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# Sr v-vi line widths in hot white dwarf atmospheres 

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#### Abstract

Missing Stark widths for 37 spectral lines of strontium ions ( $17 \mathrm{Sr} v$ lines and 20 Sr VI lines) have been calculated using a quantum-mechanical method. Twenty-three spectral lines of $\operatorname{Sr} v$ have been recently discovered, for the first time, in the ultraviolet spectrum of the hot white dwarf RE 0503-289. This recent discovery prompts us to calculate the Stark widths of the new lines. These calculations can fill the lack of the data base STARK-B and can be used to investigate the observed spectra in such stars. To perform the line broadening calculations, preliminary structure and collision calculations have been carried out using the sequence of the University College London codes (SUPERSTRUCTURE, DISTORTED WAVE, and JAJOM). Results for the 37 lines are provided for different electron temperatures and at density $N_{\mathrm{e}}=10^{17} \mathrm{~cm}^{-3}$. These results will enter the STARK-B data base, which is a node of the Virtual Atomic and Molecular Data Center. We hope that the obtained results will be useful for the non-local thermodynamic equilibrium modelling of stellar atmospheres.


Key words: atomic data - line: profiles - stars: atmospheres - stars: individual: RE 0503-289 - white dwarfs.

## 1 INTRODUCTION

Line broadening and atomic parameters of the emitters are necessary in the analysis and interpretation of the spectra recorded by spectrographs. Also, reliable measurements and calculations of these parameters are strongly needed for stellar atmosphere modelling. In Rauch et al. (2016a), the authors showed that the lack of structural and radiative atomic data of many elements is an obstacle to their abundance analysis, in particular for high ionization stages (IV-VII). Stark width data have solved many problems in the diagnostics of astrophysical plasma. Line widths of many elements are required to explore the stellar opacity and the radiative transfer (Dimitrijević 2003). Stark broadening is the main broadening mechanism of lines in different astrophysical conditions of density and temperature, especially for white dwarfs (WDs). Therefore, the lack of Stark broadening data can affect the accuracy of element abundance determination. Recently, Elabidi (2021) showed that the Stark broadening mechanism is dominant in hot WDs' atmospheres; Sahal-Bréchot \& Elabidi (2021) showed that the Stark broadening mechanism is dominant in hot stars' atmospheres; Dimitrijević (2020) showed that the mechanism of Stark broadening is dominant in WDs of types A and B; and Aloui et al. (2019a) showed that the Stark broadening mechanism is dominant in hot helium-rich white dwarfs (spectral type DO). In the past, WDs were known as heliumrich (DB) and hydrogen-rich (DA) types. Nowadays, many papers (Rauch et al. 2017a,b, 2020; Werner et al. 2018a; Werner, Rauch \& Kruk 2018b) have proved the existence of spectral lines emitted by several heavy elements in the UV spectra of hot WDs. Rauch et al. (2017b) mentioned that for the spectral analysis of high-

[^0]resolution hot WDs, accurate results of atomic data are prerequisite for advanced non-local thermodynamic equilibrium (NLTE) stellar atmosphere modelling. These models should contain the opacity of heavy elements. In the meantime, 18 trans-iron elements with atomic numbers in the range $Z=29-56$ were detected in the RE 0503-289 hot WD stars (Rauch et al. 2020). Recently, Rauch et al. (2017b) detected several heavy elements in hot WDs (Se v, Sr v, Te VI, and I VI). The inaccuracy or the lack of atomic and Stark broadening parameters represents a handicap for spectral analysis by means of NLTE model atmospheres (Rauch et al. 2007).

In our work, we concentrate on two ions: first, the Srv ion, for which Rauch et al. (2017b) discovered 23 new lines in the UV spectrum of the hot WD RE 0503-289; secondly, the Sr VI ion that Persson \& Pettersson (1984) and O’Sullian \& Maher (1989) identified several lines for the first time. Rauch et al. (2017b) showed that the strongest Sr vi lines (identified by Persson \& Pettersson 1984; O'Sullian \& Maher 1989) are belonging to the extreme ultraviolet (EUV) and X-ray wavelength range of the DO WD RE 0503-289 spectrum. Spectra have been recorded with the Far Ultraviolet Spectroscopic Explorer (FUSE) and the Hubble Space Telescope (HST).

The aim of our work is to calculate the Stark widths of 17 Sr v lines (among the 23 new lines discovered by Rauch et al. 2017b) and the Stark widths of 20 Sr VI lines (among the strongest Sr vi lines identified by Persson \& Pettersson 1984 and O’Sullian \& Maher 1989). Along our calculations, atomic data (energy levels, line strengths, oscillator strengths, and spontaneous transition probabilities) for Srv and Sr vI ions have been calculated using the University College London (UCL) codes [SUPERSTRUCTURE (SST) (Eissner, Jones \& Nussbaumer 1974)/DISTORTED WAVE (DW) (Eissner 1998)/JAJOM (Saraph 1978)]. When comparisons are possible, we evaluate and compare the current atomic parameters used in the line-width calculations to ensure a good accuracy of the results. To perform the line broadening calculations, we have used our quantum-
mechanical method (Elabidi, Ben Nessib \& Sahal-Bréchot 2004; Elabidi et al. 2008). We applied this method many times (Aloui et al. 2018; Elabidi \& Sahal-Bréchot 2019; Aloui, Elabidi \& Sahal-Bréchot 2019b, 2020, 2021), and we found that it gives accurate results compared with other approaches that can be used with confidence in plasma diagnostics. The calculations have been performed at electron density $N_{\mathrm{e}}=10^{17} \mathrm{~cm}^{-3}$ and for electron temperatures between $10^{4}$ and $5 \times 10^{5} \mathrm{~K}$. Stark-width results for Sr VI and Sr VI are missing in the literature despite their importance for stellar plasma investigation. We hope that our calculations can fill the lack and enrich the data base STARK-B (Sahal-Bréchot, Dimitrijević \& Moreau 2022). We introduce in Section 2 a brief description of our method and the numerical procedure used in the calculations. We provide our structure, radiative, and Stark broadening results and we discuss the validity conditions of the used approximations in Section 3. In Section 4, we investigate the influence of Stark broadening in the spectra of hot WDs. Finally, we conclude in Section 5.

## 2 BRIEF OVERVIEW OF THE LINE BROADENING METHOD

To calculate the electron Stark broadening of Sr V and Sr vi lines, we have used our quantum mechanical method (Elabidi et al. 2004, 2008). The full width at half-maximum (FWHM) $W$ is

$$
\begin{align*}
W= & 2 N_{\mathrm{e}}\left(\frac{\hbar}{m}\right)^{2}\left(\frac{2 m \pi}{k_{\mathrm{B}} T}\right)^{\frac{1}{2}} \\
& \times \int_{0}^{\infty} \Gamma_{w}(\epsilon) \exp \left(-\frac{\epsilon}{k_{\mathrm{B}} T}\right) \mathrm{d}\left(\frac{\epsilon}{k_{\mathrm{B}} T}\right), \tag{1}
\end{align*}
$$

where $m$ denotes the electron mass, $k_{\mathrm{B}}$ denotes the Boltzmann constant, $N_{\mathrm{e}}$ denotes the electron density, $T$ denotes the electron temperature, $\epsilon$ denotes the energy of the incident electron, and

$$
\begin{align*}
\Gamma_{w}(\epsilon)= & \sum_{J_{i}^{T} J_{f}^{T} l K_{i} K_{f}} \frac{\left[K_{i}, K_{f}, J_{i}^{T}, J_{f}^{T}\right]}{2} \\
& \times\left\{\begin{array}{c}
J_{i} K_{i} l \\
K_{f} J_{f} 1
\end{array}\right\}^{2}\left\{\begin{array}{c}
K_{i} J_{i}^{T} s \\
J_{f}^{T} K_{f} 1
\end{array}\right\}^{2} \\
& \times\left[1-\left(\operatorname{Re}\left(\mathbf{S}_{i}\right) \operatorname{Re}\left(\mathbf{S}_{f}\right)+\operatorname{Im}\left(\mathbf{S}_{i}\right) \operatorname{Im}\left(\mathbf{S}_{f}\right)\right)\right] \tag{2}
\end{align*}
$$

where $L_{i}+\mathbf{S}_{i}=J_{i}, J_{i}+l=K_{i}$, and $K_{i}+s=J_{i}^{T} . L$ and $S$ are respectively the orbital and spin momenta of the target and $l$ and $s$ are those of the incident electron. The superscript $T$ refers to the operators of the system (electron + target). $\mathbf{S}_{i}\left(\mathbf{S}_{f}\right)$ designates the scattering matrix elements for the initial (final) levels in intermediate coupling. $\operatorname{Re}(\mathbf{S})$ and $\operatorname{Im}(\mathbf{S})$ are the real and the imaginary parts of the $\mathbf{S}$ matrix, respectively. $\left\{\begin{array}{l}a b c \\ d e f\end{array}\right\}$ are the $6-\mathrm{j}$ symbols and we use the notation $[x, y, \ldots]=(2 x+1)(2 y+1) \ldots . \operatorname{Re} \mathbf{S}$ and $\operatorname{Im} \mathbf{S}$ are derived using the following expressions:
$\operatorname{Re} \mathbf{S}=\left(1-\mathbf{R}^{2}\right)\left(1+\mathbf{R}^{2}\right)^{-1}, \operatorname{Im} \mathbf{S}=2 \mathbf{R}\left(1+\mathbf{R}^{2}\right)^{-1}$.
$\mathbf{S}_{i}$ and $\mathbf{S}_{f}$ are calculated at the same electron energy $\epsilon=m v^{2} / 2$. The atomic data in intermediate coupling have been calculated by the SUPERSTRUCTURE (SST) code (Eissner et al. 1974), where configuration interaction and relativistic corrections (spin-orbit, mass, Darwin, and one-body) are taken into account according to the Breit-Pauli approach (Bethe \& Salpeter 1957). The radial wave functions are determined by diagonalization of the non-relativistic Hamiltonian using orbitals calculated in a scaled Thomas-Fermi-Dirac-Amaldi (TFDA) potential. The potential depends on $\lambda_{l}$ (scaling parameters),
which are determined by a self-consistent energy minimization on the term energies used in our calculations. The electron-ion scattering calculations are performed by the DW code (Eissner 1998), producing reaction matrices $\mathbf{R}$ in Russell-Saunders (LS) coupling. The scattering calculations in intermediate coupling (IC) are treated by the JAJOM code (Saraph 1978). This code uses the term coupling coefficients (TCCs) - resulting from SST - and the $\mathbf{R}$ matrices in LS coupling (obtained by DW) to calculate collision strengths. JAJPOLARI is the transformed version of JAJOM (Elabidi \& Dubau, unpublished results) that produces the reactance matrices $\mathbf{R}$ in intermediate coupling. The code RTOS (Dubau, unpublished results) calculates the scattering matrices $\mathbf{S}$ from the reactance matrices $\mathbf{R}$ and the real $(\mathrm{ReS})$ and the imaginary ( $\operatorname{ImS}$ ) parts of the scattering matrices $\mathbf{S}$, and arranges them as input suitable for formula (2). Feshbach resonances are included by means of the Gailitis formula (Gailitis 1963). We have extrapolated the factor $\Gamma_{w}(\epsilon)$ in formula (2), which contains the scattering matrix $\mathbf{S}$ below the threshold for the corresponding inelastic process. We have shown in Elabidi, Ben Nessib \& Sahal-Bréchot (2009) that the inclusion of Feshbach resonances improves the agreement with experimental results, especially for low temperature.

## 3 RESULTS AND DISCUSSION

### 3.1 Structure and radiative data

We have used in SST (Eissner et al. 1974) five configurations for Sr v: $3 d^{10}\left(4 s^{2} 4 p^{4}, 4 s 4 p^{5}, 4 s^{2} 4 p^{3} 4 d, 4 s^{2} 4 p^{3} 5 s\right.$, and $\left.4 s^{2} 4 p^{3} 5 p\right)$. These configurations give us 85 fine structure levels and 43 LS terms. For Sr vi, we have used three configurations, $3 \mathrm{~d}^{10}\left(4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}, 4 \mathrm{~s} 4 \mathrm{p}^{4}\right.$, and $4 s^{2} 4 p^{2} 5 s$ ), giving 21 fine structure levels and 11 LS terms. In Table 1, we display the present fine structure energy levels for Sr V in $\mathrm{cm}^{-1}$ and compare them with the National Institute of Standards and Technology (NIST) results (Kramida et al. 2021). The average error between our calculations and NIST results is less than 2 percent. In Table 2, we display our fine structure energy levels for Sr VI in $\mathrm{cm}^{-1}$ and we compare them with the multiconfiguration Dirac-Fock (MCDF) results of Charro \& Martín (1998) using the GRASP code developed by Grant et al. (1980) and Grant (1989), with the results of NIST (Kramida et al. 2021) and with the experimental results (Exp.) of Wyart \& Artru (1989). We present also in Table 2 the average errors between our calculations and all the other results which are less than 4 per cent. Table 3 displays our transition probabilities $A_{i j}$, weighted oscillator strengths $g f$, and line strengths $S$ for $\operatorname{Srv}$ allowed transitions involving the ground and first excited levels. Table 4 displays our transition probabilities $A_{i j}$ compared with the experimental results (Sansonetti 2012), weighted oscillator strengths $g f$ compared with the MCDF results provided by O'Sullian (1989) using the MCDF code of Grant et al. (1980), and line strengths $S$ for $\operatorname{Sr}$ VI allowed transitions involving the first five levels. The average error $\Delta_{\text {Exp. }}$. between our calculations and the measurements for $A_{j i}$ is $\sim 33$ per cent, the transition $4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{4} \mathrm{P}_{5 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{4} \mathrm{~S}_{3 / 2}^{0}(16-1)$ presents the higher error. The average difference $\Delta_{\text {MCDF }}$ between our calculations and the MCDF results for $g f$ is $\sim 30$ per cent. The highest difference is found for the two transitions $4 s^{2} 4 p^{2} 5 s^{4} \mathrm{P}_{5 / 2}-$ $4 \mathrm{~s}^{2} 4 \mathrm{p}^{34} \mathrm{~S}_{3 / 2}^{0}(16-1)$ and $4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{D}_{3 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{32} \mathrm{D}_{3 / 2}^{0}(20-2)$.

### 3.2 Line broadening results

### 3.2.1 Impact approximation

Before starting the calculations, we prove hereafter the validity of the impact approximation and the ideal plasma approximation for the plasma temperatures and density used in our work.

Table 1. Current $\operatorname{Sr}$ V fine structure energy levels (in $\mathrm{cm}^{-1}$ ) compared with the NIST results (Kramida et al. 2021).

| $i$ | Level | Current | NIST | $i$ | Level | Current | NIST |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{4}{ }^{3} \mathrm{P}_{2}$ | 0.0 | 0.0 | 44 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{3} \mathrm{P}^{0}$ | 288382 | 275425 |
| 2 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{4}{ }^{3} \mathrm{P}_{1}$ | 8166 | 8308 | 45 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{D}_{1}^{\mathrm{o}}$ | 288896 | 280067 |
| 3 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{4}{ }^{3} \mathrm{P}_{0}$ | 9085 | 8718 | 46 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{~s}^{3} \mathrm{D}_{2}^{0}$ | 291049 | 289117 |
| 4 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{41} \mathrm{D}_{2}$ | 23172 | 20311 | 47 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{3} \mathrm{P}_{1}^{0}$ | 291192 | 269615 |
| 5 | $4 s^{2} 4 p^{4}{ }^{1} \mathrm{~S}_{0}$ | 50557 | 44050 | 48 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{~s}^{3} \mathrm{D}_{3}^{\mathrm{o}}$ | 293001 | 291836 |
| 6 | $4 \mathrm{~s} 4 \mathrm{p}^{5}{ }^{3} \mathrm{P}_{2}^{0}$ | 149729 | 154032 | 49 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{~s}^{3} \mathrm{D}_{1}^{\mathrm{o}}$ | 293148 | 288832 |
| 7 | $4 \mathrm{~s} 4 \mathrm{p}^{5}{ }^{3} \mathrm{P}_{1}^{\mathrm{o}}$ | 155821 | 160018 | 50 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{1} \mathrm{D}_{2}^{\mathrm{o}}$ | 295986 | 285450 |
| 8 | $4 \mathrm{~s} 4 \mathrm{p}^{5}{ }^{3} \mathrm{P}_{0}^{0}$ | 159642 | 164016 | 51 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{~s}{ }^{1} \mathrm{D}_{2}^{\text {o }}$ | 297391 | 294818 |
| 9 | $4 \mathrm{~s} 4 \mathrm{p}^{5}{ }^{1} \mathrm{P}_{1}^{0}$ | 193987 | 193319 | 52 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{1} \mathrm{~F}_{3}^{\mathrm{o}}$ | 306945 | 291678 |
| 10 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{5} \mathrm{D}_{0}^{0}$ | 198843 | 202129 | 53 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{0}\right) 5 \mathrm{p}{ }^{5} \mathrm{P}_{1}$ | 309307 | 313726 |
| 11 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{5} \mathrm{D}_{1}^{\mathrm{o}}$ | 198945 | 202265 | 54 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{5} \mathrm{P}_{2}$ | 309903 | 314143 |
| 12 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{0}\right) 4 \mathrm{~d}{ }^{5} \mathrm{D}_{2}^{0}$ | 199013 | 202321 | 55 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 5 \mathrm{~s}{ }^{3} \mathrm{P}_{0}^{\mathrm{o}}$ | 310602 | 306607 |
| 13 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{5} \mathrm{D}_{3}^{\mathrm{o}}$ | 199105 | 202398 | 56 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 5 \mathrm{~s}{ }^{3} \mathrm{P}_{1}^{\mathrm{o}}$ | 311375 | 307806 |
| 14 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{5} \mathrm{D}_{4}^{\text {o }}$ | 199480 | 202913 | 57 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{5} \mathrm{P}_{2}$ | 311623 | 314143 |
| 15 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{3} \mathrm{~F}_{2}^{0}$ | 214461 | 220550 | 58 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 5 \mathrm{~s}{ }^{3} \mathrm{P}_{2}^{\mathrm{o}}$ | 314583 | 311700 |
| 16 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{3} \mathrm{D}_{3}^{\mathrm{o}}$ | 216263 | 216104 | 59 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{P}_{1}$ | 317927 | 319835 |
| 17 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{3} \mathrm{D}_{1}^{o}$ | 217174 | 216969 | 60 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 5 \mathrm{~s}{ }^{1} \mathrm{P}_{1}^{\mathrm{o}}$ | 318290 | 314736 |
| 18 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{D}_{2}^{\mathrm{o}}$ | 221806 | 213783 | 61 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{P}_{2}$ | 318878 | 321239 |
| 19 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{3} \mathrm{~F}_{3}^{o}$ | 223599 | 222368 | 62 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{P}_{0}$ | 319423 | 321641 |
| 20 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{o}\right) 4 \mathrm{~d}{ }^{1} \mathrm{~S}_{0}^{o}$ | 225196 | 221778 | 63 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{1} \mathrm{P}_{1}^{0}$ | 323767 | 306075 |
| 21 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{o}\right) 4 \mathrm{~d}^{3} \mathrm{~F}_{4}^{o}$ | 225913 | 224844 | 64 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{D}_{1}$ | 331597 | 331198 |
| 22 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{3} \mathrm{G}_{3}^{0}$ | 231576 | 229950 | 65 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{D}_{2}$ | 334606 | 336695 |
| 23 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{G}_{4}^{\text {o }}$ | 232451 | 230974 | 66 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{D}_{3}$ | 336666 | 339930 |
| 24 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{G}_{5}^{0}$ | 233779 | 232586 | 67 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{~F}_{2}$ | 337041 | 334365 |
| 25 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{1} \mathrm{G}_{4}^{\text {o }}$ | 237154 | 234783 | 68 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{1} \mathrm{P}_{1}$ | 337627 | 337454 |
| 26 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{0}\right) 4 \mathrm{~d}{ }^{1} \mathrm{D}_{2}^{0}$ | 244351 | 241479 | 69 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{1} \mathrm{~F}_{3}$ | 339092 | 338692 |
| 27 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{D}_{1}^{\mathrm{o}}$ | 246943 | 243577 | 70 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{~F}_{3}$ | 340168 | 336623 |
| 28 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{P}_{0}^{0}$ | 250870 | 246801 | 71 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{~F}_{4}$ | 340333 | 340419 |
| 29 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{D}_{2}^{0}$ | 251425 | 248383 | 72 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{P}_{2}$ | 347431 | 343583 |
| 30 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{P}_{1}^{0}$ | 252152 | 248012 | 73 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{P}_{0}$ | 347977 | 345057 |
| 31 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{~F}_{3}^{\mathrm{o}}$ | 253407 | 249673 | 74 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{P}_{1}$ | 348012 | 345344 |
| 32 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{~F}_{2}^{0}$ | 254405 | 250657 | 75 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{0}\right) 5 \mathrm{p}{ }^{3} \mathrm{D}_{2}$ | 354666 | 356567 |
| 33 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{~F}_{4}^{\mathrm{o}}$ | 254509 | 251234 | 76 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{1} \mathrm{P}_{1}$ | 356251 | 363332 |
| 34 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{D}_{3}^{0}$ | 256485 | 253340 | 77 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{~S}_{1}$ | 358639 | 357248 |
| 35 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{3} \mathrm{P}_{2}^{0}$ | 258869 | 255119 | 78 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{1} \mathrm{D}_{2}$ | 358808 | 351337 |
| 36 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{\mathrm{o}}\right) 5 \mathrm{~s}{ }^{5} \mathrm{~S}_{2}^{0}$ | 262853 | 266325 | 79 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{0}\right) 5 \mathrm{p}^{3} \mathrm{D}_{1}$ | 361113 | 353845 |
| 37 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{3} \mathrm{~S}_{1}^{o}$ | 269583 | 265179 | 80 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{D}_{3}$ | 361155 | 359647 |
| 38 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{1} \mathrm{~F}_{3}^{0}$ | 271058 | 266239 | 81 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{P}_{0}$ | 362393 | 358076 |
| 39 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{\mathrm{o}}\right) 5 \mathrm{~s}^{3} \mathrm{~S}_{1}^{o}$ | 274224 | 274952 | 82 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{P}_{1}$ | 365646 | 357554 |
| 40 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{3} \mathrm{P}_{2}^{0}$ | 280082 | 267351 | 83 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{0}\right) 5 \mathrm{p}{ }^{1} \mathrm{D}_{2}$ | 367023 | 362487 |
| 41 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{D}_{3}^{\text {o }}$ | 282970 | 271500 | 84 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{P}_{2}$ | 367172 | 364887 |
| 42 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{1} \mathrm{P}_{1}^{0}$ | 284362 | 275488 | 85 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{1} \mathrm{~S}_{0}$ | 382131 | 375152 |
| 43 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{0}\right) 4 \mathrm{~d}^{3} \mathrm{D}_{2}^{0}$ | 287858 | 276821 |  |  |  |  |

The impact approximation states that the duration $\tau$ of an interaction must be much smaller than the mean interval time $\Delta T$ between two collisions (Baranger 1958):
$\tau \ll \Delta T$.
$\tau$ can be expressed as $\frac{\rho_{\text {typ }}}{v_{\text {typ }}}$, where $\rho_{\text {typ }}$ is a typical impact parameter and $v_{\text {typ }}$ is a mean typical velocity. $\Delta T$ is of the order of the inverse of the collisional line width, that is roughly equal to $N_{\mathrm{e}} v_{\text {typ }} \rho_{\text {typ }}^{2}$. Consequently, we can write the validity condition of the impact approximation as
$\rho_{\text {typ }} \ll N_{\mathrm{e}}^{-1 / 3}$.
$\rho_{\text {typ }}^{3}$ is the 'collision volume', which must be smaller than the volume of one perturber $N_{\mathrm{e}}^{-1}$. We can write the impact approximation condition in terms of the orbital momentum of the perturber and temperature. In fact, the classical angular momentum $\boldsymbol{L}=\rho m v$ can be related to the eigenvalues of the corresponding quantum-mechanical
operator $\boldsymbol{L}^{2}$ by $\boldsymbol{L}^{2}=(\rho m v)^{2}=\hbar^{2} l(l+1) \Longrightarrow \rho^{2}=\frac{\hbar^{2} l(l+1)}{(m v)^{2}}$, and using the expression of the velocity averaged over the MaxwellBoltzmann distribution $v=\sqrt{\frac{8 k_{\mathrm{B}} T}{\pi m}}$ we find that a typical 'collision volume' can be written as (with $T_{\mathrm{typ}}=5 \times 10^{5} \mathrm{~K}$ and $l_{\mathrm{typ}}=29$ )
$\rho_{\mathrm{typ}}=\left(\frac{\pi l_{\mathrm{typ}}^{2} \hbar^{2}}{8 m k_{\mathrm{B}} T_{\mathrm{typ}}}\right)^{1 / 2}=7.65 \times 10^{-8} \mathrm{~cm}$.
With $N_{\mathrm{e}}=10^{17} \mathrm{~cm}^{-3}$, we find $\rho_{\text {typ }} \ll N_{\mathrm{e}}^{-1 / 3}=2.14 \times 10^{-6} \mathrm{~cm}$.

### 3.2.2 Approximation of ideal plasma

In order to prove that the criterion of plasma ideality is valid for the density and electron temperatures chosen in our work, it must be shown that the number of particles (perturbers) $N_{\mathrm{D}}$ inside the Debye sphere of radius $R_{\mathrm{D}}$ (the distance over which electric charges screen out the electric fields) is greater than 1 . This can be written as

Table 2. Current Sr vi fine structure energy levels (in $\mathrm{cm}^{-1}$ ) compared with the MCDF results (Charro \& Martín 1998) using the GRASP code developed by Grant et al. (1980) and Grant (1989), with the NIST results (Kramida et al. 2021) and with the experimental results (Exp.) of Wyart \& Artru (1989). $\Delta_{\mathrm{X}}$ represents the relative error between our calculations and the results of $X$.

| $i$ | Level | Present | MCDF | NIST | Exp. | $\Delta_{\text {MCDF }}$ | $\Delta_{\text {NIST }}$ | $\Delta_{\text {Exp }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{4} \mathrm{~S}_{3 / 2}^{\mathrm{o}}$ | 0.0 | 0.0 | 0.0 | - | - | - | - |
| 2 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{D}_{3 / 2}^{\mathrm{o}}$ | 24653 | 24803 | 20135 | - | 1 | 18 | - |
| 3 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{D}_{5 / 2}^{\mathrm{o}}$ | 27508 | 28684 | 23527 | - | 4 | 14 | - |
| 4 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{P}_{1 / 2}^{\mathrm{o}}$ | 45048 | 40809 | 38531 | - | 10 | 14 | - |
| 5 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{P}_{3 / 2}^{0}$ | 49123 | 46013 | 43567 | - | 7 | 11 | - |
| 6 | $4 \mathrm{~s} 4 \mathrm{p}^{4}{ }^{4} \mathrm{P}_{5 / 2}$ | 158470 | - | 153171 | - | - | 3 | - |
| 7 | $4 \mathrm{~s} 4 \mathrm{p}^{4}{ }^{4} \mathrm{P}_{3 / 2}$ | 164772 | - | 159597 | - | - | 3 | - |
| 8 | $4 \mathrm{~s} 4 \mathrm{p}^{4}{ }^{4} \mathrm{P}_{1 / 2}$ | 167575 | - | 162238 | - | - | 3 | - |
| 9 | $4 \mathrm{~s} 4 \mathrm{p}^{4}{ }^{2} \mathrm{D}_{3 / 2}$ | 212487 | - | 188319 | - | - | 11 | - |
| 10 | $4 \mathrm{~s} 4 \mathrm{p}^{4}{ }^{2} \mathrm{D}_{5 / 2}$ | 213319 | - | 189978 | - | - | 11 | - |
| 11 | $4 \mathrm{~s} 4 \mathrm{p}^{4}{ }^{2} \mathrm{~S}_{1 / 2}$ | 238724 | - | 227292 | - | - | 5 | - |
| 12 | $4 \mathrm{~s} 4 \mathrm{p}^{4}{ }^{2} \mathrm{P}_{3 / 2}$ | 258959 | - | 215697 | - | - | 17 | - |
| 13 | $4 \mathrm{~s} 4 \mathrm{p}^{4}{ }^{2} \mathrm{P}_{1 / 2}$ | 266993 | - | 216644 | - | - | 19 | - |
| 14 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}{ }^{4} \mathrm{P}_{1 / 2}$ | 331030 | 328485 | 327320 | 327472 | 1 | 1 | 1 |
| 15 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}{ }^{4} \mathrm{P}_{3 / 2}$ | 335906 | 334076 | 333260 | 333414 | 1 | 1 | 1 |
| 16 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{4} \mathrm{P}_{5 / 2}$ | 341062 | 337474 | 338650 | 338739 | 1 | 1 | 1 |
| 17 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{P}_{1 / 2}$ | 343329 | 341072 | 338240 | 338399 | 1 | 1 | 1 |
| 18 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{P}_{3 / 2}$ | 348889 | 347223 | 343870 | 343976 | 0 | 1 | 1 |
| 19 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{D}_{5 / 2}$ | 360937 | 360449 | 355820 | 355890 | 0 | 1 | 1 |
| 20 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{D}_{3 / 2}$ | 361875 | 361481 | 356820 | 356928 | 0 | 1 | 1 |
| 21 | $4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{~S}_{1 / 2}$ | 387831 | 388487 | 378990 | 379200 | 0 | 2 | 2 |

Table 3. Current spontaneous transition probabilities $A_{i j}$, weighted oscillator strengths $g f$, and line strengths $S$ for $\operatorname{Sr} \vee$ allowed transitions. $i$ and $j$ label the levels of Table 1 . We present only ten rows, and the remaining data are included in the supplementary material.

| $i-j$ | $A_{i j}\left(\mathrm{~s}^{-1}\right)$ | $g f$ | $S$ | $i-j$ | $A_{i j}\left(\mathrm{~s}^{-1}\right)$ | $g f$ | $S$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $6-1$ | $9.670 \mathrm{E}+08$ | $3.233 \mathrm{E}-01$ | 0.71093 | $6-2$ | $3.087 \mathrm{E}+08$ | $1.155 \mathrm{E}-01$ | 0.26855 |
| $7-1$ | $6.419 \mathrm{E}+08$ | $1.189 \mathrm{E}-01$ | 0.25121 | $7-2$ | $3.244 \mathrm{E}+08$ | $6.693 \mathrm{E}-02$ | 0.14923 |
| $9-1$ | $9.627 \mathrm{E}+07$ | $1.151 \mathrm{E}-02$ | 0.01953 | $8-2$ | $1.356 \mathrm{E}+09$ | $8.863 \mathrm{E}-02$ | 0.19262 |
| $11-1$ | $5.427 \mathrm{E}+07$ | $6.168 \mathrm{E}-03$ | 0.01021 | $9-2$ | $8.862 \mathrm{E}+06$ | $1.154 \mathrm{E}-03$ | 0.00205 |
| $12-1$ | $6.535 \mathrm{E}+07$ | $1.237 \mathrm{E}-02$ | 0.02046 | $10-2$ | $8.012 \mathrm{E}+07$ | $3.304 \mathrm{E}-03$ | 0.00570 |
| $13-1$ | $3.129 \mathrm{E}+07$ | $8.282 \mathrm{E}-03$ | 0.01370 | $11-2$ | $2.802 \mathrm{E}+07$ | $3.462 \mathrm{E}-03$ | 0.00598 |
| $15-1$ | $1.472 \mathrm{E}+08$ | $2.399 \mathrm{E}-02$ | 0.03683 | $12-2$ | $2.177 \mathrm{E}+05$ | $4.481 \mathrm{E}-05$ | 0.00008 |
| $16-1$ | $9.960 \mathrm{E}+07$ | $2.235 \mathrm{E}-02$ | 0.03402 | $15-2$ | $4.570 \mathrm{E}+07$ | $8.050 \mathrm{E}-03$ | 0.01285 |
| $17-1$ | $3.735 \mathrm{E}+07$ | $3.562 \mathrm{E}-03$ | 0.00540 | $17-2$ | $1.297 \mathrm{E}+08$ | $1.335 \mathrm{E}-02$ | 0.02104 |
| $18-1$ | $5.029 \mathrm{E}+07$ | $7.663 \mathrm{E}-03$ | 0.01137 | $18-2$ | $2.148 \mathrm{E}+07$ | $3.527 \mathrm{E}-03$ | 0.00544 |

Table 4. Current spontaneous transition probabilities $A_{i j}$ compared with the experimental results (Exp.) of Sansonetti (2012), weighted oscillator strengths $g f$ compared with the MCDF results of O'Sullian (1989) using the MCDF code of Grant et al. (1980), and line strengths $S$ for Sr VI allowed transitions. $i$ and $j$ label the levels of Table 2. $\Delta_{\mathrm{X}}$ represents the relative error between our calculations and the results of X . We present only ten rows, and the remaining data are included in the supplementary material.

| Levels $i-j$ | $A_{i j}\left(s^{-1}\right)$ |  |  | $g f$ |  |  | $S$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Current | Exp. | $\Delta_{\text {Exp. }}($ per cent $)$ | Current | MCDF | $\Delta_{\text {MCDF }}($ per cent $)$ |  |
| 6-1 | $4.657 \mathrm{E}+09$ | - | - | $1.668 \mathrm{E}+00$ | - | - | 3.465267 |
| 7-1 | $5.286 \mathrm{E}+09$ | - | - | $1.168 \mathrm{E}+00$ | - | - | 2.332652 |
| 8-1 | $5.631 \mathrm{E}+09$ | - | - | $6.013 \mathrm{E}-01$ | - | - | 1.181254 |
| 9-1 | $6.536 \mathrm{E}+07$ | - | - | $8.681 \mathrm{E}-03$ | - | - | 0.013450 |
| 11-1 | $8.108 \mathrm{E}+07$ | - | - | $4.266 \mathrm{E}-03$ | - | - | 0.005883 |
| 12-1 | $6.046 \mathrm{E}+08$ | - | - | $5.406 \mathrm{E}-02$ | - | - | 0.068732 |
| 13-1 | $4.594 \mathrm{E}+07$ | - | - | $1.933 \mathrm{E}-03$ | - | - | 0.002383 |
| 14-1 | $1.089 \mathrm{E}+10$ | $6.000 \mathrm{E}+09$ | 45 | $2.981 \mathrm{E}-01$ | $1.670 \mathrm{E}-01$ | 44 | 0.296414 |
| 15-1 | $1.086 \mathrm{E}+10$ | $8.500 \mathrm{E}+09$ | 22 | $5.772 \mathrm{E}-01$ | $3.050 \mathrm{E}-01$ | 47 | 0.565687 |
| 16-1 | $1.112 \mathrm{E}+10$ | $5.500 \mathrm{E}+09$ | 51 | $8.596 \mathrm{E}-01$ | $4.320 \mathrm{E}-01$ | 50 | 0.829764 |

Table 5. Our quantum full Stark widths $W$ for $17 \mathrm{Sr} v$ lines at electron density $N_{\mathrm{e}}=10^{17} \mathrm{~cm}^{-3}$ for different temperatures. The wavelengths $\lambda$ are taken from the SST code (Eissner et al. 1974).

| Transition | $T\left(10^{4} \mathrm{~K}\right)$ | $W(\mathrm{pm})$ | Transition | $W(\mathrm{pm})$ |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{0}\right) 4 \mathrm{~d}^{3} \mathrm{D}_{3}^{\mathrm{o}}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{1} \mathrm{D}_{2} \\ & \lambda=904.67 \AA \end{aligned}$ | 1 | $1.141 \mathrm{E}+01$ | $\begin{gathered} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{D}_{2}^{0}-4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{0}\right) 5 \mathrm{p}^{3} \mathrm{P}_{1} \\ \lambda=1040.35 \AA \end{gathered}$ | $1.186 \mathrm{E}+01$ |
|  | 2 | $7.703 \mathrm{E}+00$ |  | $8.024 \mathrm{E}+00$ |
|  | 4 | $4.604 \mathrm{E}+00$ |  | $4.915 \mathrm{E}+00$ |
|  | 6 | $3.515 \mathrm{E}+00$ |  | $3.863 \mathrm{E}+00$ |
|  | 8 | $2.950 \mathrm{E}+00$ |  | $3.331 \mathrm{E}+00$ |
|  | 10 | $2.585 \mathrm{E}+00$ |  | $2.996 \mathrm{E}+00$ |
| $\begin{aligned} & 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{0}\right) 4 \mathrm{~d}^{3} \mathrm{G}_{4}^{0}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{0}\right) 5 \mathrm{p}^{3} \mathrm{~F}_{3} \\ & \lambda=928.36 \AA \end{aligned}$ | 1 | $9.015 \mathrm{E}+00$ | $\begin{gathered} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 4 \mathrm{~d}{ }^{1} \mathrm{~F}_{3}^{\mathrm{o}}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{P}_{2} \\ \lambda=1040.43 \AA \end{gathered}$ | $1.982 \mathrm{E}+01$ |
|  | 2 | $6.019 \mathrm{E}+00$ |  | $1.143 \mathrm{E}+01$ |
|  | 4 | $3.486 \mathrm{E}+00$ |  | $6.254 \mathrm{E}+00$ |
|  | 6 | $2.586 \mathrm{E}+00$ |  | $4.644 \mathrm{E}+00$ |
|  | 8 | $2.127 \mathrm{E}+00$ |  | $3.841 \mathrm{E}+00$ |
|  | 10 | $1.839 \mathrm{E}+00$ |  | $3.336 \mathrm{E}+00$ |
| $\begin{aligned} & 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{0}\right) 4 \mathrm{~d}^{3} \mathrm{~F}_{4}^{\mathrm{o}}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{0}\right) 5 \mathrm{p}^{3} \mathrm{D}_{3} \\ & \lambda=937.68 \AA \end{aligned}$ | 1 | $1.444 \mathrm{E}+01$ | $\begin{gathered} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{0}\right) 4 \mathrm{~d}^{1} \mathrm{~F}_{3}^{0}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{1} \mathrm{D}_{2} \\ \lambda=1042.05 \AA \end{gathered}$ | $5.891 \mathrm{E}+01$ |
|  | 2 | $8.620 \mathrm{E}+00$ |  | $2.432 \mathrm{E}+01$ |
|  | 4 | $4.673 \mathrm{E}+00$ |  | $9.569 \mathrm{E}+00$ |
|  | 6 | $3.391 \mathrm{E}+00$ |  | $5.847 \mathrm{E}+00$ |
|  | 8 | $2.742 \mathrm{E}+00$ |  | $4.340 \mathrm{E}+00$ |
|  | 10 | $2.333 \mathrm{E}+00$ |  | $3.546 \mathrm{E}+00$ |
| $\begin{aligned} & 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{0}\right) 4 \mathrm{~d}^{3} \mathrm{P}_{1}^{\mathrm{o}}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{0}\right) 5 \mathrm{p}^{3} \mathrm{~S}_{1} \\ & \lambda=939.08 \AA \end{aligned}$ | 1 | $3.705 \mathrm{E}+01$ | $\begin{gathered} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{0}\right) 4 \mathrm{~d}^{1} \mathrm{D}_{2}^{0}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{1} \mathrm{P}_{1} \\ \lambda=1072.09 \AA \end{gathered}$ | $1.776 \mathrm{E}+01$ |
|  | 2 | $1.801 \mathrm{E}+01$ |  | $1.149 \mathrm{E}+01$ |
|  | 4 | $9.019 \mathrm{E}+00$ |  | $6.668 \mathrm{E}+00$ |
|  | 6 | $6.476 \mathrm{E}+00$ |  | $5.040 \mathrm{E}+00$ |
|  | 8 | $5.248 \mathrm{E}+00$ |  | $4.224 \mathrm{E}+00$ |
|  | 10 | $4.495 \mathrm{E}+00$ |  | $3.719 \mathrm{E}+00$ |
| $\begin{aligned} & 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{D}_{3}^{\mathrm{o}}-4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{0}\right) 5 \mathrm{p}^{3} \mathrm{P}_{2} \\ & \lambda=974.52 \AA \end{aligned}$ | 1 | $7.893 \mathrm{E}+00$ | $\begin{gathered} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{0}\right) 4 \mathrm{~d}^{3} \mathrm{D}_{2}^{0}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}^{3} \mathrm{~F}_{2} \\ \lambda=1168.01 \AA \end{gathered}$ | $2.294 \mathrm{E}+01$ |
|  | 2 | $5.329 \mathrm{E}+00$ |  | $1.463 \mathrm{E}+01$ |
|  | 4 | $3.219 \mathrm{E}+00$ |  | $8.543 \mathrm{E}+00$ |
|  | 6 | $2.500 \mathrm{E}+00$ |  | $6.511 \mathrm{E}+00$ |
|  | 8 | $2.143 \mathrm{E}+00$ |  | $5.458 \mathrm{E}+00$ |
|  | 10 | $1.925 \mathrm{E}+00$ |  | $4.777 \mathrm{E}+00$ |
| $\begin{aligned} & 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{0}\right) 4 \mathrm{~d}^{1} \mathrm{G}_{4}^{0}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{0}\right) 5 \mathrm{p}^{1} \mathrm{~F}_{3} \\ & \lambda=980.98 \AA \end{aligned}$ | 1 | $8.362 \mathrm{E}+00$ | $\begin{gathered} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{0}\right) 4 \mathrm{~d}^{3} \mathrm{D}_{1}^{\mathrm{o}}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}^{3} \mathrm{D}_{1} \\ \lambda=1181.28 \AA \end{gathered}$ | $2.018 \mathrm{E}+01$ |
|  | 2 | $5.425 \mathrm{E}+00$ |  | $1.650 \mathrm{E}+01$ |
|  | 4 | $3.135 \mathrm{E}+00$ |  | $1.121 \mathrm{E}+01$ |
|  | 6 | $2.359 \mathrm{E}+00$ |  | $8.688 \mathrm{E}+00$ |
|  | 8 | $1.969 \mathrm{E}+00$ |  | $7.267 \mathrm{E}+00$ |
|  | 10 | $1.726 \mathrm{E}+00$ |  | $6.343 \mathrm{E}+00$ |
| $\begin{aligned} & 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{0}\right) 4 \mathrm{~d}^{3} \mathrm{~F}_{3}^{0}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{0}\right) 5 \mathrm{p}^{3} \mathrm{D}_{2} \\ & \lambda=987.58 \AA \end{aligned}$ | 1 | $2.408 \mathrm{E}+01$ | $\begin{gathered} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{D}_{2}^{0}-4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{0}\right) 5 \mathrm{p}^{3} \mathrm{P}_{2} \\ \lambda=1482.52 \AA \end{gathered}$ | $3.215 \mathrm{E}+01$ |
|  | 2 | $1.239 \mathrm{E}+01$ |  | $1.878 \mathrm{E}+01$ |
|  | 4 | $6.262 \mathrm{E}+00$ |  | $1.118 \mathrm{E}+01$ |
|  | 6 | $4.449 \mathrm{E}+00$ |  | $8.891 \mathrm{E}+00$ |
|  | 8 | $3.570 \mathrm{E}+00$ |  | $7.655 \mathrm{E}+00$ |
|  | 10 | $3.037 \mathrm{E}+00$ |  | $6.822 \mathrm{E}+00$ |
| $\begin{aligned} & 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{D}_{1}^{\mathrm{o}}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}^{3} \mathrm{P}_{0} \\ & \lambda=989.77 \AA \end{aligned}$ | 1 | $5.022 \mathrm{E}+01$ | $\begin{gathered} 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{0}\right) 4 \mathrm{~d}^{3} \mathrm{P}_{2}^{\mathrm{o}}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}^{3} \mathrm{D}_{3} \\ \lambda=1767.26 \AA \end{gathered}$ | $2.992 \mathrm{E}+01$ |
|  | 2 | $2.132 \mathrm{E}+01$ |  | $1.796 \mathrm{E}+01$ |
|  | 4 | $9.999 \mathrm{E}+00$ |  | $1.189 \mathrm{E}+01$ |
|  | 6 | $7.078 \mathrm{E}+00$ |  | $1.032 \mathrm{E}+01$ |
|  | 8 | $5.735 \mathrm{E}+00$ |  | $9.444 \mathrm{E}+00$ |
|  | 10 | $4.937 \mathrm{E}+00$ |  | $8.780 \mathrm{E}+00$ |
| $\begin{aligned} & 4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}^{1} \mathrm{G}_{4}^{\mathrm{o}}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}^{3} \mathrm{D}_{3} \\ & \lambda=1004.90 \AA \end{aligned}$ | 1 | $7.568 \mathrm{E}+00$ |  |  |
|  | 2 | $5.448 \mathrm{E}+00$ |  |  |
|  | 4 | $3.367 \mathrm{E}+00$ |  |  |
|  | 6 | $2.581 \mathrm{E}+00$ |  |  |
|  | 8 | $2.174 \mathrm{E}+00$ |  |  |
|  | 10 | $1.919 \mathrm{E}+00$ |  |  |



Figure 1. Stark broadening as a function of electron temperature for the two $\operatorname{Sr} v$ transitions, $4 p^{3}\left({ }^{2} D^{o}\right) 4 d^{3} D_{3}^{o}-4 p^{3}\left({ }^{4} S^{\circ}\right) 5 p{ }^{3} P_{2}(16-61)$ (a) and $4 p^{3}\left({ }^{2} D^{\circ}\right) 4 d$ ${ }^{1} \mathrm{G}_{4}^{\mathrm{o}}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}^{3} \mathrm{D}_{3}(25-66)$ (b), and for the two Sr vi transitions, $4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{~S}_{1 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{P}_{1 / 2}^{\mathrm{o}}$ (21-4) (c) and $4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{~S}_{1 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3} 2 \mathrm{P}_{3 / 2}^{0}$ (21-5) (d). Electron density $N_{\mathrm{e}}=10^{17} \mathrm{~cm}^{-3}$.
(Dimitrijević, Sahal-Bréchot \& Bommier 1991)

$$
\begin{equation*}
N_{\mathrm{D}}=N_{\mathrm{e}} V>1, \tag{7}
\end{equation*}
$$

where $V=\frac{4 \pi}{3} R_{\mathrm{D}}^{3}$ is the volume of the Debye sphere. $R_{\mathrm{D}}$ is the Debye length (or Debye radius), which can be written as
$R_{\mathrm{D}}=\sqrt{\frac{\varepsilon_{0} k_{\mathrm{B}} T}{N_{\mathrm{e}} e^{2}}}$,
where $\varepsilon_{0}$ is the permittivity of free space and $e$ is the elementary charge in SI units. We can write the inequality (7) as
$N_{\mathrm{e}}>\frac{3}{4 \pi R_{\mathrm{D}}^{3}}$,
$N_{\mathrm{e}}<\left(\frac{4 \pi}{3}\right)^{2}\left(\frac{\varepsilon_{0} k_{\mathrm{B}}}{e^{2}}\right)^{3} T^{3}$.
So, the condition of the plasma ideality can be written by the following inequality:
$N_{\mathrm{e}}\left(\mathrm{cm}^{-3}\right)<1.9 \times 10^{6} T^{3}(\mathrm{~K})$.
In WD atmospheres, the plasma becomes non-ideal with the decrease of temperature or increase of density. As an example, if we take the lowest temperature used in our work $T=10^{4} \mathrm{~K}$, we find that $N_{\mathrm{e}}<$ $1.9 \times 10^{18} \mathrm{~cm}^{-3}$. If we take the highest temperature $T=5 \times 10^{5} \mathrm{~K}$, we find that $N_{\mathrm{e}}<2.38 \times 10^{23} \mathrm{~cm}^{-3}$. So, our plasma is ideal for the considered density $N_{\mathrm{e}}=10^{17} \mathrm{~cm}^{-3}$ and temperatures. Therefore, we can deduce the Stark line widths for other densities using a linear relationship between $W$ and $N_{\mathrm{e}}$ (for a given temperature) provided that these densities are lower than $10^{23} \mathrm{~cm}^{-3}$, at which the plasma can be considered as ideal.

### 3.2.3 Stark broadening results for $\mathrm{Sr} V$

In Table 5, we display the Stark broadening of 17 Srv lines. The calculations are performed at electron density $N_{\mathrm{e}}=10^{17} \mathrm{~cm}^{-3}$ and for electron temperatures ranging from $10^{4}$ to $10^{5} \mathrm{~K}$ using five configurations for the $\operatorname{Sr} v$ structure. There are two $\operatorname{Sr} v$ lines described as 'uncertain' ( 915.994 and $985.408 \AA$ ) and four $\mathrm{Sr} v$ lines ( $935.509,951.044,962.378$, and $1379.615 \AA$ ) described as 'blend' (blended with lines of other species) in the UV spectrum of RE 0503-289 (Rauch et al. 2017b). The 'uncertain' and 'blend' lines are considered in Table 5 because they are identified in the NIST data base (Kramida et al. 2021) and in Sansonetti (2012). We found that the Srv lines are given in the NIST data base with the corresponding initial and final levels and their wavelengths. In order to illustrate the behaviour of the Stark broadening with temperature, we display in Fig. 1 our line widths as a function of electron temperature and at electron density $N_{\mathrm{e}}=10^{17} \mathrm{~cm}^{-3}$ for the two Srv transitions: $4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{D}_{3}^{0}-4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{P}_{2}$ (16-61) (panel a) and $4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\circ}\right) 4 \mathrm{~d}$ ${ }^{1} \mathrm{G}_{4}^{\mathrm{o}}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}^{3} \mathrm{D}_{3}(25-66)$ (panel b).

### 3.2.4 Stark broadening results for Sr VI

In Table 6, we display the Stark broadening of the 20 strongest lines of Sr VI. The calculations are performed at electron density $N_{\mathrm{e}}=10^{17} \mathrm{~cm}^{-3}$ and for electron temperatures ranging from $10^{4}$ to $5 \times 10^{5} \mathrm{~K}$ required for plasma modelling. Three configurations have been used for the Sr VI structure calculation. Nine of these lines were identified for the first time by Persson \& Pettersson (1984), who identified all the levels corresponding to the ground configuration $\left(4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}\right)$ and the first excited configuration $\left(4 \mathrm{~s} 4 \mathrm{p}^{4}\right)$. The other 11 lines were identified for the first time by O'Sullian \& Maher (1989). In order to illustrate the behaviour of the Stark broadening with

Table 6. Same as Table 5 but for 20 Sr vi lines.

| Transition | $T\left(10^{4} \mathrm{~K}\right)$ | $W$ (pm) | Transition | $W$ (pm) |
| :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & 4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{~S}_{1 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{P}_{1 / 2}^{\mathrm{o}} \\ & \lambda=291.73 \AA \end{aligned}$ | 1 | $8.747 \mathrm{E}-02$ | $\begin{gathered} 4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{P}_{3 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{P}_{3 / 2}^{0} \\ \lambda=333.59 \AA \end{gathered}$ | $1.065 \mathrm{E}-01$ |
|  | 2 | $6.396 \mathrm{E}-02$ |  | $7.724 \mathrm{E}-02$ |
|  | 5 | $4.118 \mathrm{E}-02$ |  | $4.986 \mathrm{E}-02$ |
|  | 10 | $2.860 \mathrm{E}-02$ |  | $3.472 \mathrm{E}-02$ |
|  | 20 | $2.019 \mathrm{E}-02$ |  | $2.452 \mathrm{E}-02$ |
|  | 30 | $1.666 \mathrm{E}-02$ |  | $2.023 \mathrm{E}-02$ |
|  | 50 | $1.320 \mathrm{E}-02$ |  | $1.606 \mathrm{E}-02$ |
| $\begin{aligned} & 4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{4} \mathrm{P}_{5 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{4} \mathrm{~S}_{3 / 2}^{0} \\ & \lambda=293.20 \AA \end{aligned}$ | 1 | $8.005 \mathrm{E}-02$ | $\begin{gathered} 4 \mathrm{~s} 4 \mathrm{p}^{4}{ }^{2} \mathrm{P}_{1 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{D}_{3 / 2}^{0} \\ \lambda=412.64 \AA \end{gathered}$ | $3.023 \mathrm{E}-01$ |
|  | 2 | $5.795 \mathrm{E}-02$ |  | $1.800 \mathrm{E}-01$ |
|  | 5 | $3.747 \mathrm{E}-02$ |  | $8.608 \mathrm{E}-02$ |
|  | 10 | $2.613 \mathrm{E}-02$ |  | $5.739 \mathrm{E}-02$ |
|  | 20 | $1.844 \mathrm{E}-02$ |  | $4.143 \mathrm{E}-02$ |
|  | 30 | $1.518 \mathrm{E}-02$ |  | $3.494 \mathrm{E}-02$ |
|  | 50 | $1.197 \mathrm{E}-02$ |  | $2.862 \mathrm{E}-02$ |
| $\begin{aligned} & 4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{~S}_{1 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{P}_{3 / 2}^{0} \\ & \lambda=295.24 \AA \end{aligned}$ | 1 | $8.887 \mathrm{E}-02$ | $\begin{gathered} 4 \mathrm{~s} 4 \mathrm{p}^{4}{ }^{2} \mathrm{P}_{3 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{D}_{5 / 2}^{\mathrm{o}} \\ \lambda=432.06 \AA \end{gathered}$ | $3.313 \mathrm{E}-01$ |
|  | 2 | $6.499 \mathrm{E}-02$ |  | $1.974 \mathrm{E}-01$ |
|  | 5 | $4.184 \mathrm{E}-02$ |  | $9.449 \mathrm{E}-02$ |
|  | 10 | $2.905 \mathrm{E}-02$ |  | $6.301 \mathrm{E}-02$ |
|  | 20 | $2.052 \mathrm{E}-02$ |  | $4.545 \mathrm{E}-02$ |
|  | 30 | $1.693 \mathrm{E}-02$ |  | $3.832 \mathrm{E}-02$ |
|  | 50 | $1.342 \mathrm{E}-02$ |  | $3.142 \mathrm{E}-02$ |
| $\begin{aligned} & 4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{D}_{3 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{D}_{3 / 2}^{o} \\ & \lambda=296.54 \AA \end{aligned}$ | 1 | $8.084 \mathrm{E}-02$ | $\begin{gathered} 4 \mathrm{~s} 4 \mathrm{p}^{4}{ }^{2} \mathrm{~S}_{1 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{P}_{1 / 2}^{\mathrm{o}} \\ \lambda=516.32 \AA \end{gathered}$ | $1.178 \mathrm{E}-01$ |
|  | 2 | $5.827 \mathrm{E}-02$ |  | $9.987 \mathrm{E}-02$ |
|  | 5 | $3.776 \mathrm{E}-02$ |  | $8.521 \mathrm{E}-02$ |
|  | 10 | $2.644 \mathrm{E}-02$ |  | $6.916 \mathrm{E}-02$ |
|  | 20 | $1.871 \mathrm{E}-02$ |  | $5.440 \mathrm{E}-02$ |
|  | 30 | $1.544 \mathrm{E}-02$ |  | $4.709 \mathrm{E}-02$ |
|  | 50 | $1.225 \mathrm{E}-02$ |  | $3.930 \mathrm{E}-02$ |
| $\begin{aligned} & 4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{D}_{5 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{32} \mathrm{D}_{3 / 2}^{0} \\ & \lambda=297.37 \AA \end{aligned}$ | 1 | $8.133 \mathrm{E}-02$ | $\begin{gathered} 4 \mathrm{~s} 4 \mathrm{p}^{4}{ }^{2} \mathrm{D}_{3 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{D}_{3 / 2}^{0} \\ \lambda=532.39 \AA \end{gathered}$ | $1.040 \mathrm{E}-01$ |
|  | 2 | $5.846 \mathrm{E}-02$ |  | $7.619 \mathrm{E}-02$ |
|  | 5 | $3.765 \mathrm{E}-02$ |  | $5.580 \mathrm{E}-02$ |
|  | 10 | $2.625 \mathrm{E}-02$ |  | $4.972 \mathrm{E}-02$ |
|  | 20 | $1.853 \mathrm{E}-02$ |  | $4.442 \mathrm{E}-02$ |
|  | 30 | $1.527 \mathrm{E}-02$ |  | $4.068 \mathrm{E}-02$ |
|  | 50 | $1.210 \mathrm{E}-02$ |  | $3.567 \mathrm{E}-02$ |
| $\begin{aligned} & 4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{4} \mathrm{P}_{3 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{34} \mathrm{~S}_{3 / 2}^{0} \\ & \lambda=297.70 \AA \end{aligned}$ | 1 | $8.269 \mathrm{E}-02$ | $\begin{gathered} 4 \mathrm{~s} 4 \mathrm{p}^{4}{ }^{2} \mathrm{D}_{5 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{D}_{5 / 2}^{o} \\ \lambda=538.18 \AA \end{gathered}$ | $1.048 \mathrm{E}-01$ |
|  | 2 | $5.985 \mathrm{E}-02$ |  | $7.662 \mathrm{E}-02$ |
|  | 5 | $3.868 \mathrm{E}-02$ |  | $5.615 \mathrm{E}-02$ |
|  | 10 | $2.696 \mathrm{E}-02$ |  | $5.016 \mathrm{E}-02$ |
|  | 20 | $1.901 \mathrm{E}-02$ |  | $4.482 \mathrm{E}-02$ |
|  | 30 | $1.565 \mathrm{E}-02$ |  | $4.102 \mathrm{E}-02$ |
|  | 50 | $1.234 \mathrm{E}-02$ |  | $3.594 \mathrm{E}-02$ |
| $\begin{aligned} & 4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{D}_{5 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{32} \mathrm{D}_{5 / 2}^{0} \\ & \lambda=299.91 \AA \end{aligned}$ | 1 | $8.256 \mathrm{E}-02$ | $\begin{gathered} 4 \mathrm{~s} 4 \mathrm{p}^{4}{ }^{4} \mathrm{P}_{1 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{4} \mathrm{~S}_{3 / 2}^{0} \\ \lambda=596.75 \AA \end{gathered}$ | $8.626 \mathrm{E}-02$ |
|  | 2 | $5.948 \mathrm{E}-02$ |  | $6.264 \mathrm{E}-02$ |
|  | 5 | $3.850 \mathrm{E}-02$ |  | $4.808 \mathrm{E}-02$ |
|  | 10 | $2.694 \mathrm{E}-02$ |  | $4.683 \mathrm{E}-02$ |
|  | 20 | $1.905 \mathrm{E}-02$ |  | $4.442 \mathrm{E}-02$ |
|  | 30 | $1.572 \mathrm{E}-02$ |  | $4.143 \mathrm{E}-02$ |
|  | 50 | $1.246 \mathrm{E}-02$ |  | $3.673 \mathrm{E}-02$ |
| $\begin{aligned} & 4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{4} \mathrm{P}_{1 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{4} \mathrm{~S}_{3 / 2}^{0} \\ & \lambda=302.09 \AA \end{aligned}$ | 1 | $8.564 \mathrm{E}-02$ | $\begin{gathered} 4 \mathrm{~s} 4 \mathrm{p}^{4}{ }^{4} \mathrm{P}_{3 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{4} \mathrm{~S}_{3 / 2}^{\mathrm{o}} \\ \lambda=606.90 \AA \end{gathered}$ | $8.474 \mathrm{E}-02$ |
|  | 2 | $6.188 \mathrm{E}-02$ |  | $6.158 \mathrm{E}-02$ |
|  | 5 | $4.001 \mathrm{E}-02$ |  | $4.780 \mathrm{E}-02$ |
|  | 10 | $2.791 \mathrm{E}-02$ |  | $4.732 \mathrm{E}-02$ |
|  | 20 | $1.970 \mathrm{E}-02$ |  | $4.535 \mathrm{E}-02$ |
|  | 30 | $1.621 \mathrm{E}-02$ |  | $4.245 \mathrm{E}-02$ |
|  | 50 | $1.279 \mathrm{E}-02$ |  | $3.773 \mathrm{E}-02$ |
| $\begin{aligned} & 4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{P}_{3 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{D}_{5 / 2}^{0} \\ & \lambda=311.16 \AA \end{aligned}$ | 1 | $8.719 \mathrm{E}-02$ | $\begin{gathered} 4 \mathrm{~s} 4 \mathrm{p}^{4}{ }^{2} \mathrm{D}_{5 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{P}_{3 / 2}^{0} \\ \lambda=609.03 \AA \end{gathered}$ | $1.337 \mathrm{E}-01$ |
|  | 2 | $6.294 \mathrm{E}-02$ |  | $9.880 \mathrm{E}-02$ |
|  | 5 | $4.083 \mathrm{E}-02$ |  | $7.392 \mathrm{E}-02$ |

Table 6 - continued

| Transition | $T\left(10^{4} \mathrm{~K}\right)$ | $W(\mathrm{pm})$ | Transition |
| :--- | :---: | :---: | :---: |
|  | 10 | $2.860 \mathrm{E}-02$ | $W(\mathrm{pm})$ |
|  | 20 | $2.025 \mathrm{E}-02$ | $6.700 \mathrm{E}-02$ |
|  | 30 | $1.673 \mathrm{E}-02$ | $5.978 \mathrm{E}-02$ |
|  | 50 | $1.330 \mathrm{E}-02$ | $5.449 \mathrm{E}-02$ |
| $4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{D}_{3 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{P}_{3 / 2}^{\mathrm{o}}$ | 1 | $9.945 \mathrm{E}-02$ | $4.750 \mathrm{E}-02$ |
| $\lambda=319.74 \AA$ | 2 | $7.211 \mathrm{E}-02$ | $4.040 \mathrm{E}-02$ |
|  | 5 | $4.658 \mathrm{E}-02$ | $6.572 \mathrm{E}-02$ |
|  | 10 | $3.246 \mathrm{E}-02$ | $5.116 \mathrm{E}-02$ |
|  | 20 | $2.294 \mathrm{E}-02$ | $5.081 \mathrm{E}-02$ |
|  | 30 | $1.892 \mathrm{E}-02$ | $4.882 \mathrm{E}-02$ |
|  | 50 | $1.501 \mathrm{E}-02$ | $4.573 \mathrm{E}-02$ |

Table 7. Our quantum Stark widths $W$ and the results of the Cowley formula $W_{\mathrm{C}}$ (Cowley 1971) expressed in picometres for Sr V lines at two electron temperatures and at electron density $N=10^{17} \mathrm{~cm}^{-3}$. The temperature $T$ is expressed in $10^{4} \mathrm{~K}$ and $R=W_{\mathrm{C}} / W$.

| Line | $T$ | W | $W_{\text {C }}$ | $R$ |
| :---: | :---: | :---: | :---: | :---: |
| $4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{G}_{4}^{\mathrm{o}}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{~F}_{3}$ | 1 | 9.015 | 18.85 | 2.09 |
| $\lambda=928.36 \AA$ | 4 | 3.486 | 18.85 | 5.41 |
| $4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{~F}_{4}^{\mathrm{o}}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{D}_{3}$ | 1 | 14.44 | 23.29 | 1.61 |
| $\lambda=937.68 \AA$ | 4 | 4.673 | 23.29 | 4.98 |
| $4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{P}_{1}^{\mathrm{o}}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{P}^{\mathrm{o}}\right) 5 \mathrm{p}^{3} \mathrm{~S}_{1}$ | 1 | 37.05 | 19.29 | 0.52 |
| $\lambda=939.08 \AA$ | 4 | 9.019 | 19.29 | 2.14 |
| $4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}^{3} \mathrm{D}_{3}^{\mathrm{o}}-4 \mathrm{p}^{3}\left({ }^{4} \mathrm{~S}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{3} \mathrm{P}_{2}$ | 1 | 7.893 | 17.40 | 2.20 |
| $\lambda=974.52 \AA$ | 4 | 3.219 | 17.40 | 5.41 |
| $4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 4 \mathrm{~d}^{1} \mathrm{G}_{4}^{\mathrm{o}}-4 \mathrm{p}^{3}\left({ }^{2} \mathrm{D}^{\mathrm{o}}\right) 5 \mathrm{p}{ }^{1} \mathrm{~F}_{3}$ | 1 | 8.362 | 20.85 | 2.49 |
| $\lambda=980.98 \AA$ | 4 | 3.135 | 20.85 | 6.65 |

temperature, we display in Fig. 1 our line widths as a function of electron temperature and at electron density $N_{\mathrm{e}}=10^{17} \mathrm{~cm}^{-3}$ for the two $\operatorname{Sr}$ VI transitions: $4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{~S}_{1 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{P}_{1 / 2}^{0}$ (21-4) (panel c) and $4 \mathrm{~s}^{2} 4 \mathrm{p}^{2} 5 \mathrm{~s}^{2} \mathrm{~S}_{1 / 2}-4 \mathrm{~s}^{2} 4 \mathrm{p}^{3}{ }^{2} \mathrm{P}_{3 / 2}^{0}(21-5)$ (panel d). We could not find other results in the literature to compare with the present Sr V and Sr VI Stark width data. The acceptable agreement found between our atomic data and other ones shows that the current line width results have an acceptable accuracy and can be used with trust in plasma investigations. Other experimental results or calculations of $\mathrm{Sr} \mathrm{V}-$ VI broadening would be very helpful to confirm our calculations. Results of line widths in Tables 5 and 6 will be implemented in the STARK-B data base (available at http://stark-b.obspm.fr; SahalBréchot, Dimitrijević \& Moreau 2020; see also Roueff et al. 2020). STARK-B is free access and contains widths and shifts of isolated lines of ions and neutral atoms, perturbed by electron and ions for various temperatures and electron and ion densities. It is devoted to modelling and spectroscopic diagnostics of stellar atmospheres and envelopes and laboratory, fusion, and technological plasmas. It is a node of the Virtual Atomic and Molecular Data Center (VAMDC Consortium: http://www.vamdc.eu/) (Albert et al. 2020).

### 3.2.5 Comparison with the Cowley approximate formula

We calculate Stark widths for five $\operatorname{Sr} \mathrm{V}$ lines using the Cowley approximate formula (Cowley 1971) in order to compare them with our quantum results and illustrate the difference between our rigorous calculations and the approximation. The approximate formula is proposed for one electron temperature $T=10^{4} \mathrm{~K}$, and Cowley
(1971) mentioned that the formula is not recommended when detailed calculations or experimental results are available. We use it here to show that it overestimates the Stark broadening, as mentioned in Dimitrijević et al. (2005). The Stark broadening $W_{\mathrm{C}}$, expressed in angstroms, is calculated by the formula (Cowley 1971)
$W_{\mathrm{C}}=2 \times 0.77 \times 10^{-18}\left(n^{*}\right)^{4} \lambda^{2} N$,
where $N$ is the electron density in $\mathrm{cm}^{-3}, \lambda$ is the wavelength of the considered transition in centimetres, and $n^{*}$ is the effective principal quantum number of the upper level defined by
$n^{*}=Z\left(\frac{13.59}{I-E}\right)^{1 / 2}$.
In equation (13), $Z$ is the charge seen by the active electron $(Z=1$ for neutral atoms,... ), $E$ is the energy of the level, and $I$ is the appropriate series limit. Table 7 displays our quantum Stark broadening data for some Sr V lines compared with those calculated using the Cowley approximate formula (Cowley 1971) at two electron temperature values. The electron density is $N=10^{17} \mathrm{~cm}^{-3}$. We recall that formula (12) is proposed for one electron temperature $T=10^{4} \mathrm{~K}$, so the Stark broadening values $W_{\mathrm{C}}$ in Table 7 are the same for any chosen temperature.

We can see from Table 7 that in almost all the cases the approximate formula gives line widths that are greater than ours. Secondly, even at the electron temperature of $T=10^{4} \mathrm{~K}$, for which the formula is proposed, the two results disagree for almost all the lines and the ratio $W_{\mathrm{C}} / W$ varies between 0.52 and 2.49 . For the electron temperature $T=$ $4 \times 10^{4} \mathrm{~K}$, the disagreement between the two results becomes higher and the ratio $W_{\mathrm{C}} / W$ can reach 6.65 . We can predict that for other temperatures further away from $T=10^{4} \mathrm{~K}$, the agreement will be worse. Consequently, while the approximate formula (12) is very easy to use, it is not recommended when measurements or rigorous calculations can be performed.

## 4 INFLUENCE OF STARK BROADENING IN THE SPECTRA OF HOT WHITE DWARFS

In order to prove the importance of our Stark broadening calculations, it is essential to explore the usefulness of the Stark broadening mechanism in the atmosphere of the considered star. To perform this task, we have compared the effect of Stark and Doppler broadening in many atmospheric layers and for different stellar atmospheres. We have used the model atmospheres of Wesemael (1981). The expression of Doppler broadening is
$W_{\text {Doppler }}=\lambda_{0}\left(\frac{2 k_{\mathrm{B}} T}{M c^{2}}\right)^{\frac{1}{2}}$,


Figure 2. Stark $W_{\text {Stark }}$ and Doppler $W_{\text {Doppler }}$ widths for Srv line $4 p^{3}\left({ }^{2} D^{0}\right) 4 d^{3} D_{3}^{0}-4 p^{3}\left({ }^{4} S^{\circ}\right) 5 p^{3} P_{2}(\lambda=974.52 \AA)$ for the atmospheric models of Wesemael (1981) with effective temperatures $T_{\text {eff }}=70000-100000 \mathrm{~K}$ and $\log g=8$ as a function of atmospheric layer temperatures (a) and as a function of the Rosseland optical depth (b), and for the atmospheric models of Wesemael (1981) with $\log g=6-9$ and effective temperature $T_{\text {eff }}=80000 \mathrm{~K}$ as a function of atmospheric layer temperatures (c) and as a function of the Rosseland optical depth (d).
where $M$ denotes the atomic mass of the radiating atom ( Sr ) and $c$ denotes the speed of light in vacuum expressed in the SI system. When we calculated the Stark and Doppler broadening, we found that their behaviours are the same for all the chosen lines. Consequently, we chose for illustration the $\operatorname{Sr} v$ line $4 p^{3}\left({ }^{2} D^{o}\right) 4 d^{3} D_{3}^{o}-4 p^{3}\left({ }^{4} S^{o}\right) 5 p$ ${ }^{3} \mathrm{P}_{2}(\lambda=974.52 \AA)$.

We display the Stark and Doppler broadening for the $\operatorname{Sr} \mathrm{v}$ line ( $\lambda=974.52 \AA$ ) as a function of atmospheric layer temperatures (Fig. 2a) and as a function of the Rosseland optical depth (Fig. 2b) for atmospheric models with effective temperatures $T_{\text {eff }}=70000-$ 100000 K and $\log g=8$ (Wesemael 1981). For $T>70000 \mathrm{~K}$, the Stark width becomes more dominant than the Doppler width for all the atmospheric layer temperatures. We notice that the dominance is higher at deeper atmospheric layers. We come to the same conclusion if we examine the Stark and Doppler broadening as a function of the Rosseland optical depth in logarithmic scale $(\log \tau)$ for the same atmospheric models (Fig. 2b): We notice that the Stark broadening is more significant relative to the Doppler broadening even at the surface of the DO WD atmospheres. Also, the Stark and Doppler broadening behaviours have been investigated as a function of atmospheric layer temperatures (Fig. 2c) and as a function of the Rosseland optical depth (Fig. 2d) for atmospheric models (Wesemael 1981) with $\log g=6-9$ and $T_{\text {eff }}=80000 \mathrm{~K}$. For a gravity surface $\log g=7-9$, the Stark line width becomes significant for temperatures of $\sim 10^{5} \mathrm{~K}$ (Fig. 2c). For $\log g=6$, the Doppler width is more significant than the Stark width for lower temperatures $\left(5 \times 10^{4}\right.$
to $10^{5} \mathrm{~K}$ ), but for $T>10^{5} \mathrm{~K}$, the Stark width starts to dominate the Doppler width. For $\log g=9$, we find that $W_{\text {Stark }} \approx 2 \times W_{\text {Doppler }}$ for the deepest atmospheric layer $T=2.5 \times 10^{5} \mathrm{~K}$. Concerning the variation of Stark and Doppler line widths with the Rosseland optical depth, Stark broadening is most significant for all the optical depths for the four atmospheric models $\log g=6-9$ and is nearly more than twice the Doppler one for $\log g=9$. We can conclude that Stark broadening is dominant compared with the Doppler broadening for all the atmospheric models of these DO WD atmospheres.

## 5 SUMMARY

We have calculated the Stark widths of 37 strontium lines (17 Srv lines and 20 Sr vi lines) using our quantum-mechanical method. All the Stark widths are the first to be published. The calculations and comparisons of the intermediate results (energy levels and radiative atomic data) allow us to have an idea about the accuracy of our line-width calculations, since they are used in the calculations of line broadening. The obtained results will be of importance for the spectral analysis by means of NLTE model atmospheres. The results are provided for the range of temperatures from $10^{4}$ to $5 \times 10^{5} \mathrm{~K}$ suitable for many astrophysical investigations, and at electron density $N_{\mathrm{e}}=10^{17} \mathrm{~cm}^{-3}$. The idea behind our work was the recent discovery of 23 new $\mathrm{Sr} v$ lines in the UV spectrum of the hot WD RE 0503-289 (Rauch et al. 2017b). Thus, we have calculated the Stark broadening for 17 Sr v lines - among the 23 new Sr V lines in Rauch et al. (2017b)

- and for the 20 strongest lines of Sr VI, which were identified, for the first time, by Persson \& Pettersson (1984) and O'Sullian \& Maher (1989).

Finally, we have investigated the importance of the Stark broadening $W_{\text {Stark }}$ compared with the Doppler broadening $W_{\text {Doppler }}$ in hot WD atmospheres: We have examined their variation with the atmospheric layer temperatures and with the Rosseland optical depth for different atmospheric models of Wesemael (1981) $\left(T_{\text {eff }}=7 \times 10^{4}\right.$ to $10^{5} \mathrm{~K}$ and $\log g=6-9$ ). We found that, for all the plasma conditions of DO WD atmospheres, the Stark broadening is more important than the Doppler one. The accurate Stark broadening parameters for the two strontium ions will be of interest for the investigation of hot WDs and for the determination of the strontium abundance in such stars. We hope that our results can fill the lack of Stark broadening data for these two ions in the data base STARK-B and can be used for the plasma diagnostic of the studied stars.

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## DATA AVAILABILITY

The data underlying this article are available in the article and in its online supplementary material available at CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via https://cdsarc.unistra.fr/vizbin/cat/J/MNRAS.

## REFERENCES

Albert D. et al., 2020, Atoms, 8, 76
Aloui R., Elabidi H., Sahal-Bréchot S., Dimitrijević M. S., 2018, Atoms, 6, 20
Aloui R., Elabidi H., Hamdi R., Sahal-Bréchot S., 2019a, MNRAS, 484, 4801
Aloui R., Elabidi H., Sahal-Bréchot S., 2019b, J. Quant. Spectrosc. Radiat. Transfer., 239, 106675
Aloui R., Elabidi H., Sahal-Bréchot S., 2020, Contrib. Astron. Obs. Skalnaté Pleso, 50, 154
Aloui R., Elabidi H., Sahal-Bréchot S., 2021, Eur. Phys. J. D, 75, 218
Baranger M., 1958, Phys. Rev., 112, 855
Bethe H. A., Salpeter E. E., 1957, Quantum Mechanics of One-and TwoElectron Atoms. Springer, Berlin
Charro E., Martín I., 1998, A\&AS, 131, 523
Cowley C. R., 1971, The Observatory, 91, 139
Dimitrijević M. S., 2003, Astron. Astrophys. Trans., 22, 389
Dimitrijević M. S., 2020, Data, 5, 73
Dimitrijević M. S., Sahal-Bréchot S., Bommier V., 1991, A\&AS, 89, 581
Dimitrijević M. S., Ryabchikova T., Popović L. Č, Shulyak D., Khan S., 2005, A\&A, 435, 1191

Eissner W., 1998, Comput. Phys. Commun, 114, 295
Eissner W., Jones M., Nussbaumer H., 1974, Comput. Phys. Commun., 8, 270
Elabidi H., 2021, MNRAS, 503, 5730
Elabidi H., Sahal-Bréchot S., 2019, MNRAS, 484, 1072
Elabidi H., Ben Nessib N., Sahal-Bréchot S., 2004, J. Phys. B: At. Mol. Opt. Phys., 37, 63
Elabidi H., Ben Nessib N., Cornille M., Dubau J., Sahal-Bréchot S., 2008, J. Phys. B: At. Mol. Opt. Phys., 41, 025702
Elabidi H., Ben Nessib N., Sahal-Bréchot S., 2008, Eur. Phys. J. D, 54, 51
Gailitis M., 1963, J. Exp. Theor. Phys., 17, 1328
Grant I. P., 1988, in Wilson S.ed., Relativistic Atomic Structure Calculations.. Methods in Computational Chemistry, Springer, Boston, MA
Grant I. P., McKenzie B. J., Norrington P. H., Mayers D. F., Pyper N. C., 1980, Comput. Phys. Commun., 21, 207
Kramida A., Ralchenko Yu., Reader J., NIST ASD Team, 2021, NIST Atomic Spectra Database (ver. 5.9). National Institute of Standards and Technology, Gaithersburg, MD
O’Sullian G., 1989, J. Phys. B: At. Mol. Opt. Phys., 22, 987
O’Sullian G., Maher M., 1989, J. Phys. B: At. Mol. Opt. Phys., 22, 377
Persson W., Pettersson S. G., 1984, Phys. Scr., 29, 308
Rauch T. et al., 2007, A\&A, 470, 317
Rauch T., Quinet P., Hoyer D., Werner K., Demleitner M., Kruk J. W., 2016a, A\&A, 587, A39
Rauch T., Gamrath S., Quinet P., Löbling L., Hoyer D., Werner K., Kruk J. W., Demleitner M., 2017a, A\&A, 599, A142

Rauch T. et al., 2017b, A\&A, 606, A105
Rauch T. et al., 2020, A\&A, 637, A4
Roueff E., Sahal-Bréchot S., Dimitrijević M. S., Moreau N., Abgrall H., 2020, Atoms, 8, 36
Sahal-Bréchot S., Elabidi H., 2021, A\&A, 652, A47
Sahal-Bréchot S., Dimitrijević M. S., Moreau N., 2020, J. Phys. Conf. Ser., 1412, 132052
Sahal-Bréchot S., Dimitrijević M. S., Moreau N., 2022, STARK-B data base, Available at: http://stark-b.obspm.fr (accessed 30 January 2021)
Sansonetti J. E., 2012, J. Phys. Chem. Ref. Data, 41, 013102
Saraph H. E., 1978, Comput. Phys. Commun, 15, 247
Werner K., Rauch T., Knörzer M., Kruk J. W., 2018, A\&A, 614, A96
Werner K., Rauch T., Kruk J. W., 2018, A\&A, 609, A107
Wesemael F., 1981, ApJS, 45, 177
Wyart J. F., Artru M. C., 1989, Phys. Lett. A, 139, 8

## SUPPORTING INFORMATION

Supplementary data are available online at CDS via anonymous ftp to cdsarc.u-strasbg.fr (130.79.128.5) or via https://cdsarc.unistra.fr/vizbin/cat/J/MNRAS.

Table 3. Current spontaneous transition probabilities $A_{i j}$, weighted oscillator strengths $g f$, and line strengths $S$ for $\operatorname{Sr} \mathrm{V}$ allowed transitions.
Table 4. Current spontaneous transition probabilities $A_{i j}$ compared with the experimental results (Exp) of Sansonetti (2012), weighted oscillator strengths $g f$ compared with the MCDF results of O'Sullian (1989) using the MCDF code of Grant et al. (1980), and line strengths $S$ for Sr VI allowed transitions.
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