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# **Constraints on core–mantle boundary topography from models of thermal and thermochemical convection**

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## **SUMMARY**

Mantle flow induces dynamic topography at the core–mantle boundary (CMB), with distribution and amplitude that depend on details of the flow. To assess whether observations of CMB topography can give constraints on deep mantle structure, we determine CMB dynamic topography associated with different models of mantle convection, including thermochemical and purely thermal models. We investigate the influence of key controlling parameters, specifically the thermal viscosity ratio ( $\Delta \eta_T$ ) and, for thermochemical models, the density contrast ( $\Delta \rho_C$ ) and viscosity ratio ( $\Delta \eta_C$ ) between primordial and regular materials. In purely thermal models, plume clusters induce positive topography with an amplitude that decreases with increasing  $\Delta \eta$ <sub>T</sub>. In thermochemical models with moderate density contrasts, around 100–200 kg m<sup>-3</sup>, reservoirs of dense material induce depressions in CMB topography, surrounded by a ridge of positive topography. The average depression depth and ridge height increase with increasing  $\Delta \rho_C$  and  $\Delta \eta_C$ , but decrease with increasing  $\Delta \eta_T$ . We find that for purely thermal models or thermochemical models with  $\Delta \rho_C \sim 90 \text{ kg m}^{-3}$  and less, the long-wavelength (spherical harmonic degrees up to  $l = 4$ ) dynamic topography and shear wave velocity anomalies predicted by thermochemical distributions anticorrelate. By contrast, for models with  $\Delta \rho_C \ge 100 \text{ kg m}^{-3}$ and  $\Delta \eta_C > 1$ , long-wavelength dynamic topography and shear wave velocity anomalies correlate well. This potentially provides a test to infer the nature, that is, either purely or mostly thermal ( $\Delta \rho_C \le 100 \text{ kg m}^{-3} \text{ m}^{-3}$ ) or strongly thermochemical ( $\Delta \rho_C \ge 100 \text{ kg m}^{-3}$ ), of the low shear wave velocity provinces observed by global tomographic images. The presence of post-perovskite, provided that its viscosity is similar to that of bridgmanite, does not alter these conclusions.

**Key words:** Composition and structure of the mantle; Mantle processes; Structure of the Earth; Dynamics: convection currents, and mantle plumes.

#### **1 INTRODUCTION**

The seismic structure of the lowermost mantle is dominated by two large low shear wave velocity provinces (LLSVPs) below Africa and the Pacific, where shear wave speed decreases by a few per cent compared to its horizontal average. LLSVPs are observed by all global seismic tomography models, with some differences in the detailed structure and amplitude of the velocity drop (for a comparison of models published between 2005 and 2010, see Ritsema *et al.* 2011). Their presence is further supported by a variety of seismic data and methods (Lekić *et al.* 2012), suggesting that they are not simple artefacts of tomographic models. In particular, because they are seen by normal mode data (Ishii & Tromp 1999; Trampert *et al.* 2004; Mosca *et al.* 2012), they are unlikely the result of wave-propagation complexities. While the presence of LLSVPs is generally accepted, their nature is still a matter of debate (for recent discussions on this problem, see Davies *et al.* 2015; Deschamps *et al.* 2015; Garnero *et al.* 2016). LLSVPs were first associated with superplumes or clusters of smaller plumes, that is, buoyant structures triggered by purely thermal (hot) anomalies. Several hints, however, including the anticorrelation between shear wave and bulk-sound velocity anomalies (e.g. Ishii & Tromp 1999; Masters *et al.* 2000; Trampert *et al.* 2004), and the de-correlation between density and seismic velocity anomalies (Trampert *et al.* 2004), indicated that LLSVPs cannot be explained by purely thermal anomalies, but partially originate from compositional anomalies (Trampert *et al.* 2004; Mosca *et al.* 2012). Alternatively, it has been proposed that the anticorrelation between shear wave and bulk-sound speeds could be mostly explained by complex wavepropagation effects (Schuberth *et al.* 2012), or by the presence of post-perovskite (pPv; Davies *et al.* 2012).

Thus, a clear diagnosis on the nature of LLSVPs, purely thermal or thermochemical, cannot be based on current seismic velocity data only, but requires additional observational constraints independent



**Figure 1.** Influence of mantle dynamics on core–mantle boundary (CMB) topography. Thin black arrows denote the stress applied on the CMB. (a) Thermal plumes pull the CMB upwards, inducing positive topography. (b) Slabs stretch the CMB downwards, inducing negative topography. (c,d) Thermochemical piles depress the CMB, inducing negative topography with amplitude that depends on the chemical density contrast between the material of these piles and the regular mantle. Some elements of this sketch are taken from Garnero *et al*. (2016).

of seismic velocities. Two promising observables are long-period electromagnetic C-responses, which are related to the distribution of electrical conductivity in the deep mantle and are different for purely thermal and thermochemical structures (Deschamps & Khan 2016), and seismic attenuation, which is mostly sensitive to temperature and can be inferred from waveform data (e.g. Konishi *et al.* 2017). Another potential constraint is the core–mantle boundary (CMB) topography. Using Very Long Baseline Interferometry (VLBI) data, Gwinn *et al.* (1986) showed that the CMB dynamical flattening (strictly speaking, the dynamical flattening of the outer core), that is, the spherical harmonic degree and order  $l = 2$  and  $m = 0$  of CMB topography, is larger than its theoretical value for a hydrostatic Earth model by 5 per cent. If more complexities are taken into account, the excess CMB dynamical flattening reduces to 3.8 per cent (Mathews *et al.* 2002). Seismic normal modes data further indicate that the peak-to-peak amplitude of the spherical harmonic degree  $l = 2$  in CMB topography should not exceed 5.0 km (Koelemeijer *et al.* 2012). Analysis of seismic phases reflecting on the CMB underside (PKKP) and upperside (PcP) suggests that 95 per cent of the CMB topography is distributed between −4.0 and 4.0 km (Garcia & Souriau 2000). Several studies, using different CMB transmitted or reflected seismic phases, have also attempted to draw global maps, but generally disagree on both the pattern and amplitude of CMB topography (Morelli & Dziewonski 1987; Doornbos & Hilton 1989; Sze & van der Hilst 2003; Tanaka 2010).

For spherical harmonic degrees up to  $l = 4$ , the peak-to-peak amplitude ranges from 3.5 km (Koper *et al*. 2003) to 12 km (Morelli & Dziewonski 1987).

Insights on CMB topography may further be obtained from geodynamic models. In a fluid animated by convection, flow generates normal stress at its interfaces, which in turn induces dynamic topography (e.g. Ricard *et al.* 1984; Hager & Richards 1989). Plumes stretch the base and push the surface of the fluid upwards (Fig. 1a), inducing positive topography on these boundaries. In contrast, downwellings pull the surface and push the base of the system downwards, leading to negative topography (Fig. 1b). Dynamic topography is sensitive to mantle viscosity and its lateral variations, and to the density jump at the boundaries. In the Earth's mantle, the detailed CMB dynamic topography thus strongly depends on the mode of mantle dynamics, in particular on lateral variations in density due to large-scale chemical heterogeneities. The 2-D-Cartesian simulations of Hansen & Yuen (1989) indicated that piles of dense material at the bottom of the system strongly depress the CMB, inducing negative topography (Figs 1c and d). Lassak *et al.* (2007) pointed out that in models combining large thermal viscosity contrast and piles with small chemical density contrast, the negative CMB topography induced by slabs is much larger than that caused by the pile. Lassak *et al.* (2010) further showed that imposing a large thermal viscosity contrast flattens out the topography induced by thermochemical piles, because these regions are hotter, and thus less viscous, than surroundings. Using models of convection in which density anomalies are scaled from seismic tomography, Yoshida (2008) showed that if LLSVPs are purely thermal structures, they should result in positive topography with amplitude around 5 km, while, on the contrary, if they are thermochemical piles, they would induce local depressions. These models, however, are limited to moderate chemical density contrasts, around 60 kg m<sup>-3</sup> and lower, and assume that the viscosity is independent of the type of material, dense or regular.

In this study, we performed models of convection in 3-D-spherical geometry, including models with chemical density contrast larger than 100 kg m<sup>-3</sup>, which may be more appropriate for LLSVPs, models with an intrinsic viscosity ratio between primordial and regular materials, whose effects on CMB dynamic topography have not yet been investigated, and models accounting for the pPv phase transition. Results from these models provide a criteria to discriminate between possible models of LLSVPs, purely thermal or slightly thermochemical on one hand, or strongly thermochemical, that is, with chemical density contrast around 100 kg m<sup>-3</sup> or more, on the other hand.

#### **2 MANTLE CONVECTION MODELLING**

We performed numerical simulations of purely thermal and thermochemical convection in 3-D-spherical geometry using StagYY (Tackley 1998, 2008), a software that solves the conservation equations of energy, momentum, and mass for a compressible, anelastic fluid with infinite Prandtl number. Thermochemical models distinguish two types of material, regular (pyrolitic) mantle and primordial material, and further solve the conservation equation of composition. Primordial material accounts for chemical heterogeneities that may be present at the bottom of the mantle as a result of early differentiation. An additional source of chemical heterogeneity, which we do not take into account in our models, is the recycling of subducted oceanic crust (MORB). Recent models of convection (Li *et al.* 2014a) indicate that subducted MORB may be partially incorporated into pre-existing reservoirs of primordial material, and partially re-entrained to the surface by plumes, in agreement with the Basal Melange (BAM) scenario (Tackley 2012). Because subducted MORB is denser than pyrolitic mantle, their effect on CMB topography is likely similar to that of primordial material, and neglecting its contribution may not alter our conclusions.

For details on the numerical methods employed to solve the conservation equations, we refer to Tackley (2008). The setup used in this paper is essentially that used in Deschamps *et al.* (2015) except for the viscosity law, which now includes yield stress, and for the explored range of control parameters. Details of this setup can be found in previous studies (Deschamps & Tackley 2009), but for clarity we discuss them again below.

Spherical geometry is modelled by a set of Yin and Yang grids (Kageyama & Sato 2004) with resolution equivalent to a spherical grid with 256 points in latitude and 512 points in longitude at each depth. The vertical resolution is fixed to 128 or 64 nodes for models with and without pPv, respectively. Grid refinement is imposed at the top and at the bottom of the shell, allowing a good resolution of reservoirs of primordial material and thermal boundary layers. The ratio between the radius of the core and the total radius is set to its Earth value, that is,  $f = 0.55$ . The bottom and surface boundaries are free slip. The system is heated both from the bottom and from within, and the heating rate of primordial material is increased by



**Figure 2.** Thermodynamical reference state as a function of depth. Profiles shown are for temperature ( $T_{\text{ref}}$ ), density ( $\rho_{\text{ref}}$ ), thermal expansion ( $\alpha_{\text{ref}}$ ) and Grüneisen parameter ( $\gamma$ <sub>ref</sub>). The discontinuity in density at non-dimensional depth of 0.228 corresponds to the limit between upper and lower mantle.

a factor 10 compared to that of regular material. The total mantle heating rate is equivalent to a surface heat flux of 10 mW  $m^{-2}$ , which is about half the value expected for Earth's mantle (Jaupart *et al.* 2015), and leads to a ratio of internal to basal heating close to 0.3. Compressibility generates additional sinks and sources of heat, that are controlled by the dissipation number, *Di*. Because it depends on thermal expansion, *Di* varies with depth. In all our models the surface value of the dissipation number is fixed to  $Di<sub>S</sub> = 1.2$ , and the depth variations of thermal expansion (Fig. 2) imply that its volume average is equal to 0.43.

The conservation equations involve the definition of a reference state, which here consists of a set of vertical profiles for density, temperature, and thermal expansion calculated using thermodynamic relationships for the Earth's mantle (Tackley 1998). Fig. 2 plots the variations of the reference state with depth. Note that thermal expansion decreases by a factor 5 from surface to bottom, and that the Grüneisen parameter,  $\gamma$ <sub>ref</sub>, varies in such a way that its product with reference density is constant with depth. Temperature is scaled with respect to the super-adiabatic temperature difference across the system,  $\Delta T_{\rm S}$ , and density and thermal expansion are scaled with respect to their surface values. Table 1 lists the thermodynamic properties used to build the reference state, together with other scalings and properties.

Because the fluid properties (density, viscosity, thermal diffusivity, and thermal expansion) are allowed to vary throughout the system, the definition of the Rayleigh number is non-unique. In our simulations, we prescribed a reference Rayleigh number  $Ra_0$ , defined at surface values of the thermodynamic parameters and reference viscosity  $\eta_0$ . In all simulations shown here,  $Ra_0$  is set to

Parameter	Symbol	Value	Units	Non-dimensional
Non-dimensional parameters				
Reference Rayleigh number	Ra <sub>S</sub>			$3.0 \times 10^{8}$
Surface dissipation number	Dis			1.2
Volume average dissipative number	Di			0.43
Total internal heating	$H_{\rm C}$	10	$mW m^{-2}$	4.8
Compositional heating ratio	$\Delta H_C$	10		
Compositional parameters (thermochemical cases only)				
Buoyancy ratio	$B_{\rm z}$			$0.15 - 0.70$
Volume fraction of dense material (%)	$X_{\text{prim}}$			$2.5 - 7.0$
Physical & thermodynamical parameters				
Acceleration of gravity	g	9.81	$\rm m~s^{-2}$	1.0
Mantle thickness	D	2891	km	1.0
Reference adiabat	$T_{\rm as}$	1600	K	0.64
Super-adiabatic temperature difference	$\Delta T_S$	2500	K	1.0
Surface density	$\rho_S$	3300	$\text{kg m}^{-3}$	1.0
Surface thermal expansion	$\alpha_{\rm S}$	$5.0\times10^{-5}$	$K^{-1}$	1.0
Surface thermal diffusivity	$K_{S}$	$6.24 \times 10^{-7}$	$m^2 s^{-1}$	1.0
Heat capacity	$C_{\rm P}$	1200	$J kg^{-1} K^{-1}$	1.0
Surface conductivity	$k_{\rm S}$	3.0	$W m^{-1} K^{-1}$	1.0
Surface Grüneisen parameter	$\gamma$ s	1.091		
Density jump at $z = 660$ km	$\Delta\rho_{660}$	400	$\text{kg m}^{-3}$	0.1212
Clapeyron slope at $z = 660$ km	$\Gamma_{660}$	$-2.5$	$MPa K^{-1}$	$-0.0668$
Post-perovskite density jump	$\Delta \rho_{\rm pPV}$	62	$\text{kg m}^{-3}$	0.0188
Clapeyron slope of post-perovskite	$\Gamma_{\rm pPV}$	13	$MPa K^{-1}$	0.3474
CMB temperature	$T_{CMB}$	3750	K	1.5
Density jump at CMB	$\Delta \rho_{\rm CMB}$	5280	$\text{kg m}^{-3}$	1.6
Viscosity law				
Reference viscosity	$\eta_0$	$1.6 \times 10^{21}$	Pa <sub>s</sub>	1.0
Viscosity ratio at $z = 660$ km	$\Delta\eta_{660}$	30		
Logarithmic thermal viscosity ratio	$E_{\rm a}$	13.816-23.026		
Logarithmic vertical viscosity ratio	$V_{\rm a}$	2.303		
Compositional viscosity ratio	$\Delta\eta_{\rm C}$	$1 - 10^2$		
Surface yield stress	$\sigma_{0}$	290	MPa	$7.5 \times 10^{6}$
Yield stress gradient	$\dot{\sigma}_z$	0.01	Pa/Pa	0.01

**Table 1.** Parameters and scalings of numerical experiments.

 $3.0 \times 10^8$ , leading to an effective Rayleigh number (i.e. the Rayleigh number at the volume average viscosity) between  $10^6$  and  $2.0 \times 10^6$ , depending on the case.

In thermochemical cases, the compositional field is modelled with a collection of 100 million particle tracers (200 million for cases with pPv), leading to an average number of tracers per cell of 15, which is enough to properly model entrainment (Tackley & King 2003). Tracers are of two types, modelling the regular mantle and primordial material, respectively, and are advected following a fourth-order Runge–Kutta method. At each time step, the compositional field is inferred from the concentration *C* of particles of primordial material in each cell. This concentration varies between 0 (corresponding to a cell filled with regular material only) and 1 (for a cell filled with primordial material only). The primordial material is initially distributed in a basal layer, the thickness of which is controlled by fixing the volume fraction of dense material,  $X_{\text{prim}}$ . In most of our calculations, we fixed  $X_{\text{prim}}$  to 3.5 per cent, corresponding to an upper estimate of the volume of LLSVPs (Hernlund & Houser 2008). In addition, we conducted calculations for  $X_{\text{prim}} = 2.5$  per cent and  $X_{\text{prim}} = 7.0$  per cent. The primordial material is assumed to be denser than the regular

(pyrolitic) mantle, and the density contrast between the two materials is controlled by the buoyancy ratio. In our calculations, the buoyancy ratio is defined with respect to a reference density that increases with depth following a thermodynamical model of Earth's mantle,

$$
B_z = \frac{\Delta \rho_c(z)}{\alpha_S \rho(z) \Delta T_S},\tag{1}
$$

where  $\Delta \rho_c(z)$  is the density contrast between dense and regular material,  $\alpha_S$  the surface thermal expansion,  $\rho(z)$  the reference density at depth *z*, and  $\Delta T_s$  the super-adiabatic temperature jump. In our models, the reference density increases with depth but  $B<sub>z</sub>$  remains constant, implying that the chemical density contrast increases with depth proportionally to the reference density. With this definition, the buoyancy ratio required to obtain a chemical stratification of the system is smaller than when the surface density is taken as reference density. For equivalent chemical density contrast at the bottom of the system, however, results of the simulations do not differ substantially. We set  $B_z$  to 0.23 in most of our models. At the bottom of the system, and taking  $\alpha_S = 5.0 \times 10^{-5} \text{ K}^{-1}$ ,  $\rho_{\text{bot}} = 4950 \text{ kg m}^{-3}$ and  $\Delta T_{\rm S} = 2500$  K, this leads to a density contrast between dense

and regular material around 142 kg m<sup>-3</sup>, that is, about 2.5 per cent of PREM density (Dziewonski & Anderson 1981) at these depths, in agreement with the peak-to-peak chemical density anomalies mapped by normal modes data (Trampert *et al.* 2004; Mosca *et al.* 2012). Because the buoyancy ratio is certainly the most sensitive parameter controlling the dynamics of the system, we performed additional calculations with  $B_z$  between 0.15 and 0.70. This latter value allows maintaining a layer of primordial material that covers nearly all the CMB.

Viscosity is allowed to vary with depth, temperature, and composition. An additional viscosity ratio  $\Delta \eta_{660} = 30$  is added at the 660 km phase transition, and to avoid the formation of stagnant lid at the top of the system, we impose a yield stress. The viscosity is then fully described by

$$
\eta = \frac{1}{\frac{1}{\eta_b} + \frac{1}{\eta_Y}},\tag{2}
$$

where

$$
\eta_Y = \frac{\sigma_0 + \dot{\sigma}_z P}{2\dot{e}}\tag{3}
$$

is the yield viscosity, and

$$
\eta_{b} (z, T, C) = \eta_{0} [1 + 29H(z - 660)]
$$
  
 
$$
\times \exp \left[ V_{a} \frac{z}{D} + E_{a} \frac{\Delta T_{S}}{(T + T_{\text{off}})} + K_{a} C \right].
$$
 (4)

The yield viscosity (eq. 3) is defined from the yield stress,  $\sigma_Y = \sigma_0 + \dot{\sigma}_z P$ , and the second invariant of the stress tensor, *e*. The yield stress is set to  $\sigma_0$  at the surface and increases with pressure following a gradient  $\dot{\sigma}_z$ . In eq. (4),  $\eta_0$  is a reference viscosity, *H* the Heaviside step function, *z* the depth, *D* the mantle thickness,  $\Delta T_{\rm S}$  the superadiabatic temperature difference across the system and  $T_{\text{off}}$  the temperature offset, which is added to the temperature to reduce the viscosity jump across the top thermal boundary layer. The reference viscosity  $\eta_0$  is defined for the surface value of the reference adiabat (i.e.  $T_{\text{as}} = 0.64 \Delta T_{\text{S}}$ ), and at regular composition  $(C = 0)$ . The viscosity variations with temperature are controlled by  $E_a$ , modelling the activation energy. To quantify the thermally induced increase of viscosity, we define a potential thermal viscosity ratio as  $\Delta \eta_{\rm T} = \exp(E_{\rm a})$ . However, due to the adiabatic increase of temperature and to the temperature offset, which we fixed to  $T_{\text{off}} = 0.88 \Delta T_{\text{S}}$ , the effective top-to-bottom thermal viscosity contrast is smaller than  $\Delta \eta$ <sub>T</sub> by about two orders of magnitude. Here, we fixed  $E_a$  to 20.723 (corresponding to  $\Delta \eta_T = 10^9$ ) in most simulations, and did additional calculations with values of  $E_a$  in the range 13.816–23.032 ( $10^6 \le \Delta \eta_{\rm T} \le 10^{10}$ ). The viscosity variations with depth are controlled by  $V_a$ , modelling the activation volume. In all simulations performed here, we fixed the value of  $V_a$  to 2.303, leading to an increase of viscosity from top to bottom by a factor 300. This includes the viscosity jump at 660 km, but excludes the decrease due to adiabatic increase of temperature and the thermally induced increase in thermal boundary layers. The viscosity variations with composition are controlled by the parameter  $K_a$ , and the viscosity ratio between primordial and regular material (or chemical viscosity ratio) is given by  $\Delta \eta_C = \exp(K_a)$ . The viscosity of bridgmanite is larger than that of ferro-periclase by up to 3 orders of magnitude (Yamazaki & Karato 2001). If LLSVPs are enriched in bridgmanite by up to about 10 per cent, as suggested by probabilistic tomography (Trampert *et al.* 2004; Mosca *et al.* 2012), they should be intrinsically more viscous than surrounding mantle. Recent numerical experiments (Li *et al.* 2014b; Deschamps *et al.* 2015) further indicate that intrinsically more viscous primordial

material increases the topography of reservoirs of dense material and the sharpness of their edges. The value of the chemical viscosity ratio depends on poorly constrained parameters, including the rock deformation model and the distribution of phases (bridgmanite and ferro-periclase) within the aggregate, and is thus difficult to estimate. In most of the thermochemical models presented in this study, we impose primordial material to be more viscous than regular material with  $\Delta \eta_C = 30$ . Finally, it should be pointed out that our viscosity law does not account for viscosity variations with grain size, which may influence mantle dynamics and evolution. The detailed effects of grain size remain a matter of debate. For diffusion creep, viscosity is usually assumed to increase with grain size following a power law with exponent in the range 2–3 (e.g. Korenaga & Karato 2008). Large grain size further favours the transition from diffusion to dislocation creep regimes, and it has been suggested that this transition may occur for grain size as low as 0.1–1 mm (Li *et al.* 1996). Due to various physical and chemical processes, grain size may strongly vary in space and time. For instance, because in early Earth grain growth occurred in a partially molten environment, initial grain size may have been rather large, while recrystallization, in particular during the ringwoodite to bridgmanite phase transition, leads to smaller grain size. Regions with larger grain size in primordial mantle had larger viscosity, and depending on the vigour of convection, they may have mixed efficiently or, on the contrary, poorly with regions of lower viscosity (Solomatov & Reese 2008). If thermochemical reservoirs in our models resulted from early mantle differentiation, their intrinsic viscosity may differ from that of the regular mantle by up to a few orders of magnitude. A simple way to account for this effect would then be to systematically vary the chemical density contrast,  $\Delta \eta_c$ , up to very large values, for example,  $10<sup>3</sup>$  and more. This, however, neglects recrystallization effects that may affect the primordial material during its circulation in the mantle.

Fig. 3, plotting viscosity profiles along the initial temperature profile, illustrates the radial viscosity variations in our models when thermal and chemical effects are taken into account. The effect of intrinsically more viscous ( $\Delta \eta_C = 30$ ) dense material at the bottom of the mantle is denoted by the dashed curve. Note that for  $E_a = 20.723$ , which is the case of most of our models, the regular increase with depth  $(V_a = 2.303)$  in the lower mantle is nearly compensated by the decrease due to adiabatic increase of temperature.

The phase change at 660 km is modelled with a discontinuous phase transition controlled by defining a point on the phase boundary and a Clapeyron slope,  $\Gamma_{660}$ . Here, we imposed  $z = 660 \text{ km}$ and *T* = 1900 K as anchor point, and  $\Gamma_{660} = -2.5 \text{ MPa K}^{-1}$ . The density contrast at the phase transition is  $\Delta \rho_{660} = 400 \text{ kg m}^{-3}$ and is scaled with the surface density. In cases that include pPv phase, the pPv phase transition is modelled with a reference temperature of 2700 K at 2700 km depth. Lateral deviations in the transition depth are determined using the phase function approach of Christensen & Yuen (1985). The Clapeyron slope and the density contrast are set to  $\Gamma_{pPv} = 13 \text{ MPa K}^{-1}$  (Tateno *et al.* 2009) and  $\Delta \rho_{\text{pPv}} = 62 \text{ kg m}^{-3}$  (corresponding to a relative contrast of ∼1.0 per cent, Murakami *et al.* 2004), respectively. Determining the stability field of pPv further requires fixing the temperature at the CMB,  $T_{\text{CMB}}$ . Based on the numerical simulations of Li *et al.* (2015), which pointed out that values of  $T_{\text{CMB}}$  around 3750 K describe best lower mantle structure and dynamics, we assumed  $T_{\text{CMB}} = 3750 \text{ K}.$ 

The dynamic topography at the CMB,  $h_{\text{CMB}}$ , is calculated from the normal stress,  $\sigma_{zz}$ , induced by the flow on this boundary, and



**Figure 3.** Radial viscosity profiles along initial temperature profile for purely thermal models or thermochemical models with chemical viscosity contrast  $\Delta \eta_C = 1$  (plain curves), and thermochemical models with  $\Delta \eta_C = 30$ (dotted curve). Two values of the thermal viscosity contrast (controlled by the parameter  $E_a$ ) are shown.

takes into account self-gravitational effects following Zhang & Christensen (1993). At each point of the CMB, dynamic topography is given by

$$
h_{\rm CMB} = \frac{\sigma_{zz} + \Phi_{\rm CMB} \Delta \rho_{\rm CMB}}{\Delta \rho_{\rm CMB} g},\tag{5}
$$

where  $\Delta\rho_{\rm CMB}$  is the density difference between the mantle and the outer core,  $\Phi_{\rm CMB}$  the perturbation of gravitational potential at CMB, and *g* the acceleration of gravity. The normal stress is given by

$$
\sigma_{zz} = 2\eta \left( \frac{\partial v_r}{\partial r} - \frac{1}{3} \nabla \cdot \mathbf{v} \right), \tag{6}
$$

where  $v$  is velocity and  $v_r$  its vertical component. Note that the divergence of velocity in the right hand side of eq. (6) is due to compressibility. Gravitational potential perturbations are obtained by solving Poisson's equation for a distribution of density anomalies (with respect to a reference state) that includes thermal and chemical effects, and variations in CMB topography. For comparison, we also calculated dynamic topography neglecting self-gravitation, but only found small differences, mostly in amplitude, with the topography accounting for self-gravity. For a given set of parameters, the rms amplitude of dynamic topography is, on average, smaller by 5 per cent if self-gravitational effects are included. It is usually assumed that the mechanical boundary condition, free or free-slip, does not affect the boundary topography, because this topography is very small compared to the lateral lengthscale, and therefore slopes are also very small. This has been well tested for the surface boundary (Crameri *et al.* 2012). For large slopes, such as at subduction

zones trenches, differences may however be important, and a free surface may help single-sided subduction (e.g. Crameri & Tackley 2014).

The initial temperature distribution is built by adding small random perturbations to an adiabatic radial profile with thin superadiabatic boundary layers at the top and bottom of the shell. Purely thermal experiments are run up to a dimensional time of 4.5 Gyr. Thermochemical experiments start with a long (up to 1.5–2.0 Gyr) transient phase during which the bottom layer of dense material heats up, and are run up to a dimensional time of 15 Gyr. Models do not reach stationary state, that is, the location of plumes and downwellings vary with time. However, after a period of time that depends on each case, average velocity and surface and bottom heat fluxes stabilize and oscillate around constant values, thus defining a dynamic quasi-equilibrium. All the snapshots presented and discussed in Section 3 are taken in the quasi-equilibrium stage. In thermochemical models, the detailed shape of thermochemical piles varies with time, but the selected snapshots are generally representative of the thermochemical structure obtained for each case. Snapshots are taken at 2.7 Gyr for purely thermal cases, and 11.2 or 15.0 Gyr for thermochemical cases. Note that the experiments discussed here are not designed to model the detailed evolution of the Earth's mantle, for which accurate initial conditions are not yet known. This would further require adding time-decreasing radioactive heating and CMB temperature in our models. Instead, the aim is to obtain various characteristic thermochemical structures, for example, plume clusters or thermochemical piles, to estimate the influence of these structures on CMB dynamic topography. Thus, time indication in our experiments should not be used to discriminate between possible models of mantle dynamics, or to interpret early mantle evolution.

## **3 RESULTS**

Using the setup described in Section 2, we performed a series of 21 numerical experiments with various values of the buoyancy ratio, volume fraction of dense material, and thermal and chemical viscosity ratios (Table 2). All models are in the mobile-lid regime, with horizontal surface velocities of around 1 cm yr<sup>-1</sup>. The surface heat flux is in the range 35–40 mW m−2, depending on the model. These are rather low values compared to heat flux measured at the surface of the Earth, the average of which is around 86 mW  $m^{-2}$ (Davies 2013). It should however be kept in mind that the observed surface heat flux is likely overestimating the heat flux at the top of the mantle because it includes a contribution related to crustal heat production, which is difficult to estimate, but likely around 8 TW (Jaupart *et al.* 2015). In cratonic regions, for instance, this contribution may be large and the mantle heat flux could be as low as 15–20 mW m−<sup>2</sup> (Jaupart & Mareschal 2007). In addition, because our models do not include plate tectonics, they do not distinguish between continental areas and oceanic regions, where observed heat flux is usually highest. Finally, our models do not include secular cooling of the mantle, which contributes up to half of Earth's surface heat loss (Jaupart *et al.* 2015). The bottom heat flux is around 80– 100 mW m−<sup>2</sup> depending on the model, equivalent to a total power around 12–15 TW, that is, in good agreement with the expected core heat flow, in the range 5–17 TW (Jaupart *et al.* 2015).

Table 2 further lists the rms amplitude of dynamic topography for each model. To better quantify the dynamic topography caused by plumes, downwellings, and reservoirs of dense material, we define several regions above the CMB. The plume, or plume cluster,

**Table 2.** Run properties and corresponding output core–mantle boundary (CMB) topography. The prefix T and TC denote purely thermal and thermochemical cases, respectively.  $B_z$  is the buoyancy ratio,  $X_{\text{prim}}$  the volume fraction of dense material,  $\Delta \eta_C$  the intrinsic (chemical) viscosity ratio, and  $E_a$  the logarithmic thermal viscosity contrast (eq. 3). Other properties are listed in Table 1 and are the same for all runs. CMB topography statistics includes rms of global topography, and average topography  $\langle h \rangle$  in primordial reservoirs or plume clusters. For primordial reservoirs, we distinguish the average depth of their interiors  $\langle h^{-} \rangle$ , and the average elevation of their surrounding ridges,  $\langle h^{+} \rangle$ . All topographies are given in km.

Run	$B_{\rm z}$	$X_{\text{prim}}$	$\Delta \eta_C$	$E_a$	pPV	Resolution	$h_{\text{CMB (km)}}$		
							rms	$\langle h^{-} \rangle$	$\langle h^+ \rangle$
T1				20.723	no	$512 \times 256 \times 64$	2.7		1.9
T <sub>2</sub>				13.816	no	$512 \times 256 \times 64$	2.7		2.9
T <sub>3</sub>				23.026	no	$512 \times 256 \times 64$	2.4		1.6
$T1-pPv$				20.723	yes	$512 \times 256 \times 128$	2.4		2.5
$T2-pPv$				13.816	yes	$512 \times 256 \times 128$	3.1		3.9
TC1	0.23	3.5	30	20.723	no	$512 \times 256 \times 64$	2.8	$-1.5$	1.5
TC <sub>2</sub>	0.23	3.5	30	13.816	no	$512 \times 256 \times 64$	2.6	$-1.7$	1.8
TC <sub>3</sub>	0.23	3.5	30	23.026	no	$512 \times 256 \times 64$	2.7	$-1.3$	1.4
TC4	0.15	3.5	30	20.723	no	$512 \times 256 \times 64$	3.1	$-0.6$	1.3
TC <sub>5</sub>	0.50	3.5	30	20.723	no	$512 \times 256 \times 64$	3.0	$-2.4$	2.0
TC <sub>6</sub>	0.70	3.5	30	20.723	no	$512 \times 256 \times 64$	3.4	$-2.5$	2.8
TC7	0.23	3.5		20.723	no	$512 \times 256 \times 64$	2.0	$-0.7$	1.0
TC <sub>8</sub>	0.23	3.5	10	20.723	no	$512 \times 256 \times 64$	2.4	$-1.2$	1.4
TC <sub>9</sub>	0.23	3.5	100	20.723	no	$512 \times 256 \times 64$	2.5	$-1.7$	1.5
TC <sub>10</sub>	0.23	2.5	30	20.723	no	$512 \times 256 \times 64$	2.4	$-1.7$	1.3
TC11	0.23	7.0	30	20.723	no	$512 \times 256 \times 64$	2.6	$-1.3$	1.4
TC1-pPv	0.23	3.5	30	20.723	yes	$512 \times 256 \times 128$	2.8	$-1.9$	1.5
$TC2-pPv$	0.23	3.5	30	13.816	yes	$512 \times 256 \times 128$	3.8	$-2.2$	2.4
TC4-pPv	0.15	3.5	30	20.723	yes	$512 \times 256 \times 128$	3.0	$-0.9$	1.3
TC6-pPv	0.70	3.5	30	20.723	yes	$512 \times 256 \times 128$	3.9	$-2.5$	2.7
$TC7-pPv$	0.23	3.5		20.723	yes	$512 \times 256 \times 128$	2.7	$-0.9$	1.2

region is defined as the area where the temperature is larger than  $T_{\text{plume}} = T_{\text{m}} + c_{\text{plume}}(T_{\text{max}} - T_{\text{m}})$ , where  $T_{\text{max}}$  and  $T_{\text{m}}$  are the maximum and average temperatures above the CMB, respectively, and *c*plume a constant that we fixed to 0.5. The region where downwellings accumulate is defined as the region where the temperature is lower than  $T_{\text{slab}} = T_{\text{m}} - c_{\text{slab}}(T_{\text{m}} - T_{\text{min}})$ , where  $T_{\text{min}}$  is the minimum temperature above the CMB, and *c*slab a constant that we fixed, again, to 0.5. In thermochemical cases, reservoirs of dense material are defined by the region where the concentration in dense particles, *C*, is larger than 0.5. Note that because the transition between the dense reservoir and its surroundings is very sharp, the size and extension of the reservoir do not vary with threshold values of *C* larger than 0.3. By contrast, fixing  $c_{\text{plume}} = c_{\text{slab}} = 0.5$  is rather subjective, and changing these values leads to variations in the extents of plume and downwelling regions, inducing in turn variations in the estimated average topography within these regions. For instance, reducing  $c<sub>slab</sub>$  increases the area of downwelling regions by including regions with smoother topography, thus decreasing the average topography. Importantly, while the extent of plume and slab areas may influence the estimated average CMB topography in these regions, it does not affect the trend, that is, the fact that plumes induce elevations in the CMB, and slabs depressions.

Figs 4 and 5 show snapshots of the temperature, composition and CMB dynamic topography for cases T1 and TC1, respectively, which we take as reference cases for purely thermal and thermochemical models. In case T1, plumes are generated at the CMB and are grouping in two main clusters (Figs 4a and b). Plumes are interconnected through hot ridges, and the typical angular distance between two plumes is 20◦. Cold downwellings reach the CMB in the wide regions located between plume clusters. At their base, plumes generate upwards normal stress, and therefore positive dynamic topography (Figs 4c and d). In the plume clusters region, the average amplitude of dynamic topography is 1.9 km. By contrast, as they reach the CMB, downwellings induce negative dynamic topography, that is, depressions of the CMB. These depressions are strongly localized, but have large amplitude. In case T1, the slab stacking region covers less than 0.5 per cent of the total CMB area, but within this region the rms amplitude of dynamic topography is 17 km. A distribution histogram of the CMB topography (Fig. 6a) indicates that throughout most of the CMB (∼90 per cent of its total surface) dynamic topography ranges between −2.0 and 3.0 km. Downwellings slightly skew the distribution towards topography deeper than −5.0 km. Note that for convenience, the histogram is truncated to the interval [−10; 10] km, implying that topography caused by downwellings is not entirely represented. However, for topography deeper than −10 km the frequency is very small, less than  $10^{-3}$  for a 1 km-stacking bin.

In case TC1, the thermochemical structure at the bottom of the system is dominated by two large antipodal reservoirs of primordial material culminating about 500 km above the CMB (Figs 5c and d). Reservoirs are hotter than average, and plumes are generated at their edges and in their central areas (Figs 5a and b). Large downwellings reach the CMB in regions located in between the two thermochemical reservoirs. Each reservoir of dense material induces a large depression throughout most of its base, surrounded by a thin ridge of positive topography on its edges (Figs 5e and f). On average, the depth of the depression and the height of the ridge are equal to −1.5 km and 1.5 km, respectively (Table 2). As in case T1, downwellings induce deep local depressions with rms amplitude of 6.2 km. Interestingly, the CMB topography distribution is different from that obtained for purely thermal model T1 (Fig. 6b), and now follows a bimodal distribution, with a peak between −2.0 and −1.0 km, corresponding to the interior of the reservoir of primordial material, and a second, less pronounced, peak between 1.0 and



**Figure 4.** Snapshot of a purely thermal case without post-perovskite (T1). Left and right columns show two opposite views of the same snapshot. (a,b) Isosurface of the non-dimensional temperature for *T* = 0.72. (c,d) Core–mantle boundary dynamic topography (colour scale). The orange and blue dotted lines in plots (c) and (d) indicate the limits of the plumes and downwelling regions, respectively. Black dotted lines in plots (b) and (c) denote the path along which topographic profiles in Figs 15(a) and (b) are drawn.

2.0 km, corresponding to its edges. Overall, most of the CMB area (>90 per cent) has a topography between −3.0 and 4.0 km. As in case T1, the distribution is slightly skewed by downwellings towards topography deeper than  $-5.0$  km.

Figs 7 and 8 show snapshots for cases T1-pPv and TC1-pPv, which are similar to T1 and TC1, respectively, except that they include the pPv phase at the bottom of the system. Adding the pPv does not substantially modify the convection patterns obtained for cases T1 and TC1, except that downwellings are globally less well developed. For the CMB temperature we imposed, pPv is stable outside the plume clusters regions for the purely thermal case (T1 pPv; Figs 7c and d) and outside the reservoir of primordial material for the thermochemical case (TC1-pPv; Figs 8e and f). Note that in these models, the viscosities of pPv and bridgmanite are similar. Weak pPv, with a viscosity smaller than that of bridgmanite by three orders of magnitude, may slightly modify the convection pattern, in particular for the thermochemical cases (e.g. Li *et al.* 2015). The

effects on dynamic topography are similar to those obtained without the pPv phase. In purely thermal models, plume clusters induce positive topography with an average height of ∼2.4 km (Figs 7e and f), while in thermochemical models, reservoirs of primordial material cause a depression of the CMB in their interiors and a ridge on their edges, with average depth and height equal to −1.9 km and 1.5 km, respectively (Figs 8g and h). Again, downwellings cause deep local troughs. Distributions of topography are slightly more dispersed, with most of the topography ranging between −4.0 km and 4.0 km for model T1-pPv, and between −4.0 and 5.0 km for model TC1-pPv, but are globally unchanged (Figs 6c and d).

Increasing the volume fraction of dense material,  $X_{\text{prim}}$ , obviously increases the size of reservoirs of primordial material, in particular the fraction of CMB area they cover, but does not substantially modify their stability (Li *et al.* 2014b). All other parameters being equal to those of case TC1, our calculations for  $X_{\text{prim}} = 2.5$  per cent (case TC10) and  $X_{\text{prim}} = 7.0$  per cent (case TC11) further indicate that



**Figure 5.** Snapshot of a thermochemical case without post-perovskite (TC1). Left and right columns show two opposite views of the same snapshot. (a,b) Isosurface of the non-dimensional temperature for  $T = 0.67$ . (c,d) Isosurface of the composition for  $C = 0.5$ . (g,h) Core–mantle boundary dynamic topography (colour scale). The white and blue dotted lines in plots (e) and (f) indicate the limits of the reservoirs of dense material and of downwelling regions, respectively. Black dotted lines in plots (e) and (f) denote the path along which the topographic profile in Fig. 15(c) is drawn.



**Figure 6.** Distribution histograms of dynamic topography at the CMB for cases T1 (a), TC1 (b), T1-pPv (c) and TC1-pPv (d) (see Table 2 for the properties of these cases). Frequency is normalized to the total area of the CMB. For convenience, histograms are truncated to the interval [−10; 10] km, implying that topography caused by downwellings is not entirely represented.

dynamic topography is only slightly affected by a change in  $X_{\text{prim}}$ (Table 2). Other parameters of the model, in particular the buoyancy ratio and the thermal and compositional viscosity contrasts, induce more substantial changes on the flow pattern. We now further explore the consequences of these changes on the CMB dynamic topography.

#### **3.1 Buoyancy ratio**

Fig. 9 shows snapshots of models with buoyancy ratio  $B_z = 0.15$ (case TC4) and  $B_z = 0.7$  (case TC6), corresponding to chemical density contrasts of 93 and 433 kg m−3, respectively. In case TC4, the chemical density contrast is too small to prevent strong entrainment of primordial material, leading to the formation of narrow, elevated thermochemical piles with sharp edges (Figs 9a–d). The dynamic topography induced by these piles is strongly attenuated compared to that of case TC1. The average depth of central depression reaches only 0.6 km, and the average height of surrounding ridge 1.3 km (Table 2). As observed by Lassak *et al.* (2007), the depressions induced by slabs are much larger, with, in case TC4, an average depth of 11.6 km. The distribution of topography is no longer bimodal but peaks between 1.0 and 2.0 km (Fig. 10a), similar to the distributions obtained for purely thermal cases. In case TC6, on the contrary, the large chemical density contrast strongly inhibits entrainment of primordial material, leading to a nearly stratified system in which the core is almost fully covered by a layer of primordial material (Figs 9e–h). Compared to case TC1, dynamic topography is more pronounced, with average depth of depression and height of ridge around  $-2.5$  and 2.8 km, respectively (Table 2). The negative CMB topography caused by slabs, on the contrary, is attenuated, with an average depth of 4.2 km. In addition, topographic highs around the reservoir reach large values, 10 km and

more, strongly skewing the distribution of topography towards high values (Fig. 10b).

Overall, increasing the buoyancy ratio of primordial material increases the amplitude of dynamic topography generated by thermochemical piles and reservoirs. Additional cases including the pPv phase transition (cases TC4-pPv and TC6-pPv in Table 2) indicate that this trend is not altered when pPv is present.

#### **3.2 Thermal viscosity contrast**

Thermal viscosity contrast has a strong influence on the shape and stability of reservoirs of primordial material (Deschamps & Tackley 2009; Li *et al.* 2014b). These reservoirs are hotter, and therefore less viscous than their surroundings. This viscosity contrast increases with *E*a, which in turn reduces the mechanical coupling of dense material and their entrainment by plumes. Figs  $11(a)$ – (d) show a snapshot of thermochemical case TC2 with thermal viscosity contrast  $E_a = 13.816$ , corresponding to a maximum (or potential) bottom-to-top viscosity contrast,  $\Delta \eta$ <sub>T</sub>, of 10<sup>6</sup>. Compared to case TC1, for which  $E_a = 20.723$  and  $\Delta \eta_T = 10^9$ , the shape and stability of the reservoirs of dense material are substantially altered. Reservoirs have smaller length-scale, larger topography, and sharper edges, as already observed in the simulations of Li *et al.* (2014b). Changes in thermal viscosity contrast strongly affect the amplitude of CMB dynamic topography beneath reservoirs. Viscosity in reservoirs decreases with increasing thermal viscosity contrast, leading to flatter topography (Table 2). The average depth of depression and height of surrounding ridge are around −1.7 and 1.8 km for case TC2 (*E*<sup>a</sup> = 13.816), and −1.3 and 1.4 km for case TC3 ( $E_a = 23.026$ ). We observe a similar effect for purely thermal models, that is, the topography induced by plumes decreases in amplitude with increasing thermal viscosity contrast (Table 2).



**Figure 7.** Snapshot of a purely thermal case with post-perovskite (T1-pPv). Left and right columns show two opposite views of the same snapshot. (a,b) Isosurface of the non-dimensional temperature for  $T = 0.80$ . (c,d) Stability field of the post-perovskite phase. (e,f) Core–mantle boundary dynamic topography (colour scale). The orange and blue dotted lines in plots (e) and (f) indicate the limits of the plumes and downwelling regions, respectively.



**Figure 8.** Snapshot of a thermochemical case with post-perovskite (TC1-pPv). Left and right columns show two opposite views of the same snapshot. (a,b) Isosurface of the non-dimensional temperature for *T* = 0.67. (c,d) Isosurface of the composition for *C* = 0.5. (e,f) Stability field of the post-perovskite phase. (g,h) Core–mantle boundary dynamic topography (colour scale). The white and blue dotted lines in plots (g) and (h) indicate the limits of the reservoirs of dense material and of downwelling regions, respectively.



**Figure 9.** Snapshots of thermochemical cases TC4 (a–d) with buoyancy ratio  $B = 0.15$ , and TC6 (e–h), with buoyancy ratio  $B = 0.70$ . Left and right columns show two opposite views of the same snapshot. (a,b) Isosurface of the composition for  $C = 0.65$ . (c,d) Core–mantle boundary dynamic topography (colour scale). (e,f) Isosurface of the composition for  $C = 0.5$ . (g,h) Core–mantle boundary dynamic topography (colour scale). The white and blue dotted lines in topography plots indicate the limits of the reservoirs of dense material and of downwelling regions, respectively. Black dotted lines in plots (c) and (d) denote the path along which the topographic profile in Fig. 15(d) is drawn.



**Figure 10.** Distribution histograms of dynamic topography at the CMB for six thermochemical cases, (a) TC4, (b) TC6, (c) TC2, (d) TC3, (e) TC7 and (f) TC9 (see Table 2 for the properties of each case). Frequency is normalized to the total area of the CMB. For convenience, histograms are truncated to the interval [−10; 10] km, implying that topography caused by downwellings is not entirely represented.

In our models, the average elevation drops from 2.9 km for model T2 ( $E_a = 13.816$ ) to 1.6 km for model T3 ( $E_a = 23.026$ ). Interestingly, in thermochemical models, reducing the thermal viscosity contrast changes the distribution of topography. Contrary to cases TC1 (Fig. 6b) and TC3 (Fig. 10d), the distribution of topography for case TC2 (Fig. 10c) is not bimodal. In addition, it is slightly more dispersed, with most of the topography being in the range −5.0 and 5.0 km. Again, the addition of pPv does not modify this trend, as indicated by comparison between cases TC1-pPv and TC2-pPv, and T1-pPv and T2-pPv (Table 2).

#### **3.3 Chemical viscosity contrast**

Increasing the chemical viscosity ratio between primordial and regular materials,  $\Delta \eta_C$ , has the opposite effect to that of increasing the thermal viscosity contrast. The shape and stability of reservoirs are only slightly modified. Reservoirs are flatter if primordial and regular material have similar intrinsic viscosity ( $\Delta \eta_C = 1$ ; case TC7, Figs 11e and f) than if primordial material is more viscous (e.g. case TC1, Figs 5c and d). The amplitude of CMB dynamic topography beneath the reservoirs increases with increasing intrinsic viscosity.

Peak-to-peak amplitude rises from 1.8 km for case TC7 ( $\Delta \eta_C = 1$ ) to 3.2 km for case TC9 ( $\Delta \eta_C = 10^2$ ) (Table 2). For  $\Delta \eta_C = 1$ , most of CMB topography ranges between −2.0 and 3.0 km with a peak between 0 and  $-1.0$  km (Fig. 10e), while for  $\Delta \eta_C = 10$  or more, the CMB topography is more dispersed and follows a bimodal distribution (Figs 6b and 10f). Finally, comparison between cases TC7 and TC7-pPv shows that the addition of pPv does not alter the influence of  $\Delta \eta_C$ .

### **4 COM PAR I SON W I TH SEISMOLOGICAL CONSTRAINTS**

A key question is whether CMB dynamic topography, provided it can be mapped from seismic data, can discriminate between purely thermal and thermochemical models of Earth's mantle. CMB topography predicted by our models strongly differ both in amplitude and pattern depending on the properties of each model, suggesting that CMB topography may bring important insights on lowermost mantle structure. Available seismic models on CMB topography, however, are limited to long wavelengths, up to spherical harmonic degree 4, for which purely thermal and thermochemical models



**Figure 11.** Snapshots of thermochemical cases TC2 (a–d), with  $E_a = 13.816$ , and TC7 (e–h), with  $\Delta \eta_C = 1$ . Left and right columns show two opposite views of the same snapshot. (a,b) Isosurface of the composition for *C* = 0.65. (c,d) Core–mantle boundary dynamic topography (colour scale). (e,f) Isosurface of the composition for *C* = 0.5. (g,h) Core–mantle boundary dynamic topography (colour scale). The white and blue dotted lines in topography plots indicate the limits of the reservoirs of dense material and of downwelling regions, respectively.

**Table 3.** Columns 2–7 list the root mean square (rms) and peak-to-peak amplitude of long-wavelength dynamic topography for four different spherical harmonic filters. For comparison, the peak-to-peak amplitudes of CMB topography observed by Morelli & Dziewonski (1987) (MD87), Doornbos & Hilton (1989) (DH89), Sze & van der Hilst (2003) (SV03), Koper *et al*. (2003) (KPF03), Tanaka (2010) (T10) and Koelemeijer *et al*. (2012) (KDT12) are also indicated. All topographies are given in kilometres. Column 8 lists the fraction of CMB area with topography between −4.0 and 4.0 km, *x*4km. Observed value is from Garcia & Souriau (2000) (GS00). The last column lists the correlation between long-wavelength (*l* = 0–4) dynamic topography and shear velocity anomalies, χ*h*-*d*lnVs, predicted by each model of convection.

		Rms		Peak $l = 2$	to peak $l = 2, 4$	amplitude $l = 0 - 4$	$x_{4km}$	$X h - d \ln V s$ $l = 0 - 4$
	$l = 2$	$l = 2, 4$	$l = 0 - 4$					
Run								
T <sub>1</sub>	1.3	1.3	1.6	5.1	6.6	8.5	0.94	$-0.86$
T <sub>2</sub>	0.7	1.9	2.1	2.0	7.1	8.7	0.89	$-0.94$
T <sub>3</sub>	$0.8\,$	0.9	1.2	2.7	4.1	5.8	0.95	$-0.54$
$T1-pPv$	1.3	1.3	1.5	4.5	5.9	7.7	0.91	$-0.83$
$T2-pPv$	$0.8\,$	2.1	2.3	3.4	9.8	11.5	0.81	$-0.98$
TC1	0.7	$0.8\,$	1.0	2.3	3.5	4.4	0.88	0.71
TC <sub>2</sub>	$0.6\,$	$\rm 0.8$	$1.0\,$	2.3	3.1	4.5	0.89	$-0.13$
TC3	0.7	1.2	1.3	2.9	5.7	6.7	0.92	0.33
TC4	1.1	1.2	1.6	4.4	5.4	7.6	0.89	$-0.68$
TC5	1.3	1.6	2.5	5.2	7.5	9.8	0.82	0.93
TC <sub>6</sub>	2.5	2.3	2.2	7.3	9.1	8.2	0.75	0.88
TC7	0.2	0.6	0.7	0.9	2.7	3.5	0.95	0.27
TC8	0.4	$0.5\,$	0.9	1.2	2.9	4.0	0.93	0.58
TC <sub>9</sub>	0.5	0.7	1.0	1.7	3.0	4.0	0.90	0.82
<b>TC10</b>	0.4	0.7	0.9	1.8	3.4	5.1	0.93	0.58
TC11	1.0	1.2	1.5	3.4	5.8	6.8	0.92	0.65
TC1-pPv	1.1	1.3	1.6	4.6	5.2	7.1	0.87	0.54
$TC2-pPv$	0.4	$0.8\,$	1.5	1.5	3.9	6.8	0.72	$-0.29$
TC4-pPv	1.1	1.2	1.5	4.8	5.6	8.6	0.89	$-0.50$
TC6-pPv	2.3	2.4	2.9	9.1	11.5	14.9	0.70	0.89
$TC7-pPv$	0.6	0.9	1.2	2.2	4.3	6.0	0.91	0.05
Observed								
KDT12				$\leq 5.0$				
T10					5.0			
<b>MD87</b>						12.0		
DH89						8.0		
SV <sub>03</sub>						4.0		
KPF03						3.5		
GS00							0.95	

may have similar signatures (Lassak *et al.* 2010). In this section, we examine more in details the long-wavelength structure of our CMB topography models.

# **4.1 Amplitude: comparison with observed CMB topography**

Table 3 and Fig. 12(a) quantitatively compare CMB topography predicted by our models with available seismological constraints for different spherical harmonic filters. Normal modes data further suggest that the amplitude of spherical harmonic degree  $l = 2$  of topography should be smaller than 5 km (Koelemeijer *et al.* 2012). Our models fit this observation well (Table 3), with the notable exception of thermochemical models with very strong density contrast (TC5, TC6 and TC6-pPv), around 300 kg m−<sup>3</sup> and more. These later models induce a strong chemical layering (Figs 9e and f) that is not seen by seismic velocity data, and are therefore very unlikely. Note, also, that the peak-to-peak amplitude of CMB topography predicted by purely thermal model T1 is slightly larger than the 5 km limit suggested by seismic normal modes, and that models with small density contrast (TC4 and TC4-pPv), around 90 kg m<sup>-3</sup> and less, are close to this limit. Several studies have attempted mapping long-wavelength (up to spherical harmonic degree  $l = 4$ ) CMB topography

(Morelli & Dziewonski 1987; Doornbos & Hilton 1989; Koper *et al.* 2003; Sze & van der Hilst 2003; Tanaka 2010). The resulting maps differ strongly both in pattern and amplitude, a major difficulty being that CMB topography trades off with lowermost mantle seismic velocity anomalies, and upper outer core structure. Studies including all spherical harmonic degrees up to  $l = 4$  have peak-to-peak amplitude between 3.5 km (Koper *et al.* 2003) and 12 km (Morelli & Dziewonski 1987). In general, for this spherical harmonic filter, the dynamic topography predicted by purely thermal models or thermochemical models with small density contrast have peak-to-peak amplitude ranging from 6 km to 11 km, somewhat larger than that of thermochemical models with moderate density contrast (from ∼100 to 200 kg m−3), which ranges between 3.5 and 7.5 km, depending on input parameters (Table  $3$  and Fig. 12a). Using degrees  $l = 2$  and  $l = 4$  only, Tanaka (2010) found a peak-to-peak amplitude of 5 km, in fair agreement with the peak-to-peak topography predicted by thermochemical models with moderate density contrast (between 2.5 and 5.5 km), but slightly lower than that of purely thermal models, which are around 6 km and more, except for model T3 (Table 3 and Fig. 12a).

Constraints on peak-to-peak amplitude may further be inferred from seismic phases reflecting either on the core side or on the mantle side. Using PKKP and PcP phases, Garcia & Souriau (2000)



**Figure 12.** (a) Peak-to-peak amplitude of dynamic topography predicted by our models of convection (colour code) for three spherical harmonic filters  $(l = 2,$ *l* = 2 and 4 and *l* = 0–4). For comparison, amplitudes observed by Morelli & Dziewonski (1987) (MD87), Doornbos & Hilton (1989) (DH89), Sze & van der Hilst (2003) (SV03), Koper *et al*. (2003) (KPF03), Tanaka (2010) (T10), and Koelemeijer *et al*. (2012) (KDT12) are also indicated. (b) Correlation coefficient between long-wavelength (*l* = 0–4) shear-velocity anomalies and CMB dynamic topography predicted by each model of convection. See also Table 3 for numerical values.

showed that 95 per cent of CMB topography with wavelength larger than 300 km should be between −4.0 and 4.0 km. Our thermal and thermochemical models are in good agreement with this observation (Figs 6 and 10; Table 3). The fraction of CMB area with topography

ranging between −4.0 and 4.0 km calculated from unfiltered models is higher than 85 per cent except, again, for of thermochemical models with very large density contrast (Table 3). Importantly, the observations of Garcia & Souriau (2000) do not rule out the presence



**Figure 13.** Shear wave velocity anomalies in the lowermost mantle (2700–2891 km) (left column), CMB dynamic topography (middle column) and CMB isostatic topography (right column) predicted by purely thermal model T1 (Fig. 4) and thermochemical models TC1 (Fig. 5), TC4 (Fig. 9a-d), and TC7 (Fig. 11e-h), filtered for spherical harmonic degrees up to  $l = 4$ . Model properties are listed in Table 2. Shear wave velocity anomalies are calculated from the thermal and compositional fields predicted by each model using the seismic sensitivities of Deschamps *et al*. (2012), and are averaged out in the depth range 2700–2891 km, corresponding to the lowermost layer of Masters *et al*. (2000) tomographic model. For thermochemical models, primordial material is assumed to be enriched in iron and bridgmanite by 3 per cent and 18 per cent, respectively, compared to regular (pyrolitic) material. Isostatic topography is calculated from density anomalies averaged in the lowermost 400 km of the mantle (2591–2891 km). These density anomalies are directly estimated from the thermal and compositional fields predicted by each model, without using seismic sensitivity. Relative density anomalies, not shown here, are fully correlated with isostatic topography, with scaling factor between isostatic topography (in km) and relative density anomalies (in per cent), *R*h, indicated at the bottom right of each plot. Interval of contour levels are  $0.5$  per cent for dln $V<sub>S</sub>$  and 1 km for CMB topography. Root mean square (rms) of each distribution is indicated at the bottom left of each plot.

of deep troughs associated with downwellings since, according to our models, such features would be very localized and would cover a small fraction of the CMB area.

Overall, the peak-to-peak amplitude of long-wavelength dynamic topography is unlikely to provide a clear diagnosis on the nature, thermal or thermochemical, of the deep mantle. On average, thermochemical models with density contrast in the range  $100-200$  kg m<sup>-3</sup> have peak-to-peak amplitude lower than other models, but peak-topeak amplitude further depends on other parameters, in particular to the sensitivity of viscosity to temperature.

#### **4.2 Pattern: correlation between long-wavelength topography and shear wave velocity**

Lassak *et al.* (2010) showed that CMB dynamic topography induced by purely thermal and thermochemical models of convection

strongly differs at short wavelengths, but are not substantially different at long wavelengths, that is, that current seismic maps of dynamic topography, which are limited to spherical harmonic degree  $l = 4$ , would be unable to discriminate between purely thermal and thermochemical structures. They further pointed out that long-wavelength topography and shear wave velocity would be anticorrelated. This conclusion may however change, depending on details of the thermochemical model. Left and middle columns in Fig. 13 compares the long-wavelength (spherical harmonic filter  $l = 0-4$ ) distributions of lowermost mantle shear wave velocity anomalies and CMB dynamic topography for models T1, TC1, TC4, and TC7 (Table 2). For each model, we calculated shear wave velocity anomalies from the thermal and compositional distributions they predict, using the approach and seismic sensitivities described in Deschamps *et al.* (2012). We then averaged out these anomalies according to the radial parametrization of Masters *et al.* (2000), in which the lowermost layer samples the depth range 2700–2891 km. Non-dimensional temperature is rescaled with the super-adiabatic temperature jump  $\Delta T_{\rm S} = 2500 \text{ K}$ , leading to rms temperature anomalies typically around −400 K and 550 K in plume and slab regions, respectively, and 450 K within thermochemical reservoirs. For thermochemical models, we assumed that the dense material is enriched in iron and bridgmanite by 3 per cent and 18 per cent compared to regular (pyrolitic) material. For purely thermal model T1, plumes cause slower than average seismic velocity and positive topography. As a result, long-wavelength seismic velocity anomalies and CMB dynamic topography are strongly anticorrelated (Figs 13a and b). In thermochemical models with small density contrast, typically  $\sim$ 90 kg m<sup>-3</sup> and less, as model TC4  $(B_z = 0.15$ , corresponding to  $\Delta \rho_C = 93$  kg m<sup>-3</sup>) and the models of Lassak *et al.* (2010), thermochemical piles induce shallow depressions (Figs 9a–d). However, when filtered to long-wavelengths, topography beneath piles is positive, and long-wavelengths shear wave velocity anomalies and CMB topography are, again, strongly anticorrelated (Figs 13g and h). CMB topography may thus be unable to discriminate between a purely thermal and a weakly ( $\Delta \rho_{\rm C} < 100 \, \rm kg$ m<sup>-3</sup>) thermochemical structure of the mantle. However, for larger density contrasts, in particular model TC1 ( $B<sub>z</sub> = 0.23$ , corresponding to  $\Delta \rho_C = 142 \text{ kg m}^{-3}$ , reservoirs of primordial material induce slower than average shear wave velocity (because they are hotter than average and enriched in iron), and cause a depression in the CMB (Fig. 5). Shear wave velocity anomalies and CMB topography are then strongly correlated (Figs 13d and e). For model TC7, in which intrinsic viscosities of primordial and regular material are similar ( $\Delta \eta_C = 1$ ), the depression caused by reservoirs of primordial material is less pronounced (Figs 11g–h), resulting in a poorer, but still significant correlation between the maps of shear wave velocity anomalies and CMB dynamic topography (Figs 13j and k). Our models are not expected to strictly reproduce observed seismic patterns above the CMB. It is however interesting to compare long-wavelength shear wave velocity anomalies predicted by models of convection (Fig. 13, left column) with observed tomography from model SB10L18 (Masters *et al.* 2000) at  $z = 2790 \text{ km}$  depth (Fig. 14a). For model T1, shear wave velocity anomalies averaged in the layer 2700–2891 km vary in the range –0.7 to 0.7 per cent with rms amplitude around 0.3 per cent. This is much smaller than SB10L18, which varies between  $-2.5$  and 1.4 per cent, with rms amplitude of 0.9 per cent. Explaining amplitudes of shear wave velocity anomalies observed in SB10L18 would require much larger temperature anomalies, around  $\pm$  1200 K. In thermochemical models, by contrast, shear-velocity anomalies have rms amplitude comparable to that of SB10L18. For model TC1, for instance, they vary between –2.1 and 1.7 per cent with rms amplitude around 1.1 per cent. Shear-velocity anomalies patterns predicted by models TC1 and TC4 are dominated by spherical harmonic degrees 2 and 3, and their power spectra are overall in good agreement with that of SB10L18 (Fig. 14b). The pattern predicted by model TC7 is more complex, with a strong contribution of spherical harmonic degree 4 that is not seen in SB10L18.

To quantitatively compare long-wavelength patterns of topography and shear wave velocity predicted by models of convection, we calculated the correlation  $\chi_{h-dlnVs}$  between these distributions (Table 3 and Fig. 12b). Clearly, CMB topography and shear-velocity anomalies for purely thermal models and thermochemical models with small density contrast anticorrelate, with  $\chi_{h\text{-}d\text{lnVs}} \leq -0.5$ , while they correlate for most thermochemical models with moderate and strong density contrast, with  $\chi_{h\text{-}d\text{ln}}v_s \geq 0.5$ . Interesting



**Figure 14.** Long-wavelength shear wave velocity anomalies in the lowermost mantle. (a) Observed tomography (SB10L18, Masters *et al*. 2000) filtered for spherical harmonic degrees up to  $l = 4$ . Interval of contour levels is 0.5 per cent. (b) Power spectra of SB10L18 (histogram) and selected models shown in Fig. 13 (colour code) up to spherical harmonic degree  $l = 8$ 

exceptions are cases with moderate thermal viscosity contrast  $(\Delta \eta_{\rm T} = 10^6; \text{TC2} \text{ and } \text{TC2-pPv})$ , for which CMB topography and shear-velocity anomalies are de-correlated or slightly anticorrelated, and, again, models with no chemical viscosity contrast ( $\Delta \eta_C = 1$ ; TC7), for which distributions of topography and shear-velocity are only slightly correlated.

These results suggest that long-wavelength CMB dynamic topography potentially provides a test to discriminate between purely thermal models of lower mantle and thermochemical models in which LLSVPs consist of material substantially denser ( $\Delta \rho_C > 100$  kg  $m^{-3}$ , i.e. ~1.8 per cent of PREM and more) and intrinsically more viscous than the surrounding mantle. Interestingly, Tanaka (2010) found depressions of ∼2 km deep beneath Africa and the Pacific, that is, fairly correlated with LLSVPs. If correct, and following our models, this would support the hypothesis that LLSVPs are thermochemical structures denser than the surrounding mantle, with density contrast typically in the range 100–200 kg m−3. This scenario is further supported by available estimates of chemical density anomalies (Trampert *et al.* 2004; Mosca *et al.* 2012), which have a peak-to-peak amplitude around 2.0–3.0 per cent. In addition, because primordial material may be enriched in bridgmanite (Trampert *et al.* 2004; Mosca *et al.* 2012), which is more viscous than ferro-periclase by up to 3 orders of magnitude (Yamazaki & Karato 2001), LLSVPs may be intrinsically more viscous than the surrounding mantle. Other models of CMB topography, however, do not observe clear correlation or anticorrelation between shearvelocity and CMB topography patterns. For instance, the topography

observed by Doornbos & Hilton (1989) is dominated by spherical harmonic degree 1 with a depression beneath India and a topographic high beneath Western Europe and Africa, while the pattern obtained by Morelli & Dziewonski (1987) is more complex, with topographic highs beneath South Indian Ocean, Northern Atlantic and Northern Pacific.

Soldati *et al.* (2012) performed inversion of *P*-wave data and reflected seismic phases (PcP and PKP) jointly for compressional velocity anomalies and CMB topography, using a geodynamically constrained method. More precisely, density anomalies were scaled with seismic velocity anomalies and combined with CMB topography kernels calculated using a spectral method (e.g. Forte & Peltier 1991). Resulting CMB topography maps have peak-to-peak amplitude around 8 km, and are fairly anticorrelated with compressional velocity maps above the CMB. In particular, LLSVPs are associated with topography highs with strong positive topography of up to about 5 km, beneath the central Pacific and southern tip of Africa. It has further been pointed out that CMB topography models inferred from geodynamically constrained tomography fit normal mode constraints better than models deduced directly from seismic tomography (Soldati *et al.* 2013). It should be noted, however, that the approach used by Soldati *et al.* (2012) implicitly assumes that chemical anomalies are small, and that they are, at a given depth, fully correlated with seismic velocity anomalies. Furthermore it does not account for lateral variations in viscosity (e.g. related to variations in temperature), which, as illustrated by our calculations and those of Lassak *et al.* (2010), may substantially affect the amplitude of topography.

### **5 DISCUSSION**

Our calculations show strong differences between the CMB dynamic topographies induced by purely thermal and thermochemical models of convection. In purely thermal models plumes elevate the CMB, while hot thermochemical piles depress it. In both cases, increasing the thermal viscosity contrast decreases the amplitude of CMB topography. In thermochemical models, the buoyancy ratio, measuring the density contrast between primordial and regular material, and the thermal and compositional viscosity contrasts further affect the shape and stability of reservoirs of primordial material, and the amplitude of dynamic topography, as sketched in plots c and d of Fig. 1. Increasing the chemical density contrast and viscosity ratio enhances the depression beneath reservoirs.

#### **5.1 Influence of post-perovskite**

Our calculations further indicate that the presence of pPv at the bottom of the mantle does not substantially influence the dynamic topography. All other parameters being the same, the presence of pPv slightly modifies the amplitude of topography, but the effects due to varying one specific parameter are unchanged. This conclusion assumes that the viscosity of pPv is similar or close to that of bridgmanite. If, in contrast, and as suggested by *ab initio* calculations (Ammann *et al.* 2010), pPv is less viscous than bridgmanite by two to three orders of magnitude, dynamic topography may be strongly altered. Both the numerical models of Yoshida (2008) and the CMB maps of Soldati *et al.* (2012) report a strong attenuation of CMB topography when a low viscosity layer is imposed in the lowermost 200 km of the mantle completely surrounding the core. In our models, the pPv stability region does not cover the entire core surface, but forms discontinuous patches located outside

plume clusters and, in the thermochemical cases, outside reservoirs of primordial material. In these regions, and if pPv is much less viscous than bridgmanite, CMB topography may thus flatten out compared to that found in our models.

#### **5.2 Comparison with previous models**

Our models are in overall agreement with those of Lassak *et al.* (2010). In particular, the influences of buoyancy ratio and thermal viscosity contrast on CMB topography they observed are similar to what we see in our simulations. Note, however, that due to different choices of the super-adiabatic temperature jump and reference thermal expansion (Table 1), and of a different definition of the buoyancy ratio (eq. 1), the chemical density contrast at the bottom of the system for a given value of buoyancy ratio is much larger in our models. For instance, in the models of Lassak *et al.* (2010) with  $B = 0.6$  it is around 60 kg m<sup>-3</sup> (1 per cent of PREM), whereas in our models with  $B_z = 0.23$  it reaches 142 kg m<sup>-3</sup> (2.5 per cent of PREM). As a result, in model TC7 thermochemical reservoirs induce a 0.7 km deep depression in dynamic topography (Figs 8e–h), and a plateau with low elevation in Lassak *et al.* (2010) models. In model TC1 (Fig. 5), this trend is amplified by the fact that primordial material is intrinsically more viscous than the regular material by a factor 30, which deepens the depression beneath reservoirs of primordial material.

To investigate the influence of LLSVPs on dynamic topography, Yoshida (2008) ran models of convection in which density anomalies are scaled from seismic tomography model SMEAN (Becker & Boschi 2002), and arrived at similar conclusions regarding the effect of the chemical density contrast. In purely thermal models, LLSVPs result in positive topography of ∼5 km. Models assuming piles denser by 1 per cent lead to a relatively flat positive topography beneath LLSVPs, while a larger density contrast (2 per cent) causes relatively flat topography with local depressions ∼2 km deep, not unlike our model TC7. Interestingly, this negative topography flattens out when the viscosity of the lowermost mantle is decreased by one or two orders of magnitude. Note, however, that Yoshida (2008) did not run models in which LLSVP viscosity is intrinsically different from that of surrounding material.

#### **5.3 Predicted isostatic topography**

A recent analysis of Stoneley mode splitting data, which are sensitive to the lowermost mantle structure, indicates that LLSVPs might be lighter than surrounding mantle (Koelemeijer *et al.* 2017), in contradiction with earlier normal mode studies (Ishii & Tromp 1999; Trampert *et al.* 2004; Mosca *et al.* 2012). Stoneley mode are further sensitive to CMB topography, and density estimates thus trade-off with this topography. Assuming that long-wavelength  $(>1000 \text{ km})$ CMB topography is due to isostatic compensation, Koelemeijer *et al.* (2017) found that, for degree 2, their data set is best fitted if LLSVPs are lighter than PREM by about 1.4 per cent and CMB is elevated by about 1 km. For degrees 4 and 6, best fits are, by contrast, obtained for LLSVPs denser than average mantle by about 2.5 per cent and a CMB depressed by 1–5 km. When all structural degrees are taken into account, light LLSVPs with CMB topography around 1 km or more are again preferred, but the overall fit is much reduced. In addition, when accounting for seismic normal modes used in previous studies, density models do not have preference for denser or lighter LLSVPs. Finally, it should be kept in mind that splitting data are based on the self-coupling approximation (Woodhouse & Girnius 1982), which might bias the inference of density structure (Al-Attar *et al.* 2012; Yang & Tromp 2015).

Lateral variations in temperature and composition predicted by our models can be used to estimate lateral density anomalies and reconstruct CMB isostatic topography. For purely thermal models, one expects that CMB dynamic and isostatic topographies have similar trends. On the contrary, because thermochemical piles and reservoirs are hotter than average, patterns of dynamic and isostatic topographies may differ substantially, in particular for low buoyancy ratio. Right column in Fig. 13 plots CMB isostatic topography estimated from density anomalies averaged in the lowermost 400 km of the mantle for models T1, TC1, TC4 and TC7. Density anomalies, not shown here, are, by definition, fully correlated with isostatic topography, with scaling factor between topography (in km) and relative density anomalies (in per cent) around  $-0.27$ (the exact value of this scaling factor depends on the average density in the lowermost 400 km layer, which is very similar for all 4 models shown here). For the calculation of density anomalies, temperature anomalies are rescaled with the super adiabatic temperature jump, and thermal expansion and density are rescaled with their surface values (Table 1). Reference density and thermal expansion vary as indicated in Fig. 2, and density anomalies are calculated with respect to horizontal average (which is different and usually higher than the reference density). For comparison with the dynamic topography shown in the middle column of Fig. 13, we filtered density anomalies and isostatic topography for spherical harmonic degrees  $l = 0-4$ . For purely thermal model T1, isostatic topography has a pattern similar to that of dynamic topography, but its amplitude is smaller by about a factor 4. Within plume regions, the average filtered density anomaly and isostatic topography are −0.1 per cent and 0.4 km (Fig. 13c), respectively, and are thus consistent with Stoneley mode splitting measurements of Koelmeijer *et al.* (2017). In thermochemical models, thermal effects alter the effective density within reservoirs and piles of dense material. For small density contrast, as in model TC4 (Fig. 13i), thermal effects nearly compensate chemical effects within piles, leading to average density anomaly and isostatic topography of about 0.3 per cent and −1.0 km, respectively. For larger density contrast, as in models TC1 and TC7, density anomalies within piles are still dominated by chemical effects, resulting in relatively large isostatic topographies (Figs 13f and l). For instance, in model TC1, density anomalies within thermochemical reservoirs and isostatic topography beneath them are equal to 0.8 per cent and −3.2 km on average. Such reservoirs provide poorer fit to Koelemeijer *et al.* (2017) observations than light elevated plume clusters in purely thermal models, but are still in reasonable agreement with these data (see their fig. 3 for  $R_{\text{LL}} = -0.6$  and  $H = -5$ , corresponding to LLSVP total density anomaly of 0.8 per cent and isostatic topography of  $-2.5$  km).

Isostatic topography at CMB may be considered as a first order estimate of CMB topography, taking into account only the effects of hydrostatic pressure. Dynamic topography further accounts for stresses related to mantle flow, in particular slab pushing or plume pulling. This appears very clearly when comparing middle and right columns in Fig. 13. For instance, in case T1, hot, lighter plumes induce positive isostatic topography. They further pull the CMB upwards, thus increasing CMB topography. As a result, compared to isostatic topography (Fig. 13c), dynamic topography has a similar pattern, but more amplitude (Fig. 13b). For thermochemical cases, dynamical and isostatic effects are opposing each other. Dynamic and isostatic topographies have slightly different patterns, and depressions beneath thermochemical reservoirs are shallower in dynamic topography (compare, for instance, Figs 13e and f for

case TC1). Note that for small chemical density contrasts, as in case TC4, dynamic effects lead to very shallow depressions (Fig. 9c), and when filtered for long-wavelengths, dynamic topography beneath thermochemical piles is positive (Fig. 13h). Because it accounts for dynamics effects related to mantle flow, we expect dynamic topography to provide a better description of CMB topography than isostatic topography does. Interestingly, in dynamic topography predicted by case TC1 and filtered with  $l = 0-4$ , the depth of the depressions beneath thermochemical reservoirs is on average −1.0 km (Fig. 13e), which still reasonably fits Stoneley mode observations.

## **5.4 CMB excess ellipticity**

An important constraint on dynamic topography is provided by the excess ellipticity of the CMB, that is, its spherical harmonic degree  $l = 2$  and order  $m = 0$  term  $(Y_{20})$ . This excess can be deduced from Very Long Baseline Interferometry (VLBI) measurements of the retrograde annual nutation of the Earth's rotation axis. More precisely, the period of the free core nutation (FCN) depends on the CMB dynamic flattening, *e*f, and the resonance between FCN and retrograde annual nutation increases the amplitude of this annual nutation. The FCN period deduced from VLBI data, first measured by Gwinn *et al.* (1986), indicates that the CMB dynamical flattening is larger than the value expected for a hydrostatic Earth, with an excess dynamical flattening of 5 per cent. Assuming that this flattening is due to a homogeneous non-hydrostatic layer at the top of the outer core, it can be interpreted as an excess difference between the equatorial and polar radii of the CMB of  $490 \pm 110$  m. Taking into account more complexities, including ocean tides, electromagnetic coupling between core and mantle, and anelastic effects in the mantle, Mathews *et al.* (2002) found a slightly smaller excess, of ∼390 m, corresponding to an excess CMB dynamical flattening of 3.8 per cent. This excess of CMB ellipticity is usually attributed to mantle dynamics (Gwinn *et al.* 1986; Forte *et al.* 1995; Lumb *et al.* 1995). Our models do not define a polar axis and associated equatorial plane that would allow the calculation of excess CMB ellipticity. Nonetheless, one may point out that excess CMB ellipticity would be difficult to reconcile with large, deep depressions in CMB dynamic topography, as those predicted in model TC1  $(B_z = 0.23$  and  $\Delta \eta_C = 30)$ , located along the equator. This problem may be solved in models with a slightly lower buoyancy ratio, around  $B_z = 0.2$  ( $\Delta \rho_C = 124$  kg m<sup>-3</sup>), which is still consistent with density anomalies observed in the lowermost mantle (Trampert *et al.* 2004; Mosca *et al.* 2012), and/or lower chemical density contrast (typically,  $\Delta \eta_C$  around 10 and less). In these models, the depressions associated with reservoirs of primordial material are much attenuated, as illustrated by model TC7, and would therefore have a limited influence on excess CMB ellipticity. Interestingly, such models still predict long-wavelength topographies that are distinct from those obtained for purely thermal convection (Fig. 13), with, for models with  $\Delta \eta_C$  around 10 a correlation with shear wave velocity anomalies that is still important (around 0.6 for model TC8). In addition, the link between dynamic topography and observed excess ellipticity may be affected by other factors. First, it should be kept in mind that the period of the FCN constrains the dynamic flattening, and that interpreting this flattening in terms of geometric flattening requires the prescription of a non-hydrostatic layer at the top of the outer core, with thickness and density as free parameters. Moreover, it has been pointed out that other components of CMB topography than its  $Y_{20}$  term may influence the period of the FCN (Wu & Wahr 1997), and therefore the VLBI measurements



Figure 15. Topographic profiles along different great circles for (a,b) model T1 (Fig. 4), (c) model TC1 (Fig. 5), and (d) model TC4 (Figs 9a–d). Note that the scale of the vertical axis is exaggerated by about a factor 115 compared to that of the horizontal axis, that is, profiles appear much steeper than in real data.

and the estimates of the excess CMB ellipticity inferred from them. Finally, gravitational and viscous couplings between specific mantle structures (e.g. LLSVPs) and the core may also affect the period of the FCN. For instance, a recent study (Chao 2017) showed that the 6 yr periodic variations of the length of the day are well explained by gravitational coupling between the inner core and the lowermost mantle. Interestingly, this coupling implies mass excess in regions overlapping LLSVPs (Ding & Chao, submitted), thus contradicting the Stoneley mode analysis of Koelemeijer *et al.* (2017), but supporting earlier normal mode studies (Ishii & Tromp 1999; Trampert *et al.* 2004; Mosca *et al.* 2012). The effect of this coupling on the period of the FCN, however, remains to be investigated.

#### **5.5 Implications for core dynamics**

Another interesting question that remains to be investigated is the effect of dynamic topography on outer core flow. Calkins *et al.* (2012) run core flow models in cylindrical geometry with ridges (i.e. trenches on the mantle side) of Gaussian shape, and found that this topography results in stationary Rossby waves, which, in turn, increase the strength of the zonal flow and induce flow structures that remain fixed relative to the mantle. More recently, Tarduno *et al.* (2015) suggested that a step-like topography in CMB due to the African LLSVP could induce upwellings at the top of the core beneath the south of Africa, resulting in reversed magnetic flux at the CMB and persistent low magnetic field at the surface of the Earth. The gradient topography predicted by our models are rather modest, as illustrated in Fig. 15 (note that the scale of vertical axis is exaggerated by about a factor 115 compared to that of the horizontal axis). For instance, the positive topography induced by plume cluster in model T1 gently increases up to its culminating point (Fig. 15a). The depressions induced by thermochemical reservoirs in model TC1 are flat with marked slopes on their edges, but the gradient of these slopes are typically around 2–4 m km<sup>-1</sup> (Fig. 15c). In models with small chemical density contrast, the depressions induced by piles are attenuated and much shallower than the negative topography beneath slabs (Fig. 15d). Slabs induce deeper and steeper depressions on more localised areas, but again, topographic gradients remain limited, up to 15 m km<sup>-1</sup> (Fig. 15b). Thus, if CMB topography of real Earth is well described by the dynamic topography predicted by our models, it may have a limited influence on the outer core flow.

## **6 CONCLUSIONS**

We calculated the dynamic topography at CMB induced by different models of mantle convection, and investigated the influence of important input parameters of these models. In all models, cold

downwellings, modelling slabs, induce very deep, but local depressions. In purely thermal models, plumes or plume clusters induce positive topography that decreases in amplitude as the thermal viscosity ratio increases. For moderate buoyancy ratios, corresponding to compositional density contrast ( $\Delta \rho_C$ ) in the range 100–200 kg m<sup>-3</sup>, consistent with estimates of chemical density anomalies in the lowermost mantle (Trampert *et al.* 2004; Mosca *et al.* 2012), large, stable reservoirs of primordial material are generated. In their interiors, these reservoirs cause depressions in the CMB topography, surrounded by a ridge at their edges. The depth of the depressions and the height of the ridges increase with increasing  $\Delta \rho_C$  and chemical viscosity contrast ( $\Delta \eta_C$ ). The presence of the pPv phase at the bottom of the mantle does not alter these conclusions, provided that the viscosity of pPv is similar to that of bridgmanite. If, in contrast, pPv viscosity is lower by 2 orders of magnitude or more (Amman *et al.* 2010), the CMB topography may substantially flatten out, as suggested by models in which a weak (low viscosity) layer is imposed at the bottom of the mantle (Yoshida 2008; Soldati *et al.* 2012). Additional calculations are, however, needed to determine the influence of discontinuous patches of weak pPv, as those obtained in models T1-pPv (Figs 7c and d) and TC1-pPv (Figs 8e and f).

The peak-to-peak amplitude of CMB dynamic topography predicted by our models for different spherical harmonic filters is comparable to that estimated by available seismic constraints on CMB topography. Purely thermal models usually have larger amplitude than thermochemical models with similar properties, and for spherical harmonic filters including degree  $l = 2$  and degrees  $l = 2$ and  $l = 4$ , the amplitude predicted by purely thermal models is overall slightly larger than the maximum amplitude estimated from seismic data. Because it is sensitive to other model parameters, peak-to-peak amplitude alone is however unlikely to discriminate between purely thermal and thermochemical structures of lower mantle. On another hand, a comparison between long-wavelength patterns of shear wave velocity anomalies and topography may provide important clues. The positive topography induced by plumes, when filtered to long wavelengths, anticorrelates with shear wave velocity anomalies induced by the thermal field. By contrast, for thermochemical models, long-wavelength CMB topography correlates well with seismic velocity anomalies for models with  $\Delta \rho_C$ around 140 kg m−<sup>3</sup> or more and intrinsically more viscous primordial material ( $\Delta \eta_C > 1$ ). Shear wave velocity and CMB topography maps progressively decorrelate with decreasing  $\Delta \rho_C$  or decreasing  $\Delta \eta_C$ , and for  $\Delta \rho_C$  around 90 kg m<sup>-3</sup> and less, CMB topography and shear wave velocity anticorrelates, as for purely thermal cases. Long-wavelength pattern of CMB topography, provided they can be measured accurately, therefore provides a potential constraint to discriminate between different possible thermochemical structures of lowermost mantle.

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All data and models used in this study are available upon request to FD [\(frederic@earth.sinica.edu.tw\)](file:frederic@earth.sinica.edu.tw).

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