Highlights

Ion density and phase space density distribution of planetary ions Na\(^+\), O\(^+\) and He\(^+\) in Mercury’s magnetosphere


- MESSENGER FIPS ion density observation from the whole orbital phase are analyzed.
- Spatial distribution of Na\(^+\), O\(^+\) and He\(^+\) ion densities are reproduced by our model.
- Simulated Na\(^+\) and He\(^+\) ion densities are overestimated by a factor of 2-20.
- Upstream conditions vary planetary ion densities by almost an order of magnitude.
- Analysis of the ion velocities reveal an anisotropic distribution in the \(v_x - v_z\) plane.
Ion density and phase space density distribution of planetary ions Na+, O+ and He+ in Mercury’s magnetosphere

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ARTICLE INFO

Keywords: Mercury, atmosphere Ionospheres Magnetospheres Solar wind

ABSTRACT

Photo-ionization of Mercury’s tenuous exosphere contributes to the heavy ion population in the Hermean environment. Observations with the MESSENGER Fast Imaging Plasma Spectrometer (FIPS) have revealed the ion density and spatial distribution of the three most abundant planetary ions or ion groups around Mercury: The Na+ group (mass-per-charge ratio m/q = 21 – 30 amu/e), O+ group (m/q = 16 – 20 amu/e) and He+. We developed a test-particle model coupled to a neutral exosphere model and two different models of the magnetosphere to simulate the ion density distribution of Na+, He+ and O+. We compare the modeled ion density distribution at aphelion for northward interplanetary magnetic field (IMF) with FIPS observations from the entire orbital phase (23 March 2011 to 30 April 2015). Our model reproduces several observed features but the average ion density is up to 18x too high. However, we find that the discrepancy is less than 3x for other solar wind and exosphere conditions. Comparison with previous simulation studies of the Na+ ion density and magnetic field line resonance observations give an average Na+ density which is on the same order as our estimate. Finally, we model the phase space density (PSD) distribution in four different regions. We find that in three out of four regions only a fraction of the PSD distribution can typically be observed by FIPS. This is mainly due the obstruction of the field-of-view caused by the spacecraft’s sun shield, which blocks plasma with a high v_x/v_z ratio from entering the instrument.

1. Introduction

Mercury has a tenuous and nearly collisionless atmosphere (exosphere) that is rich in heavy elements. H, He, Na, K, Mg, Ca, Mn, Fe and Al have been detected through ground-based (Potter and Morgan, 1985, 1986; Bida et al., 2000; Doressoundiram et al., 2009; Bida and Killen, 2017) and in-situ observations (Broadfoot et al., 1976; McClintock et al., 2008; Vervack et al., 2016). Space probe Mariner 10 made a tentative detection of the 130.4 nm O emission line during its third flyby past Mercury (Hunten et al., 1988). O could not be observed by the more recent Mercury Surface, Space Environment, Geochemistry, and Ranging (MESSENGER) spacecraft, despite conducting regular observations of the 130 nm line for several years in orbit (Vervack et al., 2016).

The strong solar radiation at Mercury and the intense space weathering causes neutral species to be continuously released from the surface regolith, either thermally (thermal desorption), by individual photons exciting the surface-bound atoms (photo-stimulated desorption), sputtering by solar wind ions or vaporization of whole surface grains by micro-meteoroids. The relative importance of these ejection mechanisms vary depending on species, and is different between volatile species (Na, K, He) and refractory species (Mg, Ca). Because the exosphere is collisionless, the species are not coupled and have their own dynamics. Several models have been developed to determine the relative contribution of the different ejection and loss processes to the overall composition of Mercury’s exosphere (Smyth...
Ion density distribution of Na⁺, O⁺ and He⁺ in Mercury’s magnetosphere


Mercury has a highly eccentric orbit (\( \epsilon = 0.2056 \)) and is trapped in a 3:2 spin-orbit resonance with the Sun. This gives rise to cold and hot longitudes (Soter and Ulrichs, 1967) and a seasonally variable exosphere and sodium ion content (Cassidy et al., 2015, 2016; Jasinski et al., 2021). Some exospheric sources like micro-meteoroid vaporization (Janches et al., 2021) and ion sputtering vary on shorter timescales, which has an impact on both the neutral exosphere (Leblanc et al., 2009; Orsini et al., 2018) and ionized exospheric neutrals (Raines et al., 2018; Jasinski et al., 2020). Meteoroids (as opposed to micrometeoroids) have been detected as large, brief enhancements to the exosphere (Jasinski et al., 2020; Cassidy et al., 2021)

The strong solar radiation at Mercury produces a large flux of heavy ions (on the order of \( 10^{24} \) s⁻¹; Raines et al., 2015) from the ionization of the exosphere. Lesser sources of planetary ions include charge exchange and solar wind ion sputtering. MESSENGER Fast Imaging Plasma Spectrometer (FIPS) detected several mass spectrum peaks that may belong to Na⁺ (mass-per-charge ratio \( m/q = 23-24 \) amu/e), O⁺ and water group ions (16-18 amu/e), S⁺ and \( H_2S^+ \) (32-36 amu/e), Si⁺ (28 amu/e), K⁺ and Ca⁺ (39-40 amu/e) and He⁺ (4 amu/e; Zurbuchen et al., 2008). FIPS is a time-of-flight (TOF) mass spectrometer. Due to FIPS TOF uncertainty, ions with similar mass-per-charge ratio were grouped together in so-called ion groups (e.g. Appendix A in Raines et al., 2013). Na⁺ (\( m/q = 21-30 \) amu/e), O⁺-group (\( m/q = 16-20 \) amu/e) ions and He⁺ (\( m/q = 4 \) amu/e) were regularly observed during the mission orbital phase (Zurbuchen et al., 2011; Raines et al., 2013). Ca⁺ has also been detected by the Mercury Atmospheric and Surface Composition Spectrometer (MASC) UltraViolet and Visible Spectrometer (UVVS; Vervack et al., 2016).

Observations with the magnetometer (MAG) on MESSENGER have shown that Mercury possesses a weak intrinsic magnetic field that fits the profile of a axially symmetric dipole field with dipole magnetic moment of \( 195 \pm 10 \) nT-R\(_M^3\) (where \( R_M = 2440 \) km is the mean Mercury radius) and a 0.2 R\(_M\) northward offset (Anderson et al., 2011). The planet takes up a relatively large volume inside the magnetosphere, and the magnetopause standoff distance is typically located at a mere 0.45 R\(_M\) from the subsolar point on the surface (Winslow et al., 2013). Despite the weak dipole magnetic moment and the high solar wind ram pressure, the dayside magnetosphere is rarely compressed all the way to the surface (Slavin et al., 2019; Winslow et al., 2020). This is due to the existence of induction currents in Mercury’s interior that are driven by solar wind variations (Smith et al., 2012; Slavin et al., 2014; Jia et al., 2015). The Hermean magnetosphere is highly dynamic with a Dungey cycle (Dungey, 1961) time of approximately 2 minutes (Slavin et al., 2009). The same process typically takes 1 hour at Earth (Siscoe et al., 1975).

The comparatively large gyro radius of the heavy ions in relation to the small scale of the Hermean magnetosphere means that non-adiabatic effects are significant almost everywhere in the magnetosphere (Delcourt et al., 2003). Non-adiabatic effects include centrifugal ion acceleration (Delcourt et al., 2002, 2003), which may have a major impact on the ion distribution in the magnetosphere (Raines et al., 2013). The heavy ion population is likely not dense enough to influence the global structure of the Hermean magnetosphere (Exner et al., 2020) but it gives rise to other effects like diamagnetic depression of the magnetic field (Korth et al., 2011), enhancement of the formation of Kelvin-Helmholtz instabilities (Paral et al., 2010) and generation of magnetic field-line-resonances (James et al., 2019).

Analysis of the first few months of FIPS observations in orbit around Mercury revealed several ion density enhancement regions and surprising differences between He⁺ and the heavier O⁺- and Na⁺-group ions. The Na⁺- and O⁺-group ions were especially abundant near the northern magnetic cusp with a Na⁺-group ion abundance four time larger than the solar wind He⁺++. The elliptical polar orbit of MESSENGER did not permit observations at low altitudes in the southern polar region. A later study by Raines et al. (2014) identified two populations of Na⁺-group ions in the northern cusp: one at low energy (100 – 300 eV) and one at high energy (> 1000 eV). The low-energy ions are believed to be produced locally while the high-energy ions come from photo-ionized escaping neutrals that have been swept into the magnetic cusps by reconnection. The Na⁺- and O⁺-group ions also showed smaller enhancements near the dawn terminator in the equatorial plane and at high altitudes (> 2000 km) in the dusk to pre-midnight sector. He⁺ was much more evenly distributed in the magnetosphere and did not exhibit any particular enhancements in said regions. The density of all species was particularly low near 12 h local time.

The Na⁺ density enhancement near the dawn terminator may be related to the seasonal dawn enhancement in the neutral exosphere (Potter et al., 2006, 2013; Cassidy et al., 2016; Milillo et al., 2021). If this is true, it could imply a direct link between the neutral surface abundance and the ion density at low altitudes. The dusk enhancement, on the other hand, may be evidence of the non-adiabatic ion acceleration mechanism described in Delcourt et al. (2002, 2003). The difference in spatial distribution between He⁺ and the heavier ion species may imply that He⁺ is produced by a different, more diffuse source. The depression at the subsolar point may be an apparent effect caused by the effective
energy range (100 eV – 13 keV; Raines et al., 2013).

Raines et al. (2013) also studied the variation of the global average ion density as a function of true anomaly angle. The global averages also studied the variation of FIPS data taken at different altitudes, latitudes and local times, and even includes measurements taken inside the solar wind. They found two peaks for the Na\(^+\)- and O\(^+\)-group ions, a global maximum at TAA = 110\(^\circ\) and local maximum at 330\(^\circ\), and a minimum at TAA = 270\(^\circ\). He\(^+\), on the other hand, showed very little variation with TAA. More recently, Jasinski et al. (2021) estimated the TAA variation of the Na\(^+\) production rate from UVVS (Cassidy et al., 2015) and THEMIS observations (Milillo et al., 2021) of the Na exosphere and FIPS Na\(^+\)-group ion observations taken inside the northern magnetospheric cusp. They estimated a maximum ion production rate of \(3 \times 10^{24}\) s\(^{-1}\) between TAA = 0\(^\circ\) – 30\(^\circ\), where FIPS observations are missing.

In this study, we have modeled planetary ions produced from the exosphere by combining different simulations. In Section 2, we describe the models used in this study. In Section 3 we describe the modeled neutral exosphere, magnetic and electric fields in the magnetosphere and the solar wind proton density. Then, we compare the modeled ion density and phase space density distribution with FIPS observations. We discuss the results and their implications in Section 4 and summarize the main findings in Section 5.

2. Models

In order to study the inferred link between the neutral and ionized exospheres we will use a realistic description of Mercury’s neutral exosphere consistent with remote and in-situ observations to model the abundance and spatial distribution of Na\(^+\), He\(^+\) and O\(^+\) in and outside Mercury’s magnetosphere. We will account for non-adiabatic effects of the heavy planetary ions and their impact on the ion density distribution by coupling our model to two different hybrid models of the magnetosphere.

In the following subsection, we describe the Monte Carlo-model of the neutral exosphere, the two magnetospheric models and our newly developed test-particle model that computes the full equation of motion of the ions.

2.1. Exospheric Global Model (EGM)

The Exospheric Global Model (EGM: Leblanc et al., 2017b) is a parallelized Monte Carlo-model that describes the exosphere around moons and planets. EGM has been previously used to study the exospheres of Mercury (Leblanc and Johnson, 2003, 2010; Leblanc and Doressoundiram, 2011; Leblanc and Chaufray, 2011; Leblanc et al., 2013), Ganymede (Leblanc et al., 2017b), Mars (Leblanc et al., 2017a) and Europa (Oza et al., 2019). In this paper, we use EGM to simulate the density of Na, He and O in the exosphere of Mercury.

EGM reconstructs the exospheric neutral density, average velocity, kinetic temperature and ionization rate in 3-D as well as the amount of exospheric materials trapped in the surface. The quantities are computed on a spherical grid \((r, \theta, \phi)\) where \(r\) is the distance from the planet, \(\theta\) is the co-latitude and \(\phi\) is the longitude. For Mercury, the grid is centered on the planet \((r = 0)\) and extends from the surface \((r = 1\) Mercury radius; \(R_M\)) up to 5.5 \(R_M\). The grid is divided into cells that are distributed exponentially with \(r\), linearly spaced in \(\phi\) and defined in \(\theta\) such that all cells at a given altitude have the same volume. For a detailed description of the EGM parallelization scheme see Turc et al. (2014).

A large number of test-particles are ejected from the surface by different mechanisms (see below) and then continuously throughout the simulation. Each test-particle \(r\) represents a large number of actual particles, represented by a weight \(w_r\). Each test-particle is followed around Mercury taking into account the various gravity fields (those of Mercury and the Sun) and the effect of the solar radiation pressure. This is done up to the moment when the test-particle is either ionized by the solar radiation flux (calculated taking into account the relative velocity of the test-particles with respect to the Sun and its distance to the Sun), impact the surface or escape from the simulation. In the case of a surface impact, the particles can be either re-ejected or absorbed in the surface, an absorption which duration is estimated for each species and from the local surface temperature (for a detailed description of the simulation scheme, see Leblanc and Johnson, 2010; Leblanc et al., 2017b). The surface temperature is described using a one-dimensional heat conduction model (see Leblanc et al., 2017b). An EGM run last for several Mercury years in order to reach an orbital dependent stationary solution independent from the initial conditions. Once a stationary solution has been reached, the state of the exosphere can be determined at any point along the orbit. To improve the statistics, the 3D density (velocity, ionization rate etc.) at a given TAA is averaged over 20\(^\circ\) centered on the TAA in question.

In the following, we assume that the primary origin of the exospheric Na and O atoms is Mercury’s surface, either endogenic (internal by regolith diffusion) or exogenic (meteorite origin), while He is primarily coming from implanted
Ion density distribution of Na$^+$, O$^+$ and He$^+$ in Mercury’s magnetosphere

Table 1

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Species:</td>
<td>Na</td>
</tr>
<tr>
<td>Ejection processes and surface ejection rate [s$^{-1}$]:</td>
<td>3.4 $\times$ 10$^{25}$ (PSD)</td>
</tr>
<tr>
<td>Ionization frequency (at 1 AU in s$^{-1}$):</td>
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<tr>
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<td>Number of cells:</td>
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<td></td>
<td>$n\theta = 18,$</td>
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<td>$n\phi = 40$</td>
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<tr>
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<td>$0 &lt; \phi &lt; 2\pi$ rad</td>
</tr>
<tr>
<td>Grid resolution:</td>
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<tr>
<td></td>
<td>$\Delta \phi = \frac{\pi}{2}$ rad</td>
</tr>
<tr>
<td></td>
<td>$\Delta \theta = \frac{\pi}{3} - \frac{\pi}{6}$ rad</td>
</tr>
<tr>
<td>True anomaly angle (TAA):</td>
<td>180°</td>
</tr>
</tbody>
</table>
Ion density distribution of Na$^+$, O$^+$ and He$^+$ in Mercury's magnetosphere

Figure 1: The fit between EGM (black line) and the Mariner 10 He column density observations (green stars) at (a) the subsolar limb and (b) the terminator. Also shown is the (c) simulated 2-D column density map in the equatorial plane and the approximate viewing geometry of Mariner 10 during the terminator observations. The boxes in (c) represent the approximate slit size of the observations. The circled points in (b) show the X_MS0 coordinates of the boxes in (c). The correlation values $r$ between the best-fit model and the two sets of observations are written in the top right corner of (a) and (b).

2.1.2. He

Following Leblanc and Chaufray (2011), we consider He atoms ejected thermally from the surface. In the version of EGM used by Leblanc and Chaufray (2011) the ejection rate of He was set to $2.3 \times 10^{23}$ s$^{-1}$ in order to reproduce the Mariner 10 column density profiles of the 58.4 nm He emission line. Leblanc and Chaufray (2011) defined the He source area to the whole surface of Mercury but in this work we limit the He source to the magnetospheric cusps. This is likely more realistic considering that the solar wind bombardment is limited to the cusps during nominal solar wind conditions. We define the location and size of the northern cusp as $27^\circ - 54^\circ$ in latitude (where $0^\circ$ is the north pole and $90^\circ$ is the equator) and 10 - 14 h in local time. We define the southern cusp symmetrically in the southern hemisphere. The northern cusp area defined here compares well to the limits of the northern cusp inferred from MAG data (Winslow et al., 2012), although the mean latitudinal extent ($11^\circ$) of the northern cusp is smaller.

We find that we have to increase the He ejection rate to $5.9 \times 10^{23}$ s$^{-1}$ to fit the Mariner 10 column density profiles in 1. This is still much smaller than the He$^{++}$ flux during nominal solar wind conditions (Leblanc and Chaufray, 2011). The fit of the new model to the Mariner 10 observations ($5.9 \times 10^{23}$ s$^{-1}$) gives similar correlation factors to Leblanc and Chaufray (2011), but the fit to the terminator observations is slightly worse ($r = 0.82$ compared to $r = 0.93$ from Leblanc and Chaufray, 2011). In Leblanc and Chaufray (2011) the energy accommodation of the He atoms follow a linear relationship between full accommodation on the dayside ($\alpha = 1$) to weak accommodation with the surface on the nightside ($\alpha = 0.06$ at the terminator and $\alpha = 0.05$ at midnight). The new fit in Figure 1b may imply that the accommodation theory developed for neutral He in Leblanc and Chaufray (2011) may need to be tweaked to better fit this set of observations. Since our study mainly concerns the ion density distribution near the equatorial plane, where the fit to the neutral He observations is good (Figure 1a; $r = 0.95$), we expect that this will have negligible impact on our results. Neutral He could not be observed by MESSENGER due to the limited coverage of the UVVS instrument in the ultraviolet spectral range (McClintock and Lankton, 2007).

The ionization frequency calculation follows the same scheme used for Na and is estimated to $0.1 \times 10^{-6}$ s$^{-1}$ for He at 1 AU. The solar radiation pressure is also calculated as in Fulle et al. (2007), but for both He and O it is negligible with respect to Mercury’s gravity field.

2.1.3. O

As explained in the introduction, the oxygen density in the exosphere of Mercury is not well constrained by observations, only an upper limit could be derived from UVVS observations (Vervack et al., 2016). Moreover, how oxygen could be ejected from the surface into the exosphere is not known. Therefore, due to this lack of observations, oxygen...
Ion density distribution of Na\(^+\), O\(^+\) and He\(^+\) in Mercury’s magnetosphere

Table 2
Input parameters to LatHyS and AIKEF.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Lathys value:</th>
<th>AIKEF value:</th>
</tr>
</thead>
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<tr>
<td>Spatial resolution:</td>
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</tr>
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<td>–3.5 &lt; x &lt; 10.5 R(_M)</td>
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<tr>
<td>Simulated species:</td>
<td>H(^+), He(^{++}), Na(^+), H(^+)(planetary)</td>
<td>H(^+)</td>
</tr>
<tr>
<td>Number of solar wind particles per cell:</td>
<td>H(^+): 20</td>
<td>H(^+): 25</td>
</tr>
</tbody>
</table>

Solar wind number density: \(n = 30 \, \text{cm}^{-3}\)

Solar wind velocity: \(v = 400 \, \text{km/s}\)

Solar wind magnetic field: \(\mathbf{B} = (B_x, B_y, B_z) = (0, 0, +20) \, \text{nT}\)

Ram pressure: \(P_{\text{raw}} = 8 \, \text{nPa}\)

Alfvén Mach number: \(M_A = 5.2\)

Exospheric atoms will be simply simulated starting from a population of ejected atoms from the surface following a MBF distribution at the local surface temperature and proportional to the incident solar radiation flux (that is with a dependency in cosine of the solar zenith angle and no ejection from the nightside). For O we assume a uniform weak thermal accommodation with the surface \((\alpha = 0.11; \text{ Hunten et al., 1988})\). Hence, when a O test-particle impacts the surface it is immediately re-ejected into the exosphere again. We then scale the O exosphere to fit the upper emission limit \((\approx 2 \, \text{Rayleigh})\) set by UVVS based on observations of the 130.4 nm O emission line \((\text{Vervack et al., 2016; Mcclintock et al., 2018})\). The O ionization rate at 1 AU is \(3.1 \times 10^{-7} \, \text{s}^{-1}\).

More recently, Huebner and Mukherjee (2015) re-evaluated the photo-ionization cross-sections, rates and excess energies for a range of atomic species, including the species that we consider in this work. The updated photo-ionization cross sections for Na, O and He are not significantly different from ours and we are using a better resolved solar spectrum compared to Huebner and Mukherjee (2015) (which used the same solar spectrum as in Huebner et al., 1992). For this reason there is a factor 1.6 – 3.2 difference between our calculated photo-ionization rates and the values published in Huebner and Mukherjee (2015). We will only consider quiet solar wind conditions in this work, but it is noteworthy that in the case of both He and O the photo-ionization rate is a factor of 2 – 3 higher during high solar activity (Huebner and Mukherjee, 2015). The photo-ionization rate for Na is not nearly as dependent on the solar activity level as O and He (the difference is less than 10\%).

2.2. Models of Mercury’s magnetosphere

Both magnetohydrodynamic (MHD; Jia et al., 2015, 2019; Dong et al., 2019) and hybrid (Kallio et al., 2011; Müller et al., 2011; Modolo et al., 2016) models have been employed to describe the electromagnetic field environment around Mercury, which results from the solar wind interaction with Mercury’s intrinsic field. Hybrid (electron fluid, ion kinetic) models are particularly well suited to describe plasma processes in systems where the ion Larmor radius is comparable to the length scale of the obstacle itself (Glassmeier et al., 2003; Slavin et al., 2008). Hybrid models have a large computational load compared to MHD models, but they enable higher accuracy in regions where kinetic effects of the ions prevail. We will compare the solar wind H\(^+\) and planetary ion densities using static electric and magnetic fields from two such models: Latmos Hybrid Simulation (LatHyS; Modolo et al., 2016) and Adaptive Ion-Kinetic
Table 3
Input parameters to the LIZE model.

<table>
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<tr>
<th>Parameter</th>
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<td></td>
<td>$\Delta \phi = 5 - 600$ km</td>
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<tr>
<td>Energy resolution:</td>
<td>$(E_i - E_{i-1})/E_i = 0.1$, where $E_i$ is the $i$th energy step</td>
</tr>
</tbody>
</table>

Electron-Fluid (AIKEF; Müller et al., 2011).

We use a single set of solar wind ($n = 30 \text{ cm}^{-3}, v = 400 \text{ km/s}$) and IMF ($B = B_z = +20 \text{ nT}$) boundary conditions (see Table 2). This corresponds to “case a” with $B_z > 0$ described in Aizawa et al. (2021), where $B_z$ is the $z$-component of the interplanetary magnetic field (IMF) in the Mercury-Sun Orbital (MSO) system. In MSO coordinates, $x$ points toward the Sun, $z$ points toward the north pole and $y$ completes the right-handed coordinate system (i.e. positive toward dusk).

2.2.1. Latmos Hybrid Simulation (LatHyS)

LatHyS (Modolo et al., 2016) is a hybrid model that describes the 3-D plasma environment around weakly magnetized and unmagnetized planetary bodies. The model has been previously applied to Mercury (Richer et al., 2012), Mars (Modolo et al., 2016; Romanelli et al., 2018a,b), Ganymede (Leclercq et al., 2016) and Titan (Modolo et al., 2007). See Modolo et al. (2016) for further details on LatHyS.

The spatial and temporal resolution used in the LatHyS simulation are $\Delta x = 145$ km and $\Delta t = 0.02$ s. Two solar wind ion (H$^+$ and He$^{++}$) and two planetary ion (Na$^+$ and H$^+$) species are considered in the simulation. The Na$^+$ (H$^+$) ion density distribution in LatHyS is derived from a simple homogeneous Na (H) density model with a surface number density of $10^5$/cm$^3$ ($10^4$/cm$^3$) and a scale height of 50 km (1292 km). Macro-particles from the planetary ion distribution are added directly to the total particle count of the simulation.

2.2.2. Adaptive Ion-Kinetic Electron-Fluid (AIKEF)

AIKEF is another hybrid model which has also been used to describe the interaction between magnetized plasma and different types of obstacles, such as planets, moons and comets (Müller et al., 2011). AIKEF has been employed in the past to study Mercury’s apparent double magnetopause (Müller et al., 2012), the impact of a temporally variable coronal mass ejection on Mercury’s magnetosphere (Exner et al., 2018) and the influence of exospheric Na$^+$ on the magnetic and electric fields inside Mercury’s magnetosphere (Exner et al., 2020).

The AIKEF simulation employs a grid size defined by $\Delta x = 100$ km, a time step $\Delta t = 0.01$ s and a larger number of macro-particles compared to LatHyS (see Table 2). This means that the AIKEF solution have better statistics compared to LatHyS. We only consider solar wind and planetary H$^+$ in this AIKEF simulation. AIKEF uses so called “ghost
particles” with negligible density to fill vacuum regions above Mercury’s nightside surface.

2.2.3. Latmos IoniZed Exosphere (LIZE)

Even with current high-performance computing, it is still not possible to simulate directly the three ion populations in the two hybrid models with good statistics. The global structure of Mercury’s magnetosphere is not altered significantly by a tenuous sodium exosphere (Exner et al., 2020). Therefore, a valid method to reconstruct the planetary ion density with sufficient statistics under stationary upstream conditions, is to employ a test-particle model with a static electromagnetic environment.

The Latmos IoniZed Exosphere (LIZE) model is a test-particle model that describes the ion density of planetary ions in the magnetosphere of Mercury. The planetary ion populations are produced by photo-ionization of exospheric neutrals. We use the simulated ion production rate from EGM to define the statistical weights of the test-particles. The full equation of motion of the test-particles is then computed using a Fourth-order Runge-Kutta scheme employing the electromagnetic fields calculated from LatHyS or AIKEF.

The test-ions are injected in the whole 3-D volume and then tracked until they leave the simulation box, impact the surface or exceed a postulated maximum iteration count. 100 test-particles are launched in each cell with zero initial velocity. We find that a non-zero injection velocity that is comparable to the average velocity distribution of the neutrals does not change the results. We use a static spatial grid but an adaptive time step that is limited by the gyro radius and the size of the LatHyS (or AIKEF) spatial grid. We use a spherical coordinate system that is logarithmic in \( r \) and uniform in both co-latitude \( \theta \) and longitude \( \phi \) (see Table 3).

![Figure 2: The neutral He, O and Na density computed with EGM, here shown in the equatorial (top row) and the noon-midnight meridional plane (bottom row). The curved lines show the location of the magnetopause and bow shock boundaries (Winslow et al., 2013).](image)

3. Results

3.1. Neutral density

Figure 2 shows the simulated neutral He, O and Na density at aphelion from the EGM in the MSO XY plane (top row) and the MSO XZ plane (bottom row). The neutral density was averaged between \( TAA = 170 - 190^\circ \) to give an accurate description of the exosphere at aphelion (\( TAA = 180^\circ \)). At this point in the orbit the average neutral density
Ion density distribution of Na+, O+ and He+ in Mercury’s magnetosphere

typically reaches its maximum value (Cassidy et al., 2015) and the photo-ionization rate its minimum value. Rather than averaging the neutral density over all possible TAA s with the EGM, computing the ion density at aphelion may be sufficient to give us a broad idea of the average ion density that we can expect over the whole Mercury orbit. The neutral density in the XY (XZ) plane was averaged over a volume segment spanning ±10° in latitude (longitude). The He and Na exospheres are seen to extend well beyond the magnetospheric boundaries while the O exosphere concentrated to low altitudes (see Figure 2).

The location of the magnetopause boundary in Figure 2 was calculated from the Shue et al. (1997) model described in Winslow et al. (2013) that has been fitted to MESSENGER MAG data and then corrected for the solar wind ram pressure of our simulation ($P_{ram} = 8$ nPa; Table 2). The bow shock location was then determined from the Slavin et al. (2007) model and corrected for the solar wind Alfvén Mach number ($M_a = 5.2$; Table 2) following the scaling method proposed by Winslow et al. (2013).

The He exosphere is characterized by a higher density on the nightside (see Figure 2a and 2d), which is in agreement with Mariner 10 observations (Broadfoot et al., 1976). The maximum He density is $6.3 \times 10^{4}$ cm$^{-3}$ at the midnight surface. The total He supply rate ($5.9 \times 10^{23}$ s$^{-1}$) is balanced by 32% thermal escape ($1.9 \times 10^{23}$ s$^{-1}$) and 68% loss by photo-ionization (4.0 $\times 10^{23}$ s$^{-1}$).

The simulated O ejection rate $3.7 \times 10^{22}$ s$^{-1}$ was fitted to the upper limit on the average O tangent column density between 0-500 km above the subsolar point ($2.0 \times 10^{10}$/cm$^{2}$; Mcclintock et al., 2018) inferred from UVVS observations (Vervack et al., 2016). The O density is highest at noon ($9.9 \times 10^{2}$ cm$^{-3}$). The total O supply rate ($3.7 \times 10^{22}$ s$^{-1}$) corresponds to 64% loss by photo-ionization ($2.4 \times 10^{22}$ s$^{-1}$) and 36% thermal escape ($1.3 \times 10^{22}$ s$^{-1}$). We did not study the seasonal variability of the global O ion production rate with EGM.

The Na surface density is lowest on the nightside ($9.2 \times 10^{1}$ cm$^{-3}$ at the surface), has a local maximum at the dusk terminator ($1.7 \times 10^{4}$ cm$^{-3}$) and a global maximum at the dawn terminator ($5.9 \times 10^{4}$ cm$^{-3}$). Between TAA = 170 – 190°, the Na exosphere is mainly supplied by photo-desorption ($3.4 \times 10^{25}$ s$^{-1}$) and to a much lesser degree by micro-meteoroid vaporization ($1.7 \times 10^{23}$ s$^{-1}$) and solar wind ion sputtering ($1.9 \times 10^{23}$ s$^{-1}$). Thermal desorption is negligible with respect to the other ejection processes at aphelion. The global Na supply rate ($3.5 \times 10^{25}$ s$^{-1}$) is balanced by 37% loss by photo-ionization ($1.3 \times 10^{25}$ s$^{-1}$) and 63% thermal escape ($2.2 \times 10^{25}$ s$^{-1}$). When we compare the global Na+ ion production rate at different TAA, we find that the maximum photo-ionization loss rate of neutral Na occurs during aphelion ($1.3 \times 10^{25}$ s$^{-1}$) and the minimum is located at TAA = 60° ($1.5 \times 10^{24}$ s$^{-1}$). The Na+ production rate is roughly proportional to the total number of Na atoms in the exosphere (altitude range: 0-2 R$_M$), which also has a maximum at aphelion ($3.1 \times 10^{29}$ atoms) and a minimum at TAA = 60° ($1.4 \times 10^{28}$ atoms) in our model.

The seasonal variation of the global Na+ production rate from our model agrees very well with the Jasinski et al. (2021)’s estimates at perihelion and the first part of Mercury’s outbound orbit around the Sun (i.e. $3.0 \times 10^{24}$ s$^{-1}$ at TAA = 0°, $1.5 \times 10^{24}$ s$^{-1}$ at TAA = 60° and $3.8 \times 10^{24}$ s$^{-1}$ at TAA = 120°). However, during the inbound orbit our model produces much higher values than Jasinski et al. (2021) (i.e. $1.1 \times 10^{25}$ s$^{-1}$ at TAA = 240° and $5.1 \times 10^{24}$ s$^{-1}$ at TAA = 300°). There is no estimate to compare our model to at TAA = 180° due to the lack of UVVS and THEMIS observations near aphelion.

3.2. Mercury’s magnetosphere

Figure 3 shows the solar wind H+ density, the absolute magnetic and electric field ($|B|, |E|$), and the H+ plasma bulk velocity ($V_{bulk}$) in the equatorial plane from LatHyS and AIKEF.

LatHyS and AIKEF yield very similar solar wind H+ density distributions, electromagnetic fields and bulk velocities. The bow shock and magnetopause stand-off distances are smaller for AIKEF. The magnetopause boundary is also more compressed toward the tail for AIKEF (see Figure 3a and 3e). There are a few small regions with high electric field ($|E| \approx 5$ mV/m) relative to the surroundings ($|E| \approx 0$) close to the surface in both models (see Figure 3c and 3d). Test-particle ions which encounter these regions in the LIZE model may be subject to sudden particle acceleration. However, we find that these regions are too small (∼ 200 km$^2$) to have a substantial impact on the ion velocities. There exists a rather dense nightside ion ring distribution in the AIKEF simulation. The H+ ions in this region have likely become momentarily trapped in the closed field region of Mercury’s intrinsic field and experience a slow azimuthal drift toward the dayside. However, this ion population is unlikely to form a steady ion drift belt due to the small size of the magnetosphere.

In order to check the accuracy of our LIZE model, we simulated the solar wind H+ density distribution with LIZE using the input parameters of the LatHyS and AIKEF simulations (see Table 2) and compared the results to Figure 3a and 3e to validate the simulated density by LIZE. We launched 250,000 test-particles at X=3.4 R$_M$ uniformly
Ion density distribution of Na\(^+\), O\(^+\) and He\(^+\) in Mercury’s magnetosphere

Figure 3: The outputs from two hybrid simulations. (a,e) The solar wind H\(^+\) density, (b,f) the total magnetic field, (c,g) the electric field and (d,h) the bulk velocity in the equatorial plane from LatHyS (top row) and AIKEF (bottom row) respectively. The solid white lines in each figure show the location of the magnetopause and bow shock boundaries.

The H\(^+\) ion density distribution simulated with LIZE differ by less than 10% compared to Figure 3a and 3e. This is an indication that our method to reconstruct the ion density in LIZE yields accurate result.

3.3. Ion density

3.3.1. FIPS data analysis

FIPS was a TOF ion mass spectrometer with the ability to detect ions with m/q = 1-40 amu/e and an energy-per-charge E/q between 0.046 - 13.6 keV with 64 exponentially spaced energy channels (Andrews et al., 2007; Gershman et al., 2013). The effective field-of-view (FOV) of the instrument (1.15 \(\text{sr}\)) permit detection of ions coming from a wide range of directions with an angular resolution of 15°. During normal operation mode FIPS completed a scan of the full E/q range every 65 s. The second operation mode, the burst mode, was used to make frequent scans every 10 s (Gershman et al., 2013).

We extend the analysis by Raines et al. (2013) to the whole set of FIPS ion density \((n_{\text{obs}})\) observations accumulated between 23 March 2011 and 30 April 2015. Following Figure 3 in Raines et al. (2013), we plot the average ion density distribution of the Na\(^+\)- and O\(^+\)-group ions and He\(^+\) as a function of local time and altitude (see the top row of Figure 3.3.1). We restrict our analysis to the latitude range ±30° centered on the equatorial plane. We use a grid with 0.5 h resolution in local time and 100 km in altitude identical to the grid that was used to make Figure 3 in Raines et al. (2013). The color map and color scale in Figure 3.3.1a-c is also identical to Figure 3 in Raines et al. (2013).

There exist two main enhancement regions in Figure 3.3.1a-b. The low-altitude enhancement extends between 6 - 12 local time and up to an altitude of 2000 km. The second, high-altitude enhancement extends between 16.5 - 21 h up to 6000 km. Both enhancement regions roughly follow the altitude profile of the magnetopause, but extends farther into the magnetosheath around noon. He\(^+\) exhibits a low-altitude enhancement region at dawn similar to those observed for the Na\(^+\) and O\(^+\)-group ions, but no high-altitude dusk enhancement. There also exists a narrow enhancement region located inside the magnetosheath at 18 h (altitude 5000-8000 km) for all three ion species. This enhancement feature is either missing or not as prominent in the (Raines et al., 2013) data set.

The observed ion density \((n_{\text{obs}})\) by FIPS is defined as

\[
\sum_{i} f_i v_i^2 (\Delta v_i) \Delta \Omega
\]

where \(f_i\) is the phase space density (PSD), \(v_i\) is the velocity, \(\Delta v_i\) is the velocity range, \(i\) corresponds to the index of the \(E/q\) step in FIPS operation and \(\Delta \Omega\) is FIPS solid angle. The product between \(f_i\) and \(v_i^2 (\Delta v_i)\) is summed over each
Ion density distribution of Na\(^+\), O\(^+\) and He\(^+\) in Mercury’s magnetosphere

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Ion density distribution of Na⁺, O⁺ and He⁺ in Mercury’s magnetosphere

**Figure 4:** (Previous page.) Top row: The average observed ion density by FIPS of the (a) Na⁺ group, (b) O⁺ group and (c) He⁺ in the latitude range ±30°. Second row: Simulated ion density of (d) Na⁺, (e) O⁺ and (f) He⁺ with LIZE using the static magnetic and electric field description by LatHyS, including FIPS energy range and FOV constraints. Third row: Ratio between between the energy range and FOV-corrected simulated ion density and the observed ion density (grid resolution: 400 km, 2 h). The average ion density ratio below the magnetopause is 18 for Na, 0.25 for O and 5.2 for He. Bottom row: the full ion density (no energy range or FOV constraints) simulated with LIZE. The FIPS observations were accumulated between 23 March 2011 and 30 April 2015. The solid white lines show the magnetopause and bow shock boundaries as determined from Winslow et al. (2013). Do note that the sense of the magnetospheric boundaries are reversed in this Figure compared to Figure 3. Thus, points that appear to be located "inside" the parabolas in this Figure are in fact located outside the magnetosphere.

The main limitation to FIPS nominal FOV (1.4 π sr) is caused by the sunshade of the spacecraft. The sunshade always points along the positive MSO X-axis irrespective of where the spacecraft is located relative to Mercury. This means that the true FOV extends between 15° from directly behind the sunshade up to 45° from the rear. The FOV is also partially blocked by one of the solar cell panels and other smaller parts on the spacecraft, so that the effective FOV solid angle is 1.15π sr. Since this study considers the ion density distribution averaged over several Mercury years we only consider the main limitations to the FOV along the MSO X-axis (see Figure 5).

The FIPS clock angle, which is defined as the angle between the positive MSO Y-axis and the FIPS boresight, describes the rotation of the spacecraft relative to the MSO frame. Specifically, this defines whether one hemisphere is sampled more than the other. The clock angle distribution for FIPS measurements taken within 0.15 R₉ of the geocentric equator between 2011-2015 is almost equal between the dusk and dawn hemispheres. Therefore, we can assume that FIPS samples both MSO Y-hemispheres in the latitude range ±30°. Due to MESSENGER's highly elliptic polar orbit, the lowest (highest) altitude range in Figure 3.3.1 (top row) will be mostly sampled when the spacecraft is moving toward the north (south) pole. Therefore, the lowest (highest) altitude range may be dominated by ions with \( v_z < 0 \) (\( v_z > 0 \)). In this study we make the assumption that the FIPS instrument samples MSO \( Z > 0 \) and \( Z < 0 \) equally. The ions in our model tend to have small \( v_z \) velocities so the specified selection effect is likely not significant near the equatorial plane (see Section 4.4 where we will discuss the ion velocity distribution in greater detail).

The new simulated Na⁺, O⁺ and He⁺ ion density maps that have been corrected for FIPS limited energy range and...
FOV are shown in the second row of Figure 3.3.1. The average ion density has decreased for all species but density enhancement between 18 - 24 h remains. The dawn hemisphere now exhibits a sharp drop-off in ion density before 6 h, similar to what is observed in the FIPS data (top row of Figure 3.3.1). We continue our comparison by making a ratio (see the third row of Figure 3.3.1) between the new simulated and observed ion density. We use a grid with coarser resolution (2 h, 400 km) and reduce the altitude range to 800-6000 km (to exclude bins with few FIPS observations).

The average ion density ratio below the magnetopause is 18 for Na$^+$, 5.2 for He$^+$ and 0.25 for O$^+$. In this study, we have used two hybrid models. On average, AIKEF yields slightly higher ion densities compared to LatHyS but the spatial distribution is nearly identical (see Figure 6). One of the key differences between the two models is a low-altitude (< 1000 km) enhancement region which exists at all local times for AIKEF.

4. Discussion

4.1. Comparison with previous simulations of the Na$^+$ density

When we compare our uncorrected ion density estimate (see Figure 3.3.1d-f) with previous modeling studies of the Na$^+$ ion density distribution in Mercury’s magnetosphere (Leblanc et al., 2003; Yagi et al., 2010; Seki et al., 2013; Exner et al., 2020) we find a similar order of discrepancy between the different models and the observations. Leblanc et al. (2003) used the exospheric model described in Leblanc and Johnson (2003) with the analytic magnetospheric model by Delcourt et al. (2003) to trace Na$^+$ ions inside the magnetopause boundary. They found a maximum Na$^+$ density of $10^2$/cm$^3$ at aphelion ($TAA = 180^\circ$), which is close to our uncorrected simulated Na$^+$ density (see Figure 3.3.1). Paral et al. (2010) found a maximum Na$^+$ ion density on the order of $10$ cm$^{-3}$ in the equatorial plane for an IMF with a strong northward component. Yagi et al. (2010) modeled the Na$^+$ density for purely northward IMF ($B_z = 10$ nT) with the neutral exosphere model from Leblanc and Johnson (2003) and a MHD magnetospheric model to describe the electromagnetic field environment. Their Case 1 ($n_{sw} = 30$ cm$^{-3}$, $v_{sw} = 400$ km/s) results gives a similar Na$^+$ density in the dawn hemisphere ($10^2$ cm$^{-3}$). Seki et al. (2013) studied the impact of varying southward IMF strength and planetary conductivity on the Na$^+$ ion density distribution using an MHD magnetospheric model. Exner et al. (2020) studied the impact of successively denser versions of a Na$^+$ exosphere on the Mercury field environment. For the standard exosphere they found a maximum Na$^+$ density of $10$ cm$^3$ at the cusps. What is common for all these studies is that the modeled maximum Na$^+$ density is a factor of $10 - 10^3$ times too high compared to the FIPS observations.

Sarantos et al. (2009) used the exospheric Na model from Mura et al. (2007), with a maximum Na surface density of $10^5$ cm$^{-3}$ and a MHD simulation with the solar wind IMF profile of the first MESSENGER flyby Benna et al. (2010) to model the distribution of Na$^+$ pickup ions. They studied the ion density distribution of Na$^+$ produced from neutral Na ejected by different source mechanisms. Sarantos et al. (2009) derived a maximum Na$^+$ density of $1$ cm$^{-3}$, which is relatively similar to the observed Na$^+$ ion density by FIPS compared to other modeling studies. The MHD simulation...
Ion density distribution of Na$^+$, O$^+$ and He$^+$ in Mercury’s magnetosphere

Figure 6: The (a) Na$^+$, (b) O$^+$ and (c) He$^+$ ion density simulated with LIZE using the static magnetic and electric field description by AIKEF.

used in Sarantos et al. (2009) simulation has a lower spatial resolution (122-1952 km) compared to the magnetospheric models in our study. Perhaps for this reason the mean energy of the Na$^+$ plasma sheet ions in their simulation is $10^2$ times higher than in our simulation (see Figure 4 in Sarantos et al., 2009).

4.2. Comparison with other estimates of the ion density

It is also possible to derive the Na$^+$ density distribution around Mercury from the study of magnetic field-line-resonance (FLR) events (James et al., 2019). FLR events occur when a fast-mode MHD wave converts into a shear Alfvén wave in a non-uniform plasma environment. If this occurs near Mercury’s dipole magnetic field, the resonant wave coupling may cause the formation of a standing wave in the closed magnetic field lines, oscillating at the fundamental plasma frequency (Glassmeier et al., 2004). At Mercury a subset of these waves has a frequency that lies below the local Na$^+$ ion gyro frequency, which indicates that the field line resonance is formed in a plasma dominated by Na$^+$ ions. James et al. (2019) identified such events using MAG data, the KT17 magnetic field line model (Korth et al., 2015, 2017) and a simple power-law model of the plasma mass density to map the ion density inside the closed field-line-region in the dayside magnetosphere. The plasma density estimate that can be inferred using this method is not limited by a specific energy range or FOV. Using a relaxed Earth-type FLR event criteria James et al. (2019) inferred a maximum plasma mass density of 500 amu/cm$^3$, which would imply a dayside Na$^+$ surface density of approximately 22/cm$^3$ (Exner et al., 2020).

Figure 7 shows the Na$^+$ ion density in the equatorial plane in units of amu/cm$^3$ (comparable to Figure 6e in James et al., 2019). The contribution from He$^+$ and O$^+$ to the total plasma mass density is negligible. Although our simulated Na$^+$ density is higher compared to Figure 6e in James et al. (2019), the difference is considerably lower than direct comparison with the FIPS observations. Most importantly, the maximum simulated plasma mass density near the surface (550 amu/cm$^3$ or 24 Na$^+$/cm$^3$) is a close match to James et al. (2019)’s estimate.

Another in-situ observation we could refer to get some clues about the ion density magnitude in the Hermean magnetosphere are the Mariner 10 Mercury flybys. During the Mariner 10 flyby on 1974 March 29, the electrostatic analyzer took electron density measurements in Mercury’s plasma wake (Ogilvie et al., 1974). The spacecraft entered the magnetosphere from dusk in the southern magnetospheric lobe and exited at dawn in the north. The spacecraft reached a minimum altitude of 700 km from the surface near midnight local time in the equatorial plane at closest approach.

We model the Na$^+$, O$^+$, He$^+$ and solar wind H$^+$ ion density with LIZE along the trajectory of Mariner 10. For the electric and magnetic fields, we use the northward $B_z$ LatHyS simulation with $n_{sw} = 45.7$/cm$^3$ and $v_{sw} = 500$ km/s from the end of Section 3. The solar wind properties of this run matches the observed electron energy spectra just.
prior to the spacecraft’s entry into the magnetosphere (Ogilvie et al., 1974). We compare the observed electron density with the different simulated ion densities (full energy range and FOV) between 20:41-20:47 UTC which is when the spacecraft first enters the planet’s shadow until the time of closest approach. We find that the modeled Na\(^+\) ion density in this region is much smaller (0.5-1.0 Na\(^+\)/cm\(^3\)) than the H\(^+\) (3.7-9.0 H\(^+\)/cm\(^3\)) or the electron density (< 6.2 e/cm\(^3\)). The He\(^+\) and O\(^+\) densities are negligible. The comparatively low Na\(^+\) density implies that the model does not give results which directly contradicts the Mariner 10 electron density observations.

4.3. Intrinsic limits of our simulated ion density

In our EGM simulation of the Na exosphere the near-surface density is ~ 5 times higher at the dawn terminator compared to the subsolar point. The EGM model reproduces the dusk-dawn asymmetry at aphelion observed by UVVS Cassidy et al. (2016). UVVS and THEMIS observations of the Na exosphere near aphelion indicates however that the maximum Na density in the exosphere is located near the subsolar point Milillo et al. (2021); Cassidy et al. (2016). This discrepancy is unlikely to affect the large-scale ion density distribution due to the fast configuration speed of the ions.

Due to the special geometry of the MESSENGER orbit, the ion density at each local time was sampled by FIPS at a particular TAA. The data at 6 - 12 h local time was, for instance, taken when Mercury was located between TAA= 0° – 90°. The Na exosphere has a strong dawn peak during this part of the orbit (Cassidy et al., 2015, 2016), which might help explain the Na\(^+\) enhancement at dawn in Figure 3.3.1a.

The static electromagnetic field environments used in our study may be responsible for the large underestimation of the ion density upstream of the magnetopause (Figure 3.3.1). Without a time-dependent electromagnetic field description it is not possible to account for temporal variations of the position of the magnetic boundaries, magnetic reconnection and other plasma processes.

The average O\(^+\) ion density in our simulation is low in comparison to Na\(^+\) or He\(^+\). Since the O\(^+\)-group includes several species it is possible that O\(^+\) is not the main constituent of the total O\(^+\)-group ion density (Vervack et al., 2016). It may therefore be necessary to consider the photo-ionization of water ices on Mercury. The Na\(^+\)-group includes several ion species with similar mass-per-charge ratio to Na\(^+\), which includes Mg\(^+\), Al\(^+\) and Si\(^+\). The neutral Mg exosphere is thin (5-50/cm\(^3\) at the surface; Merkel et al., 2017) and the Mg photo-ionization rate (6.5 \(\times\) 10\(^{-7}\) s\(^{-1}\); Huebner and Mukherjee, 2015) is low compared to Na. Therefore Mg\(^+\) is unlikely to make a large contribution to the total Na\(^+\)-group ion density. Evans et al. (2012) inferred a Si (weight) surface abundance of 24.6% with observations by the Gamma-Ray and Neutron Spectrometer (GRNS) on MESSENGER, which corresponds to a number density that is approximately half that of Na. Al has been observed in Mercury’s exosphere with ground-based observations (Bida et al., 2000; Bida and Killen, 2017) and by MESSENGER (Vervack et al., 2016). In addition, both Al and Si
Ion density distribution of Na$^+$, O$^+$ and He$^+$ in Mercury’s magnetosphere

Table 4
Parameters of the LIZE simulations with different solar wind and IMF conditions. The ion density ratio is defined as the average ratio between the simulated and observed ion density in the altitude range 800-6000 km and below the magnetopause boundary.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Nominal case</th>
<th>Case 1</th>
<th>Case 2</th>
<th>Case 3</th>
</tr>
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<td>11 cm$^{-3}$</td>
</tr>
<tr>
<td>Solar wind velocity:</td>
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<td>500 km/s</td>
<td>400 km/s</td>
<td>400 km/s</td>
</tr>
<tr>
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<td>(-10, 7.5, 13)</td>
<td>(-9.3, 7.7, -13)</td>
<td>(-9.3, 7.7, -13)</td>
</tr>
<tr>
<td>Ion density ratio:</td>
<td>Na$^+$: 18</td>
<td>Na$^+$: 2.7</td>
<td>Na$^+$: 1.6</td>
<td>Na$^+$: 0.8</td>
</tr>
<tr>
<td></td>
<td>He$^+$: 5.2</td>
<td>He$^+$: 1.1</td>
<td>He$^+$: 0.8</td>
<td>He$^+$: 0.5</td>
</tr>
</tbody>
</table>

have very high photo-ionization rates (Al: $1.2 \times 10^{-3}$ s$^{-1}$ and Si: $2.29 \times 10^{-5}$ s$^{-1}$; Huebner and Mukherjee, 2015) compared to Na. Jasinski et al. (2020)’s estimate of the Al and Si ion production rate (3-7.5/cm$^3$ at 1500 km) during a large meteoroid impact event can be considered as an upper limit.

Our simulated ion densities reflect a single set of solar wind plasma conditions, IMF orientation and orbital phase. In comparison, the FIPS data displayed in Figure 3.3.1a-c represent an average over 17 Mercury years of observations, and accounts for a wide range of solar wind and exospheric conditions. As the FIPS data reflect the average state of the exosphere, some features may not be as prominent in the FIPS observations as in the simulated ion density. The dusk enhancement region is very dense compared to other regions in our simulation and extends to higher altitudes compared to the observations. This may be an effect of the electric field environment that the test-particle encounter at the flanks of the dayside magnetopause boundary. For solar wind IMF $B_z > 0$ we get $E_y < 0$ in the solar wind (and the magnetosheath). Ions that encounter the duskside magnetopause flank are affected by a strong $E_x < 0$ environment and $E_y < 0$, which will cause these ions to be pushed deep into the low electric field environment of the nightside plasma sheet. The pink-purple Na$^+$ test-particle trajectory in Figure 8 shows an example of this effect. Ions that approach the magnetopause flank from the dawnside experience $E_x > 0$, which makes them more likely to be picked up by the solar wind and quickly escape the Mercury environment. Therefore, for the specific solar wind IMF studied here we will naturally get a low-density, high-energy dawnside ion population and a high-density duskside. The dusk enhancement could also be due to the non-adiabatic ion acceleration mechanism described in Delcourt et al. (2003), but the northward IMF $B_z$ may inhibit its effects. The blue-cyan Na$^+$ test-particle trajectory in Figure 8 shows a possible example of this acceleration mechanism in action. The sudden increase in energy after 4 minutes when the test-particle was located close the surface near the north pole indicates that it may have experienced centrifugal ion acceleration (compare to Figure 2 in Delcourt et al., 2003).

The strictly northward solar wind IMF and the low solar wind ram pressure of the electromagnetic field environment considered in this work is not necessarily the most commonly observed solar wind environment at Mercury (Sarantos et al., 2007). In order to consider the impact of different solar wind conditions on the modeled ion density, we model Na$^+$, O$^+$ and He$^+$ using three additional LatHyS simulations (see Table 4). We find that the average ion densities computed from these simulations are much closer to the observed values. The difference between model and observations range between a factor of 0.8-1.5 for Na$^+$ and 0.5-1.1 for He$^+$. The O$^+$ density tends to be underestimated. However, although the average ion density ratio is improved the spatial distribution is very different from our nominal case. Following the argument concerning the sign of $E_x/E_y$ and their impact on the properties of the ion populations on either side of the nightside plasma sheet, we find that Cases 1-3 result in weaker dusk- and stronger dawn enhancement than expected from the FIPS observations. The LatHyS simulations corresponding to Cases 1-3...
Ion density distribution of Na$^+$, O$^+$ and He$^+$ in Mercury’s magnetosphere

Figure 8: Model test-particle trajectories of Na$^+$ ions from the Latmos IoniZed Exosphere model in the (a-c) MSO XZ-plane and the (d-f) XY-plane. The time-evolution of the test-particle ion energy are shown in (g-i). The dashed curves in (a-f) shows the average location of Mercury’s magnetopause. The three test-particles were launched in the dayside magnetosphere (b, c) near the north pole and (a) near the subsolar point (start location shown by the dot markers). The test-particles experience different electromagnetic fields: (a, c) solar wind and IMF conditions corresponding to the nominal case in Table 4 and (b) Case 2 in Table 4. The color gradient in each trajectory shows the evolution of time.

have a lower resolution compared to our nominal case, which may result in higher electric fields in low-density regions inside the magnetosphere which would result in higher test-particle acceleration and lower densities. Regardless, it is clear that the ion density distribution of heavy ions around Mercury have the potential of being highly variable. Since the ion density observations by FIPS discussed in this paper reflects a wide range of solar wind and exosphere conditions, it may be necessary to test more representative solar wind and IMF conditions in order to re-produce the observed distribution as closely as possible.
Global models of Mercury’s magnetosphere tend to underestimate the magnetopause reconnection rate for northward solar wind IMF boundary conditions. In effect, this likely causes the average level of Dungey cycle circulation (Dungey, 1961) to be underestimated. Therefore the planetary ion population in our nominal $B_z > 0$ simulation may experience an uncharacteristically weak electric field environment. This aspect could partly explain why we’re seeing such a large factor difference between our model results and the FIPS observations for that specific IMF orientation.

The low-altitude enhancement in the modeled ion density profiles with AIKEF may be another effect of the underestimated ion dynamics on the magnetosphere. This ion population is comparatively energetic (10^5 eV) compared to ions at higher altitudes and may be the result of a quasi-trapped ion ring, similar to what has been proposed in Yagi et al. (2010, 2017). Indeed, the yellow-orange $Na^+$ test-particle trajectory in Figure 8 and other test-particle trajectories in this region show a remarkable similarity to Figure 10 in Yagi et al. (2010) and Figure 3 in Yagi et al. (2017) respectively. The large magnetopause standoff distance during northward IMF and the steady-state magnetospheric fields used in our simulations are likely favorable for the formation of a quasi-steady ring distribution. If the IMF is southward or the short-term variability of the IMF is accounted for the ring distribution may not be as complete as indicated here.

4.4. Reconstruction of the phase space density (PSD)

Judging from Figure 3.3.1j-l the ratio between the simulated and the observed ion densities are not homogeneous. The simulated ion densities tend to diverge more from the observed values with increasing distance from the surface, which is most evident at midnight local time. The ratio is higher in the dusk enhancement region than at dawn, and it is very low near the magnetopause boundary at noon. To investigate the impact of FIPS FOV on the ion density distribution in the magnetosphere in more detail it is necessary to model the phase space density (PSD) distribution.

We model the PSD distribution in four different regions and investigate how FIPS energy range and FOV affects the sampling of the simulated ion density distribution. We select regions located at noon and the dawn enhancement region in the dayside magnetosphere, the dusk enhancement region on the nightside and the dawn magnetosheath (see Figure 9a). The four regions are all centered in the magnetic equatorial plane and range in size between $(\Delta x)^3 = (300\text{km})^3$ to $(\Delta x)^3 = (750\text{km})^3$. Inside the magnetic equatorial plane the FIPS clock angle is such that the boresight of the instrument is predominantly directed toward the dusk hemisphere (approximately 4 times more frequently). Therefore we will only consider the $v_y < 0$ sector in the $v_x - v_y$ plane (see Figure 9). We first compute the PSD on a spherical grid $(E, \theta, \phi)$ with LIZE and then make a transformation to Cartesian velocity coordinates $(v_x, v_y, v_z)$. This allows us to plot $v_x - v_y$ and $v_y - v_z$ slices of the 3-D PSD distribution.

As shown by Figure 9, the $Na^+$ PSD has a distinct spatial distribution in each of the four region. The PSD in Region A is dominated by a dawnward ($v_y < 0$) drift (see Figure 9b). The proximity of Region A to the magnetopause and the strong influence of the dawn- and anti-sunward drift of the solar wind convection field near Region A may be the cause of this particular distribution. Since the FIPS boresight is typically pointing toward the dusk hemisphere in this region, it is well suited to sample a PSD of this type. However, a slice of the same PSD distribution in the $v_x - v_z$ plane reveals that the PSD is concentrated to a narrow region around the MSO X-axis that is blocked from FIPS FOV by the sunshade (Figure 9c). This means that only a fraction of the PSD will be detected by FIPS despite the favorable distribution of the PSD in the $v_x - v_y$ plane. The distribution is far from being isotropic, yet the PSD tends to be more isotropic at lower energies (see Figure 9c).

Region B has a ring-like PSD distribution in the XY plane (Figure 9d) and is rather isotropic in the XZ plane (Figure 9g). Although the maximum of the PSD distribution in Region C (Figure 9e) appears to be located inside FIPS energy range, the global maximum is actually located below FIPS lower energy range (at approximately 10 eV). The PSD in Region D (Figure 9f) resembles a pick-up ion distribution. This implies that the $Na^+$ ions in Region D have been accelerated from outside the magnetopause into the dawn magnetosheath. The PSD distribution of this region peaks at velocities well outside the upper energy range of FIPS in both the $v_x - v_y$ and the $v_x - v_z$ plane, which makes the ions in this region invisible to FIPS.

Although the relative intensity of the PSD differs between the three different species, the spatial distribution is very similar in the MSO XY and XZ plane (see Figure A1-A3 in the appendix). The PSD distribution in Region D has been omitted for $O^+$ due to poor statistics. It is interesting to note that in contrast to $Na^+$, the $He^+$ PSD distribution in Region D falls inside the upper limit of FIPS energy range. In the XZ plane, the PSD distribution is generally concentrated to the non-observable part of phase space for FIPS. The PSD in Region B has the most dispersion in the XZ plane, likely because this region is located far away from the planet and the ions transported here have had more time to disperse. On average LatHyS and AIKEF yields very similar PSD distributions. One key difference between the two models is that...
the PSD computed with AIKEF in Region B is concentrated to lower energies in the XY plane and is less dispersed in the XZ plane compared to LatHyS. This suggests that the electric field in Region B is lower in the AIKEF simulation than for LatHyS. Indeed, the anti-sunward component of the electric field in the AIKEF simulation is -0.09 mV/m in Region B compared to -0.8 mV/m for LatHyS.
5. Conclusions

We have analyzed the average ion density and spatial distribution in the equatorial plane inside Mercury’s magnetosphere of the Na⁺-group, O⁺-group and He⁺, which were observed by FIPS onboard MESSENGER during the whole orbital mission from 23 March 2011 to 30 April 2015. We developed a test-particle model that describes the full equation of motion of planetary ions produced from photo-ionization of Mercury’s neutral exosphere. The model is coupled to a test-particle model of the neutral exosphere (EGM; Leblanc et al., 2017b) and two hybrid models of the electric and magnetic fields in the magnetosphere (LatHyS and AIKEF; Modolo et al., 2016; Müller et al., 2012).

We modeled the neutral Na, O and He exospheres at aphelion with EGM and used static electromagnetic field simulations from the two models using the same set of solar wind input parameters to model the ionized Na⁺, O⁺ and He⁺ exospheres for northward IMF conditions. We take the FIPS energy range and FOV constraints into account when we later compare our simulated ion densities with the FIPS ion density observations.

The model reproduces the spatial distribution of the FIPS observations but the average ion density (corrected for FIPS FOV) is between 5-18 times too high compared to the observations. These values were calculated for strictly northward IMF conditions ($B_z = +20$ nT), which might have caused the average Dungey cycle strength to be underestimated (and the ion density to be overestimated). The discrepancy between model and observations is lower (0.8-2.7 for Na⁺ and 0.5-1.1 for He⁺) for other solar wind and IMF conditions. The model based on a simple neutral O exosphere tends to underestimate the observed O⁺ density. The magnitude of the simulated Na⁺ density uncorrected for the FIPS energy range and field-of-view is roughly in agreement with previous simulation studies (Leblanc et al., 2003; Paral et al., 2010; Yagi et al., 2010; Seki et al., 2013; Exner et al., 2020) even for the nominal case ($B_z = +20$ nT). We also compare our results with plasma mass density measurements inferred from FLR event observations with the MAG instrument (James et al., 2019) and electron density measurements taken by Mariner 10 in the wake of the planet on 29 March 1974 (Ogilvie et al., 1974).

Finally, we model the phase space density distribution in four different regions: at noon and dawn in the dayside magnetosphere, in the dusk magnetotail and the dawn flank of the magnetosheath. We find that the PSD is commonly concentrated to a narrow region surrounding the $v_x$ axis in the $v_x - v_z$ plane. This particular region in phase space is blocked from FIPS FOV due to MESSENGER’s sunshade, meaning that only a fraction of the total PSD can be observed. Only the relative magnitude of the PSD distribution appears to be mass-dependent and the distribution in phase space is very similar between the three different species.

The results of this study highlight the limitations of using a steady-state electromagnetic field simulation to model the ion density distribution around Mercury. The phase space density distribution of heavy planetary ions are not necessarily isotropic and vary across different regions around Mercury. One of the largest assets of EGM is its capability to give an accurate description of the exosphere at several points along Mercury’s orbit. The results by Raines et al. (2013); Jasinski et al. (2021) on the variation of the global Na⁺-group ion density along the Mercury year may suggest there is a link between the seasonal neutral Na exosphere and the Na⁺-group ion distribution in the magnetosphere. We plan to investigate this link with LIZE in more detail in future work.

BepiColombo, which will enter into orbit around Mercury in late 2025, will provide the first in-situ measurements around Mercury since the end of the MESSENGER mission in 2015. Planetary Ion Camera (PICAM) on the Mercury Planetary Orbiter (MPO) has an energy resolution between 1 eV - 3 keV and instantaneous 2π sr FOV (Orsini et al., 2010) and is uniquely suited to study low-energy ions near the surface and ions which have been recently formed. The Mercury Ion Analyzer (MIA) and the Mercury mass Spectrum Analyzer (MSA) on the Mercury Magnetospheric Orbiter (MIO; renamed to MIO after the launch) will be able to sample ions with a wide range of energies (5 eV/e - 30/40 keV/e; Saito et al., 2010). Both instruments have an instantaneous 8-10° × 360° of view, which will also make it possible to obtain the full three-dimensional distribution function of the observed ions. Finally, the UV spectrometer Probing of Hermean Exosphere By Ultraviolet Spectroscopy (PHEBUS; Chassefière et al., 2010) on MPO will make the first in-situ measurements of the neutral He exosphere since Mariner 10 and, for the first time, enable the study of the coupling between the neutral and ionized He exosphere.

6. Acknowledgments

A.L.E.W., F.L., J.-Y.C. and R.M acknowledges the support by ANR of the TEMPETE project (grant ANR-17-CE31-0016). S.A., F.L., J.-Y.C., R.M and A.L.E.W. would like to acknowledge the support of CNES for the BepiColombo mission. W.E. was supported by DFG (German Research Foundation) under contract HE8016/1-1. C.S.
A. Appendix

This appendix includes additional figures of the PSD distribution for Na$^+$ (Figure A1), O$^+$ (Figure A2) and He$^+$ (Figure A3). The figures show the PSD distribution in the MSO $v_x - v_y$ and $v_x - v_z$ plane for both the LatHyS and AIKEF. Figure A2 only includes Region A-C.

![Figure 10](image-url)

**Figure 10:** Slices of the Na$^+$ PSD in the MSO $v_x - v_y$ plane ($v_z = 0$) and the $v_x - v_z$ plane ($v_y = 0$) in Regions A-D computed with the magnetic and electric fields supplied by LatHyS and AIKEF.
Figure 11: Slices of the O\(^+\) PSD in the MSO \(v_x - v_y\) plane \((v_z = 0)\) and the \(v_x - v_z\) plane \((v_y = 0)\) in Regions A-C computed with the magnetic and electric fields supplied by LatHyS and AIKEF.
Figure 12: Slices of the He$^+$ PSD in the MSO $v_x - v_y$ plane ($v_z = 0$) and the $v_x - v_z$ plane ($v_y = 0$) in Regions A-D computed with the magnetic and electric fields supplied by LatHyS and AIKEF.
References


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