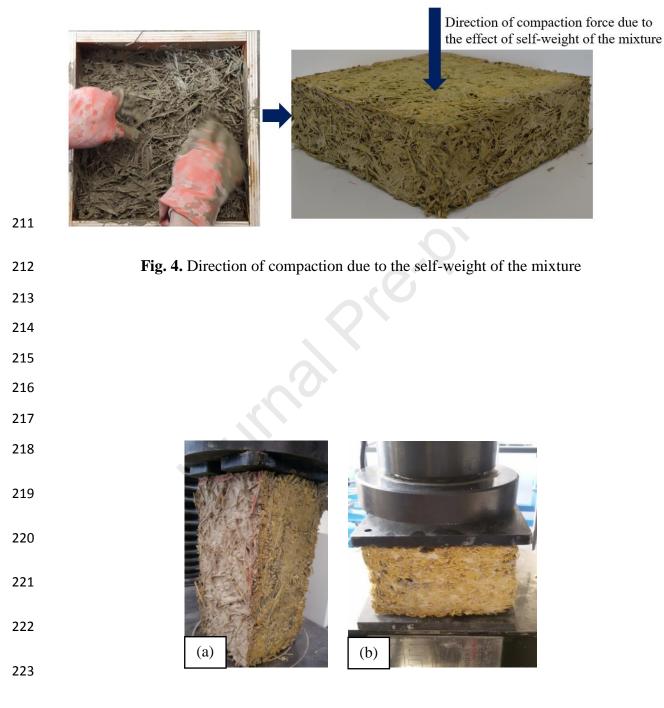
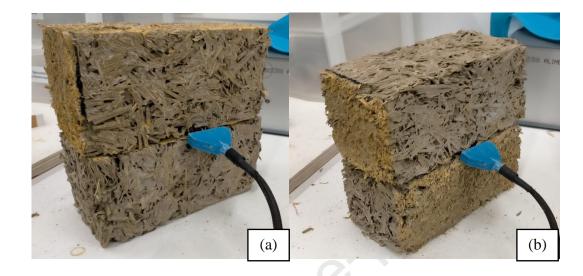


Fig. 5. Uniaxial compression test (a) horizontal direction (b) vertical direction Thermal conductivity was measured using a NeoTIM conductivity meter based on the hot wire technique. The measurements were made on samples with the dimensions 20 cm  $\times$  10 cm  $\times$  10 cm in horizontal (Fig. 6a) and vertical direction (Fig. 6b). The probe was placed in five different positions and the test was repeated three times in each position. The test was carried out in a dry state (the composites were dried in a ventilated oven at 60 °C until mass stabilization).



231

Fig. 6. Thermal conductivity measurement (a) horizontal direction (b) vertical direction. 232 The thermal and mechanical characterization carried out in the horizontal and vertical 233 direction highlighted the effect of the aggregate's orientation on the behavior of the materials. 234 Fig. 7 shows a comparison between the stress-strain curves evaluated from the uniaxial 235 compression tests on the composites studied in both directions. The mechanical behaviour 236 obtained in the horizontal direction is similar to what is observed for hemp concrete [36]. The 237 curve has three zones: an elastic zone, where the binder supports the compressive stress, a 238 nonlinear zone depicting the progressive cracking of the binder until failure, and a post peak 239 zone where the binder is totally damaged and the vegetal aggregate supports most of the 240 stresses. Contrary to the horizontal direction, the loading of the composites in the vertical 241 direction results a behavior which is characterized by the absence of a fracture peak (Fig.7b), 242 the curve shows a continuous compaction with increase of the stress with large strain. 243

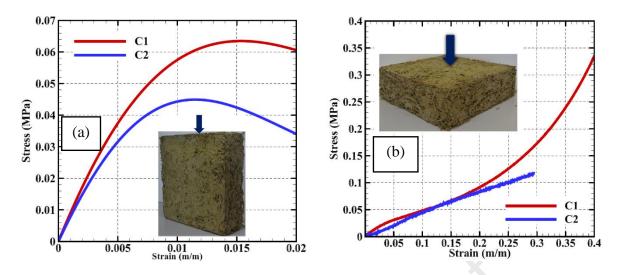


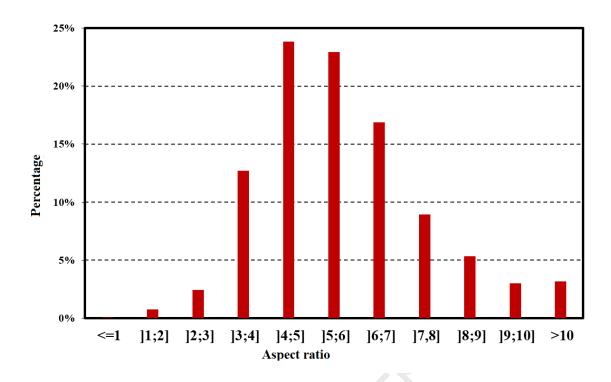
Fig.7. Mechanical behavior of composites (a) horizontal direction (b) vertical direction.
A difference in thermal conductivity was also noted in both directions. The values measured
in the vertical direction are higher than those obtained in the horizontal direction for both
composites as presented in Tab.3.

These results show that the fibre orientation strongly influences the properties of the composites and leads to a transverse isotropy of the materials [30].

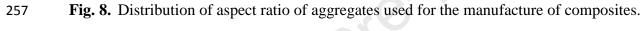
	S.	Thermal conducti			
	Composites	Vertical direction	Vertical direction Horizontal direction		
	C1	$0.075 \pm 0.02$	0.064±0.013		
	C2	$0.057 \pm 0.017$	0.051±0.019		
Tab.3. Thermal conductivity of composites in horizontal and vertical direction					

- 250
- 251 2.2.3 Distribution of fiber aspect ratio

Fig.8 show the results of the distribution of fiber aspect ratio obtained from the granulometric analysis of aggregates [35], it can be seen that more than 75% of the aggregates have an aspect ratio in the range of 3-7, with the largest percentage being assigned to aspect ratio in the interval ]4 ;5].









259 **3.1** Conceptual model of the microstructure of the biocomposites

The microstructural information obtained from the experimental characterization described in the previous section was used to create a three-dimensional microstructure using the Digimat software. The straw aggregates were represented by curved sphero-cylindrical inclusions (Fig. 9a) with a constant aspect ratio equal to 4 and the porosity (intergranular porosity or straw porosity) was represented by spherical inclusions (Fig. 9b) randomly distributed. Also, in order to take into account the anisotropy demonstrated in previous section, the spherocylindrical inclusions were randomly oriented in the plane (2D) (Fig. 10).





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Fig. 9. Shapes of inclusion adopted for (a) straw (b) Porositiy

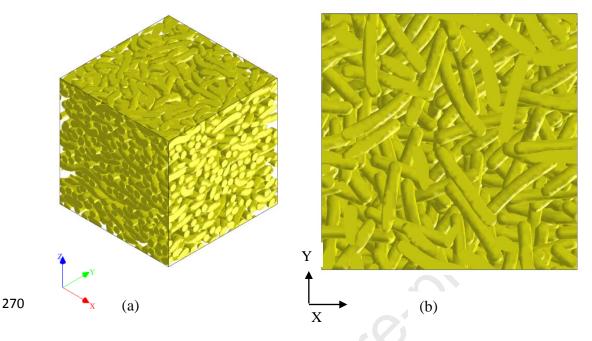
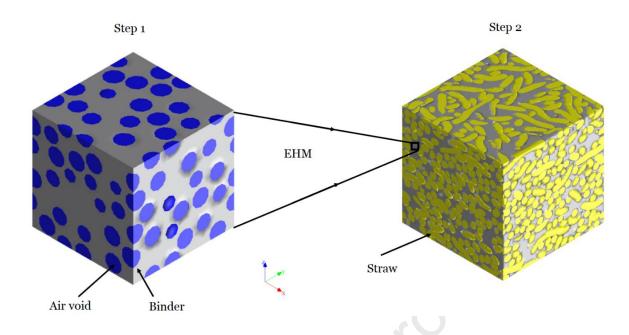


Fig. 10. Example of a RVE showing the random orientation in the plane of inclusions.
In order to highlight the influence of the microstructure on the effective thermal conductivity
of the biocomposites, five different configurations of the conceptual model of the

biocomposite microstructure have been adopted:

275 Configuration 1: It consists of introducing the heterogeneities of the material in two 276 successive steps. First, the binder and porosity were homogenized. Then, the obtained 277 equivalent homogeneous medium (EHM), constituted the matrix in the second step, while the 278 straw inclusions were integrated to determine the effective conductivity of the final 279 homogenized material (Fig. 11).

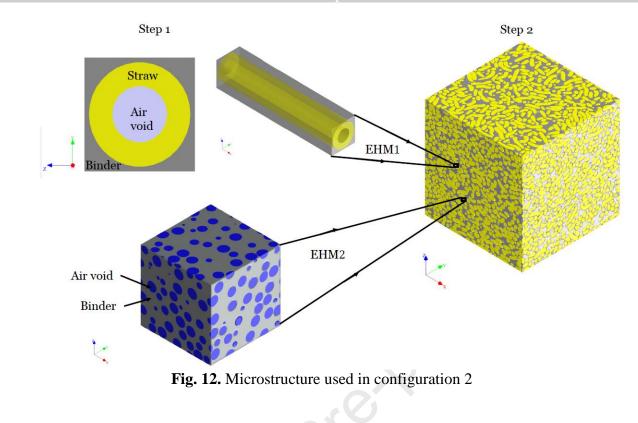




# Fig. 11. Microstructure used in configuration 1

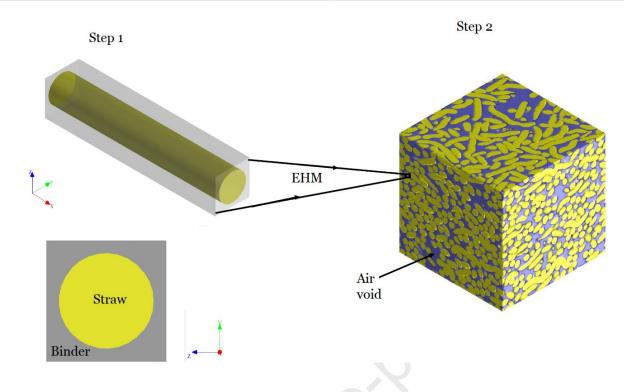
Configuration 2: The binder has been divided into two parts: a large part (95%) that coats the 282 fibers and another part (5%) that provides the bonding bridges (porous binder) between them. 283 Therefore, the heterogeneities were represented by a tri-composite inclusion containing the air 284 surrounded by the straw and itself coated with the layer of binder. Then, a two-step 285 homogenization was also adopted: the first step consists in determining separately the 286 effective thermal conductivity of the tri-composite inclusion (air + straw + binder) and the 287 porous binder. Then for the second step, the RVE contain the two homogeneous media 288 determined in the first one to obtain the final effective behavior (Fig. 12). 289





293 Configuration 3: we assume in this case that the material consists of a network of fibers 294 coated by the binder and embedded in the void matrix. The process consists in a first step in 295 determining the effective thermal conductivity of a bi-composite inclusion representing the 296 straw coated by the binder. Then, this conductivity will be assigned to heterogeneities 297 immersed in a matrix completely represented as a void and a second homogenization was 298 carried out. Note that the contact between the binder and the straw is considered as perfect 299 (Fig. 13).

290 291



300

# Fig. 13. Microstructure used in configuration 3

Configuration 4: Similar to the second configuration, the binder was divided into two parts, a 95% percentage that coats the fibers and another 5% which connects the fibers with each other. In a first step, the equivalent homogeneous medium of the bi-composite inclusion and the porous binder were determined, then in a second step, the two equivalent homogeneous mediums were integrated in an RVE where the matrix represents the porous binder and the heterogeneities represent the coated straw. A perfect interface was also considered in this case (Fig. 14).

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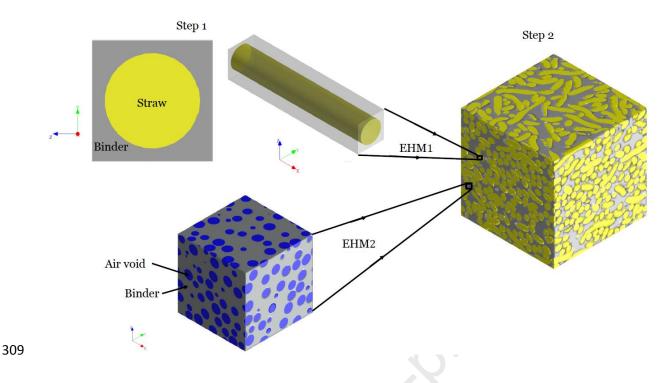
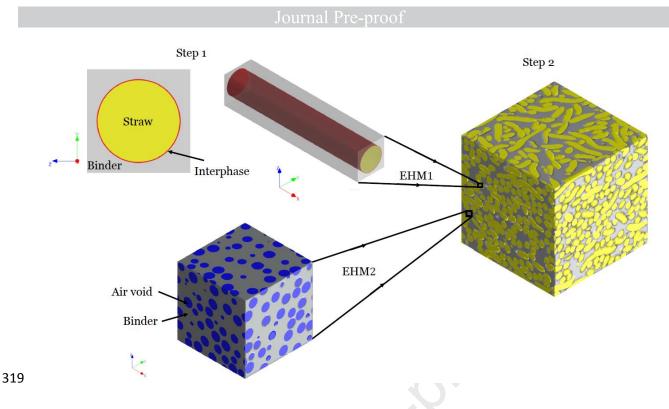


Fig. 14. Microstructure used in configuration 4

Configuration 5: The same previous approach was followed in this configuration but an interphase between binder and straw was introduced. The properties of this zone were determined by calibrating the numerical model on the experimental results. As for its thickness, it is assumed to be very small compared to the diameter of inclusion (interphase thickness≃1% of diameter of inclusion) (Fig. 15).

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# Fig. 15. Microstructure used in configuration 5

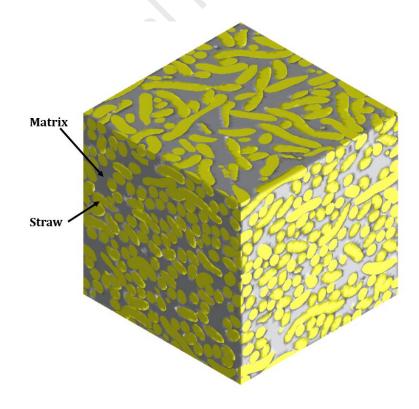
## 321 322

# **3.2** Size of the representative Volume Element (RVE)

The relevant choice of a representative volume element (RVE) is the first step to accurately 323 324 describe the microstructure of the material to be modelled. Several approaches have been proposed in the literature to determine its size. According to Hill.1963 [37], the RVE is a 325 sample which contains sufficient heterogeneities for the macroscopic properties to be 326 independent of the boundary conditions. Hashin.1983 [38] indicates that the RVE must be 327 large enough in relation to the scale of the heterogeneity and small enough in relation to the 328 329 macroscopic scale of the composite material. Kanit et al. 2003 [39], Gitman et al. 2007 [40], Pelissou et al. 2009 [41] proposed a statistical analysis based on the convergence of the 330 effective properties to set the size of the representative volume. Indeed, the approach consists 331 332 in estimating the apparent properties of the material by performing several numerical calculations on different sizes of the microstructure containing the same volume fraction of 333 the heterogeneities and under the same boundary conditions. The size of the micro-structure 334

from which the apparent properties converge corresponds to the size of the RepresentativeVolume Element (RVE).

A similar approach is used here to determine the RVE size of straw composite in the thermal 337 and mechanical case. We consider five sizes of a cubic RVE whose dimension of the edge is 338 between 1 and 3 cm. We aim to determine for each size the effective thermal conductivity as 339 well as the Young's modulus. We also consider that the RVE contains a single form of 340 inclusion (curved sphero-cylindrical inclusions) with constant size and randomly oriented in 341 the plane (Fig.16). Five simulations were carried out for each size to determine the standard 342 deviation of the estimated parameters. The approach was applied for two volume fractions of 343 344 inclusions: 25% and 60%. The simulations and the generation of the microstructure were carried out using the Digimat software. A set of parameters given in table 4, for lime matrix 345 and straw inclusion is used for all simulations. 346



347



Fig. 16. Microstructure used to determine the RVE size

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352

	Matrix	Inclusion
Young's modulus E(MPa)	100	0.2
Poisson's ratio v	0.3	0.1
Thermal conductivitiy $(\lambda/W/m.K)$	0.168	0.051

Tab. 4. Parameters used to determine effective properties.

353

Fig. 17 shows the evolution of thermal conductivity and Young's modulus as a function of the edge size of RVE for the two volume fractions considered. We can notice in the thermal case that the effective conductivity converges from a size of 2 cm for a volume fraction of 25% while for a fraction of 60% the convergence is shifted to a size of 2.5 cm.

In the case of Young's modulus, for a fraction of 25% the convergence was observed in the vicinity of 2.5 cm while for a percentage of inclusions of 60%, it is reported at a size of 3 cm. We can also note that in the different cases, the standard deviation decreases as the size of the RVE increases.

These results show that the size of the RVE can depend on the volume fraction of the 362 heterogeneities in both linear elasticity and heat conduction. According to these results, a 363 representative cubic volume element with an edge of 3 cm was adopted to estimate the 364 thermal conductivity and the mechanical behavior of the studied straw composites. We note 365 that the average straw size is about 2.9 cm, determined from granulometric analysis of studied 366 particles [35]. However, to reduce the computation time of the simulations, we used in the 367 conceptual model of the microstructure an inclusion with an average size of about 1 cm which 368 allows to have a same ratio of 3 between the size of the inclusion and the RVE edge. 369

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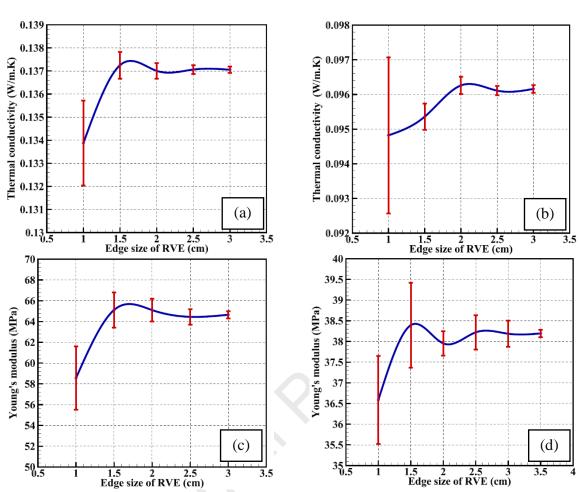


Fig. 17. Variations of the effective apparent properties as a function of the edge size of the
RVE: (a) and (b) Thermal conductivity respectively for a fraction of 25 % and 60%; (c) and
(d) Young's modulus respectively for a fraction of 25% and 60%

**376 3.3 Modeling of thermal conductivity** 

As it was described above, we consider a cubic RVE with an edge of 3 cm, composed of a 377 matrix and two types of inclusions: spherical representing the porosity (inter-granular and 378 tubular pore of straw) and curved sphero-cylindrical corresponding to the vegetable 379 aggregates. Tab. 5 shows the input data used for the three components. The thermal 380 conductivities given for the matrices were measured on samples of the binder pastes using the 381 hot wire method. The numerical simulations were performed using a Digimat software. 382 A temperature difference of 20°C was imposed between two opposite hot and cold faces and 383 periodicity boundary conditions on the other faces (Fig. 18). The thermal loading was applied 384

in the perpendicular direction in order to compare the numerical results with the experimental measurements. A tetrahedral mesh was used in simulations because of its flexibility in modelling complex 3D geometries (Fig. 19). The effective thermal conductivity ( $\lambda_{eff}$ ) is calculated as:

389

$$\lambda_{eff} = \frac{q_h}{\Delta T} \tag{1}$$

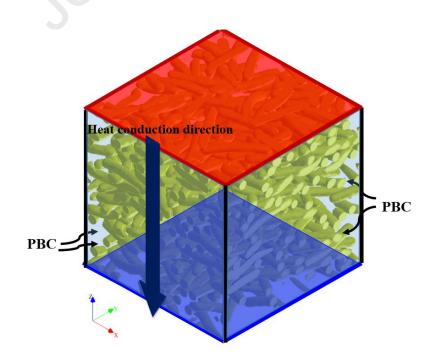
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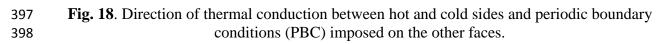
where  $q_h$  is volume-averaged heat flux in the RVE along the Z-direction and  $\Delta T$  is the imposed temperature difference.

Constituents	Thermal conductivity (W/m.K)
Matrix of C1-composite	0.168
Matrix of C2-composite	0.143
	0.071
Straw	0.051
Air	0.026

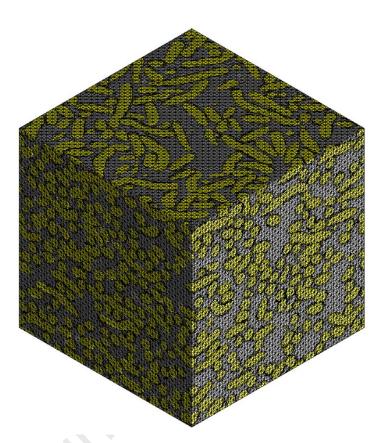
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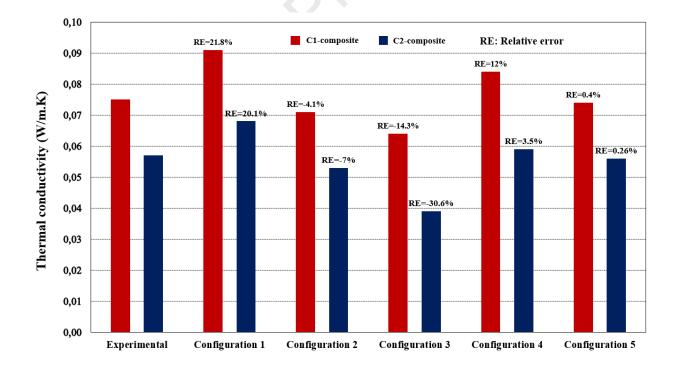
401 **Fig. 19.** Three-dimensional mesh of the RVE using tetrahedral elements.

Fig. 20 shows the results obtained in the different configurations presented above. It appears that the classical representation of the microstructure by inclusions embedded in a matrix with perfect interface between the matrix and the inclusion, provides results is far away from those obtained experimentally with an error of about 20% for the two biocomposites.

The microstructure adopted in the second configuration has improved the obtained numerical results. Indeed, the numerical values are close to those obtained experimentally, the relative errors are of the order of 4.13% and 7.03%, respectively for the composite with a high and low binder content. Moreover, the third proposed configuration by introducing coated fibers in a void volume has largely underestimated the thermal conductivity of the materials with an error of up 30 % for the C2 biocomposite. However, the replacement of this matrix (void) by

a porous matrix allowed satisfactory results, particularly for the low-dosage composite C2.
Finally, considering another phase between the binder and the matrix allowed to reproduce
faithfully the experimental results in the case of both composites.

415 We can confirm from these results the significant impact of the choice of microstructure on the estimation of the effective thermal conductivity of materials. Indeed, although the volume 416 fractions of the three phases of the material are the same in the five configurations considered, 417 the results were very variable. This result confirms that the effective properties of 418 heterogeneous material depend not only on the properties of the constituents but also on their 419 interactions represented by the different conceptual models of the microstructure. Therefore, 420 421 choosing a microstructure close to that of the real material is an essential step to be able to accurately predict the effective thermal conductivity. 422



423

Fig. 20. Comparison between experimental and modelled thermal conductivities.

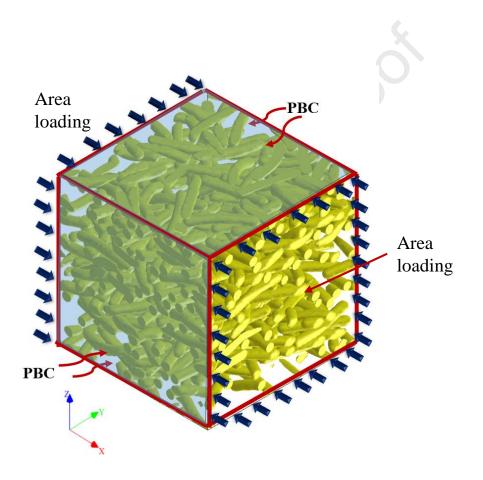
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Numerical homogenization was also used to reproduce the mechanical behavior of the two 428 studied straw composites. As well as the problem of heat conduction, a representative volume 429 element is considered, which consists of elastic heterogeneities and an elastoplastic matrix. 430 Two shapes of inclusion were adopted, spherical representing the porosity (inter-granular and 431 432 tubular pore of straw) and curved sphero-cylindrical corresponding to the vegetable fibres. The boundary and loading conditions were imposed on the surfaces as shown in the Fig. 21. 433





435

436 Fig. 21. Direction of mechanical loading and periodic boundary conditions (PBC) imposed on the other faces. 437

Tab. 6 gives 438

439	properties of		Straw	Air void	the inclusions
		Young's modulus E (MPa)	0.2	$10^{-6}$	
440	used in the	Poisson's ratio v	0.1	0.001	simulations.

the elastic

441

443 **Tab.6**. Elastic parameters of the inclusions (Straw + air)

444 The behavior of the matrix is described by a J<sub>2</sub>-plasticity model with nonlinear isotropic 445 hardening. This model is based on the Von Mises equivalent stress  $\sigma_{eq}$  defined as :

$$\sigma_{eq} = \sqrt{J_2(\boldsymbol{\sigma})} = \sqrt{\frac{3}{2}(\boldsymbol{s};\boldsymbol{s})}$$
(2)

where  $J_2(\sigma)$  is the second invariant of the deviatoric stress tensor s, and is expressed as:

$$J_{2}(\sigma) = \frac{3}{2}(\mathbf{s}; \mathbf{s})$$

$$= \frac{2}{3} \left[ (\sigma - \frac{1}{3}Tr(\sigma)\mathbf{I}) \right] : \left[ (\sigma - \frac{1}{3}Tr(\sigma)\mathbf{I}) \right]$$

$$= \frac{1}{2} \left[ (\sigma_{11} - \sigma_{22})^{2} + (\sigma_{22} - \sigma_{33})^{2} + (\sigma_{33} - \sigma_{11})^{2} \right] + 3 \left[ (\sigma_{12}^{2} + \sigma_{23}^{2} + \sigma_{31}^{2}) \right]$$
(3)

In this constitutive model, the response is assumed to be linear elastic as long as the followingcondition is satisfied:

$$\sigma_{eq} \le \sigma_{Y} \tag{4}$$

449 where  $\sigma_{\rm Y}$  is the initial yield stress.

450 The total strain is assumed to be the sum of the plastic strain and elastic strain:

$$\boldsymbol{\epsilon} = \boldsymbol{\epsilon}^{\mathbf{e}} + \boldsymbol{\epsilon}^{\mathbf{p}} \tag{5}$$

451 The Cauchy stress and the elastic strain are then related by :

$$\boldsymbol{\sigma} = \underline{\underline{\mathbf{C}}} : (\boldsymbol{\epsilon} - \boldsymbol{\epsilon}^{\mathbf{p}}) \tag{6}$$

452 where  $\underline{\underline{C}}$  is Hooke's operator. When  $\sigma_{eq}$  exceeds  $\sigma_{Y}$ , the response becomes nonlinear and

453 plastic deformation appears. In this case, the Cauchy stress is given by

$$\sigma_{eq} = \sigma_{Y} + R(p) \tag{7}$$

454 where R(p) is the hardening stress expressed by a exponential and linear law:

$$R(p) = kp + \sigma_{\infty}[1 - exp(-mp)]$$
(8)

455 Where k : is a linear hardening modulus,  $\sigma_{\infty}$  : is a hardening modulus, m : is a hardening 456 exponent and p the accumulated plastic strain, expressed as,

$$p(t) = \int_0^t \dot{p}(\tau) \, d\tau \tag{9}$$

457 With

$$\dot{\mathbf{p}} = \frac{2}{3}\sqrt{J_2(\dot{\mathbf{e}}^{\mathbf{p}})} = \sqrt{\frac{2}{3}\dot{\mathbf{e}}^{\mathbf{p}}:\dot{\mathbf{e}}^{\mathbf{p}}}$$
(10)

458 A yield function  $f(\sigma, R)$  can be defined,

$$f(\sigma, R) = \sigma_{eq} - \sigma_Y - R(p) \le 0$$
(11)

459 If f (σ,R)≤0, the material evolves in the elastic domain. Otherwise it is in the plastic region.
460 The evolution of the plastic strain tensor ε<sup>p</sup> is given by the normality rule :

$$\dot{\boldsymbol{\epsilon}^{\mathbf{p}}} = \dot{\mathbf{p}} \frac{\partial \mathbf{f}}{\partial \sigma} \tag{12}$$

461 To determine the parameters ( $\sigma_{Y,}\sigma_{\infty,}$  k, m) of the micromechanical model, uniaxial 462 compression tests were carried out on binder pastes for each case, Fig. 22 illustrates the stress-463 strain curves obtained for the two matrices and Tab. 7 shows the parameters identified from 464 these curves.

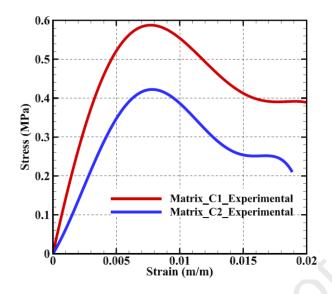


Fig. 22. Mechanical behavior of pure binders

465

	Matrix_C1	Matrix_C2
Poisson's ratio v	0.3	0.3
Young's modulus E(MPa)	100	85
Limite d'élasticité $\sigma_Y$ (MPa)	0.25	0.09
Hardening modulus $\sigma_{\infty}$ (MPa)	0.38	0.37
Hardening exponent m (MPa)	1400	1396
Linear hardening modulus k (MPa)	-5.5	-3.8

468

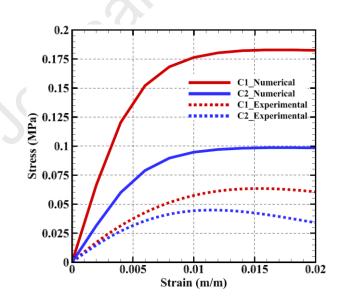
Tab. 7 Parameters used for the mechanical modelling

469

The mechanical behavior of the two composites was estimated by following the steps of configuration 1 (Fig. 11). First, the spherical inclusions and the matrix were homogenized. Then, in a second step, the curved fibers were integrated in the equivalent medium determined in the first step and a new homogenization is performed to obtain the effective mechanical behavior of the composite. The simulations were carried out by imposing on one face of the RVE a uniaxial deformation (in the x-direction, Fig. 21) and periodic conditions in the other faces. A tetrahedral mesh was also used here in both calculation steps.

Fig. 23 compares the experimental stress-strain curves with those predicted by the numericalhomogenization. The numerical curves are well above the experimental ones in both the

elastic and plastic region. This discrepancy can be associated with the matrix input data, 479 evaluated from the compression tests on binder pastes alone. In other words, the behaviour of 480 pure binders may be different from that of binders mixed with fibres, leading to significant 481 errors. The binder alone has a compactness that is totally different in the presence of 482 aggregates. This problem was also discussed by Akkaoui et al. 2017 [28]. Indeed, to 483 determine the elastic properties of the constituent phases of wood concrete, the authors carried 484 out a calibration of the developed model on the experimental results of the composite. They 485 noticed that the calibrated modulus arelower than those measured on the pure binder paste. 486 This difference is due to the interactions between the plant fibers and the binder. The presence 487 of the fibers strongly impacts the hydration and drying process of the binder [42–44]. In 488 addition, the cracks that appear in certain area of the fiber-matrix interfaces lead to additional 489 porosity which can also be the cause of the weakness of the calibrated properties for the 490 491 binder.



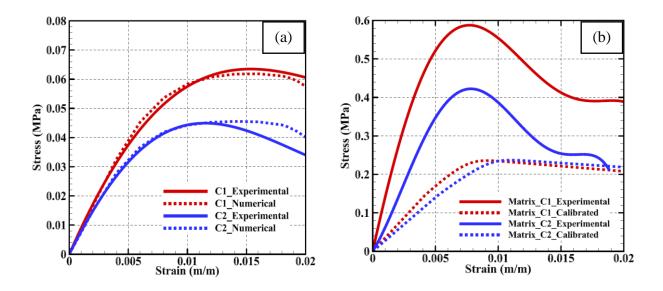


493 Fig. 23. Modeled and experimental mechanical behavior of the two composites 494 Therefore, we propose to determine the behavior of the matrix using an inverse analysis based 495 on numerical homogenization. For this, we assume the following hypotheses: (i) The 496 representative volume element is cubic with an edge equal to 3 cm (ii) Vegetable fibers have a 497 curved sphero-cylindrical shape, randomly oriented in the plane and they have the same

aspect ratio (iii) Porosity has a spherical shape (iv) The behavior of the inclusions is elastic as 498 shown in the Tab. 8. (v) The behavior of the matrix is elastoplastic. The macroscopic stresses 499 and strains are calculated from the mean relations of the local stresses and strains of the RVE. 500 We aim to evaluate the properties of the matrix (parameters of J2-plasticity model). In a first 501 step, we determine the elastic properties of the matrix allowing to minimize the difference 502 between the experimental and numerical curve by using least squares. Once this condition is 503 504 satisfied, we fix the elastic parameters and we proceed to determine the plastic parameters  $(\sigma_{Y}, \sigma_{\infty}, k, m)$  of the J2-plasticity model using the same algorithm. 505

Fig. 24(a) shows a good agreement between the effective behavior and that obtained from the experimental tests, whether for the composite with high or low binder content. In fact, the Young's modulus and the estimated mechanical strengths are very close to the experimental values, the standard deviation does not exceed 3%. Fig. 24(b) shows the stress-strain curves deduced from the compression tests on pure binders and those obtained by inverse analysis. This result confirms the major impact of plant fibres on the reduction of the mechanical properties of the matrices.

513 The approach proposed in this study can be used to orient the formulations of studied 514 materials by proposing composites suitable for each use with a well-defined criterion.



	Matrix_C1	Matrix_C2
Poisson's ratio v	0.3	0.3
Young's modulus E(MPa)	30	35
Limite d'élasticité $\sigma_Y$ (MPa)	0.15	0.145
Hardening modulus $\sigma_{\infty}$ (MPa)	0.098	0.097
Hardening exponent m (MPa)	1800	1795
Linear hardening modulus k (MPa)	-2.9	-2.5

515 Fig. 24. Calibrated and experimental mechanical behavior (a) composites (b) matrices

Tab. 8 Parameters used for the modeling of the mechanical behavior

Model application and discussion

517 518 4

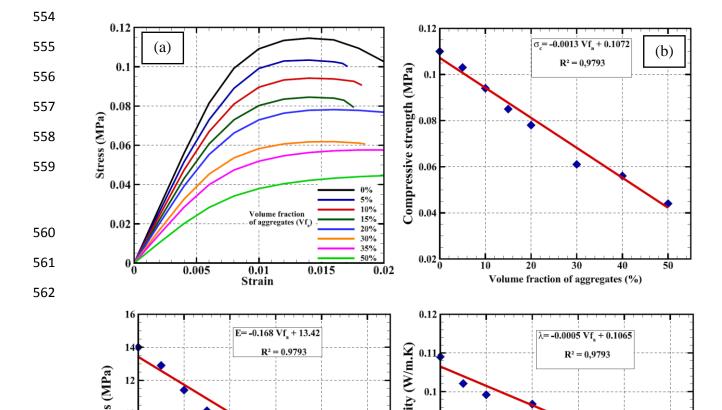
As previously mentioned int the state of the art section, the characterization of biobased materials, has shown that their macroscopic properties are closely related to the manufacturing parameters, such as, the nature and fraction of the binder, the nature and fraction of the aggregates, the size of the aggregates, and the casting process (compaction) which strongly influences the orientation of the aggregates. Other works in the literature have also shown the great sensitivity of the thermal conductivity to moisture content of the material [22–24].

The numerical model proposed in this work represents a good tool which could be used to optimize the properties of these materials as a function of physical properties of the components and microstructural description.

Among the manufacturing parameters of biocomposites that this proposed modelling will be able to give is the proportions of components or component volume fraction of the binder, the aggregates and the porosity. Fig. 25 shows an example of the results obtained by the model on the variation of thermal and mechanical properties of C1-composite as a function of volume fraction of the aggregates (Vfa).

Numerical simulations were performed using the microstructure described in configuration 1 (Fig. 11). In the first step, the binder and porosity were homogenized and in the second step several volume fractions (between 5% and 50%) of the aggregates were tested and

homogenized. These simulations were carried out using the VERs and the boundary 537 conditions presented previously in the figures 18 and 21. Fig.25-a shows the variation of the 538 mechanical behavior of the composite as a function of the volume fraction of the aggregates. 539 540 It is clear that the stress strain curves become more ductile with the increase in volume fraction of the aggregates. As expected, the more this fraction of the aggregates decreases, the 541 more the behavior of the composite becomes close to that of the matrix. Similar results were 542 obtained by Arnaud et al. 2012 [21] for the hemp concrete. Moreover, as displayed in Fig. 25-543 b and 25-c, a quasi-linear correlations were found between the mechanical properties and the 544 volume fraction of the aggregates. The compressive strength and Young's modulus decrease 545 proportionally with increasing percentage of aggregates. These results are in agreement with 546 the results found by Akkaoui.2015 [45] for wood-aggregate concrete, Mazhoud et al. 2017 547 [46] for hemp clay composite, and Pham 2014 [27] for hemp concrete. Fig. 25-d also shows a 548 549 quasi-linear evolution between the thermal conductivity and the volume fraction of the aggregates. As known, the increase in percentage of aggregates leads to a decrease in thermal 550 551 conductivity. The same trend was obtained also by Cerezo.2005 [25], Tran-Le et al. 2018 [29] and Pham.2014 [27] that used analytical models to predict the thermal conductivity of hemp 552 553 concrete.



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 Fig. 25. Variation of mechanical and thermal properties as a function of volume fraction of the aggregates (Vf<sub>a</sub>) (a) nonlinear mechanical behavior (b) Compressive strength (c) Young modulus (d) thermal conductivity

575

The use of the modelling approach presented here can make it possible to propose optimal 576 mixtures with an attractive thermal and mechanical properties depending on the final 577 applications and the criteria for use in buildings. The numerical modelling is able to predict 578 the stress-strain curve of the materials and to estimate their mechanical strength even for high 579 fraction of aggregate unlike analytical models used in literature which are limited only to 580 581 fractions not exceeding 30 %. Despite the advantage of this promising modelling method that 582 allows to study complex microstructures, the proposed methodology is based on some assumptions that affect certain results. The first, is that the mechanical properties of the 583 binder is determined by inverse analysis assuming that the volume fraction of the aggregates 584 585 in composite is constant. The variation of aggregate fraction can impact significantly the intrinsic characteristics of the matrix due to the interactions between the plant aggregates and 586 the binder as we previously stated. Therefore, it will be interesting to evaluate the influence of 587 plant aggregates on the intrinsic properties of the matrix. Moreover, the aggregate-matrix 588 interface is assumed to be perfect. This assumption is not realistic as it has been shown by the 589 microscopic observation. The experimental characterization of this interface and its 590

consideration in the material modelling in terms of thickness and properties has not yetreached a complete consensus, and remains an important point of investigation.

593

# 594 **5** Conclusion

595

The purpose of this paper was to model the thermal and mechanical behavior of two types of 596 straw biocomposites. Given the limitations of the analytical methods in taking into account all 597 microstructure characteristics influencing the behavior of biobased materials, a numerical 598 599 homogenization was adopted in this work to model their complex behavior. First, a detailed description of morphology, size and spatial distribution of inclusions was carried out. The X-600 ray microtomography is used to determine the volume fractions of the different phases of the 601 bio-based materials. Then, a statistical approach based on the convergence of the apparent 602 properties was applied to determine the size of the representative volume element. The results 603 604 showed that the RVE size depends on the fraction of inclusions in the case of mechanical or thermal loading. Subsequently, the effective conductivity and the non-linear behavior of the 605 606 composites were modeled. In the case of thermal conductivity, five configurations were 607 proposed to show the effect of microstructure on the prediction of the effective properties. The obtained results have shown that the classical representation of materials by 608 heterogeneities embedded in a matrix is inappropriate for the complex materials of this study 609 contrary to the classical polymer or metallic composites with a low ratio of fibers. The 610 compressive mechanical behavior was first modeled using as input data for the matrix, the 611 parameters determined from the experimental tests on the pure binders. This led to a large 612 overestimation of the mechanical behavior. Therefore, a calibration of the numerical model 613 with the experimental curves of the composites was necessary to access the properties of the 614 matrices. The results showed that the properties determined from the experimental curves of 615 pure binders are much lower than those identified, by inverse analysis, from the curves of the 616

- 617 composites. These results confirm the need to consider the fiber-matrix interaction in the
- 618 numerical model to accurately predict the mechanical behavior of biobased composites.
- However, the approach proposed in this work remains useful to guide the optimization of the
- 620 mixtures design of the biocomposite materials.

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# Modelling of thermal conductivity and nonlinear mechanical behavior of straw insulation composite by a numerical homogenization approach

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# Tables

Composites	Binder	Straw/Binder (kg/kg)	Water/Binder (kg/kg)	Density (kg/m <sup>3</sup> )
C1	Lime	0.2	1.1	450
C2	Lime+20% gelatin	0.4	1.1	300

Tab. 1. Composite designation and detailed mixture proportions

	C1	C2
Binder	33%	11%
Straw	30%	35%
Porosity (intergranular)	37%	54%

Tab. 2 . Volume fractions of the different phases for the two composites

		Thermal conductivitiy ( $\lambda/W/m.K$ )		
	Composites	Vertical direction	Horizontal direction	
ſ	C1	$0.075 \pm 0.02$	0.064±0.013	
	C2	0.057±0.017	0.051±0.019	

Tab.3. Thermal conductivity of composites in horizontal and vertical direction

	-	
	Matrix	Inclusion
Young's modulus E(MPa)	100	0.2
Poisson's ratio v	0.3	0.1
Thermal conductivitiy ( $\lambda/W/m.K$ )	0.168	0.051

Tab. 4. Parameters used to determine effective properties.

Constituents	Thermal conductivity (W/m.K)			
Matrix of C1-composite	0.168			
Matrix of C2-composite	0.143			
Straw	0.051			
Air	0.026			

Tab. 5. Thermal conductivities of constituents

	Straw	Air void
Young's modulus E (MPa)	0.2	10–6
Poisson's ratio v	0.1	0.001

Tab.6 . Elastic parameters of the inclusions (Straw + air)

	Matrix_C1	Matrix_C2
Poisson's ratio v	0.3	0.3
Young's modulus E(MPa)	100	85
Limite d'élasticité $\sigma_Y$ (MPa)	0.25	0.09
Hardening modulus $\sigma_{\infty}$ (MPa)	0.38	0.37
Hardening exponent m (MPa)	1400	1396
Linear hardening modulus k (MPa)	-5.5	-3.8

 Tab. 7 Parameters used for the mechanical modelling

	6.2		
	Matrix_C1	Matrix_C2	
Poisson's ratio v	0.3	0.3	
Young's modulus E(MPa)	30	35	
Limite d'élasticité $\sigma_Y$ (MPa)	0.15	0.145	
Hardening modulus $\sigma_{\infty}$ (MPa)	0.098	0.097	
Hardening exponent m (MPa)	1800	1795	
Linear hardening modulus k (MPa)	-2.9	-2.5	

Tab. 8 Parameters used for the modeling of the mechanical behavior

### **Declaration of interests**

 $\boxtimes$  The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

The authors declare the following financial interests/personal relationships which may be considered as potential competing interests: