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A procedure for quantitative characterization of superparamagnetic minerals in environmental magnetism

Arua S. Leite,1,2 Carlos A. Mendonça,1 Pedro L.A. Moraes1 and Andrea T. Ustra1
1Department of Geophysics, University of São Paulo, São Paulo, Brazil. E-mail: arualeite@gmail.com
2Geosciences Environnement Toulouse, University Paul Sabatier, Toulouse, France.

SUMMARY
Ultrafine grains of magnetic minerals provide reliable recordings of both naturally occurring and anthropogenically generated particulate matter in polluted air; magnetic data can be used to understand biogenic iron-cycling in anaerobic environments, as well as pedogenesis and palaeoclimate studies of loess soils. The ultrafine fraction is produced under specific conditions and can be easily recognized by its superparamagnetic (SP) behaviour. Many proxies have been proposed to account for the SP contribution by measuring its susceptibility dependency with frequency (frequency effect) or the magnetization loss after removing an external inducing field. Here we introduce the Superparamagnetic Concentration and Dipole Moment (SPCDM) procedure for quantitative interpretation of SP magnetization. This procedure is well suited to SP carriers with a fast magnetization decay (<1 s), as would be expected for magnetic minerals with a grain size distribution lying below the blocking volume for stable, single-domain (SD) magnetization. SPCDM requires a dedicated experimental procedure to isolate the SP response from the paramagnetic and remnant effects, as observed in samples with mixed contributions. The proposed technique was tested using synthetic, nanoparticles of magnetite and then to characterize the magnetic properties of air particulate matter (PM) sampled at Jânio Quadros tunnel in São Paulo, Brazil. For nano-sized magnetite, SPCDM estimates for dipole moment are invariable with mass concentration and consistent with the published results; estimates for particle concentration are strongly correlated with true mass concentration ($R^2 = 0.96$). For air PM, SPCDM estimates a particle size with a diameter of 7.7 ± 0.1 nm, a kind of ultrafine magnetic material not previously recognized in air pollutants.

Key words: Magnetic properties; Environmental magnetism; Rock and mineral magnetism; Inverse theory.

1 INTRODUCTION
Fine and ultrafine agnetic minerals (<μm) found in rock, soils and air particulate matter are indicators of natural and anthropogenic processes affecting the iron cycling in shallow and deeper levels of the Earth’s crust. Such magnetic mineral fractions are important for two reasons. First, few geochemical and biogeochemical processes are able to produce or modify such small grains in soils and rocks (Taylor et al. 1987; Maher & Taylor 1988; Maxbauer et al. 2016) and secondly, their characteristic superparamagnetic (SP) response can be recognized with common soil and rock magnetism procedures (Moskowitz et al. 1989, 1993; Tadurno 1995).

In general, the SP content can be recognized in the frequency domain by the susceptibility ‘frequency effect’ (Dearing et al. 1996), from measurements achieved in at least two frequencies (470 and 4700 Hz, for Bartington Instruments Ltd). The susceptibility variation with frequency is minor (to null) in the absence of SP minerals and so no frequency effect is produced in such cases. The SP behaviour can also be identified in time domain measurements by measuring the magnetization decay (‘viscous decay’) after turning off an inducing magnetic field applied to the sample (Worm 1999; Wang et al. 2010). Measurements in the time domain require an adequate time window and resolution tag to capture the magnetization decay waveform. A time window of 100 s is usually employed (Wang et al. 2010) and the decay rate is evaluated by the difference between magnetization at $t = 0$ and 100 s after the external field removal, normalized by the initial ($t = 0$) magnetization. This quantitative proxy for recognizing SP contents was introduced by Worm (1999) and improved by Machac et al. (2007) by introducing a set of intervals and field intensities. A close association between time and frequency domain percentage parameters was observed (Machac et al. 2007) despite the fact that both approaches only provide semiquantitative estimates for mass or volume concentration of SP minerals. It can be explained because both time and fre-
frequency percentage parameters (frequency effect and magnetization decay) result from mixed contributions of mineral type, grain size and concentrations, therefore they are not simple indicators of concentration itself. These percentage proxies are partly conditioned by acquisition parameters, making the comparison of different datasets no simple matter. Magnetization decay, evaluated in time windows of 15 s (Worm 1999) and 60 s (Machac et al. 2007), for example, are not necessarily correlated because decay rates are sensitive to minor variations in grain size. Wang et al. (2010) improved time-domain studies by using a J-meter coercivity spectrometer (Jasonov et al. 1998; Wang et al. 2010) and measuring the magnetization immediately after the external field removal. There is also an extensive literature on using relaxation-based methods based on Néel theory for characterization of nanoparticle populations, under conditions for which the net magnetization is time-dependent over the measurement interval (e.g. Worm & Jackson 1999; Shcherbakov & Fabian 2005; Jackson et al. 2006; Egli 2009; Kodama 2013).

Previous works proposed different approaches to deal with magnetite grains exhibiting SP behaviour. Through the fitting of the Langevin function for a magnetization curve, they allow reconstructing the magnetic moment (or volume) distribution in synthetic samples. Berkov et al. (2000), using diluted ferrofluid samples propose fitting sums (or weighted integrals) through the singular value decomposition (SVD) technique and linear constraints to recover the distribution of magnetic moments. Woodward et al. (2007) compare measuring methods for the particle-size distribution of magnetic nanoparticles (transmission electron microscopy; Langevin fitting and small-angle neutron scattering). The Langevin fitting was accomplished by least-squares routines taking a priori assumptions about the distribution form. As developed in SPCDM, the Langevin fitting is applied after correcting IRM contributions, thus allowing the study of mixed samples as found in geological and environmental investigations. The SPCDM application to pure SP samples have much in common with previous work with synthetic materials.

A better characterization of the SP fraction allows the investigation of a diversity of problems in environmental magnetism. SP minerals can be formed as a consequence of variable redox conditions during wet and dry cycles (Maxbauer et al. 2016) and these result in indicators that allow recovery environmental and depositional conditions in complex sedimentary basins, as well as helping us to understand records of climate change in palaeosols and loess deposits (Maher & Thompson 1991; Porter 2001). SP particles are also generated during dissimilatory iron reduction (DIR) in anoxic conditions, where oxidation of organic matter becomes coupled with microbial reduction of Fe(III) oxides, with extracellular precipitation of ultrafine magnetite (Moskowitz et al. 1989; Jimenez-Lopez et al. 2010; Li et al. 2013).

In addition to natural processes, ultrafine magnetic minerals are also generated by industrial and transportation systems (fossil fuel combustion, disk-breaks, pavement abrasion, etc.) and these allow the application of magnetic measurements in pollutant provenance studies and air quality in urban areas (Sagnotti & Winkler 2012). Magnetic fractions in air particulate matter also serve as tracers for associated pollutants with ultrafine grain size (Sagnotti et al. 2006), for which safe exposure limits are not well established (Donaldson et al. 2015; Bealey et al. 2007). Air particulate matter (PM) with aerodynamic dimensions below 0.1 μm (PM_{0.10}) has been a topic of concern in health sciences because of their capacity to reach deeper parts of the respiratory system, thereby enhancing the deleterious effects of associated hazardous substances (Morrisey et al. 1995; Pope et al. 2002; Calderón-Garcidueñas et al. 2008).

Despite their importance in environmental magnetism, the common techniques used to characterize SP fractions are not effective in answering key questions (Evans & Heller 2003) about quantitative estimates for mass/volume concentration, grain size distribution and mineral types, among others. Most techniques based on data acquisition proxies (frequency effect or decay rate, for example) can be regarded as not being effective in addressing such questions. We develop a quantitative procedure—SPCDM (Superparamagnetic Concentration and Dipole Moment)—to determine the concentration and the dipole moment of the magnetic carriers with SP behaviour. When the magnetic mineral is known (or assumed a priori), quantitative estimates of mean grain size (though not of the size distribution) and particle concentration are obtained. An adequate database and processing scheme is required in order to isolate the SP response before determining the unknown parameters in the Neél’s model (sample specific saturation magnetization and grain dipole moment) with non-linear data inversion procedures. Particle concentration is then estimated from a basic, constitutive relationship relating the model parameters obtained from data inversion. SPCDM is validated by a control experiment, comprising samples with different concentrations of nano-sized synthetic magnetite within a narrow size distribution and then applied to analyse air particulate matter from air-quality monitoring stations installed in the Jânio Quadros tunnel in São Paulo, Brazil.

2 THEORY

2.1 Model construction

Single-domain, ferromagnetic minerals exhibit an SP response when reduced to grain sizes down to a critical blocking volume that is not able to sustain permanent magnetization at room temperature. Below this blocking volume, the orientation of the particles magnetic moments is disturbed by thermal fluctuations resulting in bulk magnetization. When exposed to an external static field, the dipole moments are aligned with the inducing field sustaining a net magnetization as long as the inducing field is kept active, otherwise it vanishes. For an assemblage of uniform grains, this unstable magnetization decays according to the formula (Evans et al. 2003)

$$M(t) = M_0 e^{-	au t},$$

(1)

starting from magnetization $M_0$ when $t = 0$ (when the inducing field is turned off). Magnetization $M(t)$ decays according to a characteristic relaxation time $\tau$ given by Néel (1955) and

$$\tau = \tau_0 e^{-\frac{\mu_0 M_0}{\kappa T}},$$

(2)

where $\tau_0$ is a time-factor varying from $10^{-12}$ to $10^{-8}$ s (Dormann et al. 1996; Worm 1998) and accounts for a characteristic time-lag between successive random thermal fluctuations (Berndt et al. 2015). $E_M = \kappa V$ represents the magnetostatic energy barrier required to switch the magnetic dipole direction, $K$ [Jm$^{-1}$] is the grain coefficient of anisotropy and $\nu$ [m$^3$] is its volume. Thermal energy ($E_T = k_B T$) counteracts magnetic ordering by randomly flipping the grain dipole directions; $k_B = 1.38 \times 10^{-23}$ [JK$^{-1}$] is the Boltzmann constant and $T$ [K] is the temperature. The coefficient of anisotropy is given by the equation $K = \mu_0 H_s \sigma / 2$, where $H_s$ [Am$^{-1}$] is the microscopic coercivity of the grain, such that $H_s = 2.09 H_c$ (Stoner & Wohlfarth 1948). Term $H_c$ is the sample macroscopic coercivity and $\sigma$ is the saturation magnetization of the mineral species.
Figure 1. (a) Variations of relaxation time with diameter of spherical magnetite-like minerals and (b) corresponding magnetization decay normalized by initial magnetization $M_0$. Blocking volume with stable magnetization (blue), thermally active particles with viscous (green and magenta) and fast (red) magnetic relaxation as expected in 100 s window.

For measurements at a constant temperature, the relaxation time $\tau$ is conditioned by grain size $v$ and magnetic anisotropy $K$; both parameters express physical properties of the magnetic carriers. Fig. 1 illustrates the wide variation of relaxation times from minor changes in diameter that would be expected from spherical particles of magnetite (mineral specific saturation magnetization $\sigma_S = 480$ kAm$^{-1}$, $K = 2.31 \times 10^4$ Jm$^{-1}$). The magnetization decay can be relatively fast ($\tau = 1.98 \times 10^{-4}$ s) for grains with diameters of 10 nm, in the 100 s time window for grains with diameters of 20 nm, and stable ($9.4 \times 10^{11}$ yr) for grains with diameters of about 28 nm. Experimental data shows that blocking volume for magnetite has a diameter between 25 and 30 nm (Dunlop & ¨Ozdemir 2001) and approximately 17 nm for hematite (Jiang et al. 2014).

Fig. 1(b) is effective in showing how minor grain size variations may lead to substantial changes in the magnetization decay rate. This change is particularly sensitive in particles below a few nanometres in diameter with respect to a reference grain diameter for a blocking volume, sustaining stable magnetization in SD grains. It can be seen that a very narrow grain size distribution is associated with magnetization decay waveforms that are able to be captured in the 100s time-window, as have been observed in SP studies (e.g. Worm 1999; Wang et al. 2010). For broader ranges of grain sizes below this limit fast decay rates (in milliseconds or microseconds) are expected. This faster decay behaviour may be within the time resolution interval of common equipment or in the range of transient coil induction fields, preventing further analysis based on modelling the magnetization waveform decay. Nevertheless, a ‘slow’ decay rate (e.g. one captured in the 100 s time-windows) is indicative of a coarser SP fraction nearing the characteristic blocking volume for SD grains.

For pure (non-mixed) ultrafine grains, the transient magnetization vanishes to zero within intervals of microseconds, henceforth termed ‘fast SP decay’. This type of fast decay can be associated with particles of a grain size well below the critical volume for stable magnetization. For mixed SP-SD or SP-MD mineral fractions, the SP magnetization appears superimposed to stable magnetization. Fig. 2 illustrates cases of fast decay rates observed for pure (Figs 2a and b) and mixed (Figs 2c and d) SP samples. Fast decay rates are observed in samples with nanoparticles of magnetite dispersed in paraffin (see Section 3) in a similar way to rates seen in air PM collected in the Jânio Quadros tunnel in São Paulo (Section 4). The air PM sample also exhibits IRM acquisition, according to the intensity of the inducing field and, as such, indicates a mixed contribution of magnetic carrier with grain sizes in the SP and SD-MD fractions.

Slower magnetization decay is observed in the sediments from the Jaraguá Cavern in São Paulo, as magnified in Fig. 3 for samples exposed to an external field of 500 mT. Fig. 3 illustrates that fast decay SP relaxation does occur in samples from air PM and are, therefore, indicative of ultrafine grain size distributions that have not been well accounted for in previous studies.

For pure (non-mixed) ultrafine grains (e.g. Figs 2b and c), the transient magnetization vanishes to zero in microseconds; and is associated with particles of grain sizes well below the critical volume for stable magnetization. In exploration geophysics terms, this type of magnetization is known as ‘induced magnetization’ (Telford et al. 1990) and it appears superimposed to stable magnetization in mixed SP-SD or SP-MD mineral fractions.

The SP contribution under the $H_0 [\text{Am}^{-1}]$ external field is given by eq. (3) (Dunlop & ¨Ozdemir 2001)

$$M (H_0, T) = M_s L (\alpha),$$

where

$$\alpha = \frac{\mu_0 v \sigma_S H_0}{k_B T}$$

and $L (\alpha)$ is the Langevin function:

$$L (\alpha) \equiv \coth \left( \frac{\mu_0 v \sigma_S H_0}{k_B T} \right) - \frac{k_B T}{\mu_0 v \sigma_S H_0}.$$ 

In eq. (3), $M_s$ is the sample specific saturation magnetization and $\mu_0 = 4\pi \times 10^{-7}$ [Hm$^{-1}$] is the free space permeability. For hematite, $\sigma_S$ is approximately 0.5 per cent that of magnetite (Dunlop & ¨Ozdemir 2001). The grain dipole moment is $\mu = \sigma_S [\text{Am}^2]$ and the sample saturation magnetization is $M_s = n \mu [\text{Am}^2]$. Term $n [\text{m}^{-1}]$ is the concentration (number of particles per volume) of the magnetic carriers. For a sample with density $\rho [\text{kgm}^{-3}]$, the mass-concentration of the magnetic carriers is obtained by $n/\rho$. The concentration of SP carriers ($n$) does not necessarily express the concentration of particulate matter, except under a very particular condition in which single magnetic particles are attached to single grains in the soil or particulate matter.
Figure 2. Hysteresis curves (left) normalize by high-field magnetization $M_h$ (magnetization expressed in fields of 1 and 0.5 T) and magnetization decay curves (right) normalized by in field magnetization $M_0$ (magnetization measured during external fields applications); (a) calibrator 2853 YIG Sphere with pure SP behaviour; (b) nanoparticles of synthetic magnetite with 8 nm diameter; (c) air particulate matter collected in Jánio Quadros tunnel, São Paulo; (d) sediments from Jaraguá Cave, São Paulo with subtle magnetic decay in 100s window. Pure SP response is observed in sample (a), (b); combined SP and IRM responses observed in samples c and d. Zero-crossing in hysteresis curves for sample b is consistent with pure SP composition; low coercivity in samples (c) and (d) is indicative of magnetite-like minerals comprising a coarser fraction with IRM response. The decay curves for in fields of 10, 25, 60, 120, 220 and 340 mT. SPCDM data have 17 in field inductions, for illustration only 6 are presented.
Under isothermal conditions, the SP magnetization dependence on the external field $B = \mu_0 H_0$ is written as $M(B) = M(B, T)$, such that

$$M(B) = M_S L \left( \frac{\mu B}{k_B T} \right).$$  

(6)

From estimates of grain dipole moment $\mu$, and by assuming that the magnetization saturation $\sigma_S$ is known, particle volume $v$ can be determined by constitutive relationship $\mu = v \sigma_S$. By assuming particles with spherical shape, diameter estimates can be achieved.

### 2.2 Inverse problem formulation

According to eq. (6), SP magnetization is described in terms of two unknown parameters: $M_S$ and $\mu$. These parameters can be determined under an inverse problem formulation by considering a data set with $N$ measurements of magnetization, $M_i^\sigma$ = $M(B_i)$, when exposed to external fields $B_i$, $i = 1 : N$. The unknown parameters can be determined by minimizing a least-squares functional $Q(M_S, \mu)$ such that

$$Q(M_S, \mu) = \sum_{i=1}^{N} \left[ M_i^\sigma - M^\mu(B_i, M_S, \mu) \right]^2,$$

(7)

where the superscript $\sigma$ and $\mu$ stand for ‘observed’ and ‘calculated’ magnetization values. According to inverse problem terminology (Aster et al. 2011), the minimization of functional in eq. (7) configures a non-linear problem because one of the unknown parameters ($\mu$) appears as an argument of a non-linear function. The determination of the unknown parameters then requires a non-linear optimization procedure, usually converging with iterative steps, starting from an initial solution (or set of solutions) until reaching a data fitting criterion $Q(M_S, \mu) \leq \varepsilon$ or stop condition. Parameter $\varepsilon$ establishes the acceptability condition for data fitting, according to experimental error in the data.

The set of solutions minimizing the functional $Q$ can be accessed by mapping this function within a parameter space window and providing a visual representation of solutions satisfying $Q \leq \varepsilon$ as well as possible alternative solutions (if they exist). This mapping is done by evaluating functional $Q(M_S, \mu)$ for a mesh of values $(M_S, \mu)$ in the parameter window $M_S \leq M_S \leq M_{S2}$ and $\mu_1 \leq \mu \leq \mu_2$, as defined by the lower (1) and upper (2) limits for the searched parameters. The solutions domain in this mapping appear below a contour level (‘water level’) which is established by threshold $\varepsilon$. Domain projection towards the coordinate axes $M_S$ and $\mu$ with the unknown parameters provides a visual representation for the uncertainty of the parameters in this modelled solution. Uncertainty analysis can also be carried out by finding multiple solutions or computing the parameters covariance for single solutions (Aster et al. 2011).

### 2.3 Experimental aspects

An experimental procedure was devised to isolate the SP response in mixed carrier samples. The proposed procedure is well suited for samples with fast SP decay, as expected for ultrafine particles discussed in Section 2.2. For mixed SP-SD (or SP-MD) samples, the magnetization decays from magnetization $M_0 = M_0(B_i)$, achieved under field $B_i$, at $t = 0$ s to isothermal, remnant magnetization $M_q = M_q(B_i)$. Once corrected for paramagnetic effects, the difference $M_0 - M_q$ can be regarded as isolating the SP response and, as such, well suited to be modelled according to eq. (6). For pure SP response, the magnetization decay rate is represented as $M(t) = M_0 = \exp(-t/\tau)$ (eq. 1) and for mixed SP-IRM contributions, by the expression $[M(t) - M_q]/[M_0 - M_q] = \exp(-t/\tau)$. The MicroMag3900-VSM measures the sample dipole moment $S_D$ [Am²], and not the magnetization $M$ [Am⁻¹]. The relationship between the two is $S_D = MV$ (Evans & Heller 2003), where $V$ is the volume [m³] of the sample. Thus, the sample dipole saturation $SDS$ [Am²] is given by $SDS = M_S V$.

The procedure devised to provide a database for the proposed technique followed the following steps. Initially, the sample was AF-demagnetized (120 Hz, from 1T to zero in 2 per cent increments) and then subjected to external fields $B_i$ of 5, 10, 15, 20, 25, 30, 40, 60, 80, 100, 120, 140, 180, 220, 260, 300 and 340 mT, where $i = 1 : 17$ during 10 s intervals. Longer exposures of 20 and 40 s were tested but this gave equivalent results. The magnetization $M_0$ is measured when the external field is on, setting $t = 0$ s when this field is turned off. Magnetization decay $M(t)$ is then recorded and averaged between 2 and 4 s to obtain equilibrium magnetization $M_q$. In general, a flat baseline for magnetization was achieved as fast as 10 to 20 ms after the external field was turned off, within coil inductive effects. For the tested samples, the averaging window from 2 to 4 s was unaffected by such effects, thus giving a baseline equilibrium for magnetization $M_q$. The differences $M_i^\sigma = M_i(B_i) - M_q(B_i)$ were then computed for external fields $B_i$ to isolate the sample SP response. Magnetization decay of SD and MD grains occurs at time lengths above 100 s (Fabian 2003; Williams & Muxworthy 2006) and tends to be cancelled when computing $M_0 - M_q$. This is strictly true when viscous decay is not observed in the time-window in which $M_q$ is averaged and this difference computed. Errors were estimated by repeating the acquisition procedure for the calibrator sample (2853 YIG Sphere) 15 times. The percentage error was then evaluated and applied to measurements with tested samples. Paramagnetic
correction was carried out by the approach to saturation method, developed by Jackson & Solheid (2010). This correction was implemented through the scripts introduced by Paterson et al. (2018), using the estimated paramagnetic susceptibility \(\chi\) and calculated it for each field \(B_i\) as \(\chi B_i\) to remove the paramagnetic response from \(M_i\) estimates.

2.4 Computational aspects

The SPCDM codes were implemented in two main steps. Data files from MicroMag3900 were processed according to the procedures described in Section 2.3, to isolate the SP response. An inverse procedure (as described in Section 2.2) was then applied to minimize \(Q(S_{DS}, \mu)\). The minimization of this function was achieved with the FMINCON function of the Matlab Optimization Toolbox, based on the interior point algorithm of Byrd et al. (2000). As an iterative procedure, FMINCON requires an initial solution, which, in SPCDM, was chosen randomly within a feasibility interval, guaranteeing the parameters positivity. The optimization procedure was applied 10 times for each data set, starting from random initial solutions in order to probe alternative solutions and uncertainty. The set of resulting solutions were then used to evaluate mean \(S_{DS}\) and \(\mu\) model parameters and their respective standard deviations. These mean-solution values were used to check data fitting and evaluate SP concentration according to \(\hat{\mu} = S_{DS}/\hat{\mu}\). It is worth noting that SPCDM estimates for concentration did not necessarily give the particulate matter concentration, except under very particular situations in which single magnetic carriers were attached to single particles in the particulate matter. A factor expressing how many magnetic particles are attached to air PM grains is required to better evaluate air PM concentration from SPCDM estimates.

2.5 Quantifying SP contribution in total magnetization

In order to evaluate the contribution of the SP fraction in total magnetization we apply the parameter

\[
\%SP = \left( \frac{M_{SP,1T}}{M_{H,1T}} \right) \times 100,
\]

which relates SP magnetization \(M_{SP,1T}\equiv M(\hat{\mu}, S_{DS}, B_{1T})\) calculated from eq. (6) and total magnetization \(M_{H,1T}\) as measured in the hysteresis curve. This parameter can be evaluated under other external field intensities but the value of 1T is advised to take into account contributions from high coercivity (hematite-like) minerals, as well as to saturate SP and IRM magnetization. Parameter \%SP is not related to data acquisition parameters (frequency range, time intervals or field intensity), especially considering that it varies little, when evaluating for external fields high enough to saturate both SP and IRM magnetizations.

3 SPCDM APPLICATIONS

3.1 Nanoparticles of synthetic magnetite

The first set of samples to test the SPMMDM procedure comprised nanoparticles of synthetic magnetite with a mean diameter of 8 nm. These nanoparticles were synthesized according to a thermal-decomposition process reducing a Fe(III) solution under boiling temperature (\(\sim 200\) °C) in the presence of stabilizing agents, controlling the growth of the magnetite precipitates. A common aliquot of nanoparticles was used to prepare 0.2, 1.0, 1.9, 3.2, 4.4 and 5.0 per cent of mass concentration by mixing with paraffin. As illustrated in Fig. 2(b) for a 5 per cent concentration sample, the nanoparticles have a pure SP behaviour at room temperature, as expressed by null coercivity in the hysteresis curve and fast magnetization decay. Its fast SP decay rate is compatible with the analysis based on Fig. 1. Fig. 4 shows SPCDM results with inverted model parameters and respective data fitting for a sample with a concentration of 5 per cent. Fig. 4(b) shows the objective function mapping, centred at the solution model obtained from data inversion. The narrow domain of alternative solutions and the absence of alternative local minima, guarantees the uniqueness for the inverted parameters.

Table 1 presents SPCDM results for the samples tested, with nanoparticles of magnetite at different concentrations. For each sample, the inversion procedure was repeated 10 times, starting with a randomly chosen solution to determine the spreading range for the inverted solutions.

The results in Table 1 show that, independent of sample concentration, the grain dipole moment estimated for the magnetic carrier is practically the same. This gives consistency to SPCDM results regarding that all tested samples were prepared with particles sharing common specifications, in terms of grain size and composition. As suggested by this test, the SPCDM estimates for grain dipole moment are not distorted by particle concentration, thus recovering an important property of magnetic carriers. The mean grain dipole moment of \(1.07 \times 10^{-19}\) \(\pm 0.01\) Am² was estimated for the grains, which is in agreement with previous estimates of \(0.85 \times 10^{-19}\) Am² for grains of magnetite with 8 nm diameter, as presented by Ge et al. (2007).

Fig. 5 shows the SPCDM estimate for the mean grain dipole moment for nanoparticles of magnetite, in addition to published results for magnetite with different grain sizes (Goya et al. 2003; Ge et al. 2007; Sievers et al. 2012). Also in Fig. 5, is a reference to curve for model \(\mu = v\sigma_{S}\), assuming \(\sigma_{S}=480\) kAm⁻¹ (saturation magnetization for magnetite) and spherical particles when evaluating volume \(v\). Despite a paucity of dipole moment data for nano-sized magnetite, one can observe a good agreement between data and model predictions, suggesting that dipole moment estimates can be used for preliminary inferences about the particle diameter of magnetite-like minerals with fast SP decay. For the nanoparticles of magnetite tested here, a mean diameter of 7.5 ± 0.2 nm was estimated, in agreement with diameter determination from the TEM image (Fig. 5), which points to real diameters of 8.0 ± 0.7 nm. It should be stressed that this is a preliminary inference but, in principle, it promises to be useful in environmental studies where pollutant provenance for distinctive grain sizes can be indicative of specific sources.

SPCDM estimates for mass-concentration (parameter \(n_{m}\)) from Table 1 were plotted in Fig. 6 with respect to true mass concentration, producing a clear linear dependence \((R^2 = 0.96)\). This result validates the SPCDM procedure as a quantitative technique to determine concentrations of magnetic fractions in fine and ultrafine grain sizes.

Estimates for parameter %SP (Table 1), representing the contribution of SP magnetization in total magnetization under the 1 T field, reach 98.5 per cent. This result confirms that magnetization of nano-sized magnetite keeps no IRM, holding magnetization only \((\sim 100\) per cent) from the SP contribution. The \(\sim 1.5\) per cent difference may be due to accuracy limits in retrieving model parameters from the inversion of noisy data and experimental errors or measuring total field magnetization.
Figure 4. Inversion products of the SPCDM procedure; (a) data fitting and estimated parameters grain dipole moment $\mu$ [Am$^2$]; sample dipole saturation $S_{DS}$ [Am$^2$] and number of magnetic carriers $N$. Measured data (black circles) and fitting curve (red) from the inverted model parameters. (b) Objective function with inverted model solution (white cross). For the sake of graphical representation the value of $10^\varepsilon$ is contoured (black) for a threshold data fitting $\varepsilon$ equal to 5.0E-8, with stop criterion $Q_{\text{min}} < \varepsilon$. 
**Table 1.** SPCDM results for synthetic samples of nanoparticles of magnetite with variable mass-concentration (per cent) in paraffin; \( \mu \) and \( S_{DS} \) are the grain dipole moment and sample dipole saturation, respectively; \( n_{m} \) is mass-concentration of magnetic carriers (number of magnetic carriers per sample mass); \( \%SP \) is the contribution of SP magnetization in total magnetization under external field of 1 T. \( S_{DS} = M_{S} V \) where \( M_{S} \) is sample saturation magnetization and \( V \) is sample volume.

<table>
<thead>
<tr>
<th>Conc. (%)</th>
<th>( \mu \times 10^{-19} ) Am(^2)</th>
<th>( S_{DS} \times 10^{-5} ) Am(^2)</th>
<th>( n_{m} \times 10^{5} ) g(^{-1})</th>
<th>%SP</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.2</td>
<td>(1.07 \pm 0.01)</td>
<td>(0.39 \pm 0.00)</td>
<td>(0.99 \pm 0.03)</td>
<td>98.5</td>
</tr>
<tr>
<td>1.0</td>
<td>(1.06 \pm 0.00)</td>
<td>(1.39 \pm 0.01)</td>
<td>(4.38 \pm 0.15)</td>
<td>98.7</td>
</tr>
<tr>
<td>1.9</td>
<td>(1.06 \pm 0.01)</td>
<td>(2.99 \pm 0.01)</td>
<td>(8.78 \pm 0.31)</td>
<td>98.9</td>
</tr>
<tr>
<td>3.2</td>
<td>(1.07 \pm 0.01)</td>
<td>(4.30 \pm 0.00)</td>
<td>(12.50 \pm 0.40)</td>
<td>98.6</td>
</tr>
<tr>
<td>4.4</td>
<td>(1.08 \pm 0.01)</td>
<td>(6.71 \pm 0.02)</td>
<td>(15.20 \pm 0.50)</td>
<td>98.6</td>
</tr>
<tr>
<td>5.0</td>
<td>(1.06 \pm 0.00)</td>
<td>(4.13 \pm 0.00)</td>
<td>(15.60 \pm 0.60)</td>
<td>98.9</td>
</tr>
</tbody>
</table>

**Figure 5.** SPCDM estimate for the grain dipole moment (red cross) for nanoparticles of magnetite with particle size distribution diameters centred at 8(1) nm (inset histogram) and published values from previous studies. Dashed curve evaluated from constitutive equation \( \mu = \sigma S V \) for \( \sigma S \approx 480 \) kAm\(^{-1}\) (saturation magnetization of magnetite). Samples with nanoparticles of magnetite and Transmission Electron Microscopy (TEM) picture (inset) provided by D.G. da Silva, S.H. Toma and K. Araki.

**Figure 6.** SPCDM estimates for particle concentration versus true mass concentration.

3.2 Air PM in the Jânio Quadros tunnel

Samples of air PM were collected from air quality monitoring stations in the Jânio Quadros tunnel in São Paulo, from 2004 March 23 to 25. These samples were analysed by Martins et al. (2006) and Sanchez-Ccoyllo et al. (2009) and then stored in the Laboratory of Palaeomagnetism and Rock Magnetism of IAG-USP. Each sampling day was divided into five intervals of 2 hr, from 08:00 a.m. to 18:00 p.m. The air PM samples were acquired using a Mini-VolTM Air Sampler (Airmetrics Eugene, OR, USA), with a flow volume of 7 L min\(^{-1}\) (Baldauf et al. 2001; Sanchez-Ccoyllo et al. 2009). The particulate was sieved through a sequence of 10 filters, using a MOUDITM (micro-orifice uniform deposit impactor, MSP Corporation, Shoreview, MN, USA). As well as being analysed by the SPCDM procedure, the air PM samples were subjected to magnetic susceptibility measurements using a Multifunction Kappabridge MKF1-FA (Agico). SPCDM data were measured with a MicroMag3900-VSM (Lake Shore Cryotronics). To enhance the magnetic response, the set of 10 filtered fractions was grouped into pairs, according to adjacent grain size specifications, and then measured as a single sample.

As illustrated in Fig. 2(c), the magnetic relaxation of the air PM collected in the Jânio Quadros tunnel has a fast SP behaviour and growing IRM acquisition with increasing external fields, which is indicative of samples of mixed carriers with different properties (grain size and/or composition). A magnetic response indicating mixed contributions in air PM was also observed by Maher (2009). In the Jânio Quadros tunnel, the finer-grained minerals exhibit fast SP decay (Fig. 3b) and the coarser ones show low coercivity (1.93–4.55 mT) in the hysteresis curve; this is indicative of magnetite as a contributor in the IRM response.

SPCDM results for air PM in the Jânio Quadros tunnel are presented in Table 2. The grain dipole moment for these samples has a mean value of \(1.14 \times 10^{-19} \pm 0.05\) Am\(^2\), which does not significantly change in the time intervals in which the samples were collected. This result suggests that the magnetic properties of the air PM in the tunnel atmosphere are practically invariant, in terms of the carrier magnetic properties (size and composition) despite variable traffic conditions being observed during the test period. This result could be indicative of a uniform atmosphere in the tunnel (at least in terms of its ultrafine content properties) but it could also result from bias introduced by the filtering procedure, possibly through...
selecting specific grain fractions along the chain of filters. A better evaluation is required to allow continuity of this study. The mean value of the air PM grain dipole moment is $1.14 \times 10^{-19} \pm 0.05$ Am$^2$ which, by applying the constitutive model $\mu = n_S S_D$ as previously discussed, gives a mean diameter of $7.7 \pm 0.1$ nm for air PM in the tunnel. The estimate of such ultrafine content in the air particulate can probably be representative of a set of substances with common aerodynamic properties. From this point of view, the magnetic content in air PM may serve as a surrogate for hazardous substances (heavy metals, organics, etc.) that are also present in air PM but possibly deserving of more attention in air quality policies.

Although the magnetic carrier that comprises the air PM is rather homogeneous, its concentration covers a broad variation range. The sample dipole saturation varies from $1.76 \pm 0.06 \times 10^{-7}$ to $6.05 \pm 0.08 \times 10^{-7}$ Am$^2$ and corresponds to volume-concentrations from $1.84 \pm 0.18 \times 10^{12}$ to $6.46 \pm 0.26 \times 10^{12}$ m$^{-3}$. Despite a three-fold variation, there was no clear association with traffic density, which may suggest a dependency on sources not related to engine-combustion and contributions from sources like disk-brakes or suspended matter from pavement abrasion, among others. The %SP parameter varies from 88.9 to 98.7 per cent, suggesting that contributions from stable magnetization (in the coarser fractions) varies

### Table 2. SPCDM results for particulate matter in the Jânio Quadros tunnel in São Paulo, Brazil; $\mu$ and $S_{DS}$ are the grain dipole moment and sample dipole saturation; $n_v$ is volume-concentration of magnetic carriers (number of magnetic carrier per air flow volume in each sampling interval), and %SP the contribution of SP magnetization under external field of 1T.

<table>
<thead>
<tr>
<th>Day</th>
<th>Sampling Interval</th>
<th>$\mu$ ($10^{-19}$ Am$^2$)</th>
<th>$S_{DS}$ ($10^{-7}$ Am$^2$)</th>
<th>$n_v$ ($10^{12}$ m$^{-3}$)</th>
<th>% SP</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>08:00–10:00</td>
<td>$1.14 \pm 0.09$</td>
<td>$1.76 \pm 0.06$</td>
<td>$1.84 \pm 0.18$</td>
<td>98.7</td>
</tr>
<tr>
<td></td>
<td>10:00–12:00</td>
<td>$1.11 \pm 0.03$</td>
<td>$1.94 \pm 0.01$</td>
<td>$2.08 \pm 0.06$</td>
<td>96.5</td>
</tr>
<tr>
<td></td>
<td>12:00–14:00</td>
<td>$1.20 \pm 0.07$</td>
<td>$2.20 \pm 0.06$</td>
<td>$2.19 \pm 0.16$</td>
<td>95.6</td>
</tr>
<tr>
<td></td>
<td>14:00–16:00</td>
<td>$1.22 \pm 0.02$</td>
<td>$2.13 \pm 0.20$</td>
<td>$2.08 \pm 0.03$</td>
<td>88.9</td>
</tr>
<tr>
<td></td>
<td>16:00–18:00</td>
<td>$1.22 \pm 0.05$</td>
<td>$2.83 \pm 0.04$</td>
<td>$2.77 \pm 0.69$</td>
<td>96.4</td>
</tr>
<tr>
<td>2</td>
<td>08:00–10:00</td>
<td>$1.11 \pm 0.04$</td>
<td>$6.05 \pm 0.08$</td>
<td>$6.46 \pm 0.26$</td>
<td>79.1</td>
</tr>
<tr>
<td></td>
<td>10:00–12:00</td>
<td>$1.11 \pm 0.05$</td>
<td>$4.49 \pm 0.07$</td>
<td>$4.82 \pm 0.23$</td>
<td>96.8</td>
</tr>
<tr>
<td></td>
<td>12:00–14:00</td>
<td>$1.18 \pm 0.02$</td>
<td>$5.12 \pm 0.04$</td>
<td>$5.16 \pm 0.11$</td>
<td>97.4</td>
</tr>
<tr>
<td>3</td>
<td>08:00–10:00</td>
<td>$1.14 \pm 0.03$</td>
<td>$3.08 \pm 0.04$</td>
<td>$3.23 \pm 0.10$</td>
<td>97.5</td>
</tr>
<tr>
<td></td>
<td>10:00–12:00</td>
<td>$1.13 \pm 0.05$</td>
<td>$4.58 \pm 0.08$</td>
<td>$4.84 \pm 0.27$</td>
<td>98.7</td>
</tr>
<tr>
<td></td>
<td>12:00–14:00</td>
<td>$1.22 \pm 0.09$</td>
<td>$1.84 \pm 0.04$</td>
<td>$1.81 \pm 0.16$</td>
<td>93.5</td>
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<tr>
<td></td>
<td>14:00–16:00</td>
<td>$1.14 \pm 0.01$</td>
<td>$4.48 \pm 0.03$</td>
<td>$4.66 \pm 0.79$</td>
<td>97.6</td>
</tr>
</tbody>
</table>
from day-to-day. This result was unexpected, especially regarding the uniformity of the SP content. For all samples, the magnetization from SP contribution was prevalent.

The concentration of Fe for air PM in the Jânio Quadros tunnel (Sanchez-Ccoyllo et al. 2009) varies between 0.73 and 3.21 μg m⁻³ (~4x), which is a range comparable to variations (~3x) in sample dipole saturation ($R^2 = -0.57$, in Fig. 7d) and particle concentration ($R^2 = -0.61$ in Fig. 7e). The correlation between true Fe concentration and inverted particle concentration is an inverse one, suggesting that the SP mineral fraction decreases as Fe content increases. This kind of behaviour can be explained by assuming that the higher Fe content comprises non-ferromagnetic minerals and, therefore, has only a minor contribution to SP properties. Such incursions of high Fe content could, for example, be hosted by paramagnetic or hematite-like minerals, with secondary contributions to the SP response often being modulated by magnetite-like minerals. The possibility of a second mineral phase could also explain the minor variations in magnetic susceptibility (Fig. 7a), as all samples showed susceptibility within the error margin 2.03 ± 0.33 SI. No correlation between Fe content and the grain dipole moment (Fig. 7b) and particle diameter (Fig. 7c) can be inferred due to the uniformity of the magnetic fraction in the particulate matter of the tunnel atmosphere. The negative correlation between Fe content and IRM suggests that high iron content is not forming ferromagnetic minerals in the SD-MD fractions with stable magnetization.

4 CONCLUSION

We have presented the SPCDM procedure to enable quantitative interpretation of SP magnetization for particles with grain sizes below the characteristic diameter for stable SD grains (at least by 1 or 2 nm). This condition encompasses a wide range of fine and ultrafine particles that can be characterized using the Néel model parameters for superparamagnetism, in terms of its grain dipole moment, magnetization saturation and, from both parameters, quantitative inferences about particle concentration. A constitutive model for the grain dipole moment (in terms of grain volume and magnetization saturation) allows estimation of the grain size diameter by assuming spherical shaped particles and magnetite-like carriers. Testing by the SPCDM procedure, using synthetic samples with nanoparticles of magnetite of different concentrations, produced a clear linear dependency between inverted and true concentrations as well as correct estimates for the grain dipole moment, estimated as 7.5 ± 0.2 nm for a true distribution (TEM image) of 8.0 ± 0.7 nm. Grain dipole moment (and, therefore, grain diameter) did not vary with concentration, thus validating the proposed procedure.

For air PM samples collected in the Jânio Quadros tunnel, SPCDM provided useful information about particle diameter (7.7 ± 0.1 nm), which was well below the critical volume for stable magnetization. To our knowledge, the existence of such ultrafine particles in air PM had not previously been identified. This is a promising result, when considering better assessment of air quality related to pollutants in the fine and ultrafine fractions because magnetic particulates can serve as a surrogate for other particulate fractions exhibiting the same aerodynamic behaviour, but with deeper concerns to public health or environmental pollution. The quantitative evaluation of grain properties may also be useful in studies of provenance or proxies to evaluate assimilation of particulate pollutants by living beings. As proposed, SPCDM is well suited for ultrafine SP fractions when the equilibrium magnetization after the external field removal, is observed in a few seconds. This procedure must be revised when handling samples with slower magnetization decay as this is indicative of coarser SP fractions. SPCDM works well however, for mixed samples with fast SP decay and stable IRM associated with low-coercivity (magnetite-like) minerals, as is characteristic of the samples analysed.

The SPCDM procedure has limitations that should be pointed out to the reader. First, since based on Langevin data fitting, the SPCDM method is well suited for SP fractions with ‘fast’ magnetization decay (as such, for grain-size distributions well below the thermally stable volume grains in room temperature). It is unsuited for mineral fractions with ‘viscous’ decays (grain volumes nearing the blocking volume) for which the relaxation times are comparable to measurement timescale. Secondly, it is assumed that the grain size of the ‘fast’ decay SP fraction is narrow enough (or unimodal) to be represented by a uniform grain size, as in the Néel model. Real estimates for grain size distribution may require observations with variable timescales (e.g. temperature, frequency) to reconstruct the distribution of size-dependent activation energy (Worm & Jackson 1999; Sheberbakov & Fabian 2005; Jackson et al. 2006; Egli 2009; Kodama 2013), which are not implemented in SPCDM. Thirdly, the magnetization saturation of the mineral SP fraction must to be known a priori to evaluate grain volume. It is not required, however, to obtain concentration estimates, which are provided by rationing two independent parameters obtained from data inversion.

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