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Properties of the Hyades, the eclipsing binary HD 27130, and the oscillating red giant ϵ Tauri[★]

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ABSTRACT

Context. The derivation of accurate and precise masses and radii is possible for eclipsing binary stars, allowing for insights into their evolution. When residing in star clusters, they provide measurements of even greater precision, along with additional information on their properties. Asteroseismic investigations of solar-like oscillations offers similar possibilities for single stars.

Aims. We wish to improve the previously established properties of the Hyades eclipsing binary HD 27130 and re-assess the asteroseismic properties of the giant star ϵ Tau. The physical properties of these members of the Hyades can be used to constrain the helium content and age of the cluster.

Methods. New multi-colour light curves were combined with multi-epoch radial velocities to yield masses and radii of HD 27130. Measurements of T_{eff} were derived from spectroscopy and photometry, and verified using the *Gaia* parallax. We estimated the cluster age from re-evaluated asteroseismic properties of ϵ Tau while using HD 27130 to constrain the helium content.

Results. The masses, radii, and T_{eff} of HD 27130 were found to be $M = 1.0245 \pm 0.0024 M_{\odot}$, $R = 0.9226 \pm 0.015 R_{\odot}$, $T_{\text{eff}} = 5650 \pm 50$ K for the primary, and $M = 0.7426 \pm 0.0016 M_{\odot}$, $R = 0.7388 \pm 0.026 R_{\odot}$, $T_{\text{eff}} = 4300 \pm 100$ K for the secondary component. Our re-evaluation of ϵ Tau suggests that the previous literature estimates are trustworthy and that the HIPPARCOS parallax is more reliable than the *Gaia* DR2 parallax.

Conclusions. The helium content of HD 27130 and, thus, of the Hyades is found to be $Y = 0.27$ but with a significant model dependency. Correlations with the adopted metallicity result in a robust helium enrichment law, with $\frac{\Delta Y}{\Delta Z}$ close to 1.2. We estimate the age of the Hyades to be 0.9 ± 0.1 (stat) ± 0.1 (sys) Gyr, which is in slight tension with recent age estimates based on the cluster white dwarfs. The precision of the age estimate can be much improved via asteroseismic investigations of the other Hyades giants and by future improvements to the *Gaia* parallax for bright stars.

Key words. binaries: eclipsing – open clusters and associations: individual: Hyades – stars: oscillations – stars: abundances – stars: individual: HD27130 – stars: individual: ϵ Tau

1. Introduction

Open star clusters offer the opportunity to investigate stellar evolution in detail thanks to the shared properties of their mem-

ber stars. The analysis of eclipsing binary stars and asteroseismology are strong tools for improving such studies further (e.g. Brogaard et al. 2011, 2012, 2017, 2018a,b; Miglio et al. 2012, 2016; Handberg et al. 2017; Arentoft et al. 2019; Sandquist et al. 2020). Here, we investigate the eclipsing binary HD 27130 and the oscillating giant ϵ Tau in order to constrain the properties of the Hyades open cluster.

[★] Tables 8–16 are only available at the CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via <http://cdsarc.u-strasbg.fr/viz-bin/cat/J/A+A/645/A25>

The Hyades is a relatively young open cluster. According to the literature, it is 625–790 Myr (e.g. [Perryman et al. 1998](#); [Brandt & Huang 2015](#); [Gossage et al. 2018](#); [Martín et al. 2018](#); [Gaia Collaboration 2018](#)), has super-solar metallicity (with $[\text{Fe}/\text{H}]$ determinations ranging from +0.1 dex to +0.2 dex, [Takeda & Honda 2020](#) and references therein), and is located at a distance from the Sun of 46.75 ± 0.46 pc ([Gaia Collaboration 2017](#)).

HD 27130 (BD +16 577, vB 22, V818 Tau, HIP 20019) is a double-lined eclipsing binary system ([Schiller & Milone 1987](#)) in the Hyades open cluster (see its membership information in [Griffin et al. 1988](#); [Schwan 1991](#); [Perryman et al. 1998](#); [Douglas et al. 2014](#)). According to previous studies, the components constituting the HD 27130 binary system are G8 V (hereafter primary) and K3-5 V (hereafter secondary) stars ([Schiller & Milone 1987](#); [Svechnikov & Perevozskina 2004](#)), with a period of about 5.6 days ([McClure 1982](#); [Svechnikov & Perevozskina 2004](#); [Watson et al. 2006](#); [Peterson & Solensky 1987, 1988](#)).

[Schiller & Milone \(1987\)](#) carried out *UBVRI* observations of HD 27130 and used the light curves to obtain the effective temperatures of 5470 K and 3977 K for the primary and secondary components, respectively. Slightly higher T_{eff} values equal to 5530 ± 100 K and 4220 ± 150 K were determined by [Torres & Ribas \(2002\)](#). [Schiller & Milone \(1987\)](#) also derived masses of $1.08 \pm 0.017 M_{\odot}$ and $0.771 \pm 0.011 M_{\odot}$ as well as radii of $0.905 \pm 0.019 R_{\odot}$ and $0.773 \pm 0.010 R_{\odot}$ for the primary and secondary members of the system, respectively. Similar mass values of $1.064 \pm 0.011 M_{\odot}$, $1.072 \pm 0.010 M_{\odot}$, $1.0591 \pm 0.0062 M_{\odot}$ for the primary and $0.763 \pm 0.005 M_{\odot}$, $0.769 \pm 0.005 M_{\odot}$, $0.7605 \pm 0.0062 M_{\odot}$ for the secondary components were attributed by [Peterson & Solensky \(1987, 1988\)](#), [Torres & Ribas \(2002\)](#), respectively.

The observational spectroscopic data and orbital elements of the star system were reviewed by [Griffin \(2012\)](#), including the detection of a faint third component. The impact of this on the physical parameters of HD 27130 seems to have gone unnoticed. Recently, [Torres et al. \(2019\)](#), [Torres \(2019\)](#) re-examined the mass- M_V relation for the Hyades based on new and updated parameters for some of the astrometric spectroscopic binaries in the cluster. Along with their new measurements, they included literature measurements for other spectroscopic binaries, including HD 27130, for which they adopted the measurements of [Torres & Ribas \(2002\)](#). As stressed by [Torres \(2019\)](#), significant improvements are to be expected from new measurements of more of these systems. Specifically, some of the systems have properties that are based on rather old measurements. [Torres et al. \(2019\)](#) mention, in their introduction, that HD 27130 has masses that have been measured with an accuracy of better than 1%, presumably based on published numbers, including those of [Torres & Ribas \(2002\)](#), which they adopted for their mass-luminosity relation of the Hyades. However, given the triple nature of the system and the updated spectroscopic parameters given by [Griffin \(2012\)](#), the previously published masses ([Peterson & Solensky 1987, 1988](#); [Torres & Ribas 2002](#)) are not likely to be accurate at the precision level of 1%.

In this work, we obtain new photometric and spectroscopic measurements of HD 27130 and measure new precise and accurate properties of the components. These results are used to constrain the helium content of the Hyades open cluster.

The giant star ϵ Tau is also a member of the Hyades. Given its late evolutionary stage, it is much better suited for an age estimate than the main-sequence components of HD 27130.

[Arentoft et al. \(2019\)](#) showed that ϵ Tau displays solar-like oscillations and measured its asteroseismic parameters, $\Delta\nu$ and ν_{max} . We adopt the asteroseismic measurements of [Arentoft et al. \(2019\)](#) and re-assess the physical properties of ϵ Tau to estimate the age of the Hyades cluster.

The paper outline is as follows. First, we present our observations of HD 27130 in Sect. 2. Section 3 contains our data reduction and basic analysis, while Sect. 4 describes our eclipsing binary modelling. Then, ϵ Tau is presented and re-assessed in Sect. 5. The properties of HD 27130 and ϵ Tau are used in Sect. 6 to establish the helium content and the age of the Hyades. Our summary, conclusions, and outlook are given in Sect. 7.

2. Observations

HD 27130 was observed both photometrically and spectroscopically. The time series of photometric and spectral observations were taken at the Molėtai Astronomical Observatory of Vilnius University (MAO, Lithuania). Additional photometric observations of the secondary eclipse were performed at the Astronomical Observatory of the University of Siena (AO SU) in Italy. We also include a light curve from the MASCARA telescope. All the light curves are available as electronic tables at CDS. The spectral observations were also obtained from the Stellar Observations Network Group (SONG) Hertzsprung telescope located at the Teide Observatory of the Astrophysics Institute of the Canary Islands, Spain.

2.1. Photometric observations at the Molėtai Astronomical Observatory

At MAO, we used a 51 cm Maksutov-type telescope with a 35 cm working diameter of the primary mirror and the Apogee Alta U47 CCD camera. The observations were carried out in a semi-robotic mode. During the period between 16 September, 2018 and 22 October 2019, we observed 17 runs and took a total of 11906 images in the Johnson-Cousins photometric system *B*, *V*, and *I* filters. Exposure times varied between 2.5 s for the *I* filter and 5 s for the *B* filter. In Table 1, we present information about the observing runs at MAO.

2.2. Photometric observations at the Astronomical Observatory of the University of Siena

At AO SU, we used a 0.30-m f/5.6 Maksutov-Cassegrain type telescope atop a Comec 10 micron GM2000-QCI equatorial mount. Image acquisition was provided by a Sbig STL-6303 CCD camera (with a 3072×2048 pixels of 1.15 arcsec size) and an Optec TCF-S precision focuser with temperature compensation. The images were acquired alternating the Johnson-Cousins photometric system *V* and *I* filters with exposure times of 20 seconds for both filters and defocusing the telescope to increase the signal to noise ratio (S/N). HD 27130 was observed on the night of 22 October 2019, when a secondary eclipse of HD 27130 was expected.

2.3. Photometric observations with MASCARA

In addition to the *BVI* photometry, we also use observations obtained by the MASCARA survey ([Talens et al. 2017](#)). The MASCARA survey utilises two stations, located in the northern and southern hemisphere, to search for transiting exoplanets. For this purpose, it obtains continuous, high-cadence observations of

Table 1. Dates of runs and numbers of images in different filters observed for HD 27130 at MAO and AO SU.

Dates of runs (JD-2458000)	<i>B</i> images	<i>V</i> images	<i>I</i> images
378.46496–378.56400	122	136	134
383.43266–383.56133	120	119	110
393.43604–393.59516	46	23	5
401.41744–401.46681	55	51	54
402.41152–402.64392	218	236	232
403.41291–403.64824	362	368	370
404.41396–404.63789	340	354	338
405.42203–405.62959	338	323	286
406.42025–406.62940	395	400	397
407.42510–407.62244	372	366	344
409.40506–409.64799	463	300	314
451.42251–451.59986	286	270	259
452.42069–452.59040	222	220	224
493.15244–493.39132	443	426	101
555.21378–555.35725	bad	144	133
751.39102–751.62263	–	444	443
779.54398–779.62327	–	101	99
779.38032–779.68534	–	246	242

Notes. The last line corresponds to observations at AO SU.

the brightest stars in the sky ($4 < V < 8.4$), and such observations are also very well-suited for use in variable star studies (Mellon et al. 2019). HD 27130 passes over the east, west and zenith pointing cameras of the northern MASCARA station and we use data obtained between February 2015 and August 2018. MASCARA uses no filter in its optics; as such, the bandpass is determined by the transmission of the windows and lenses and the response of the CCDs. No laboratory measurement of this combined response was carried out, however, an investigation of the measured relative MASCARA magnitudes reveals no deviations from *V*-band magnitudes. The quantum efficiency as a function of wavelength for the CCD can be seen in Fig. 4 of Talens et al. (2017). The raw MASCARA photometry was initially processed with the primary and secondary calibration steps of the MASCARA calibration pipeline (Talens et al. 2018), removing common mode systematics present in all the light curves and residual systematics in individual light curves, respectively. In order to better disentangle the eclipse signal and the residual systematics, we obtained a running mean of the fully calibrated phase-folded light curve using a period of 5.6092159 days and window size of 15 minutes. The running mean was then subtracted from the post-primary calibration light curve before re-running the secondary calibration step and this procedure was iterated until convergence was reached.

2.4. Spectroscopic observations at the Moléai Astronomical Observatory

Spectral observations of HD 27130 were carried out on the f/12 1.65 m Ritchey-Chretien telescope at MAO with the high-resolution Vilnius University Echelle Spectrograph (VUES, Jurgenson et al. 2014, 2016). A log of these observations is provided in Table 2. The VUES is designed to observe spectra in the 4000 to 8800 Å wavelength range with three spectral resolution modes ($R = 30\,000$, 45 000, and 60 000). The observations of HD 27130 were carried out using the 60 000 mode, however the

Table 2. Information on spectroscopic observations with the MAO 1.65 m telescope.

Midtime of exp. (JD-2458000)	Exp. time (s)	Resolution	Altitude (deg)
493.33566	600	68 740	51.28
493.34305	600	68 740	50.89
493.35039	600	68 740	50.41
512.30415	1800	68 280	49.97
521.29437	1800	68 113	48.57
525.18322	1800	68 115	50.04
525.20444	1800	68 115	51.35
525.22566	1800	68 115	51.79
537.21869	1800	68 344	51.12
555.26402	1800	68 220	39.50
575.28386	1800	68 054	25.06
576.27406	1800	68 049	26.50
578.25433	1800	68 370	29.39
587.26544	1800	68 014	22.11

actual resolution of this mode that is measured using Thorium-Argon (ThAr) lines is around 68 000. The data were reduced and calibrated following standard reduction procedures which included a subtraction of the bias frame, correction for flat field, extraction of orders, wavelength calibration, and a cosmic ray removal as described by Jurgenson et al. (2016). The spectra consist of 83 spectral orders. For most spectra, the ThAr lamp spectra were taken just prior and just after each exposure and 1583 ThAr lines used for the wavelength calibration.

2.5. Spectroscopic observations with the Hertzprung SONG telescope

Spectroscopic data were obtained with the Hertzprung SONG telescope (Andersen et al. 2014; Grundahl et al. 2017; Frandsen et al. 2018; Fredslund Andersen et al. 2019) at the Teide observatory on Tenerife island between 9–26 January, 2018. A log of these observations is provided in Table 3. Briefly, the observations were carried out with the SONG spectrograph at a resolution of 90 000 (1.2'' slit width) and exposure times of 1800 s. The spectra consist of 51 spectral orders, spanning 4400–6800 Å. To ensure a precise wavelength calibration, we obtained one spectrum of a ThAr calibration lamp just prior and just after each exposure. The number of ThAr lines used in the wavelength calibration varied between 1053 and 1102.

3. Data reduction and analysis

Phased light curves of the photometric observations are presented in Figs. 1 and 2. The photometric images observed at MAO were processed with a Muniwin program from the software package C-Munipack¹ (Hroch 2014). The Muniwin program is built on the basis of the software package DAOPHOT for stellar photometry in crowded stellar fields (Stetson 1987) and is designed for time series differential aperture photometry and search for variable stars. We used the *Advanced* image calibration procedure, to perform the bias and dark frame subtraction, and flat-field correction. For this purpose, we used more than ten images of the bias, dark and sky flat fields in each filter for the CCD image calibration of each night observations.

¹ <http://c-munipack.sourceforge.net/>

Table 3. Information on spectroscopic observations with SONG.

Midtime of exp. (JD-2458000)	Slit	Exp. time (s)	Flux (ADU)	Altitude (deg)
128.32321	6	1800.0	5743	59.00
130.44565	6	1800.0	7634	72.37
131.36576	6	1800.0	3844	73.48
132.42151	6	1800.0	6536	76.50
133.42460	6	1800.0	5150	75.34
139.30799	6	1800.0	5209	63.49
140.30879	6	1800.0	2029	64.55
140.33224	6	1800.0	2212	71.19
141.30902	6	1800.0	1516	65.41
141.38665	6	1800.0	4756	78.02
143.35550	6	1800.0	1541	77.78
144.33251	6	1800.0	4204	74.01
144.55573	6	1800.0	2174	26.77

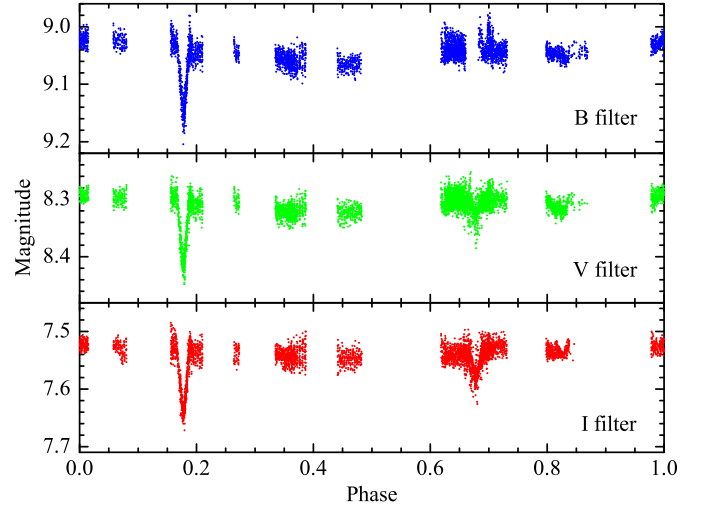
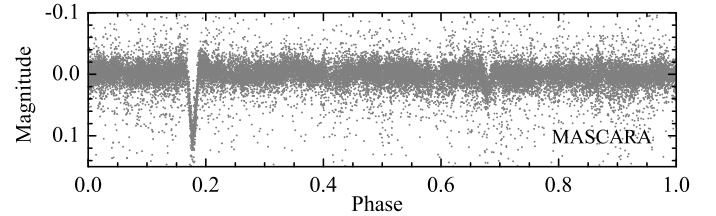
We used the Muniwin program to determine the instrumental magnitudes of all detected stars in the field using an aperture of 8 arcsec and selected among them one comparison star which was the brightest possible comparison star in the field and which did not show any signal indicating variability. For the further analysis, we calculated differential magnitudes of the target using the selected comparison star.

Photometric analysis of images observed at AO SU was done with the MaxIm DL² software using an aperture of 14 arcsec for the *V* filtered images and of 18 arcsec for the *I* filtered images. Differential photometry was performed using a photometric sequence from the AAVSO Variable Star Charts service³.

We calculated apparent magnitudes of HD 27130 in the Johnson *B* and *V* filters observed at MAO using HD 285678 as a reference star. We transformed the B_T and V_T magnitudes of the reference star from the Tycho-2 catalogue (Høg et al. 2000) to Johnson $B = 11.45$ and $V = 10.64$ magnitudes using equations in Appendix C of Mamajek et al. (2002), accounting for the sign error as corrected in Mamajek et al. (2006). There was no suitable reference star with known magnitude in *I* filter. The observed light curve of HD 27130 in the *V* filter at AO SU was fitted to the MAO observations. We could combine light curves observed at two different observatories since both observatories have observed HD 27130 at the same phase. The apparent magnitude in the *I* filter was calculated using the AO SU observations, as its field of view is larger and we could use another reference star HD 27110 recommended by AAVSO. Its value of *I* magnitude, which is 7.852 mag, was taken from The Amateur Sky Survey (TASS, Droege et al. 1997). Then the MAO observed light curve of HD 27130 in the *I* filter was fitted to the AO SU observations at certain phases of the light curve. Since the reference stars were chosen to optimise relative photometry rather than absolute, we do not use our measurements to derive precise absolute magnitudes of HD 27130. The light-curve analysis we perform afterwards is invariant with regard to the photometric zero point.

3.1. Radial velocity measurements

For measuring radial velocities (RVs) of the binary components at each epoch and to separate their spectra, we used a

**Fig. 1.** Phased *BVI* light curves of HD 27130 calculated with a period of 5.6092159 days.**Fig. 2.** Phased MASCARA light curve of HD 27130 calculated with a period of 5.6092159 days.

spectral separation code based on the description of González & Levato (2006) combined with the broadening function (BF) formalism by Rucinski (1999, 2002). This method works best when the observations sample a wide range in radial velocity as evenly as possible. Calculations were done order by order. For each epoch, the final radial velocity was taken as the mean of the results from each order and the rms scatter across orders divided by the square root of number of orders was taken as a first estimate of the uncertainty. Later, when we fitted the binary solution, we found that the first estimate of the RV uncertainties of the primary component were significantly smaller than the rms of the O–C of the best fit to the RVs. Our first solutions had O–C errors of up to 0.5 km s^{-1} in a systematic pattern identical for the primary and secondary components. This indicated that the radial velocity errors were dominated by radial velocity zero-point offsets between epochs. Since (almost all) our spectra are calibrated with ThAr spectra taken immediately after the stellar spectra, these offsets cannot be attributed to wavelength calibration errors.

As discussed by Griffin (2012), HD 27130 is a hierarchical triple system with a very faint tertiary star that shifts the system velocity of the primary-secondary orbit periodically with a semi-amplitude of about 2.3 km s^{-1} and a period of about 3079 days. Our observations with VUES were spread randomly in time over almost 100 days (see Table 2) and were therefore significantly affected by this. The SONG spectra, by contrast, were all observed within just 17 days (see Table 3) and should therefore not be significantly affected. This led us to continue with the radial velocity measurements only for the SONG spectra, given that we did not have spectra covering a long enough period to model the presence of the third component. We did first attempt

² <http://diffractionlimited.com/product/maxim-dl/>

³ <https://www.aavso.org/variable-star-charts/>

to use radial velocities from the VUES spectra by correcting for the motion of the inner pair's centre of mass in the outer orbit at each epoch using the elements from [Griffin \(2012\)](#). However, we could not reach a precision level on the orbit comparable to that with the SONG spectra. This is likely due to a combination of several issues; we mention some significant ones here: (1) five VUES epochs happened to be observed at times where RV differences between components were small, resulting in overlapping spectral lines, and thus potential systematic uncertainties on the radial velocities; (2) although we had the elements of [Griffin \(2012\)](#) to correct for the outer orbit, we found that our measurements were not on the same RV zero point for the SONG spectra, and even when accounting for that, we still found an additional mean offset in systemic velocity between SONG and VUES spectra of more than 1 km s^{-1} . Given a remaining larger-than-expected RV O-C scatter among the VUES spectra, it was not clear how to best subtract this additional RV offset; (3) we therefore attempted to force an RV offset so that at each VUES epoch the RV of the primary matches the orbital solution and use the so obtained corrected RVs for the secondary to improve on the solution. However, this also did not work well. The secondary component RVs still had O-C scatter of the order of 1 km s^{-1} , much larger than for the SONG spectra. A significant cause for this is the lower resolution of the VUES spectra compared to SONG, meaning that more systematic noise will be smoothed into the BF peak. Future simultaneous observations with the two instruments SONG and VUES will help improve the understanding of these issues.

Assuming that the radial velocities from SONG spectra were not significantly affected by the third component, another reason had to be found for their large O-C errors. These occurred because the starlight cannot be exactly centred across the SONG spectrograph slit width. This shifts the spectrum in wavelength relative to a star perfectly centred across the slit, thereby mimicking a radial velocity shift. To correct for this shift, we used the following procedure originally developed for the analysis of [Brogaard et al. \(2011\)](#): We identified a spectral order with very strong telluric absorption lines ($\lambda = 6282\text{--}6311 \text{ \AA}$). In the adjacent order we measured the combined BF profile of both components using a template spectrum. Tests show that the best reproduction of the combined spectrum from the BF is obtained when the template spectrum matches the dominant contributor. Therefore, we used a template from [Coelho et al. \(2005\)](#) with parameters matching the primary component. The BF profile obtained in this way is nearly identical for close-by orders. We then convolved our synthetic stellar template spectrum, covering the wavelength region with telluric absorption lines, with the obtained BF, to produce the expected stellar spectrum in that order. This spectrum was then multiplied with a synthetic telluric spectrum ([Bertaux et al. 2014](#)) which was broadened to the spectrograph resolution, shifted in radial velocity from -1 to $+1 \text{ km s}^{-1}$ in steps of 10 m s^{-1} , and multiplied with factors between 0.5 and 1.5 in steps of 0.1. The resulting set of artificial spectra of stellar+telluric lines were all cross-correlated with the observed spectra, and the one giving the highest cross correlation determined the shift of the telluric lines. This shift corresponds to the radial velocity zero-point correction since the telluric absorption lines are always at zero radial velocity (except for small shifts due to winds in the Earth's atmosphere), and the observed shift can only be caused by imperfect slit centring. Applying the zero-point radial velocity shifts reduced the errors on the orbital parameters very significantly from O-C RMS of 300 m s^{-1} to about 100 m s^{-1} . The uncertainties were, nonetheless, still underestimated. Therefore, a RV zero-point uncertainty of 100 m s^{-1}

Table 4. Radial velocity measurements of HD 27130.

BJD-TDB	RV primary (km s^{-1})	RV secondary (km s^{-1})
58 128.32814	3.15 ± 0.11	88.50 ± 0.16
58 130.45043	98.85 ± 0.11	-43.47 ± 0.12
58 131.37047	60.62 ± 0.11	9.41 ± 0.13
58 132.42615	-5.37 ± 0.11	100.26 ± 0.12
58 133.42916	-17.43 ± 0.11	116.92 ± 0.12
58 139.31208	-8.25 ± 0.11	103.97 ± 0.12
58 140.31280	52.79 ± 0.11	20.17 ± 0.13
58 140.33625	54.20 ± 0.11	17.77 ± 0.13
58 141.31295	98.25 ± 0.11	-42.65 ± 0.13
58 141.39057	99.39 ± 0.11	-43.99 ± 0.13
58 143.35926	9.85 ± 0.11	79.09 ± 0.13
58 144.33618	-21.48 ± 0.11	122.88 ± 0.12
58 144.55938	-19.20 ± 0.11	119.79 ± 0.13

was added in quadrature to the RV uncertainties in order for the binary analysis to yield a reduced χ^2 close to 1 for the RV of both components. The final radial velocity estimates are given in Table 4.

3.2. Light ratio

The light ratio between the components is an important parameter for both the spectral separation before the spectroscopic analysis and for the binary analysis of systems without a total eclipse, as is the case for HD 27130. We estimated the light ratio from an iterative procedure.

First, we identified HD 27130 in the *Gaia* colour-magnitude diagram (CMD) of the Hyades by [Lodieu et al. \(2019\)](#). We then fitted the shape of the main sequence of the Hyades with a low-order polynomial. The light ratio in the *G*-band was estimated by requiring that both components be located on this main sequence while reproducing the system photometry when combined. The colours of the components were then used to estimate the T_{eff} values of the components; guess values for T_{eff} were adjusted until bolometric corrections from the calibration of [Casagrande & VandenBerg \(2018\)](#) reproduced the component colours. These T_{eff} estimates were used to select template spectra from the library of [Coelho et al. \(2005\)](#) to fit the spectroscopic broadening functions of the separated spectra with a rotational profile. For this fit, we assumed a fixed linear limb darkening coefficient of 0.6. The ratio of the areas under the rotational profiles of the binary components corresponds to the luminosity ratio of the stars assuming that the effective temperatures are correct. The luminosity ratio is wavelength dependent, so we weighted results from the individual spectral orders in order for the averaged value to correspond to the *V*-band. This was then extended to the *Gaia G*-band by the use of Planck functions and the T_{eff} estimates. With the new *G*-band estimate of the luminosity ratio, the next iteration begins. In this iteration, the light ratio is fixed in the CMD and both components cannot be forced to be on the main sequence. We required the primary star to be on the sequence, and allowed for the secondary to deviate. It came out a bit redder than the main sequence, which is perhaps a sign of the very faint third component. In just a few iterations, we obtained $(L_2/L_1)_V = 0.127 \pm 0.015$, $T_p = 5660 \text{ K}$, and $T_s = 4235 \text{ K}$.

3.3. Spectral analysis

The separated spectra of the binary components resulting from the spectral separation procedure were adjusted according to the light ratio based on the *Gaia* CMD analysis and BF area ratios (cf. Sect. 3.2) to recover the true depths of the spectral lines. This was done to remove the continuum contribution from the other component. Specifically, for the primary star, this was achieved by multiplying the separated spectrum by a factor of $\frac{L_1+L_2}{L_1}$ followed by a subtraction of $\frac{L_2}{L_1}$. Here, L_1 and L_2 refer to the luminosities of the primary and secondary star, respectively. We used the light ratio from the *G*-band CMD solution (cf. Sect. 3.2) scaled linearly to the *V*-band. After this procedure, we estimated the S/N of the spectra as the RMS scatter in narrow wavelength-regions that were visually inspected and judged to be without spectral lines. In this way, the S/N of the separated SONG spectra were found to be roughly 150 for the primary component and 30 for the secondary at 5000 Å, increasing to 250 and 55 at 6000 Å. The corresponding numbers for the separated VUES spectra are 90 and 25 at 5000 Å, and 200 and 45 at 6000 Å.

We then performed classical equivalent width spectral analysis. This was done using two different methods – separately for the SONG and the VUES spectra. The first setup was as described in Slumstrup et al. (2019) with $\log g$ fixed to the values from the binary solution (cf. Sect. 4). This yielded $T_{\text{eff}} = 5750 \pm 107$ K and $[\text{Fe}/\text{H}] = +0.14 \pm 0.02$ from the SONG spectrum of the primary star, and $T_{\text{eff}} = 4630 \pm 202$ K and $[\text{Fe}/\text{H}] = +0.05 \pm 0.03$ from the SONG spectrum of the secondary star. The micro turbulence for the secondary was unrealistically high when unconstrained (2.30 ± 0.62). If the micro turbulence for the secondary was fixed according to, for example, the calibration of Bruntt et al. (2010), $[\text{Fe}/\text{H}]$ came out higher, and in agreement with that of the primary. Repeating the analysis for the VUES spectra gave $T_{\text{eff}} = 5650 \pm 99$ K and $[\text{Fe}/\text{H}] = +0.03 \pm 0.02$ for the primary star, while robust results were not obtained for the secondary.

In the second setup, $\log g$ was not fixed, but results converged naturally to the expected values. For the spectra from SONG (VUES), the analysis made use of 161 (164) Fe I lines and 21 (14) Fe II lines for the primary star, and 64 (87) Fe I lines and 2 (2) Fe II lines for the secondary star. This yielded $T_{\text{eff}} = 5614 \pm 40$ (5571 ± 48) K and $[\text{Fe}/\text{H}] = +0.00 \pm 0.12$ (-0.07 ± 0.10) for the primary star and $T_{\text{eff}} = 4484 \pm 51$ (4534 ± 63) K and $[\text{Fe}/\text{H}] = -0.07 \pm 0.11$ (-0.05 ± 0.10) for the secondary star, using the spectra from SONG and VUES (in brackets), respectively.

As mentioned previously, we used the *Gaia* CMD to establish a first-estimate of the luminosity ratio of HD 27130. The *Gaia* colours obtained from this exercise resulted in the first estimate T_{eff} values of 5645 K and 4420 K for the primary and secondary, respectively. For the second iteration, with the light ratio constrained from the relative spectral line strengths, the T_{eff} of the primary changed slightly to 5660 K, while that of the secondary changed more significantly. Enforcing the spectroscopic constraint on the luminosity ratio, the secondary is no longer on the main-sequence if the colours are to be matched. In this case, the secondary T_{eff} becomes 4235 K, while it is 4310 K if we just choose the point on the main sequence giving the correct light ratio in *Gaia G*-band, but not for the G_{RP} -band.

From all the different spectroscopic T_{eff} estimates and the corresponding photometric measurements, we adopt 5650 ± 50 K and 4300 ± 100 K as our best estimates of the effective temperatures. For the secondary this T_{eff} is somewhat lower than all our spectroscopic estimates above. However, the S/N is very low

for the spectra of the secondary star, and the procedure to re-establish the true line-depths of the faint component of a spectroscopic binary is very sensitive to uncertainties in the adopted light ratio. Therefore, we put more reliance on the photometric measurements. Our after the fact comparison using the *Gaia* parallax in Sect. 4 supports this choice, with an agreement that is within 40 K.

The $[\text{Fe}/\text{H}]$ values that we obtained are generally below the current best estimates of the metallicity of the Hyades, for example, $+0.15$ (Arentoft et al. 2019). We suspect that this is due to systematic effects arising from the spectral separation and light ratio correction procedures on these relatively low S/N spectra, especially for the secondary star.

4. Eclipsing binary analysis

To determine model independent stellar parameters, we used the JKTEBOP⁴ eclipsing binary code (Southworth et al. 2004) which is based on the EBOP program developed by P. Etzel (Etzel 1981; Popper & Etzel 1981). We made use of non-linear limb darkening (Southworth et al. 2007) and a simultaneous fitting of the light curve and the measured radial velocities (Southworth 2013).

As seen in Fig. 1, the light curves of HD 27130 display small variations outside the eclipses that are likely due to spot activity. Consequently, the magnitude level is different just before and after the primary eclipse compared to just before and after the secondary eclipse. To minimise this effect in the binary analysis, we only kept the parts of the light curves that are very close to or in eclipse. We adjusted the light curves on individual night basis such that the mean magnitude of observations taken outside eclipse aligned. We did not use the *B*-band light curve because we did not succeed in obtaining coverage of the secondary eclipse.

For the other three filters separately, we fitted for the following parameters: orbital period P , time of first primary eclipse T_0 , central surface brightness ratio J , sum of the relative radii $r_1 + r_2$, ratio of the radii $k = \frac{r_2}{r_1}$, orbit inclination i , $e \cos \omega$, $e \sin \omega$, semi-amplitudes of the components K_1 and K_2 and system velocity of the components γ_1 and γ_2 . We allowed for two system velocities because the components and their analysis could be affected differently by gravitational redshift and convective blueshift (Gray 2009) effects. As it turns out, they appear not to be.

We used a quadratic limb darkening law with coefficients calculated using JKTLTD (Southworth 2015) with tabulations for the *V* and *I* bandpasses by Claret (2000). We ran JKTEBOP iteratively, starting with limb darkening coefficients from first guesses based on the *Gaia* CMD analysis of HD 27130 and then using T_{eff} values from the spectral analysis. New limb darkening coefficients were then calculated with JKTLTD using these T_{eff} and $\log g$ values from the solution in the next JKTEBOP iteration.

Gravity darkening coefficients were taken from Claret & Bloemen (2011), although even very large changes to these numbers had negligible effects as expected for nearly spherical stars. The same is true for reflection effects, which were set to zero due to our pre-analysis adjustment of the out-of-eclipse magnitude level.

As is usually the case for eclipsing binary stars without a total eclipse, k , the ratio of the radii was poorly constrained by the light curve. We ran tests with k fixed to different values

⁴ <https://www.astro.keele.ac.uk/~jkt/codes/jktebop.html>

Table 5. Binary solutions for HD 27130.

Parameter	V	MASCARA	I_C
Constraints:			
L_s/L_p	0.127(15)	0.128(15)	–
$k = (r_s/r_p)$	–	–	0.7962 ^(*)
P (days)	5.609217(7)	5.609209(5)	5.609233(6)
Inclination i	85.830(54)	85.495(112)	85.640(19)
$k = r_s/r_p$	0.790(27)	0.815(47)	0.7962 ^(*)
$r_s + r_p$	0.1008(7)	0.1053(17)	0.1043(4)
J_s/J_p	0.2374(48)	0.2148(121)	0.4180(52)
L_s/L_p	0.133(15)	0.129(15)	0.248
σ (mmag)	8.38	14.88	9.23
K_p (km s ^{−1})	60.705(41)	60.702(41)	60.702(41)
K_s (km s ^{−1})	83.754(47)	83.750(47)	83.751(47)
γ_p (km s ^{−1})	39.049(31)	39.039(31)	39.040(31)
γ_s (km s ^{−1})	39.041(36)	39.052(36)	39.052(36)
e	0.0013	0.0013	0.0013
ω	15.47	1.38	1.98
a (R_\odot)	16.05	16.06	16.06
M_p (M_\odot)	1.0239	1.0251	1.0246
M_s (M_\odot)	0.7421	0.7430	0.7426
R_p (R_\odot)	0.9033	0.9317	0.9330
R_s (R_\odot)	0.7139	0.7597	0.7429

Notes. ^(*)The value was fixed.

and found that a very large range of k values produced almost equally good solutions. Therefore, without an external constraint on k , the derived stellar parameters are too uncertain to be useful. This suggests that Schiller & Milone (1987) were too optimistic when estimating uncertainties in their light curve analysis. To circumvent this problem, we added the light ratio $(L_2/L_1)_V = 0.127 \pm 0.015$ as an external constraint in JKTEBOP. This light ratio was derived using the separated spectra and the *Gaia* CMD (cf. Sect 3.2). Using Planck functions, we also determined and employed the corresponding light ratio for the MASCARA filter, which is very close to the V -band, since these filters have nearly the same effective wavelength despite the MASCARA filter being much broader. For the I_C -band we proceeded differently, since I -filter transmissions are not so similar. We derived the k values for the other filters first and then fixed the k value in the I_C -band solution to the weighted mean from the other two filters.

The JKTEBOP solutions are given in Table 5 and compared to the observed light curves and measured radial velocities in Fig. 3. To estimate uncertainties, we used the residual-permutation uncertainty estimation method of JKTEBOP, which estimates parameter uncertainties while accounting for correlated noise. The 3σ ranges of these parameter distributions correspond roughly to the filter-to-filter solution differences and we therefore adopted these as our final 1σ uncertainties. This inflation of internal errors seems justified by the comparison of V -band and MASCARA light curve solutions in the middle panel of Fig. 3; both limb darkening coefficients and light ratios are very close to identical for these two filters. Therefore, the difference in model eclipse depth is related to a combination of measurement errors and improper rectification of the light curves, time-variable spot patterns on the stars, and potential blended light from other sources in the MASCARA light curve –

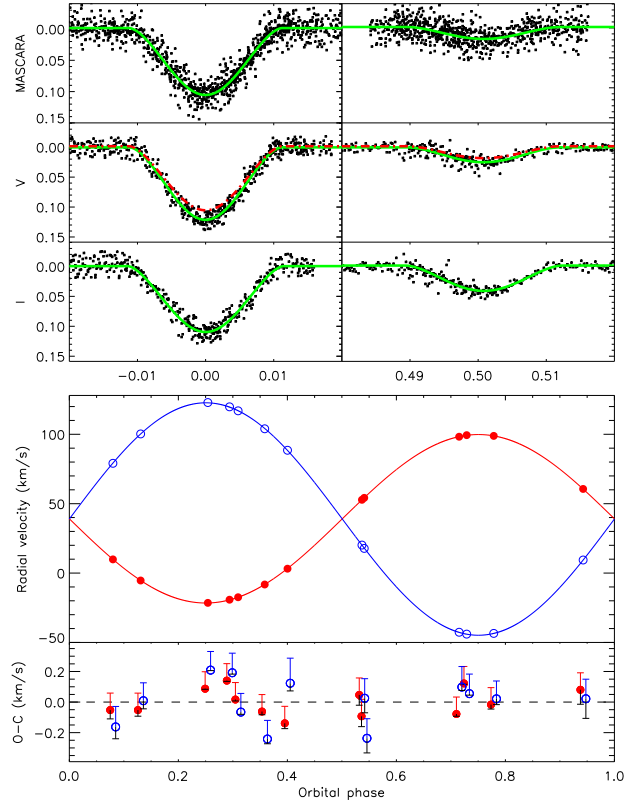


Fig. 3. Light curves and radial velocity measurements of HD27130 compared to eclipsing binary models. *Upper panels:* phased light curves showing relative magnitude in MASCARA V and I filters at phases at or close to eclipse. Green lines are the best model for the given filter. In the V -band panel, the red dashed line is the best model using the MASCARA light curve. *Bottom panels:* radial velocity measurements of the HD 27130 components from SONG spectra. Red indicates the primary component and blue is the secondary. In the O–C panel, the measurements of the primary and secondary component are shifted by ± 0.005 , respectively, in phase for clarity. We note that the upwards-pointing error bar gives the measurement error, while the downwards-pointing error bar indicates the maximum difference between models based on different light curves.

neither of which is accounted for by the internal errors. A flat mean of the three different filter solutions were used as the best parameter estimate.

We did not attempt to derive a precise V -band system magnitude for HD 27130 from our photometry since it was obtained with relative photometry in mind and not absolute. Instead, We estimated the apparent magnitude of the binary components by correcting the HD 27130 system photometry in the V -band by Kharchenko (2001) according to our spectroscopically measured V -band light ratio of 0.127. We then calculated the luminosity of the components from their radii and T_{eff} and used Eq. (10) of Torres (2010) generalised to an arbitrary filter X to calculate their absolute component magnitudes:

$$M_X = -2.5 \log \left(\frac{L}{L_\odot} \right) + V_\odot + 31.572 - (BC_X - BC_{V,\odot}). \quad (1)$$

Here, $V_\odot = -26.76$ as recommended by Torres (2010) and $BC_{V,\odot} = -0.068$ as obtained from the calibration of Casagrande & Vandenberg (2014). Bolometric corrections were calculated from the calibration of Casagrande & Vandenberg (2014).

Table 6. Properties of HD 27130.

IDs	HD 27130, vB 22, V818 Tau
α_{J2000}	04 17 38.946
δ_{J2000}	+16 56 52.21
G_{TOT}	8.098
V_{TOT}	8.315 ¹
$T_p(K)$	5650(50)
$T_s(K)$	4300(100)
$M_p(M_\odot)$	1.0245(24)
$M_s(M_\odot)$	0.7426(16)
$R_p(R_\odot)$	0.9226(150)
$R_s(R_\odot)$	0.7388(260)
V_p	8.445(14)
V_s	10.685(210)
$BC_{V,p}$	-0.080
$BC_{V,s}$	-0.746
Parallax, <i>Gaia</i> DR2 (mas)	21.399(69)
Parallax, derived, primary (mas)	21.38
Parallax, derived, secondary (mas)	22.33

Notes. Adopted from [Kharchenko \(2001\)](#).

With an assumed zero interstellar reddening and absorption, we then calculated a predicted parallax for the components from the V-band magnitudes:

$$\pi = 10^{\left(\frac{M_V - V - 5}{5}\right)}. \quad (2)$$

The predicted parallaxes are given in Table 6 along with the *Gaia* DR2 parallax ([Gaia Collaboration 2018](#)). As seen, they are in excellent agreement; a T_{eff} decrease of less than 10 K would be enough to obtain exact agreement for the primary. Even for the secondary, which is more sensitive to the assumed light ratio, a T_{eff} increase of less than 40 K is needed for exact agreement with the *Gaia* DR2 parallax. Given the relatively large parallax of the Hyades, the systematic parallax offset of the order of 0.05 mas in *Gaia* DR2 that has been investigated quite extensively by now (e.g. [Brogaard et al. 2018a](#), and references therein, [Khan et al. 2019](#)) is impossible to address. The distance to HD 27130 is thus 46.5 pc as calculated from the binary parameters, very close to the 46.7 pc implied by the *Gaia* DR2 parallax. The final parameters and their uncertainties for HD 27130 are given in Table 6. The masses are in agreement, within the uncertainties, with what was obtained from spectroscopy by [Griffin \(2012\)](#).

Our velocity semi-amplitudes, $K_p = 60.703(41) \text{ km s}^{-1}$ and $K_s = 83.752(47) \text{ km s}^{-1}$ are much more precise, but still in reasonable agreement with those derived by [Griffin \(2012\)](#), $K_p = 60.87(6) \text{ km s}^{-1}$ and $K_s = 84.09(49) \text{ km s}^{-1}$. Our mass estimates are also seen to be in good agreement with the masses given in Table 17 of [Griffin \(2012\)](#), which are just very slightly larger than ours. Given that all other mass estimates we have been able to find in the literature are even larger, our mass estimates are lower than any previous estimates. We ascribe this to the effects of the third component, which was extensively discussed by [Griffin \(2012\)](#), but not properly accounted for in other studies.

5. Re-evaluation of the properties of ϵ Tau

In order to get a tight age constraint on the Hyades age, we need a more evolved star than the components of HD 27130. Thus, we turned our attention to the giant Hyades member ϵ Tau

Table 7. Properties of ϵ Tau.

IDs	HD 28305, ϵ Tau
α_{J2000}	04 28 36.999
δ_{J2000}	+19 10 49.54
V (mag)	3.53
$T_{\text{eff}}(K)$	4950 ± 22 (*)
BC_V (mag)	-0.257
$\nu_{\text{max}}(\mu\text{Hz})$	56.4 ± 1.1 (*)
$\Delta\nu(\mu\text{Hz})$	5.00 ± 0.01 (*)
θ_{LD} (mas)	2.493 ± 0.019 (*)
Parallax, <i>Gaia</i> DR2 (mas)	20.31 ± 0.43
Parallax, HIPPARCOS (mas)	22.24 ± 0.25
Asteroseismic parameters constrained by exact HIPPARCOS π , Arentoft et al. (2019) :	
$M(M_\odot)$	2.458 ± 0.072 (*)
$R(R_\odot)$	12.06 ± 0.16 (*)
Asteroseismic parameters constrained by HIPPARCOS π , This work:	
$\nu_{\text{max}}(\mu\text{Hz})$	55.3
$M(M_\odot)$	2.458
$R(R_\odot)$	12.17
Parallax, derived (mas)	22.03
Asteroseismic parameters NOT constrained by HIPPARCOS π , This work:	
$M(M_\odot)$	2.607
$R(R_\odot)$	12.42
Parallax, derived (mas)	21.60

Notes. (*) Derived by [Arentoft et al. \(2019\)](#).

(HD 28305). The physical properties of ϵ Tau were measured by [Arentoft et al. \(2019\)](#) from a combination of their own asteroseismic, interferometric, and spectroscopic measurements, coupled to photometric observations and the parallax measurement from HIPPARCOS data ([van Leeuwen 2007](#)). They obtained a radius of $R = 12.06 \pm 0.16 R_\odot$ and mass of $M = 2.458 \pm 0.072 M_\odot$ using a method that empirically determines also the correction needed for the asteroseismic scaling relations. However, as mentioned by [Arentoft et al. \(2019\)](#), that solution suggests that ϵ Tau is an RGB star, in conflict with timescales of the secondary clump (RC2) compared to the RGB, the CMD position, and even a neural network evaluation of the oscillation power spectrum. Therefore, we consider properties that were obtained instead by using a model-predicted correction to the asteroseismic scaling relation assuming that ϵ Tau is in the RC2 phase of evolution. Using this approach, we obtained $R = 12.42 R_\odot$ and mass of $M = 2.607 M_\odot$ for a self-consistent model-predicted correction $f_{\Delta\nu} = 1.005$ from the figures of [Rodrigues et al. \(2017\)](#) and corresponding unpublished ones showing the correction as a function of ν_{max} (priv. comm. A. Miglio, see Appendix A.1). This solution requires a parallax of $\pi = 21.60$ mas for an exact match between the asteroseismic and interferometric radius, 2.56σ away from the HIPPARCOS measurement of 22.24 ± 0.25 mas. However, if using the $1 - \sigma$ lower boundary value for ν_{max} , the parallax increases to $\pi = 22.03$ mas, just within the $1 - \sigma$ lower boundary of the HIPPARCOS parallax. The values of radius and mass for this solution are $R = 12.17 R_\odot$ and mass of $M = 2.458 M_\odot$, close to those of [Arentoft et al. \(2019\)](#). This solution seems to be the one that best agrees with all observations. We summarise the parameters of ϵ Tau in Table 7.

Both Schröder et al. (2020) and Gray & Martinez (2019) find significantly larger radii for ϵ Tau and the other three well-known Hyades giants. Gray & Martinez (2019) do so while noting that for the four Hyades giants, the HIPPARCOS and *Gaia* DR2 parallaxes have “disquieting differences of about 10%”, which can also be seen in Table 7. In addition, even the relative star-to-star differences are inconsistent. The fact that the *Gaia* DR2 parallax of ϵ Tau is 20.31 ± 0.43 mas, many σ away from the HIPPARCOS value calls for a reconsideration of the physical properties in the future, when we have better estimations of the *Gaia* parallaxes of bright stars. Part of the larger radii found by both Schröder et al. (2020) and Gray & Martinez (2019) is, however, not related to the parallax but, rather, that they use bolometric corrections (BCs) that are quite different from the ones we adopt from Casagrande & VandenBerg (2014). For instance, Schröder et al. (2020) adopts a BC_V of -0.5 mag, also remarking the consequences for radius and mass given a BC of -0.4 mag. Gray & Martinez (2019) do not mention the source or value of the BCs they use, but reversing their calculations of the radii under the assumption that $BC_{V,\odot} = -0.068$ (Casagrande & VandenBerg 2014), we found that they used $BC_V = -0.39$ for ϵ Tau (and δ Tau, and $BC_V = -0.36$ for the other two giants).

The value we use for ϵ Tau, corresponding to $T_{\text{eff}} = 4950$ K and $\log g = 2.7$ from Casagrande & VandenBerg (2014) is $BC_V = -0.257$. By comparing the physical radius obtained from interferometry to the physical radius obtained from the spectroscopic T_{eff} and V-band magnitude for the same parallax value, the validity of the bolometric correction can be tested. In doing this, we confirmed the excellent agreement for our value of $BC_V = -0.257$ that was also established in Arentoft et al. (2019); the two radius estimates agree within 0.2%. Using instead the bolometric corrections suggested by Schröder et al. (2020) or Gray & Martinez (2019), the radii become 12% or 7% larger than the interferometric radius. This disagreement remains regardless of which parallax is adopted, suggesting that the BC_V of Casagrande & VandenBerg (2014) is the more accurate one.

6. Stellar models and isochrone comparisons

We used Victoria models (VandenBerg et al. 2014), PARSEC models (Bressan et al. 2012), and two different MESA model grids (Paxton et al. 2011, 2018). The Victoria models assume the Asplund et al. (2009) solar abundances, scaled to different [Fe/H] values. Choi et al. (2016) find that an initial $Z = 0.015$ and $Y = 0.261$ are reduced to the Asplund Z and Y consistent with asteroseismology when diffusion acts for the solar age (4.57 Gyr). For the Victoria models generated here:

[Fe/H] = 0.10, $Y = 0.27$, $Z = 0.0163$;

[Fe/H] = 0.10, $Y = 0.30$, $Z = 0.0155$;

[Fe/H] = 0.15, $Y = 0.27$, $Z = 0.0182$;

we might expect that the Hyades would have Y fairly close to 0.27 if it has [Fe/H] between 0.10 and 0.15 suggested by spectroscopic investigations (Victoria models do not include diffusion of metals, only settling of helium, but at an age of <1 Gyr, the effects of metals diffusion will be minimal.) The PARSEC model are those of Bressan et al. (2012) with revised and calibrated surface boundary conditions in low-mass dwarfs described by Chen et al. (2014).

We use two different versions of the MESA models, which both include diffusion of helium and metals; The MIST models (Dotter 2016; Choi et al. 2016) that assume the Asplund et al. (2009) solar abundances and those from a specific grid of Miglio

et al. (2020) that assume Grevesse & Noels (1993) solar abundances. The latter models are as described in Rodrigues et al. (2017), except that they include diffusion.

6.1. Model comparisons to HD 27130

Figure 4 shows the Mass-Radius and Mass- T_{eff} diagrams of the HD 27130 components compared to selected isochrones. The primary component matches most of the isochrones well; In the mass-radius diagram, all isochrones except the one assuming a very high helium content agree well within 1σ . In the Mass- T_{eff} diagram, both the high helium and lower metallicity Victoria isochrones and the PARSEC isochrone are hotter than the HD 27130 primary. The secondary is larger and cooler than all the isochrones. For comparison, we also show the measurement by Torres & Ribas (2002). They also found the secondary to be larger and cooler than the isochrones, but their estimates for the primary also does not match the isochrones shown.

At the mass range spanned by the components of HD 27130, the isochrones have no significant dependence on age. Therefore, the measurements of HD 27130 can be used to make predictions about the helium content of the Hyades by adopting a measured [Fe/H] for the cluster. We disregard the secondary component, since it is larger and cooler than all the isochrones regardless of the composition. This is likely related to inflation caused by magnetic fields, as suggested for other binary components of similar mass in the literature (e.g. Sandquist et al. 2016). The PARSEC isochrones are corrected empirically to match the lower main-sequences of open and globular clusters (Chen et al. 2014). This can be seen in both panels of Fig. 4, where the PARSEC isochrones bend slightly at a mass very close to the mass of the HD 27130 secondary. However, the effect is too insignificant to make a difference, which is in accord with the findings of Chen et al. (2014) that the effects are very small at this mass. Thus, the inflated radius and decreased T_{eff} of the HD 27130 secondary relative to isochrone predictions are likely caused by an increased magnetic activity relative to single low mass stars.

Comparing the position of the primary to the Victoria isochrones, we estimate $Y = 0.274 \pm 0.017$ from the Mass-Radius diagram and $Y = 0.267 \pm 0.006$ from the Mass- T_{eff} diagram at [Fe/H] = +0.15. $Y = 0.27$ implies a helium enrichment law close to $\frac{\Delta Y}{\Delta Z} = 1.2$ when calculated from a primordial value of $Y = 0.248$. This is in agreement with $\frac{\Delta Y}{\Delta Z} = 1.4 \pm 0.1$ estimated for the open cluster NGC6791 by Brogaard et al. (2012) through analysis of eclipsing members. It thus appears that the helium enrichment of the Hyades is similar to other open clusters.

The MIST models, which also assume the Asplund et al. (2009) solar abundances, suggest very close to the same helium content, $Y = 0.274$ from the Mass-Radius diagram but $Y = 0.277$ from the Mass- T_{eff} diagram. This illustrates that different assumptions about model physics contributes at least 0.005 the uncertainty in Y when determined from the Mass-Radius and Mass- T_{eff} diagrams.

The PARSEC models assume another solar abundance reference (Caffau et al. 2011). They suggest $Y = 0.285$ from the Mass-Radius diagram but $Y = 0.277$ from the Mass- T_{eff} diagram. A higher [Fe/H] is needed in order for these isochrones to yield a consistent value for Y . Therefore, although these models suggest a larger helium content, the predicted helium enrichment law will be similar, because of the corresponding larger Z value.

The lower helium content of $Y = 0.255$ derived by Lebreton et al. (2001) from HD27130 was likely an artifact mostly resulting from the previous mass overestimate due to the unseen third component.

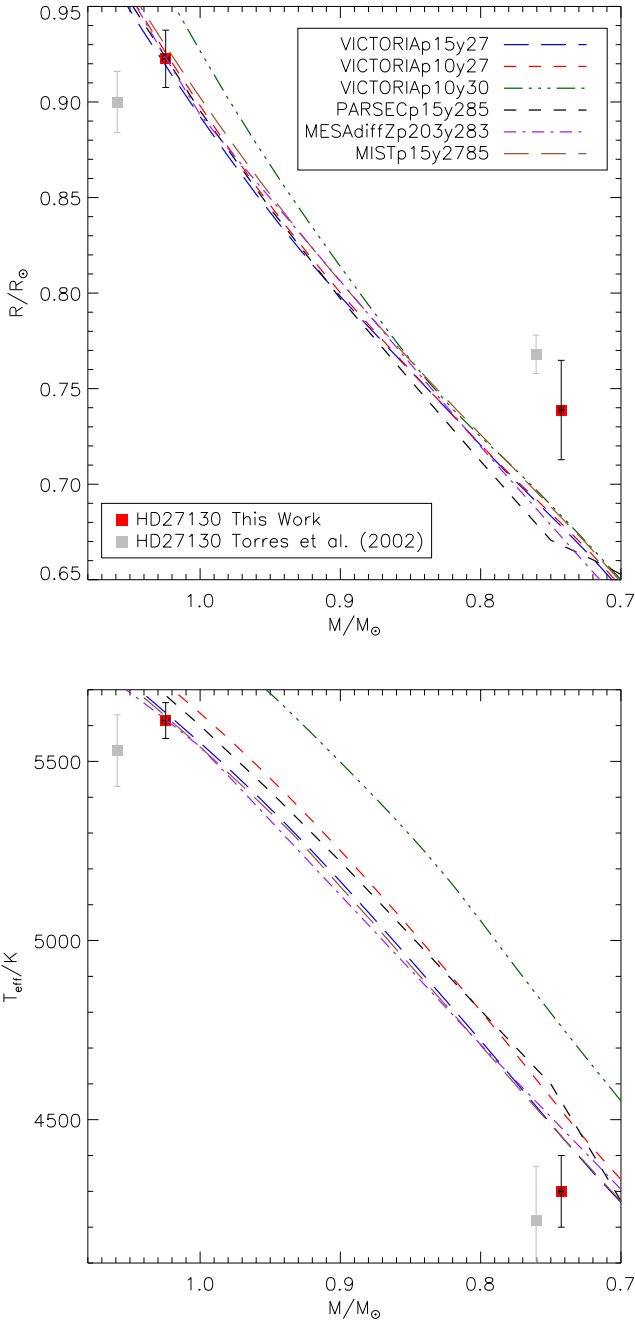


Fig. 4. Mass-radius (*upper panel*) and Mass- T_{eff} (*lower panel*) diagrams comparing the components of HD 27130 to isochrones from different model sets and different compositions. Notation is such that e.g. p15y27 means $[\text{Fe}/\text{H}] = +0.15$ and $Y = 0.27$. The red squares are the measurement from this work, while the gray squares are the corresponding values from Torres & Ribas (2002).

6.2. Model comparisons to ϵ Tau

With the helium content constrained by the primary component of HD 27130, we can constrain the age of the Hyades using an evolved star. We made use of the secondary clump star member ϵ Tau with properties determined by Arentoft et al. (2019) as re-evaluated in the present paper. Since our best estimates of the mass and radius were very close to those of Arentoft et al. (2019), we used their measured values in Fig. 5, where we compare to some of the same isochrones as in Fig. 4. As seen in the upper panel, an age close to 0.8 Gyr is compatible with the

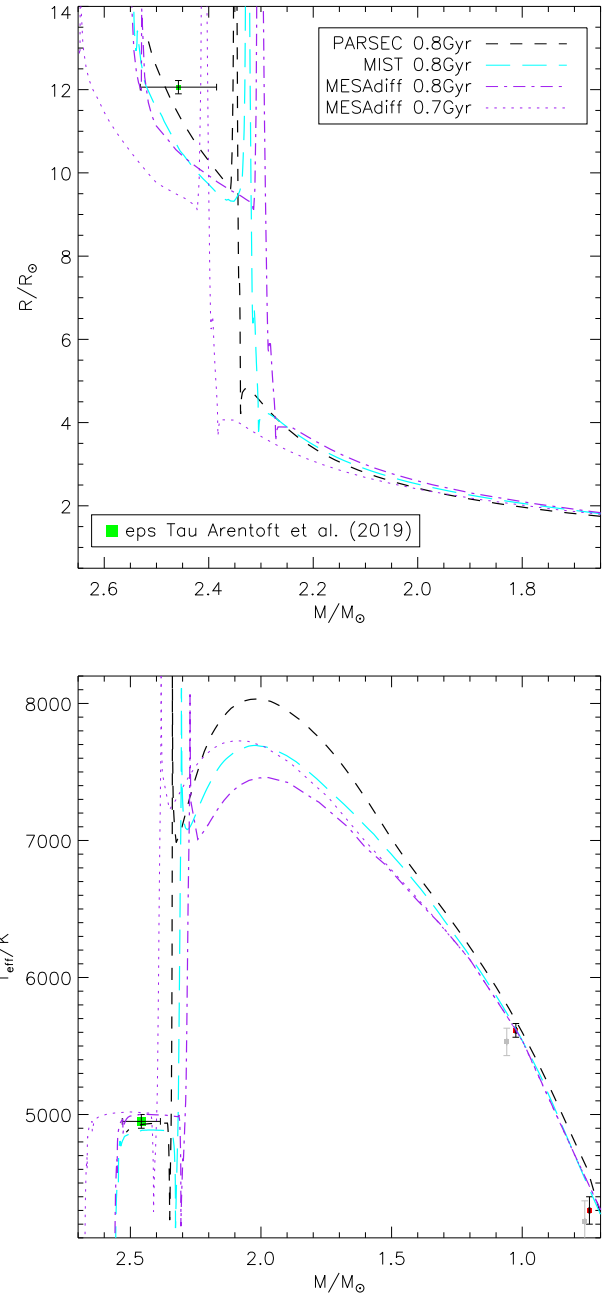


Fig. 5. Mass-radius (*upper panel*) and Mass- T_{eff} (*lower panel*) diagrams comparing the asteroseismic measurements of ϵ Tau to isochrones from different models and different compositions. The green square is the measurement of ϵ Tau from Arentoft et al. (2019). The red squares are the measurements of HD 27130 from this work, while the gray squares are the corresponding values from Torres & Ribas (2002).

observations if ϵ Tau is in the secondary clump phase, as the evidence strongly suggests.

The age needed for an exact match at the measured mass of ϵ Tau is 0.90 Gyr for the MESA isochrones and 0.83 Gyr for the PARSEC isochrone (the Victoria models were not extended to the core He-burning phase.). The extent of the $1 - \sigma$ uncertainty in mass can be seen to correspond to a 0.1 Gyr $1 - \sigma$ uncertainty in age. It is also worth noting that due to the mass-radius correlation in the asteroseismic estimates, the best age estimates are younger by only about 0.1 Gyr if we adopt our alternative mass and radius estimates of ϵ Tau that was not consistent with the HIPPARCOS distance.

The lower panel of Fig. 5 compares ϵ Tau to the same models in the mass- T_{eff} diagram. The effective temperatures of all models are within or just outside the $1-\sigma$ uncertainty in T_{eff} although different models show differences of more than 100 K for the same age. Unfortunately, the model T_{eff} of evolved stars is sensitive to e.g. the calibration of the mixing length parameter, adopted surface boundary conditions, the detailed abundance pattern, and convective overshooting. Therefore, it makes little sense to attempt to force a finer match within the level of the $1-\sigma$ error-bar. While all of the many spectroscopic investigations of the Hyades giants have found their T_{eff} to be below 5000 K, some of the mentioned model assumptions may be responsible for the model reaching such high T_{eff} . The two isochrones with identical assumptions except the age clearly demonstrate that the T_{eff} of ϵ Tau is insensitive to the assumed age. Instead, the good level of agreement show that these stellar models self-consistently predict the correct T_{eff} of the secondary clump (ϵ Tau) within errors if constrained to do so at the unevolved part of the main-sequence (HD 27130).

6.3. Mass-luminosity and Gaia CMD analysis

Figure 6 reproduces the Mass- M_V diagram of Torres (2019), along with the addition of our measurements of HD27130 and the measurements of ϵ Tau by Arentoft et al. (2019). Some of the isochrones from previous figures are also shown for comparison. Although the positions of the HD 27130 components in this diagram have changed with our measurements relative to those of Torres & Ribas (2002), they have shifted along the isochrone in such a way that the same isochrone would be preferred from either set of measurements. The measurements of ϵ Tau also falls nicely along the model predictions.

In the upper panel of Fig. 7, we compare the same models as in Fig. 5 to the *Gaia* CMD of selected *Gaia* members from Lodieu et al. (2019). The M_G magnitudes have been obtained by adjusting the G magnitudes according to their parallax. The four giants have been marked individually. θ_1 Tau was added, since it was not selected as a member by Lodieu et al. (2019).

As seen, the upper main sequence and turn-off of these models are quite different even though they predict a very similar mass for ϵ Tau. However, unfortunately, the upper main sequence close to the terminal age main sequence (TAMS) is very poorly defined, and the measurements refer to merely one subgiant star. Without further investigation, it would not be justified to demand that the isochrones need to match this one star. The star marked with a blue diamond is θ_2 Tau, a known binary where two stars contribute to the combined light, which demonstrates that isochrones should not match this point. Further investigations of the stars close to the TAMS would be needed if tight isochrone constraints are to be obtained from this *Gaia* CMD. However, it does appear that the PARSEC models are too blue as they fail to match the upper main-sequence stars of the Hyades, which is consistent with the isochrones being too hot compared to the HD 27130 primary in Fig. 5. The 0.8 Gyr MESA isochrone is somewhat too red before it bends back to the blue at the end of the core H-burning phase.

The lower panel of Fig. 7 shows only the four giants in the CMD. Squares mark their CMD positions if using the *Gaia* DR2 parallaxes, while circles indicate their positions if HIPPARCOS parallaxes are used. As seen, it makes a very significant difference if one or the other measures of parallaxes are used. On top of this, the T_{eff} differences among the four giants implied by the relative $G_{BP} - G_{RP}$ colours amount to a range of 218 K, while relative spectroscopic studies suggest a much smaller T_{eff} range of

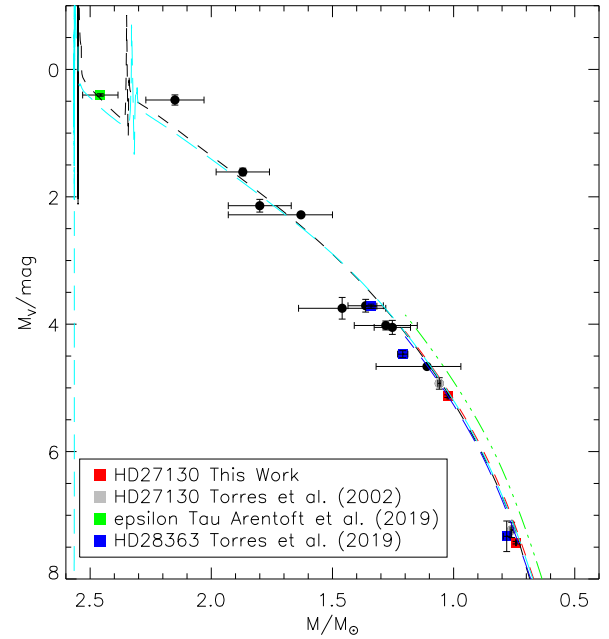


Fig. 6. Mass- M_V diagram comparing the components of HD 27130 to isochrones from different model sets and different compositions. The red squares are the measurement from this work. The gray squares are the corresponding values from Torres & Ribas (2002) according to Torres (2019) (we were unable to recover those numbers in Torres & Ribas 2002). Blue squares are measurements of the triple HD 28263 by Torres et al. (2019). Black circles are measurements of additional binary stars belonging to the Hyades, measured by different authors and presented by Torres et al. (2019), Torres (2019). The green square is the asteroseismic measurements of ϵ Tau by Arentoft et al. (2019). Isochrones are a selected subset of those given in the legend of Fig. 4. Those covering the full mass range are both of age 800 Myr. The Victoria models are only calculated for low masses where the isochrone shape is not significantly affected by age.

only 50 K or less (Gray & Martinez 2019; Schröder et al. 2020). $B - V$ colour differences suggest a range of 130 K among the giants.

This leads to substantial complications in trying to compare the Hyades giants to *Gaia* CMD observations. If, however, these four giants all belong to the secondary clump (as suggested by evolutionary timescales, their similar spectroscopic T_{eff} , and the asteroseismic analysis of mixed modes (Bedding et al. 2011; Arentoft et al. 2017, 2019) in ϵ Tau), then the lower panel of Fig. 7 implies that the HIPPARCOS parallaxes are the correct ones. The *Gaia* DR2 parallaxes simply position the giants too far away from each other in both colour and magnitude for them to be matched by the secondary clump phase of any isochrone. We checked that applying the *Gaia* saturation effect corrections in Appendix B of Evans et al. (2018) does not affect this conclusion in any significant way. Applying these corrections changes the magnitudes of all four giants by close to identical amounts, which is not surprising since their magnitudes are similar. The G -mags change by very close to +0.11 mag for all four stars, moving them closer to the isochrone predictions for the clump phase. The $G_{BP} - G_{RP}$ colours change by less than 0.01 mag for each star, but in such a way that the colour-range covered by the stars decreases by 0.016 mag corresponding to a reduction in the photometric T_{eff} range by 38 K to 180 K, which is still very large. Therefore, if saturation effects are at play, we suspect that random star-to-star saturation variations are significant. We did not apply saturation corrections in Fig. 7.

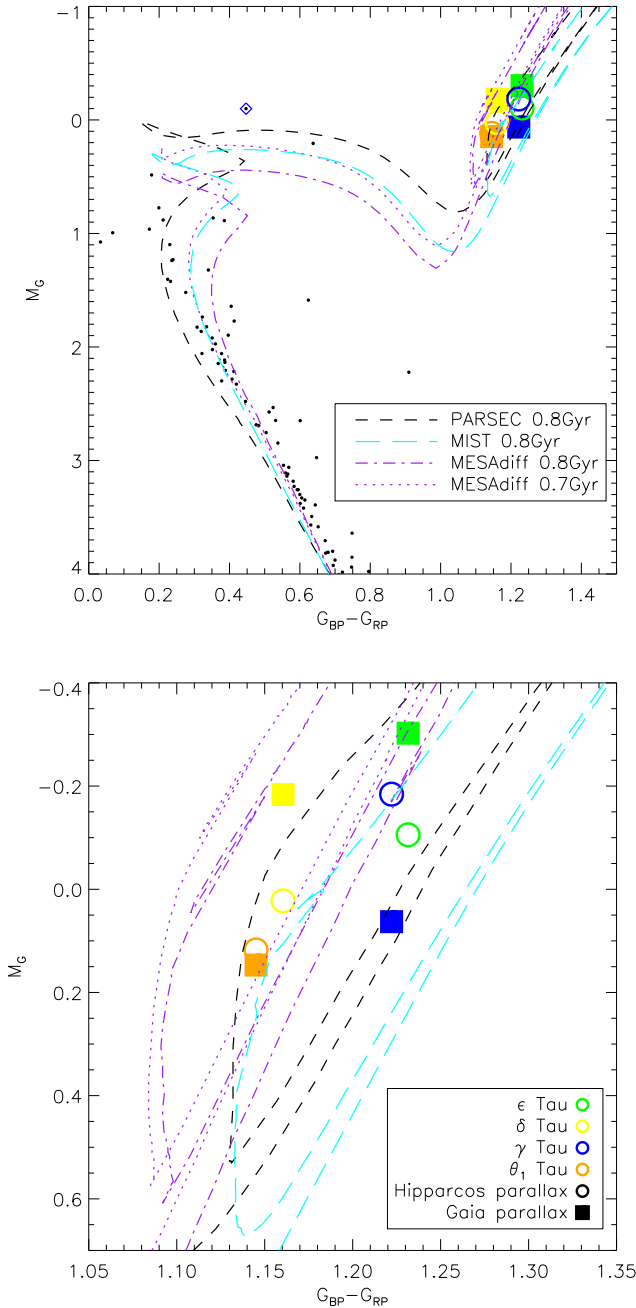


Fig. 7. *Upper panel:* Gaia colour-magnitude diagram of the Hyades with members from Lodieu et al. (2019) compared to isochrones with the same ages as in Fig. 5 and compositions as in Fig. 4. *Lower panel:* zoom on the giant part of the same colour-magnitude diagram. The positions of the four well-known Hyades giants are marked. Circles indicate their positions when adopting the HIPPARCOS parallaxes. Squares mark the corresponding positions if adopting the Gaia parallaxes.

6.4. Comparisons to other cluster age estimates.

Our investigations above suggest that the age of the Hyades is 0.9 ± 0.1 (stat) ± 0.1 (sys) Gyr. This age estimate is significantly larger than the 588 ± 60 Myr found by Schröder et al. (2020). Part of the age difference (60 Myr) is explained by differences in the bolometric corrections as discussed above and in Schröder et al. (2020). Thus, in light of our investigation of the bolometric corrections for the Hyades giants, the best age estimate from Schröder et al. (2020) is instead 648 ± 60 Myr. This is still younger than our age estimate.

The age of the Hyades derived in this work is also larger than the white dwarf (WD) cooling age of 640^{+67}_{-49} Myr found by El-Badry et al. (2018). However, we believe that their younger age could be partly due to their assumption of solar composition for the calculation of the pre-WD evolution time, and perhaps also the assumption of solar composition in the derivation of the initial-final mass relation (IFMR). Salaris & Bedin (2018) derive the IFMR for the Hyades by assuming an age of 800 Myr, which is closer to the age that we found. This IFMR is not very different from the one by El-Badry et al. (2018) for the lower-mass WDs, but deviates for the higher-mass WDs. This indicates that perhaps the slight age discrepancy arises due to inaccuracies in the model treatment of convective core overshooting, which affects the pre-WD age, and thus the initial masses.

7. Summary, conclusions, and outlook

We used new observations to establish the physical properties of the components of the eclipsing Hyades member HD 27130 as given in Table 6. The properties of the primary component were used to constrain the helium content, which we found to be $Y = 0.27$, corresponding to a helium enrichment law close to $\frac{\Delta Y}{\Delta Z} = 1.2$.

The properties of ϵ Tau were re-analysed, finding that the mass and radius established by Arentoft et al. (2019) seem robust. A higher mass is only likely if the HIPPARCOS parallax of ϵ Tau is too large by 2.56σ . We estimated the age of the Hyades to be 0.9 ± 0.1 (stat) ± 0.1 (sys) Gyr in slight tension with recent age estimates based on the cluster white dwarfs and based on the Hyades giants, but without asteroseismic constraints.

The age precision can be much improved through asteroseismic investigations of the other three Hyades giants in a similar fashion as was done for ϵ Tau by Arentoft et al. (2019). That would reduce the random error on the age, and help assessing the accuracy of the HIPPARCOS parallaxes of the Hyades giants. Potential future improvements to the Gaia parallax of bright stars would also help clarify the situation. Only then the age of the Hyades can be accurately established and used to investigate convective core overshoot through its effects on the turn-off morphology, the mass of the helium-burning giants, and the WD cooling sequence. We have taken the first steps down this path by providing constraints on the helium content from HD 27130 and investigating the constraints on the mass of the giant ϵ Tau.

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Note added in proof. The Gaia EDR3 catalogue (Gaia Collaboration 2020) was released during the proof stage of this publication. The Gaia EDR3 parallax value for ϵ Tau is 22.37 ± 0.17 , close to the HIPPARCOS value.

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Appendix A: Theoretical corrections to the asteroseismic scaling relations.

For reference, here we include the theoretical corrections to $\Delta\nu$ in the asteroseismic scaling relations that we used. These originate from the work of [Rodrigues et al. \(2017\)](#), which however only shows the correction as a function of T_{eff} . We also include the corresponding diagrams for the $\Delta\nu$ correction as a function of ν_{max} (A. Miglio, priv. comm.).

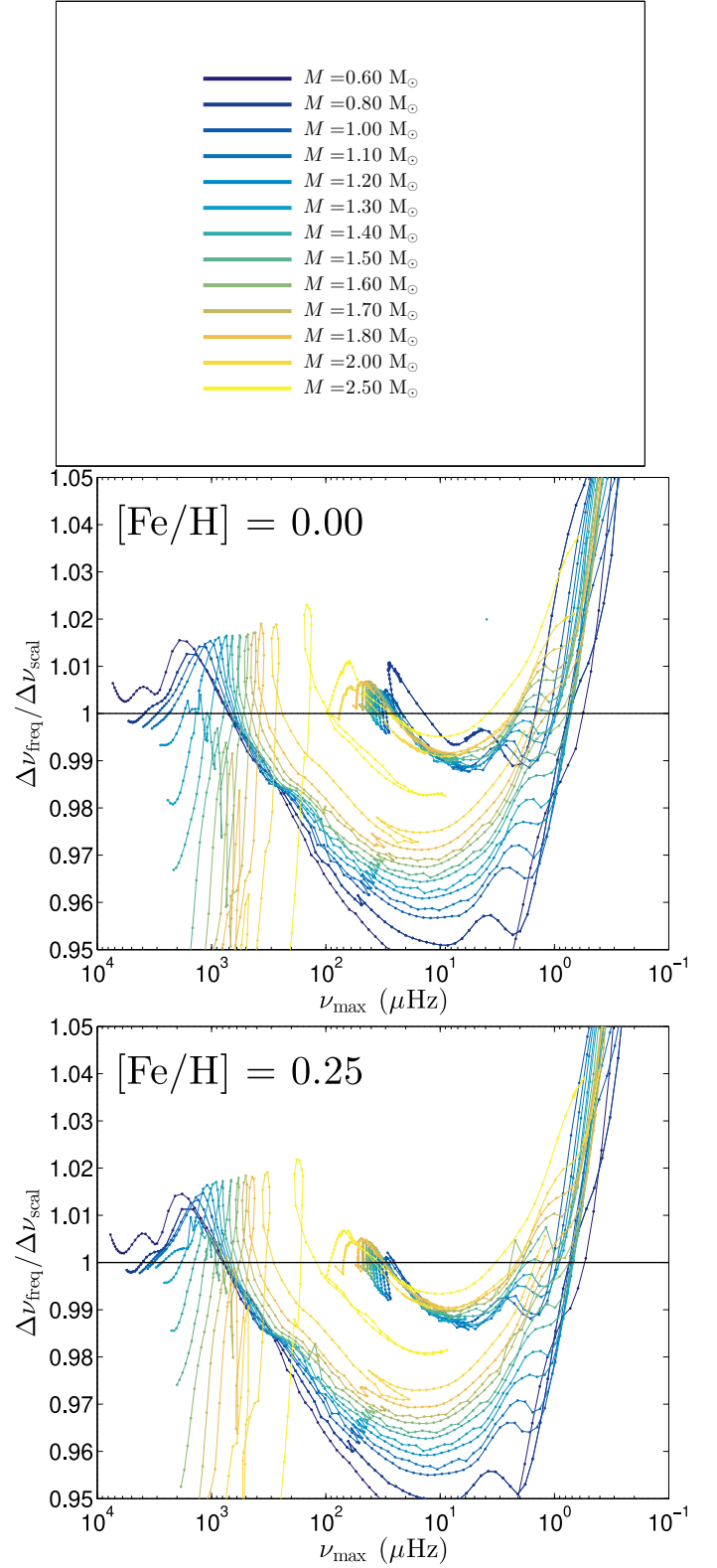


Fig. A.1. Theoretical corrections to $\Delta\nu$ in the asteroseismic scaling relations. See [Rodrigues et al. \(2017\)](#) for details.