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Profile of the horizontal wind variance near the ground in near neutral flow – K-theory and the transport of the turbulent kinetic energy

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Abstract. This paper deals with the characteristics of the atmospheric turbulent flow in the vicinity of the ground, and particularly with the profile of the horizontal wind variance. The study is based on experimental measurements performed with fast cup anemometers located near the ground at 5 different levels (from 0.25 to 4 m) and sampled at 1 Hz. The experiment was carried over two agricultural plots with various tillage treatments in a fallow semiarid area (Central Aragon, Spain). The results of this study reveal that near the ground surface and under moderate wind, the horizontal wind variance logarithmically increases with height, in direct relationship with the friction velocity and the roughness length scale. A theoretical development has allowed us to link this behaviour to the modeling of the turbulent kinetic energy (TKE) transport through the eddy diffusivity. Thus, the study proposes a formulation of the similarity universal function of the horizontal wind variance. Besides, the formulation offers a new method for the determination of the friction velocity and the roughness length scale and can be used for the evaluation of the TKE transport rate.

Keywords. Meteorology and atmospheric dynamics (Turbulence; Instruments and techniques; General or miscellaneous)

1 Introduction

The wind velocity variance, which represents the turbulent kinetic energy (TKE), is an important parameter of the atmospheric surface layer (ASL) since it conditions many phenomena taking place in this layer, such as the diffusion of chemical and physical aerosols, energy transfer between the mean and the turbulent flows, heat and mass transfer, extreme wind force exercised on structures, etc.

Despite the existence of long established relationships (Panofsky et al., 1977), the behaviour of the variance of the horizontal wind components in the ASL stills discussed, specially the definition of their pertinent scaling parameters. In this very specific study, which concerns the very lower layer of the ASL, also called the “eddy surface layer (ESL)” (see Hunt and Carlotti, 2001), one has to highly consider the definition of the pertinent parameters.

In this regard, the present study will briefly present some of the literature models, of which some are empirical ones while others stem from well known theories. This will, on one hand, underline the importance of the subject and help in the definition of the pertinent parameters and, on the other hand, provide a base for comparison with the developed results.

Then, the paper will develop a range of equations showing, very near the ground, that the horizontal wind variance (or the horizontal component of the kinetic energy) is a function of the vertical coordinate z . Then, a logarithmic profile model will be proposed for the variation of the variance.

The model will then be validated with data deriving from WELSONS (Wind Erosion and Losses of Soil Nutrients in semiarid Spain), which is a European research project



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devoted to the study of desertification and land degradation by wind erosion in the European Mediterranean area (Frangi and Richard, 2000; Gomes et al., 2003) (see also Sect. 4).

2 Some bibliographical recalls

For Kaimal and Finnigan (1994), the horizontal wind components, contrary to the vertical one, are not governed by the Monin-Obukhov ASL similarity theory, which states that various atmospheric parameters and statistics, such as gradients, variances and co-variances, when normalized by appropriate powers of the scaling velocity U_* and the scaling temperature θ_* , become universal functions of the stability parameter, $\zeta = z/L$, where z is the height and L the Monin-Obukhov length. It is so because the variances of the wind horizontal components do not depend on height throughout the surface layer and most of the ABL, even in highly unstable conditions (Garraat, 1992).

In a study carried out by Hedde and Durand (1994) over the Mediterranean Sea, for heights between 30 and 50 m and for wind velocity ranging from 6 to 20 m/s, it was shown that the horizontal wind components followed the similarity theory yielding for free convection:

$$\frac{\sigma_u}{U_*} = \frac{\sigma_v}{U_*} = 2.8 \left(-\frac{z}{L} \right)^{1/3} \quad (1)$$

Saïd (1988) and Idé (1991) reported the same “1/3 power law” with a constant of 2.0 and 5.4, respectively, instead of 2.8. Contrary to the other studies, the latter one was carried out over land, in the semiarid Sahel region of Africa.

Recently, in stable conditions, Pahlow et al. (2001) analysing data from a set of five experiments, distinguished two cases according to the stability parameter. The five experiments were carried out in the ASL at heights ranging from 0.96 to 4.32 m. In weak stability conditions, i.e. when the stability parameter $\zeta \leq 0.1$, they observed that the normalized horizontal wind components adopted a local z -less stratification behaviour, thus, becoming constant (Table 1). When the stability parameter exceeds this value, they proposed the following equation:

$$\frac{\sigma_i}{U_*} = a + b \left(\frac{z}{L} \right)^c \quad (2)$$

where i represents u and v . a , b and c equal 2.3, 4.3, and 0.5, respectively, for the longitudinal component, and 2.0, 4.0 and 0.6 for the transversal wind.

As reported in Table 1 (i.e., Raupach et al., 1990; Hedde and Durand, 1994), in neutral or near neutral conditions, many authors reported a ratio of 2 between the longitudinal and the transversal variances (Grant, 1986, 1992; Drobinski et al., 2004).

For turbulence in near-neutral ASL, Solari (1987) proposed a relationship in which the normalised longitudinal variance, β_u , depends on the terrain roughness, Z_0 , i.e.:

$$\beta_u = \frac{\sigma_u^2}{U_*^2} = \begin{cases} 7.5 & \text{for } Z_0 \leq 0.03 \\ 4.5 - 0.856 \ln(Z_0) & \text{for } 0.03 \leq Z_0 \leq 1 \\ 4.5 & \text{for } Z_0 \geq 1 \end{cases} \quad (3)$$

where Z_0 is expressed in meters.

In a recent study, Carlotti (2001) proposed a pure blocking Rapid Distortion Theory (RDT) model adapted for sheared neutral boundary layers and taking into account a -1 intermediate subrange in the longitudinal velocity spectrum (E_{11}) only. This model shows:

$$\begin{cases} \frac{\overline{u'^2}}{U_*^2} \approx \frac{c_{11}}{c_{13}} \left[1 + 0.5 \ln \left(\frac{\Lambda}{z} \right) \right] + \frac{c_{33}}{c_{13}} \beta_{13}^2 \\ \frac{\overline{v'^2}}{U_*^2} \approx \frac{c_{22}}{c_{13}} \left[1 + 0.5 \ln \left(\frac{\Lambda}{z} \right) \right] \\ \frac{\overline{w'^2}}{U_*^2} \approx \frac{c_{33}}{c_{13}} \end{cases} \quad (4)$$

where the constant c_{ij} are of order one, Λ is the length scale characterising the lower limit of the -1 range in the spectrum ($\Lambda \approx z_i U / U_*$, see Hunt and Morrison, 2000) and β_{13} an unknown shear parameter.

3 Theoretical background

The above bibliographical study has allowed for presenting the different theories, concepts and results encountered in the literature related to the modeling of the horizontal wind variance. This section is intended to present a different theoretical approach to the modeling of the horizontal wind variance profile, in ASL.

Departing from the Navier-Stokes equations of the turbulent flow (cf. Appendix A) and assuming the existence of horizontal homogeneity, in order to neglect the horizontal variation of the different parameters, the equation of the horizontal wind fluctuations is (see also Eq. A5):

$$2\overline{u'u'} \frac{\partial \overline{u}}{\partial z} + \frac{\partial \overline{w'u'^2}}{\partial z} + \frac{\partial \overline{w'v'^2}}{\partial z} + 2\varepsilon_h = 0 \quad (5a)$$

where:

- $\overline{u}$ and u' are the mean and the fluctuation of the longitudinal wind velocity
- v' , the fluctuation of the transversal wind velocity
- w' , the fluctuation of the vertical wind velocity
- z , the vertical coordinate or height
- $\varepsilon_h = \varepsilon_1 + \varepsilon_2$, the horizontal components of the TKE dissipation rate, i.e.:

$$\varepsilon_1 = \nu \left[\left(\frac{\partial u'}{\partial x} \right)^2 + \left(\frac{\partial u'}{\partial y} \right)^2 + \left(\frac{\partial u'}{\partial z} \right)^2 \right] \quad \text{and}$$

Table 1. Variances of the horizontal wind components in neutral and stable conditions in the ASL, according to authors.

Atmospheric conditions	Authors	Specific conditions	$\frac{\sigma_u^2}{U_*^2}$	$\frac{\sigma_v^2}{U_*^2}$	$\frac{\sigma_u^2 + \sigma_v^2}{U_*^2}$
Neutral	Raupach et al. (1990)	Flat terrain	5.76	3.61	
		Rolling terrain	11.56	8.41	
	Hedde and Durand (1994)	Over sea	4.00	1.69	
	Stull (1988)		6.1 to 6.5	2.9 to 6.1	8.5
	Drobinski et al. (2004)	Flat terrain (55 m)	5 to 6	3	8 to 9
	Solari (1987)	$Z_0 < 0.03$ m	7.5		
Stable	Moraes and Epstein (1987)		4.71	3.17	
	Stull (1988)		–	–	8.5
	Pahlow et al. (2001)	$\zeta \leq 0.1$	5.29	4.0	

$$\varepsilon_2 = \nu \left[\left(\frac{\partial v'}{\partial x} \right)^2 + \left(\frac{\partial v'}{\partial y} \right)^2 + \left(\frac{\partial v'}{\partial z} \right)^2 \right]$$

– ν the viscosity diffusivity

otherwise:

$$2\overline{u'w'}\frac{\partial \bar{u}}{\partial z} + \frac{\partial (\overline{w'u'^2} + \overline{w'v'^2})}{\partial z} + 2\varepsilon_h = 0 \quad (5b)$$

The description of the experimental plots (see Sect. 4.1) and the location of the measurement stations justify the approximation of the transversal homogeneity. Concerning the longitudinal homogeneity, the ratio of the Eulerian length integral scale to the length of the experimental plots (less than 50%) broadly justifies this hypothesis.

Regarding the first term of Eq. (5b), for an ASL with constant flux, one has:

$$2\overline{u'w'}\frac{\partial \bar{u}}{\partial z} = -\frac{2U_*^3}{kz} \quad (6)$$

where U_* is the friction velocity and k the Von Karman's constant, equal to 0.4.

Then we can come to the second term of Eq. (5b). According to the K-theory, the vertical fluxes of the different ASL parameters are assumed to flow down the local gradient of these parameters. For the specific case of the TKE, this scheme was envisaged by many authors, De Moor (1983), Stull (1988) and Yadav et al. (2003). Thus, we can write:

$$\overline{w'((p'/\bar{\rho}) + e)} \approx \overline{w'e} = -K\frac{\partial \bar{e}}{\partial z} \quad (7a)$$

where e is the TKE, p' , the pressure fluctuations, $\bar{\rho}$ the mean density and K the eddy diffusivity.

For the horizontal components of the TKE, this can be written in the form:

$$\overline{w'u'^2} + \overline{w'v'^2} = -K\frac{\partial (\overline{u'^2} + \overline{v'^2})}{\partial z} = -2K\frac{\partial \bar{e}_h}{\partial z} \quad (7b)$$

where e_h is the horizontal component of the TKE, i.e.:

$$\bar{e}_h = \frac{1}{2} (\overline{u'^2} + \overline{v'^2})$$

Third term of Eq. (5b). Considering the fundamental parameters of turbulence and relying on dimensional analysis, André et al. (1978), Louis et al. (1983), and De Moor (1983) come to the formulation of the following relationship:

$$\bar{\varepsilon} = \frac{(\bar{e})^{3/2}}{l} \quad (8a)$$

where l is the dissipation length scale. Redelsperger et al. (2001) showed that this relationship can be demonstrated. Their calculation led to a slightly different equation:

$$\bar{\varepsilon} = \frac{C_\varepsilon}{L} (\bar{e})^{3/2} \quad (8b)$$

where L is a length scale and C_ε a constant. For the horizontal component of the TKE, the previous equation becomes:

$$\bar{\varepsilon}_h = \frac{C_\varepsilon}{L} (\bar{e}_h)^{3/2} \quad (8c)$$

Assuming a light variation of the constants C_ε and L .

New form of Eq. (5b). Combining with the previous equations, i.e. Eqs. (6), (7b) and (8c), Eq. (5b) becomes:

$$-\frac{U_*^3}{kz} - \frac{\partial}{\partial z} \left(K \frac{\partial \bar{e}_h}{\partial z} \right) + \frac{C_\varepsilon}{L} (\bar{e}_h)^{3/2} = 0 \quad (9)$$

Parameterization of the eddy diffusivity (cf. Eq. 7a). Relying on the $\bar{e}$ – ε closure (or k – ε closure in the engineering literature) approach, Stull (1988) proposed a parameterization of the eddy diffusivity in the form of:

$$K = C_\varepsilon \frac{(\bar{e})^2}{\bar{\varepsilon}} \quad (10)$$

where C_ε is a constant equal to 0.09.

The previous equation, combined to Eq. (8a), led to:

$$K = l C_\varepsilon (\bar{e})^{1/2} \quad (11a)$$

Redelsperger et al. (2001) deduced the same relationship in the form of:

$$K = L C_K (\bar{e})^{1/2} \quad (11b)$$

where C_K is a constant and L a length scale.

For the horizontal component of the TKE, the previous equation becomes:

$$K = L C_K (\bar{e}_h)^{1/2} \quad (11c)$$

Thus, Eq. (9) becomes:

$$-\frac{U_*^3}{kz} - \frac{2C_K}{3} \frac{\partial}{\partial z} \left(L \frac{\partial (\bar{e}_h)^{3/2}}{\partial z} \right) + \frac{C_\varepsilon}{L} (\bar{e}_h)^{3/2} = 0 \quad (12)$$

Combining some equations for the subgrid scheme and for similarity laws, Redelsperger et al. (2001) deduced that the length scale L can be expressed as follows:

$$L = kz \quad (13)$$

where k is the Von Karman constant.

With Eq. (13), Eq. (12) becomes:

$$z \frac{\partial}{\partial z} \left(z \frac{\partial (\bar{e}_h)^{3/2}}{\partial z} \right) - \frac{3C_\varepsilon}{2k^2 C_K} (\bar{e}_h)^{3/2} = -\frac{3U_*^3}{2k^2 C_K} \quad (14)$$

which can be rewritten in:

$$z^2 \frac{\partial^2 (\bar{e}_h)^{3/2}}{\partial z^2} + z \frac{\partial (\bar{e}_h)^{3/2}}{\partial z} - \frac{3C_\varepsilon}{2k^2 C_K} (\bar{e}_h)^{3/2} = -\frac{3U_*^3}{2k^2 C_K} \quad (15)$$

The mathematical resolution of the previous equation leads to (see Appendix B):

$$\frac{\bar{e}_h}{U_*^2} = \left(\frac{1}{C_\varepsilon} + a z^n + b z^{-n} \right)^{2/3} \quad (16)$$

with $n = \frac{1}{k} \sqrt{\frac{3C_\varepsilon}{2C_K}}$ and a and b , two constants.

Three conclusions can be drawn from the above expression of the horizontal variance profile:

1. in the close vicinity of the ground, the normalized kinetic energy is a variable of z ;
2. many configurations of the normalized kinetic energy variation can be envisaged, including a constant ratio or a power of z , according to the degree of approximation;
3. when z tends toward 0, $f(z) = \bar{e}_h / U_*^2$ tends toward ∞ ; and when z tends toward ∞ , $f(z)$ tends towards ∞ too. This indicates that $f(z)$ is somewhat similar to the logarithm function;

When the contribution of z is negligible, Eq. (16) becomes:

$$\frac{\bar{e}_h}{U_*^2} = \left(\frac{1}{C_\varepsilon} \right)^{2/3} \quad (17)$$

Relying on the values of $\bar{e}_h / U_*^2$ in Table 1, it is possible to predict the values C_ε . These values are reported in Table 2. Thus, it can be noticed that the values of C_ε is of the same magnitude as the ones given by Stull (1988), i.e. 0.04 versus 0.09.

It is not really convenient to treat Eq. (16) with the data collected from the WELSON experiment. It can be recalled that, in modeling the mean wind velocity profile, two kinds of relationships are proposed, i.e., the power model and the logarithmic one (cf. Appendix C). So, as for the mean wind velocity, we proposed a logarithmic relationship instead of the power relationship, since the first one will be more treatable with the available data.

In regard to Eq. (16), the profile of the wind velocity variance must have a logarithmic behaviour with a constant part. So the proposed relationship:

$$\frac{\sigma_h^2}{U_*^2} = \alpha \ln(z) + b \quad (18)$$

where σ_h^2 is the variance measured by the cup anemometer (see below for more specification on this parameter), z the height and, α and b two constants.

This relationship is a version of the one proposed by Carloti (2001), which has been reported in Eq. (4).

4 Experiments

The data of this study derived from WELSONS (Wind Erosion and Losses of Soil Nutrients in semiarid Spain), which is a European research project devoted to the study of desertification and land degradation by wind erosion in the European Mediterranean area. The main objective of the project was to provide a better understanding of the impacts of climate and land-use changes on soil degradation by wind erosion for agricultural soils in the semiarid region of Northern Spain (Central Aragon, Spain, 1996–1998, see Fig. 1).

In a first paper, Frangi and Richard (2000) presented some results regarding the dynamics of the atmospheric surface layer (ASL) and the energy budget. After determining the main ASL parameters (friction velocity, roughness length, temperature scale, Monin-Obukhov length scale, etc.), it was pointed out that the two tillage methods induced differences in both dynamic characteristics and energy budget partitioning between the two plots. In a second paper, Yahaya et al. (2003) presented the influences of soil tillage treatment on some turbulent parameters, such as the Euler integral scales, the TKE dissipation rate, the spectral range of turbulence, the spectral energy containing-scale and the horizontal wind variance.

4.1 Description of the experimental site

For a complete description of the WELSONS experiment, with a detailed description of the site, one should refer to

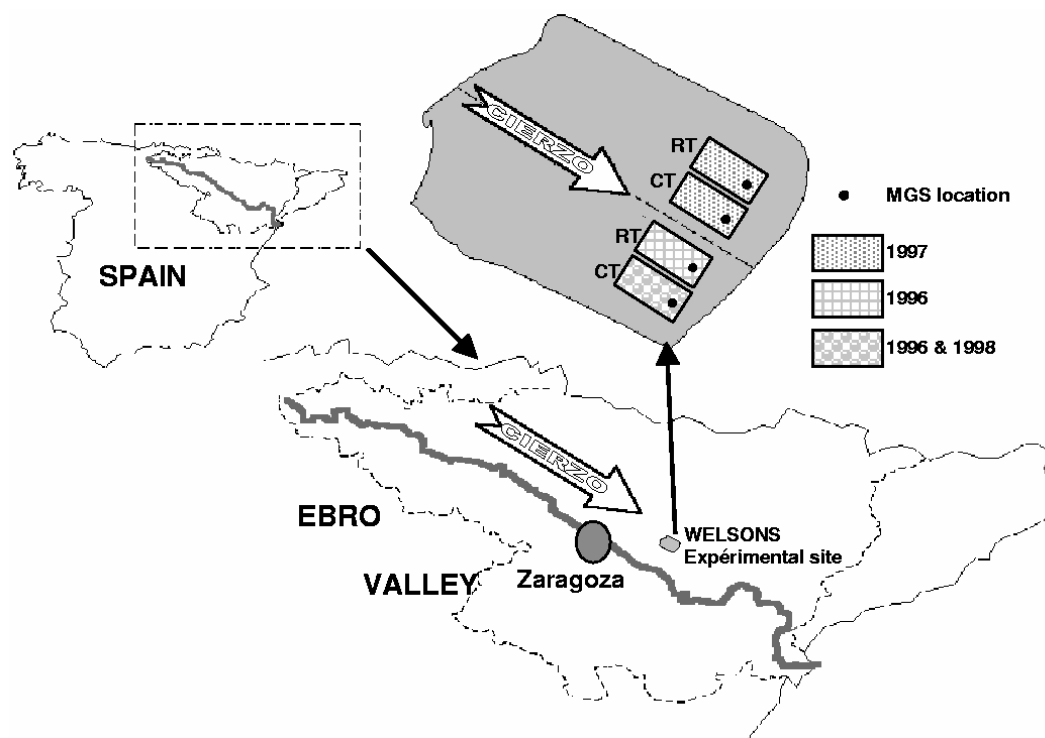


Fig. 1. General fetch of the WELSONS experimental site. One can notice the location of the conventional tillage (CT) and reduced tillage (RT) plots, changing according to years and the main wind direction following the Ebro valley (after Yahaya et al., 2003).

Table 2. Some values of C_ε according to the values of the normalised kinetic energy.

Atmospheric conditions	Authors	Specific conditions	$\frac{\sigma_u^2 + \sigma_v^2}{U_*^2}$	C_ε
Neutral	Stull (1988)	Flat terrain (55 m)	8.5	0.040
	Drobinski et al. (2004)		8 to 9	0.044
Stable	Stull (1988)		8.5	0.037

Frangi and Richard (2000) and Gomes et al. (2003). The climate of this Spanish region is strongly influenced by two winds, namely Cierzo and Borchono, which are bound to a specific orography. The Cierzo is the wind from the WNW direction, a very cold air stream in winter and cool in summer. In the opposite direction blows the Borchono, with an ESE main direction, which appears when a pressure gradient exists between Mediterranean and Cantabrico Seas, with a low pressure field over the latter one.

The experimental field, located in an area called El Saso ($41^\circ 36' \text{ N}$, $0^\circ 32' \text{ W}$, 285 m above mean sea level), 35 km away from Zaragoza in the Ebro Valley (Fig. 1), is oriented in the direction of the Cierzo prevailing wind (WNW). It remained untilled after a barley fallow rotation. Fields surrounding it, in the upwind edge, had very sparse vegetation. On both sides, at a distance of about 200 m, there were wheat

fields, with a vegetation canopy lower than 30 cm. Some fallow fields of stubble separated these wheat fields from the experimental plots. The experimental field was divided into two adjacent plots ($140 \times 180 \text{ m}^2$, each) for the application of two tillage treatments with a 20 m separation distance: conventional tillage (CT) and reduced tillage (RT). The CT treatment consisted of mouldboard ploughing, at a depth of 30–35 cm, followed by the pass of a compacting roller to obtain a very flat ground: it constitutes the traditional practice in this area. The RT treatment, an alternative practice of conservation tillage (Lopez et al., 1996), consists of a unique pass of a chisel plough at a depth of about 15–20 cm, giving a ground with furrows. In both cases, the tillages were done in the WNW direction. So the soil was bare with very different surface conditions during the whole experiment.

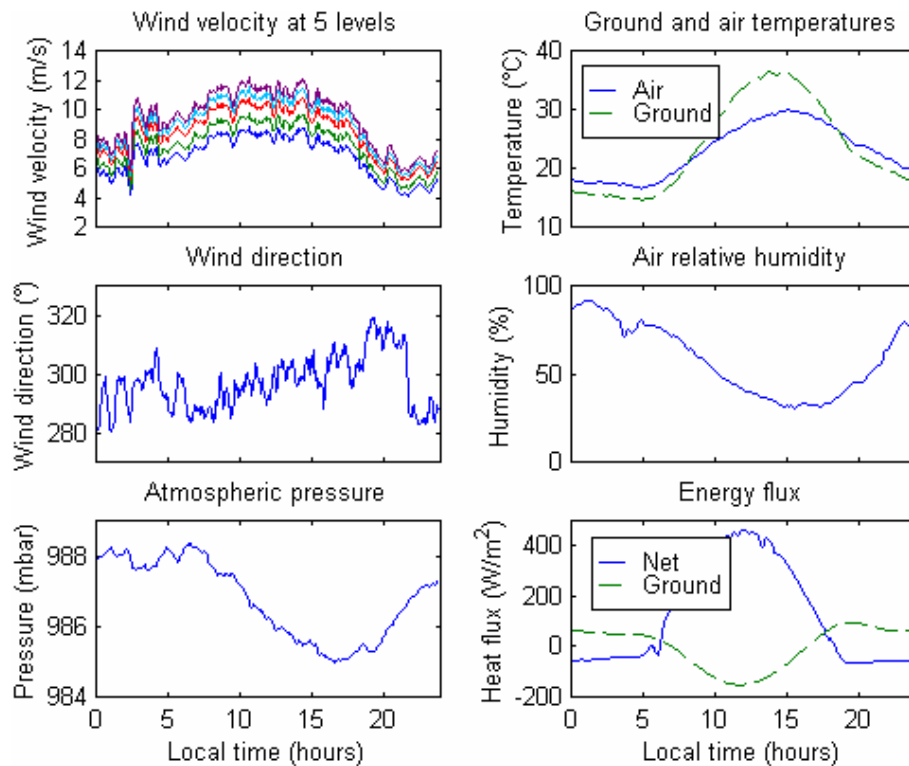


Fig. 2. Micro meteorological parameters measured during the experiment (Plot CT, 25 July 1997).

4.2 Instrumentation

Two micrometeorological ground station (MGS) systems (Frangi and Richard, 2000) have been developed and set up on the experimental field to study the dynamical characteristics of the soil surface and the energy budget partitioning in both plots. They were installed in the downwind edge of the field so as to monitor the fetch effects. The devices measure the energy budget parameters: wind speed and direction, air temperature and vapor pressure at two levels, net radiation and ground heat flux, soil and surface temperature, and atmospheric pressure. In addition, they record the wind profile every second, through a set of 5 cup anemometers installed along a 4 m height vertical mast (Frangi and Poullain, 1997). The five anemometer heights are 28, 53, 118, 203 and 402 cm. We notice that the bottom height complies with the recommendation of Fritschen and Gay (1979), which stated that the anemometer height should be fivefold greater than the roughness length, Z_0 (i.e. 0.3 and 3 mm, respectively, in plots CT and RT, see Table 7). The two MGS are synchronized. The 1997 WELSONS experiment was conducted from 29 June to 25 September.

The mean wind velocity at the highest level of plot CT is around 11 m s^{-1} during the daytime of 25 July 1997 and the turbulence intensity confined between 12% and 16% throughout the same day at the same level (cf. Fig. 2).

4.3 Measurement uncertainty

Some concerns could arise about the uncertainty of the measurement of the wind variance with cup anemometer. These concerns are of five orders: (i) the sampling error due to the fact that the sampling rate of the experiment is low; (ii) the spatial scales of the turbulence compared to the anemometer constant (iii) the instrumental error stemming from the inertial effects of the cup anemometer, (iv) the error due to the height variation and the ground proximity, and (v) the statistical atmospheric uncertainty.

First, let us consider the error related to the sampling rate. Then, the question is, from which eddy scale can a measurement be considered as having integrated the substance of the wind velocity variance? In a previous study, relating to the same experiment, Yahaya et al. (2003) showed that the length scales of the spectral peaks, range from 187 m (bottom level) to 522 m (upper level), on plot CT, and from 95 m to 450 m, on plot RT. So, in the light of these results, we can affirm that the sampling cut-off scales represent about a tenth of the energy containing ones. In terms of energy, the ratio must be even lower. A complementary study carried out in an urban area, at University Diderot (Paris 7), with a three-dimensional sonic anemometer (Campbell CSAT3), shows variance losses of about 10% between samplings of 32 and 1 Hz, for wind velocity around 4 m s^{-1} with turbulence intensity of about 40% (Yahaya, 2004). In addition,

this accordance between experimental data and the von Karman modelling spectra, notably in the upper frequency part, reinforces credit to the quality of the measurements (cf. Yahaya et al., 2003).

On the one hand, a previous study (cf. Yahaya et al., 2003) focused on the relationship between the turbulence structure and the terrain surface. The study considered the fourth levels of measurements of the two plots. The spectral gap, which separates the turbulent flow from the influences of the mean flow has been located. The location of the gap allowed determining the best sample's time interval separating the two scales of the flow. On the other hand, the study allowed verification that, the turbulence scales depend, not only on the height level, but also on the terrain roughness.

The instrumental error, which stems from the inertial effects of the cup anemometer, has been deeply studied in Yahaya and Frangi (2004). Given the anemometers' distance constants ($L \approx 1.3 \pm 0.35$ m) and the mean wind velocity (cf. Fig. 2), the variance reduction due to the inertial effects was estimated at a small percentage. In this regard, Kristensen (1998) states that the overspeeding phenomenon of the cup anemometer is only relevant when the mean wind speed is concerned. Otherwise, it is possible to use a cup anemometer for measuring the fluctuating, streamwise velocity component with a spatial resolution that corresponds to almost that of a sonic anemometer.

Three phenomena could affect the measurement of the wind variance from one height to another. The first one is the proximity of the ground which could hinder the device efficiency. This question has already been dealt with in the previous section. The second one is the variation of the mean wind with height. As it has been reported, the mean distance constant of the studied anemometers is $L = 1.3$ m. The maximum accessible frequency, corresponding to the cutoff frequency at the amplitude attenuation coefficient $\alpha = \sqrt{2}/2$ (cf. Guyot, 1997), is given by:

$$f_{co} = \frac{U}{2\pi L} \quad (19)$$

where U is the mean wind velocity. Given that the mean wind speeds, at the bottom levels, during the study period (25 July 1997; 07:00–17:00 LT), are 8.0 and 6.7 m s⁻¹ on plots CT and RT, thus the maximum accessible frequencies are 0.9 and 0.8 Hz. These frequencies are greater than the sampling Nyquist frequency of the experiment (i.e. 0.5 Hz). For the higher levels, where the mean wind speeds are higher, the anemometers accuracy is then better. The third phenomenon is linked to the variation of the embraced spectrum, which also changes with heights. The spectral cut toward higher wave numbers with increasing altitude makes the spectral range wider for lower levels, i.e.:

$$\kappa_{s1} = \frac{2\pi}{T_s U} = \frac{2\pi k}{U_* T_s \ln\left(\frac{z_1}{Z_0}\right)} > \kappa_{s5} = \frac{2\pi k}{U_* T_s \ln\left(\frac{z_5}{Z_0}\right)} \quad (20)$$

where z_1 and z_5 are heights at levels 1 and 5, κ_s and T_s are the sampling wave number and period, U_* the friction velocity, k the von Karman constant and Z_0 the roughness length. This has the effect of increasing the lower altitude variance whereas the aim of this study is to show that the variance decreases with decreasing altitude. So this phenomenon will have no effect on the conclusion of this paper.

Even if the cutoff frequency, f_{co} , of the used anemometer is about 2 Hz in temporal mode, its upper frequency limit attains 12 Hz as it is reported in Yahaya and Frangi (2004). In fact, the sampling rate of 1 Hz is an average of the higher frequencies measurement. The effective frequency measurement of the anemometer, as well as the upper frequency limit, are determined by the mean wind velocity.

The relative statistical atmospheric uncertainty of the second moment, for a Gaussian distribution with zero mean, is given by Lumley and Panofsky (1964):

$$\text{Err} = 2\sqrt{\frac{T_u}{T_s}} \quad (21)$$

where Err is the relative uncertainty, T_u the Eulerian time integral scale and T_s the sampling time interval. The time integral scale, which is given by the integral of the correlation function, $\rho(t)$, between 0 and ∞ , represents the time scale within which the considered turbulent parameter remains auto-correlated. Table 3 gives the values of the Eulerian time integral scale T_u , stemming from a previous study relating to the same experiment (Yahaya et al., 2003). With these values, we determined the expected relative uncertainty on the variance measurement (second moment of the wind velocity), under the assumption of normal distribution, for an averaging interval of 14 min (see also Table 3). We notice that the parameter varies from 15% to 20% according to the considered height and the experimental site. It is possible to bring these figures to about 10% by increasing the average interval, for example to 30 min. But this conceivable operation is unlikely to change the results of this study.

5 Results

The wind data logged during the WELSONS experiment concern the bottom part of the ASL since the lowest anemometer is located at 0.25 m from the ground while the highest one is at 4 m (thus covering a height scale ratio of 16). This particularity of the experiment, due to its specific objectives, is expected to produce different results from common micro-meteorological experiments, which were carried out in the upper eddy surface layer to the shear surface layer (cf. Drobinski et al., 2004, for the subdivision of the surface layer).

The WELSONS experiment somewhat marks off from the cases reported in Sect. 2, since it took place in the very vicinity of the ground. At these heights, the ground effects become important and thus the roughness length becomes a

Table 3. Statistical atmospheric uncertainty of the second moment (variance) for a Gaussian probability distribution. The integral scales stem from a previous study relating to the same experiment (Yahaya et al., 2003).

Plot CT				Plot RT			
Height (m)	Integral scales, Euler Time (s)	Length (m)	Relative uncertainty	Height (m)	Integral scale, Euler Time (s)	Length (m)	Relative uncertainty
0.28	5.48	43.7	16%	0.29	4.26	28.0	14%
0.53	5.85	51.6	17%	0.54	4.52	34.1	15%
1.18	6.72	66.1	18%	1.19	5.08	42.9	16%
2.03	7.21	75.3	19%	2.03	5.74	54.1	17%
4.04	8.17	90.0	20%	4.03	7.19	76.9	19%

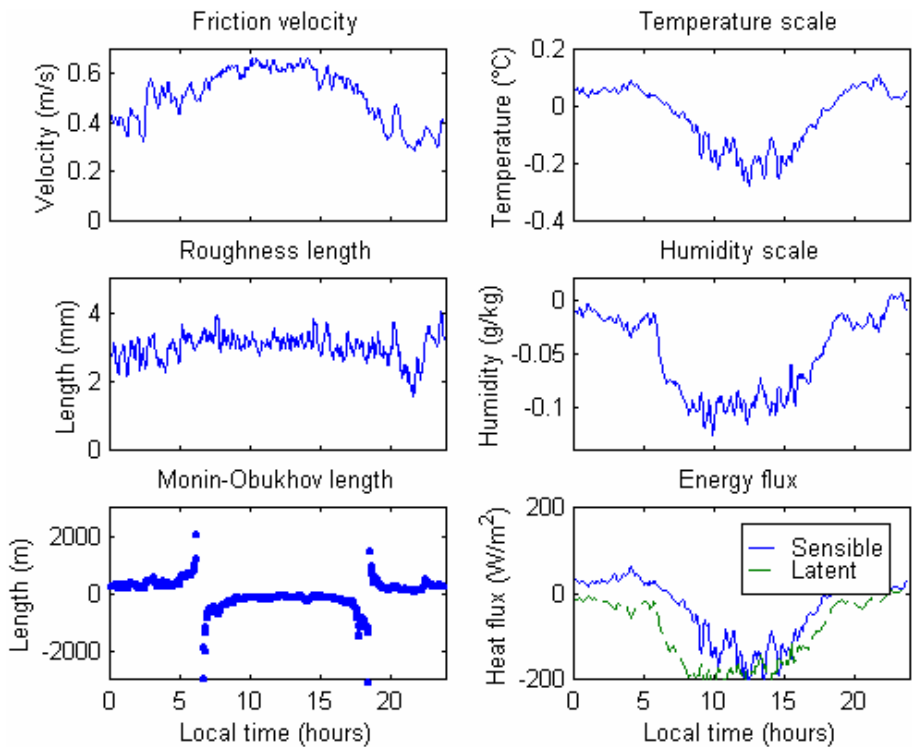


Fig. 3. Dynamic parameters of that ASL (Plot CT, 25 July 1997).

relevant parameter, as it is in the case reported by Solari (1987). In addition, Hedde and Durand (1994) and Pahlow et al. (2001) reported that, in some circumstances, the variances of the horizontal wind components depend on the height. Besides any thermal stability considerations, the layer studied in the WELSONS experiment is rather a dynamic one because the considered heights are negligible compared to the Monin-Obukhov length (Fig. 3) and the friction velocity is high (respectively 0.4 and 0.5 m s⁻¹ in the two plots). These conditions of the occurrence of the dynamic layer were specified by De Moor (1983).

Since the study does not include the vertical wind component, the turbulent wind fluctuations were linearly detrended in order to remove the mean flow influences. The variances

are calculated over 14 min time intervals to match with the friction velocity and the roughness length data reported by Frangi and Richard (2000).

5.1 Modelling the profile of the horizontal wind variance

As demonstrated in Sect. 3, Fig. 4 shows that, in the specific conditions of this experiment, the wind horizontal variance varies with the height. In this figure, as well as in Fig. 5, independently to the wind speed values and to the local time (thus to the stability parameter), there is a reduction of the horizontal wind variance as the anemometer height decreases. One can notice that the variance reduction is an

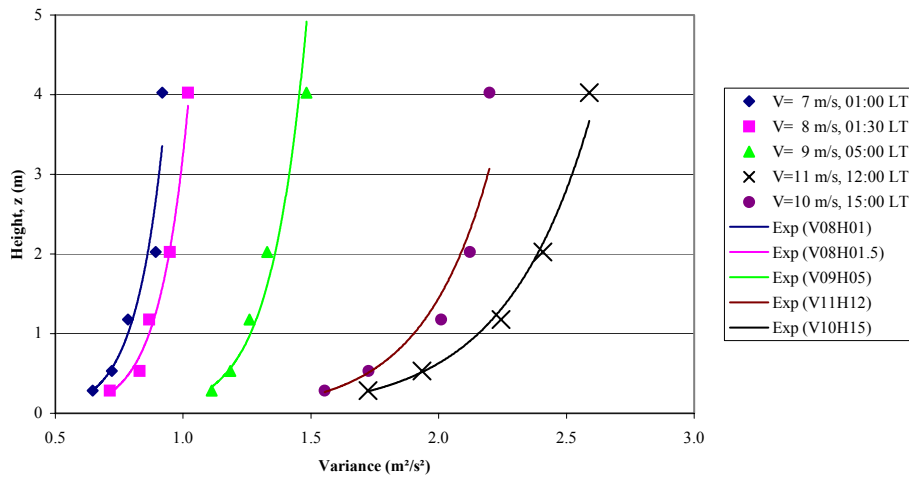


Fig. 4. Variation of the horizontal wind variance with height (Plot CT, 25 July 1997).

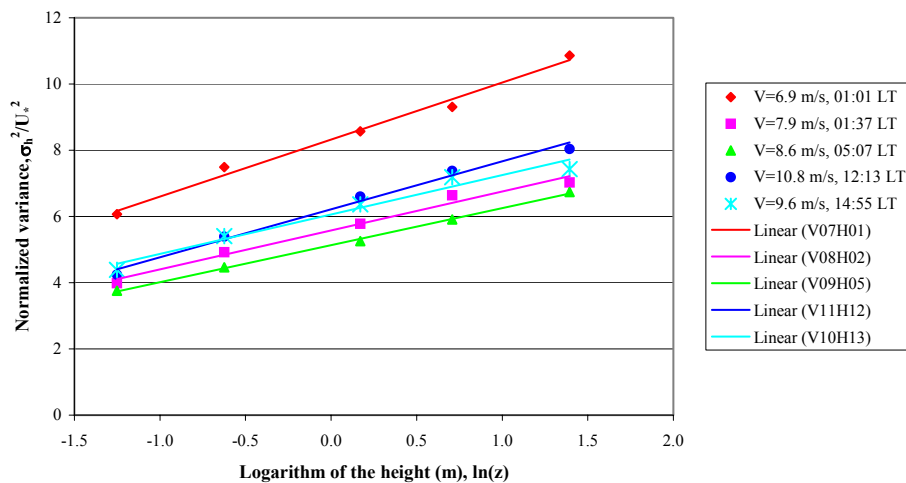


Fig. 5. Variance normalized by the square of the friction velocity as a function of height logarithm (Plot RT, 25 July 1997).

increasing function of the wind speed. Although the plots include some night data, however, the study concerns only the period 07:00–17:00 LT, where the mean wind is roughly stationary.

This reduction of the horizontal wind variance has been reported by Drobinski et al. (2004). Thus, they showed that, in the quasi-neutral flow, the normalised horizontal variances increase between the ground and $0.015 Z_i$ (i.e., about 10 m), where they reach a maximum, then decrease with height.

Recalling Eq. (18), it can be noticed, in Fig. 5 and Table 4, that the variance, normalised by the square of the friction velocity, is a linear function of the logarithm of the height. The data of this analysis, notably the values of the friction velocity, stem from the MW method where the results have been previously published (Frangi and Richard, 2000). One can also notice in Table 4 that the linear correlation coefficient R^2 is higher than 0.9 in 95% of the 475 cases at plot CT and in 97% of cases at plot RT.

This confirms the validity of the previous approximations and of the model stemming from the RDT and proposed by Carlotti (2001). However, it can be noticed that, on the contrary to the Carlotti's relationship, Fig. 4 shows that the variance is a growing function of z . This is in accordance with the prediction of Drobinski et al. (2004).

As the variance measured by cup anemometers, σ_h^2 , is the sum of the longitudinal and transversal variance, from Eq. (18), we have:

$$\frac{\sigma_h^2}{U_*^2} = \frac{\overline{u'^2} + \overline{v'^2}}{U_*^2} = \alpha \ln \left(\frac{z}{Z_0} \right) - \delta \quad (22)$$

Combining Eqs. (18) and (22), we have a relationship between b and $-\ln(Z_0)$ in the form of:

$$b = -(\delta + \alpha \ln(Z_0)) \quad (23)$$

It can be noticed, in Table 4, that α is roughly constant in the two plots while the roughness length increases tenfold and the friction velocity by 25% from plot CT to plot RT.

Table 4. Linear regression parameters of the function $\sigma_h^2/U_*^2 = f(\ln(z)) = \alpha \ln(z) + b$, using the values of U_* stemming from the MW method.

$R^2 > 0.90$ (total of cases = 475)		Slope, α		Intercept, b		$-\ln(Z_0)$
		Average	Variation coefficient	Average	Variation coefficient	
Plot CT	95%	1.160	32%	8.074	15%	8.11
Plot RT	97%	1.156	26%	5.311	17%	5.81

Table 5. Values of α and correlation between “ b ” and Z_0 , according to the determination methods of U_* and Z_0 .

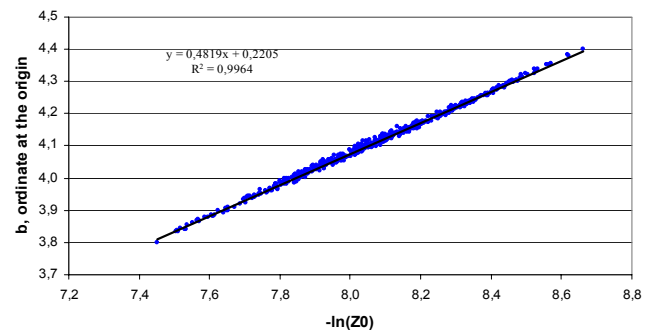
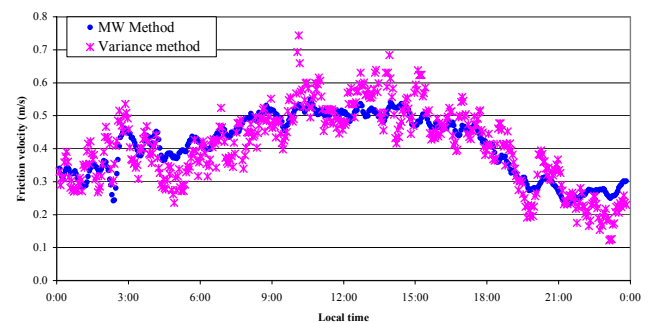
Considered plot	Constant α according to the determination method of U_* :		Correlation between b and $-\ln(Z_0)$ according to the determination method of Z_0 :	
	MW Method	Simple logarithmic method	MW method	Simple logarithmic method
Plot CT	1.160	1.22	0.21	0.36
Plot RT	1.156	1.18	0.56	0.46

Table 6. Experimental values of the remainder, δ .

Considered plot	Level 1	Level 2	Level 3	Level 4	Level 5
Plot CT	1.45	1.35	1.51	1.36	1.44
Plot RT	1.41	1.25	1.41	1.29	1.38

Besides the accuracy of the anemometers, the experimental value of α also depends on the determination method of U_* and Z_0 . Thus, Table 5 presents the values of α and of the correlation between “ b ” and Z_0 (cf. Eq. 23) according to the methods used for the determination of U_* and Z_0 . These parameters have been calculated through the MW method, introduced by Frangi and Richard (2000), which takes into account the energy budget parameters, and through the logarithmic model of the mean wind velocity, neglecting thermal effects (cf. Appendix D). Thus, we state that α varies by less than 3%, between the two plots, no matter the used method, while the correlation between b and $-\ln(Z_0)$ is higher with the logarithmic model method. This correlation has been evaluated through the 475 case studies with the imbedded Microsoft Excel function of the working computer.

In Table 6, it can be noticed that the values of the remainder, δ , of Eq. (22), are constant and do not depend on the experimental plots and neither on the anemometer heights. In addition, a strong correlation has been noticed between “ b ” and the roughness length, particularly when the latter is determined through the mean velocity logarithmic model, neglecting thermal effects. Figure 6 suggests that the slope of the linear regression between “ b ” and $-\ln(Z_0)$ is very close to $1/2$, in the two plots. However, the vertical intercept of the regression is somewhat different from zero.

**Fig. 6.** Linear regression between the ratio b'/a' and the opposite of the logarithm of the roughness length.**Fig. 7a.** Friction velocity. Comparison between the statistical method MW and the variance method (Plot CT, 25 July 1997).

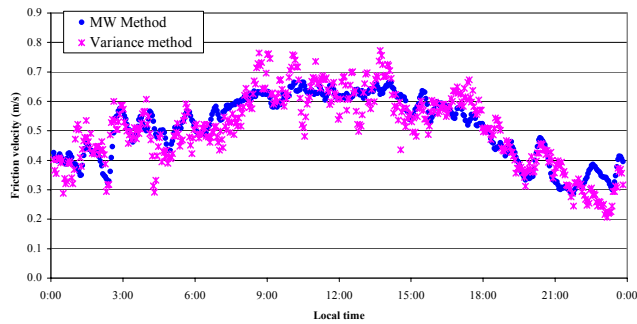


Fig. 7b. Friction velocity. Comparison between the statistical method MW and the variance method (Plot RT, 25 July 1997).

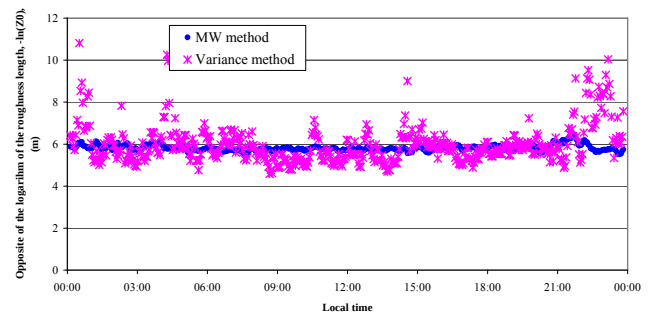


Fig. 8b. Roughness length. Comparison between the statistical method MW and the variance method (Plot RT, 25 July 1997).

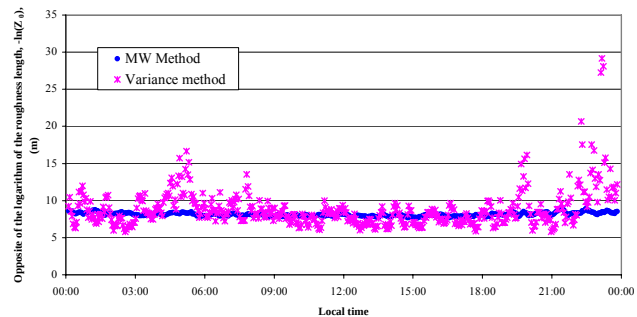


Fig. 8a. Roughness length. Comparison between the statistical method MW and the variance method (Plot CT, 25 July 1997).

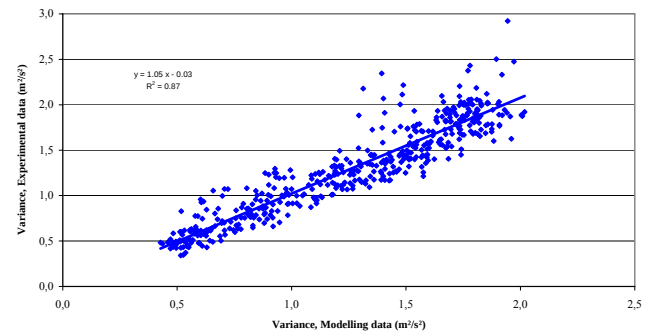


Fig. 9. Variance. Comparison between the experimental and the modeled data, for $\alpha=1.20$ and $\delta=1.36$ (Plot RT, Level 2).

5.2 Determination of the friction velocity and the roughness length from the profile of the horizontal wind variance

After adopting the experimental value of the previously defined constants α and δ (cf. Tables 5 and 6), it is proposed to determine, exclusively from Eq. (22), the friction velocity and the roughness length, in order to show that the equation can be used in a way or a reverse. For this purpose, this equation is rewritten in the form:

$$\sigma_h^2 = \alpha U_*^2 \ln(z) - U_*^2 (\alpha \ln(Z_0) + \delta) \quad (24a)$$

This can be rewritten as:

$$\sigma_h^2 = a_1 \ln(z) + b_1 \quad (24b)$$

with $a_1 = \alpha U_*^2$ and $-\ln(Z_0) = \frac{b_1}{a_1} + \frac{\delta}{\alpha}$.

The friction velocity, U_* , and the roughness length, Z_0 , may be determined, through linear regression, from Eq. (23b), by using the measurements of the five anemometer levels.

Figures 7a, b, 8a and b compare the values of the friction velocity and the roughness length stemming from the variance Eq. (23b) and those determined by Frangi and Richard (2000), through the statistical method MW. Table 7 completes the comparison between the two data sets by presenting the mean values and the correlation coefficients. Thus,

a good agreement is noticed between the two methods with a correlation of about 0.9 for the friction velocity. For the roughness length, which varies slightly, the correlation coefficients are somewhat lower.

5.3 Generation of the horizontal wind variance from the friction velocity and the roughness length

From Eq. (23a), and after adopting the experimental value of α and δ (cf. Tables 5 and 6), we can generate the variance for every anemometer height. It is to be specified that α and β have been determined through the combination of five measurement levels. Now, the same constants will be used for each given single level. Figure 9 presents a comparison between the experimental and the modeled variance data (cf. Eq. 21). The friction velocity and the roughness length values were calculated through the logarithmic profile of the mean wind velocity (neglecting thermal effects). Table 8 reports the parameters of the linear regression between the modelling and the experimental data, for the five anemometer heights of each plot. It may be noticed that the linear correlation coefficient, the slope and the vertical intercept indicate good agreement between the two data sets. Comparable results were also obtained with the friction velocity and the roughness length calculated through the statistical method MW.

Table 7. Comparison parameters between the values of the friction velocity and the roughness stemming from the statistical method MW and the variance method, for $\alpha=1.16$ and $\delta=1.4$ (25 July 1997, over 24 h).

		Plot CT	Plot RT
Mean values of the friction velocity, U_*	Statistical method MW	0.41	0.51
	Variance method	0.41	0.51
	Correlation between the two data sets	0.86	0.87
Mean values of the logarithm of the roughness length	Statistical method MW	8.14	5.82
	Variance method	8.79	5.98
	Correlation between the two data sets	0.71	0.35

Table 8. Horizontal wind variance. Linear regression parameters between the experimental and the modelling data, $\alpha=1.20$ and $\delta=1.36$.

		Linear correlation coefficient (R^2)	Slope (a)	Vertical intercept (b)	Ratio of $ b $ to mean variance
Plot CT	Level 1	0.88	1.02	−0.02	2%
	Level 2	0.87	1.06	−0.04	3%
	Level 3	0.86	1.07	−0.09	6%
	Level 4	0.84	1.07	−0.07	5%
	Level 5	0.85	1.13	−0.18	10%
Plot RT	Level 1	0.88	1.09	−0.01	1%
	Level 2	0.87	1.05	−0.03	2%
	Level 3	0.84	1.01	−0.08	6%
	Level 4	0.83	0.97	−0.06	4%
	Level 5	0.83	0.98	−0.16	9%

It appears that the studied model gives values of the horizontal wind variance in good agreement with experimental data. Thus, it can be used for more accurate modelling of parameters involving the variance or the standard deviation of the horizontal wind (e.g. wind velocity peak or gust factors, rate of TKE transport, etc.)

6 Conclusion

This study showed that, in the vicinity of the ground, the variance of the horizontal wind varies logarithmically with height. The parameters of the logarithmic function include the friction velocity and the roughness length scale. Thus, the study leads to a formulation of the similarity universal function of the horizontal wind variance, near the ground, i.e.:

$$\frac{\sigma_h^2}{U_*^2} = f_{\sigma_h} \left(\frac{z}{Z_0} \right) = \alpha \ln \left(\frac{z}{Z_0} \right) - \delta \quad (25)$$

where α and δ are two constants. As a matter of fact, the values of α varies by less than 3%, between the plots, while the roughness length increases tenfold and the friction velocity by 25% from plot CT to plot RT (cf. Table 4). The values of

δ reveal to be independent from the experimental plots and the anemometer heights (cf. Table 6).

The model, introduced by this study, allowed us to determine the friction velocity and the roughness length in good accordance with data provided by other methods, such as the MW method or the mean velocity logarithmic profile method (cf. Table 7).

These results could be used for accurate calculations of the wind velocity standard deviation and variance in models involving these two parameters (e.g., wind velocity peak or gust factors). They could also be used in the evaluation the TKE transport rate near the ground.

Further studies are necessary to investigate the limits of the model, the validity of which is presently limited to a few meters, and under the limiting assumptions made herein. Future studies will also have to confirm the values of constants α and δ .

Abbreviations and acronyms

ABL	Atmospheric Boundary Layer
ASL	Atmospheric Surface Layer
CT	Conventional Tillage
ESE	East-South-East
ESL	Eddy Surface Layer
MGS	Micrometeorological Ground Station
MW	Statistical method of the computation of the ASL parameters, introduced by Frangi and Richard (2000)
RDT	Rapid Distortion Theory
RT	Reduced Tillage
TKE	Turbulent kinetic energy
WELSONS	Wind Erosion and Losses of Soil Nutrients in semiarid Spain
WNW	West-North-West

List of symbols

a	Constant, generally slopes of linear regressions
b	Constant, generally the vertical intercept of linear regressions
C	Constant
c_{ij}	Constant of order one
C_K	Constant relating to the parameterization of the eddy diffusivity
C_ε	Constant relating to the equation of the TKE dissipation rate
$\bar{e}$	Mean kinetic energy
E_{11}	longitudinal velocity spectrum
Err	Relative uncertainty
$f_{\max}$	Maximum frequency accessible by a cup anemometer
f_{σ_h}	Universal function related to the horizontal wind variance
k	Von Karman constant
K	Eddy diffusivity
K_u	Eddy viscosity relating to the momentum
l	TKE dissipation length scale
L	TKE dissipation length scale
L	Monin-Obukhov length, Distance constant of the cup anemometer
T	Averaging time interval
T_s	Time, sampling rate
T_u	Time integral scale
u	Longitudinal wind velocity
U	Mean wind velocity
U_*	Friction velocity
v	Transversal wind velocity
w	Vertical wind velocity
z	Height

Z_0	Roughness length
Z_i	Daytime atmospheric boundary layer depth
Z_h	Atmospheric boundary layer depth
α	Constant, slope of variance profile
β_{13}	Unknown shear parameter
β_u	Constant ratio between the longitudinal wind variance and the square of the friction velocity
γ	Proportionality “constant” between the eddy viscosity and the eddy diffusivity
δ	Constant relating to the universal function
ε	TKE dissipation rate
ζ	Stability parameter
κ	Wave number
Λ	Length scale characterising the lower limit of the –1 range in the spectrum
σ	Standard deviation
σ_h^2	Horizontal wind variance measured by cup anemometers
σ_u	Longitudinal wind standard deviation

Appendix A

The Navier-Stokes equations of the turbulent flow for each wind component, using the Einstein notations (with summation on j), are:

$$\frac{\partial \overline{u_i'^2}}{\partial t} + \overline{u_j} \frac{\partial \overline{u_i'^2}}{\partial x_j} = 2\delta_{i3}g \frac{\overline{u_i'\theta_v'}}{\theta_v} - 2\overline{u_i'u_j'} \frac{\partial \overline{u_i}}{\partial x_j} - \frac{\partial (\overline{u_j'u_i'^2})}{\partial x_j} - \frac{2}{\bar{\rho}} \frac{\partial (\overline{u_i'p'})}{\partial x_i} - 2\varepsilon_i \quad (\text{A1})$$

with $\varepsilon_i = \nu \left(\frac{\partial \overline{u_i'}}{\partial x_j} \right)^2$.

By choosing the x -axis aligned with the mean wind ($\overline{\vec{\alpha}}$ =mean wind vector) and the z -axis the upward vertical ($\overline{\vec{\alpha}}$ =upward vertical), then we have: $\overline{V}=0$ et $\overline{W}=0$. For a steady flow, the previous equations become for each component:

$$\overline{u} \frac{\partial \overline{u'^2}}{\partial x} = -2 \left(\overline{u'^2} \frac{\partial \overline{u}}{\partial x} + \overline{u'v'} \frac{\partial \overline{u}}{\partial y} + \overline{u'w'} \frac{\partial \overline{u}}{\partial z} \right) - \left(\frac{\partial \overline{u'^3}}{\partial x} + \frac{\partial \overline{v'u'^2}}{\partial y} + \frac{\partial \overline{w'u'^2}}{\partial z} \right) - \frac{2}{\bar{\rho}} \frac{\partial \overline{u'p'}}{\partial x} - 2\varepsilon_1 \quad (\text{A2a})$$

$$\overline{u} \frac{\partial \overline{v'^2}}{\partial x} = - \left(\frac{\partial \overline{u'v'^2}}{\partial x} + \frac{\partial \overline{v'^3}}{\partial y} + \frac{\partial \overline{w'v'^2}}{\partial z} \right) - \frac{2}{\bar{\rho}} \frac{\partial \overline{v'p'}}{\partial y} - 2\varepsilon_2 \quad (\text{A2b})$$

$$\overline{u} \frac{\partial \overline{w'^2}}{\partial x} = 2g \frac{\overline{w'\theta_v'}}{\theta_v} - \left(\frac{\partial \overline{u'w'^2}}{\partial x} + \frac{\partial \overline{v'w'^2}}{\partial y} + \frac{\partial \overline{w'^3}}{\partial z} \right) - \frac{2}{\bar{\rho}} \frac{\partial \overline{w'p'}}{\partial z} - 2\varepsilon_3 \quad (\text{A2c})$$

Summing Eqs. (A2a) and (A2b) yields:

$$\begin{aligned} \bar{u} \frac{\partial (\overline{u'^2} + \overline{v'^2})}{\partial x} = & -2 \left(\overline{u'^2} \frac{\partial \bar{u}}{\partial x} + \overline{u'v'} \frac{\partial \bar{u}}{\partial y} + \overline{u'w'} \frac{\partial \bar{u}}{\partial z} \right) \\ & - \left(\frac{\partial \overline{u'^3}}{\partial x} + \frac{\partial \overline{v'u'^2}}{\partial y} + \frac{\partial \overline{w'u'^2}}{\partial z} \right) + \\ & - \left(\frac{\partial \overline{u'v'^2}}{\partial x} + \frac{\partial \overline{v'^3}}{\partial y} + \frac{\partial \overline{w'v'^2}}{\partial z} \right) \\ & - \frac{2}{\bar{\rho}} \left(\frac{\partial \overline{u'p'}}{\partial x} + \frac{\partial \overline{v'p'}}{\partial y} \right) - 2(\varepsilon_1 + \varepsilon_2) \quad (\text{A3}) \end{aligned}$$

It is generally admitted (Stull, 1988) that the transport terms of the pressure are lower than the ones relating to the turbulent kinetic energy. Thus, it can be written:

$$\begin{aligned} \frac{\partial}{\partial x} \left(\overline{u'v'^2} + \frac{2}{\bar{\rho}} \overline{u'p'} \right) & \approx \frac{\partial \overline{u'v'^2}}{\partial x} \quad \text{and} \\ \frac{\partial}{\partial y} \left(\overline{v'^3} + \frac{2}{\bar{\rho}} \overline{v'p'} \right) & \approx \frac{\partial \overline{v'^3}}{\partial y} \quad (\text{A4}) \end{aligned}$$

Thus, Eq. (A3) becomes:

$$\begin{aligned} \bar{u} \frac{\partial (\overline{u'^2} + \overline{v'^2})}{\partial x} = & -2 \left(\overline{u'^2} \frac{\partial \bar{u}}{\partial x} + \overline{u'v'} \frac{\partial \bar{u}}{\partial y} + \overline{u'w'} \frac{\partial \bar{u}}{\partial z} \right) \\ & - \left(\frac{\partial \overline{u'^3}}{\partial x} + \frac{\partial \overline{v'u'^2}}{\partial y} + \frac{\partial \overline{w'u'^2}}{\partial z} \right) + \\ & - \left(\frac{\partial \overline{u'v'^2}}{\partial x} + \frac{\partial \overline{v'^3}}{\partial y} + \frac{\partial \overline{w'v'^2}}{\partial z} \right) \\ & - 2(\varepsilon_1 + \varepsilon_2) \quad (\text{A5}) \end{aligned}$$

Appendix B

Equation (15) is expressed:

$$z^2 \frac{\partial^2 (\bar{e})^{3/2}}{\partial z^2} + z \frac{\partial (\bar{e})^{3/2}}{\partial z} - \frac{3C_\varepsilon}{2k^2 C_K} (\bar{e})^{3/2} = -\frac{3U_*^3}{2k^2 C_K} \quad (\text{B1})$$

otherwise:

$$x^2 f''(x) + x f'(x) + a f(x) = b \quad (\text{B2})$$

with:

$$x = z \text{ and } f(x) = (\bar{e})^{3/2}$$

$$a = \frac{-3C_\varepsilon}{2k^2 C_K} \text{ and } b = \frac{-3U_*^3}{2k^2 C_K}$$

Equation (B2) can be rewritten:

$$x^2 f''(x) + x f'(x) + a \left(f(x) - \frac{b}{a} \right) = 0 \quad (\text{B3})$$

Assuming:

$$g(x) = f(x) - \frac{b}{a}$$

we have:

$$x^2 g''(x) + x g'(x) + a g(x) = 0 \quad (\text{B4})$$

It also can be assumed:

$$g(x) = x^n h(x)$$

which gives:

$$x^{n+2} h''(x) + (2n+1) x^{n+1} h'(x) + (n^2 + a) x^n h(x) = 0 \quad (\text{B5})$$

otherwise:

$$x^2 h''(x) + (2n+1) x h'(x) = 0 \quad (\text{B6a})$$

with:

$$n^2 = -a = \frac{3C_\varepsilon}{2k^2 C_K}$$

Thus, it gives:

$$x h''(x) + (2n+1) h'(x) = 0 \quad (\text{B6b})$$

otherwise:

$$(x h'(x))' + 2n h'(x) = 0 \quad (\text{B6c})$$

which gives:

$$x h'(x) + 2n h(x) = C_1 \quad (\text{B7a})$$

otherwise:

$$\frac{h'(x)}{C_1 - 2n h(x)} = \frac{1}{x} \quad (\text{B7b})$$

Integrating the previous equation, we have:

$$\ln[C_1 - 2n h(x)] = -2n \ln(x) + C_3 \quad (\text{B8})$$

After arrangements, we obtain:

$$f(x) = C_5 x^n + C_6 x^{-n} + \frac{b}{a} \quad (\text{B9})$$

Which leads to:

$$\frac{\bar{e}}{U_*^2} = \left(\frac{1}{C_\varepsilon} + C_7 z^n + C_8 z^{-n} \right)^{2/3} \quad (\text{B10})$$

with:

$$n = \frac{1}{k} \sqrt{\frac{3C_\varepsilon}{2C_K}}$$

Appendix C

In dealing with the mean wind velocity profile, two kinds of relationship are indifferently proposed and used, i.e. the power relationship and the logarithmic one. These relationships are:

1. The power relationship

$$\frac{\overline{u(z)}}{\overline{u(z_{\text{ref}})}} = \left(\frac{z}{z_{\text{ref}}} \right)^\alpha \quad (\text{C1})$$

where

- $\overline{u(z)}$ is the mean wind velocity at level z
- $\overline{u(z_{\text{ref}})}$ is the mean wind velocity at level of reference z_{ref}
- α is the power law exponent, generally taken to 1/7 (or 0.143).

2. The logarithmic relationship

$$\frac{\overline{u(z)}}{U_*} = \frac{1}{k} \ln \left(\frac{z}{z_0} \right) \quad (\text{C2})$$

where

- $\overline{u(z)}$ is the mean wind velocity at level z
- U_* is the friction velocity
- Z_0 Roughness length
- k the Von Karman's constant, equal to 0.4.

Appendix D

Brief description of MW method (i.e. Statistical Method for the Calculation of the Dynamic Parameters of the ASL and the Energy Balance).

The goal of the method is the determination of the dynamic parameters of the ASL (i.e. U_* , θ_* , q_* , Z_{0m} , L), by taking into account the measurement uncertainties relating to the measurement of different parameters and by using the energy balance, as well as the information pertaining to the net radiation and the heat flux into ground.

For a naked ground and while ignoring the advection effect, the steady state equation of the energy balance is:

$$H + \lambda E = -(Rn + G) \quad (\text{D1})$$

where H , E , G , Rn and λ represent, respectively, the flux of sensible heat, evaporation, heat into ground, net radiation and latent heat of vaporization.

Using the Monin-Obukhov similarity theory, and taking into account the effect of water vapor on the atmospheric stability (Brook, 1978; Busch, 1973; Riehl et al., 1978) and

the attribution of different roughness lengths for momentum, heat and humidity equations (Brutsaert, 1975; Garrat et Hicks, 1973; Mascart et al., 1995; Wood et Mason, 1991), the profiles of wind, temperature and humidity, specific to the turbulent flow of atmospheric air in the ASL are described through:

$$\bar{u}(z) = \frac{u_*}{k} \left[\ln \left(\frac{z}{z_{0m}} \right) - \Psi_u \left(\frac{z}{L} \right) + \Psi_u \left(\frac{z_{0m}}{L} \right) \right] \quad (\text{D2a})$$

$$\begin{aligned} \Delta \bar{\theta} &= \bar{\theta}(z_2) - \bar{\theta}(z_1) \\ &= \frac{\theta_*}{k} \left[\ln \left(\frac{z_2}{z_1} \right) - \Psi_\theta \left(\frac{z_2}{L} \right) + \Psi_\theta \left(\frac{z_1}{L} \right) \right] \end{aligned} \quad (\text{D2b})$$

$$\begin{aligned} \Delta \bar{q} &= \bar{q}(z_2) - \bar{q}(z_1) \\ &= \frac{q_*}{k} \left[\ln \left(\frac{z_2}{z_1} \right) - \Psi_q \left(\frac{z_2}{L} \right) + \Psi_q \left(\frac{z_1}{L} \right) \right] \end{aligned} \quad (\text{D2c})$$

with

$$L = \frac{u_*^2 \bar{\theta}_v}{kg \theta_*} \approx \frac{u_*^2 \bar{\theta} (1 + 0.608 \bar{q})}{kg (\theta_* + 0.608 \bar{\theta} q_*)}$$

The roughness length Z_{0m} , which is a local parameter bound to the ground surface, must be considered as an empirical coefficient in Eq. (D2a).

Many kinds of stability functions can be utilized for the resolution of these equations.

The temperature and humidity specific scales are bound to the sensible and latent heats through:

$$\begin{aligned} H &= c_p \rho u_* \theta_v^* \\ E &= \rho u_* q_* \end{aligned} \quad (\text{D3})$$

Equation (D1) is taken into account by adding an equation evaluating the gap between the evaluated flux of heat (i.e. $H + \lambda E$) and the radiation flux (i.e. $Rn + G$):

$$\delta = Rn + G + c_p \rho u_* \theta_v^* + \lambda \rho u_* q_* \quad (\text{D4})$$

With 5 points of wind profile, a temperature gradient, a humidity gradient and an energy balance equation, one has 8 equations for 4 unknown parameters, i.e. u_* , θ_* , q_* and Z_{0m} , the Monin-Obukhov length deduced from 3 first previous parameters. This leads to the utilization of the mathematical technique of optimization.

As the roughness length and the friction velocity only appear in Eq. (D2a), it is more convenient to add supplementary equations in order to make the calculation of Z_{0m} more accurate. This can be obtained by expressing the profile of the mean wind velocity between two levels, as it follows:

$$\begin{aligned} \Delta \bar{u}_i^j &= \bar{u}(z_i) - \bar{u}(z_j) \\ &= \frac{u_*}{k} \left[\ln \left(\frac{z_i}{z_j} \right) - \Psi_m \left(\frac{z_i}{L} \right) + \Psi_m \left(\frac{z_j}{L} \right) \right] \end{aligned} \quad (\text{D5})$$

where the index “ i ” is taken $1 \leq i \leq 5$ while “ j ” is taken $i < j \leq 5$.

Finally, there are 4 unknowns for 17 equations in the system make up with Eqs. (D2a), (D2b), (D2c), (D4) and (D5).

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