



HAL
open science

From stellar haloes to intracluster light: the physics of the Intra-Halo Stellar Component in cosmological hydrodynamical simulations

Rodrigo Cañas, Claudia del P. Lagos, Pascal J. Elahi, Chris Power, Charlotte Welker, Yohan Dubois, Christophe Pichon

► To cite this version:

Rodrigo Cañas, Claudia del P. Lagos, Pascal J. Elahi, Chris Power, Charlotte Welker, et al.. From stellar haloes to intracluster light: the physics of the Intra-Halo Stellar Component in cosmological hydrodynamical simulations. *Monthly Notices of the Royal Astronomical Society*, 2020, 494, pp.4314-4333. 10.1093/mnras/staa1027 . insu-03748056

HAL Id: insu-03748056

<https://insu.hal.science/insu-03748056>

Submitted on 28 May 2024

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

From stellar haloes to intracluster light: the physics of the Intra-Halo Stellar Component in cosmological hydrodynamical simulations

Rodrigo Cañas^{1,2★}, Claudia del P. Lagos^{1,2}, Pascal J. Elahi^{1,2}, Chris Power^{1,2},
Charlotte Welker^{1,2,3}, Yohan Dubois^{4,5,6} and Christophe Pichon^{4,5,6}

¹International Centre for Radio Astronomy Research, University of Western Australia, 35 Stirling Highway, Crawley, WA 6009, Australia

²ARC Centre of Excellence for All Sky Astrophysics in 3 Dimensions (ASTRO 3D)

³Department of Physics and Astronomy, McMaster University, Hamilton, Ontario, Canada

⁴Institut d'Astrophysique de Paris, CNRS and UPMC Univ. Paris 06, UMR 7095, 98 bis Boulevard Arago, F-75014 Paris, France

⁵Institute for Astronomy, University of Edinburgh, Royal Observatory, Blackford Hill, Edinburgh EH9 3HJ, UK

⁶Korea Institute of Advanced Studies (KIAS), 85 Hoegiro, Dongdaemun-gu, Seoul 02455, Republic of Korea

Accepted 2020 April 10. Received 2020 April 9; in original form 2019 August 8

ABSTRACT

We study the Intra-Halo Stellar Component (IHSC) of Milky Way-mass systems up to galaxy clusters in the Horizon-AGN cosmological hydrodynamical simulation. We identify the IHSC using an improved phase-space galaxy finder algorithm which provides an adaptive, physically motivated, and shape-independent definition of this stellar component, that can be applied to haloes of arbitrary masses. We explore the IHSC mass fraction – total halo’s stellar mass, $f_{M_*,\text{IHSC}} - M_*$, relation, and the physical drivers of its scatter. We find that on average, the $f_{M_*,\text{IHSC}}$ increases with total stellar mass, with the scatter decreasing strongly with mass from 2 dex at $M_{*,\text{tot}} \simeq 10^{11} M_\odot$ to 0.3 dex at group masses. At high masses, $M_{*,\text{tot}} > 10^{11.5} M_\odot$, $f_{M_*,\text{IHSC}}$ increases with the number of substructures, and with the mass ratio between the central galaxy and largest satellite, at fixed $M_{*,\text{tot}}$. From mid-size groups and systems below $M_{*,\text{tot}} < 10^{12} M_\odot$, we find that the central galaxy’s stellar rotation-to-dispersion velocity ratio, V/σ , displays the strongest (anti)-correlation with $f_{M_*,\text{IHSC}}$ at fixed $M_{*,\text{tot}}$ of all the galaxy and halo properties explored, transitioning from $f_{M_*,\text{IHSC}} < 0.1$ per cent for high V/σ , to $f_{M_*,\text{IHSC}} \approx 5$ per cent for low V/σ galaxies. By studying the $f_{M_*,\text{IHSC}}$ temporal evolution, we find that, in the former, mergers not always take place, but if they did, they happened early ($z > 1$), while the high $f_{M_*,\text{IHSC}}$ population displays a much more active merger history. In the case of massive groups and galaxy clusters, $M_{*,\text{tot}} \gtrsim 10^{12} M_\odot$, a fraction $f_{M_*,\text{IHSC}} \approx 10 - 20$ per cent is reached at $z \approx 1$ and then they evolve across lines of constant $f_{M_*,\text{IHSC}}$ modulo some small perturbations. Because of the limited simulation’s volume, the latter is only tentative and requires a larger sample of simulated galaxy clusters to confirm.

Key words: methods: numerical – galaxies: evolution – galaxies: formation.

1 INTRODUCTION

In the hierarchical formation scenario, large galaxies are assembled via a sequence of interactions and mergers with smaller galaxies (White & Rees 1978). During such events, tidal forces strip stars from these smaller, satellite galaxies, which become part of the more massive, central galaxy, or are deposited in its outskirts in the form of streams, shells, and a diffuse component (e.g. Zwicky 1952; Toomre & Toomre 1972; Barnes & Hernquist 1991; Mihos & Hernquist 1996). The properties of these stellar remnants should contain important information about the assembly history and

dynamical age of Milky Way (MW)-like systems (e.g. Ibata et al. 2005; Martínez-Delgado et al. 2008; McConnachie et al. 2009; Watkins, Mihos & Harding 2015; Merritt et al. 2016; Monachesi et al. 2016), galaxy groups (e.g. Da Rocha & Mendes de Oliveira 2005; Durbala et al. 2008), and galaxy clusters (e.g. Mihos et al. 2005; Montes & Trujillo 2014; Mihos et al. 2017; Morishita et al. 2017). However, the study of such stellar remnants is a complicated task because of their diffuse nature, which leads them to have low surface brightnesses (LSB). This has led to the development of multiple techniques to study them in both observations and simulations.

From the observational perspective, this requires the use of telescopes and techniques to detect LSB features, as well as careful treatment of noise, scattered light, masking of foreground and

* E-mail: rodrigo.canas@icrar.org

background objects, and instrument systematics that can affect measurements in this faint regime (see e.g. Ibata et al. 2005; Mihos et al. 2005; McConnachie et al. 2009; Barker et al. 2009; Martínez-Delgado et al. 2010; Abraham & van Dokkum 2014; Monachesi et al. 2016). Moreover, the definition of the diffuse stellar component is likely to depend on characteristics of the telescope and observation, as well as the system of interest. For studies in which individual stars can be resolved, the diffuse stellar outskirts are often defined by their location. Specifically, studies of MW-like galaxies measure stellar haloes using asymptotic giant branch stars along the minor axis of the central galaxy (e.g. Mouhcine et al. 2005; Greggio et al. 2014; Monachesi et al. 2016), and along the major axis at sufficiently large distances from the galaxy (Monachesi et al. 2016). In contrast, studies that use integrated light either treat galaxies on an object by object basis (e.g. Mihos et al. 2005; Krick & Bernstein 2007; Martínez-Delgado et al. 2010; Merritt et al. 2016), or stack samples of galaxies (e.g. Zibetti et al. 2005; D’Souza et al. 2014; Zhang et al. 2019). In the first approach, the light from a galaxy is separated from that of the diffuse component by fitting single or multiple Sérsic (1963) profiles, and the diffuse envelope is treated as either the outermost component (e.g. D’Souza et al. 2014; Zhang et al. 2019) or is defined by the excess light or mass from fits to the inner regions of the galaxies (e.g. Merritt et al. 2016; Morishita et al. 2017). In the second, a surface brightness threshold separates the light from galaxies and from the diffuse envelope (Feldmeier et al. 2004; Zibetti et al. 2005; Montes & Trujillo 2014; Burke, Hilton & Collins 2015), which we note is a method also adopted by some numerical studies (e.g. Rudick, Mihos & McBride 2006).

From the theoretical perspective, reliable predictions of stellar haloes and intracluster light (ICL) require simulations to realistically trace the accretion and subsequent disruption of the satellite galaxies that give rise to these structures, and to resolve the sparsely populated outskirts of galaxies. Early studies of stellar haloes, such as Bullock & Johnston (2005) and Gauthier, Dubinski & Widrow (2006), used idealized non-cosmological N -body simulations with satellite populations whose properties (e.g. orbital parameters and accretion histories) informed by cosmological simulations. Others, for example Rudick et al. (2006), used dark matter haloes drawn from cosmological N -body simulations, populated with galaxies using an occupation distribution formalism, to study the formation and evolution of the ICL. Cooper et al. (2010) studied stellar halo formation in a self-consistent cosmological context by coupling a semi-analytical model to a cosmological N -body simulation, in which subhaloes’ most bound dark matter particles are tagged and used as dynamical tracers of the stellar populations predicted, to predict the properties of stellar haloes; here it was assumed that stellar haloes are composed of stellar particles that were accreted from satellites and reside outside a spherical aperture of 3 kpc (see also Cooper et al. 2013, 2015).

The current generation of cosmological hydrodynamical simulations (e.g. Dubois et al. 2014; Vogelsberger et al. 2014; Schaye et al. 2015) are now sufficient to model self-consistently the formation and hierarchical assembly of statistical samples of galaxies, and consequently track the formation of stellar streams, shells, and haloes. This provides important new insights into formation processes (e.g. *in situ* versus *ex situ* haloes; cf. Font et al. 2011), but it also complicates the separation of galaxies from their stellar components. In uniform resolution cosmological boxes, this has led the diffuse component to be defined as the stellar material outside spherical apertures, which can be either fixed (e.g. Font et al. 2011; Pillepich et al. 2018b) or dependent upon the mass distribution of the system (e.g. Pillepich et al. 2014; Elias et al.

2018). In zoom cosmological simulations of late-type galaxies, a more ad hoc approach has been used. For example, Pillepich, Madau & Mayer (2015) used a cylindrical volume to separate galaxies from their stellar haloes, while Monachesi et al. (2019) used rectangular windows, mirroring an observational 2D approach, to separate components. While such spatial definitions are simple and easy to compare between studies, they ignore the sometimes complex galaxy morphology, and, most importantly, they do not exploit the velocity information that is available in simulations.

However, this is not the case for all existing methods in the literature. For example, at galaxy clusters scales, velocity information has been used to separate the brightest galaxy cluster from the ICL, either by comparing particles’ binding energy in which the ICL is the stellar material bound to the cluster but not to a particular galaxy (e.g. Murante et al. 2004, 2007; Rudick, Mihos & McBride 2011), or by using its kinematics and fitting Maxwellian distributions to the total velocity distribution being the diffuse component the one with the largest dispersion (e.g. Puchwein et al. 2010; Dolag, Murante & Borgani 2010; Cui et al. 2014; Remus, Dolag & Hoffmann 2017). These are both physically motivated definitions; however, in applying the first method, it is not clear how to properly disentangle the contribution from individual cluster members to the global gravitational potential (Murante et al. 2004; Rudick et al. 2011), while in applying the second method, how particles are assigned to the distributions is not unique (Dolag et al. 2010; Cui et al. 2014) and the number of distributions needed to describe the system can vary between clusters (Remus et al. 2017).

Studies of the diffuse stellar component in the literature have focused on MW-like galaxies, in which case the diffuse stellar component is equivalent to a stellar halo, or on galaxy groups and clusters, in which case it is the IGL and ICL, respectively. This, in addition to the variety of definitions of the diffuse stellar component and the techniques used to identify it, has limited our understanding of how it is built across the dynamic range of galaxy formation. This critical limitation has resulted in a disconnect between the study of the assembly of galaxies and the build up of the diffuse stellar component, despite hierarchical growth underpinning both. Some theoretical studies have addressed this issue either by applying the same technique or definition to systems of a wide mass range (e.g. Cooper et al. 2010, 2013, 2015; Pillepich et al. 2018b), or using an adaptive definition of what the diffuse component is (e.g. Pillepich et al. 2014; Elias et al. 2018). However, there is still not yet a physically motivated adaptive definition that can be reliably applied to the whole dynamic range of systems resolved by cosmological hydrodynamical simulations.

In this work, we present the first results of a new method to identify the diffuse stellar component in simulations based on the galaxy finding algorithm described in Cañas et al. (2019) developed within the phase-space structure finder code VELOCIRAPTOR (Elahi, Thacker & Widrow 2011; Elahi et al. 2019a). In this method, the diffuse stellar component is defined as kinematically hot stellar particles that are distinct from the stellar components of phase-space overdense galaxies. The algorithm is adaptive and capable of separating the diffuse component in fairly isolated systems as well as in complex ones such as galaxy groups and clusters. We have decided to refer to the diffuse stellar component as the Intra-Halo Stellar Component (IHSC).

This study aims to characterize the mass content of the IHSC across different mass ranges and epochs by exploring to detail the IHSC mass fraction–stellar mass relation, $f_{M_*,\text{IHSC}} - M_*$. In particular, we want to understand the origin of the large scatter observed in the IHSC mass fraction of MW-mass-like galaxies (over

~ 2 dex difference from peak-to-peak), which has been measured recently by Merritt et al. (2016) using integrated light observations of the Dragonfly Telephoto Array (Abraham & van Dokkum 2014), and later confirmed by Harmsen et al. (2017) with stellar counts observations of the GHOSTS Survey (Radburn-Smith et al. 2011). We also want to understand whether the ICL fraction¹ correlates with cluster mass (Murante et al. 2007; Rudick et al. 2011) or not (Krick & Bernstein 2007; Contini et al. 2014; Cui et al. 2014), as well as, if its evolution is strong (Burke et al. 2015), or rather weak or non-existent (Krick & Bernstein 2007; Rudick et al. 2011; Montes & Trujillo 2018); this is an unresolved problem, from both observational and theoretical perspectives. In this first study, we use the Horizon-AGN simulation (Dubois et al. 2014), to address this problem. This state-of-the-art simulation has a volume big enough to contain galaxy groups and low-mass galaxy clusters (~ 400 haloes with $M_{200c} > 10^{13} M_{\odot}$), as well as, enough resolution to explore MW-like systems.

This paper is organized as follows. We first describe in Section 2 the Horizon-AGN simulation and the algorithm used to identify galaxies and the IHSC, as well as a description of how properties used throughout the paper are calculated. In Section 3, we show visually the IHSC for systems ranging in mass from the MW up to galaxy clusters. We also describe the $z = 0$ $f_{M_*, \text{IHSC}} - M_*$ relation and show how the mass content in galaxies and the IHSC is affected by parameters of our identification method, as well as how our method compares to spherical aperture definitions of the IHSC. In Section 4, we explore the origin of the scatter observed in the $f_{M_*, \text{IHSC}} - M_*$ relation and correlations with galaxy properties. In Section 5, we investigate the evolution of the IHSC for individual systems, as well as entire galaxy populations. Finally, in Section 6, we present a summary and conclusions of this work. In Appendix A, we present a comparison between our method to separate the IHSC and widely used definitions in the literature, and also show the mass fraction in the IHSC as a function of halo mass.

2 METHODOLOGY

2.1 Horizon-AGN Simulation

Horizon-AGN, first described in Dubois et al. (2014), is a state-of-the-art hydrodynamical simulation of a statistically representative volume of the universe in a periodic box of $L_{\text{box}} = 100 h^{-1}$ Mpc on each side, with a Λ cold dark matter (Λ CDM) cosmology. It adopts values of a total matter density $\Omega_m = 0.272$, dark energy density $\Omega_{\Lambda} = 0.728$, amplitude of the linear power spectrum $\sigma_8 = 0.81$, baryon density $\Omega_b = 0.045$, Hubble constant $H_0 = 70.4 \text{ km s}^{-1} \text{ Mpc}^{-1}$, and spectral index $n_s = 0.967$, in concordance to results from the *Wilkinson Microwave Anisotropy Probe 7* (Komatsu et al. 2011).

The simulation follows the formation and evolution of galaxies using the adaptive mesh refinement code RAMSES (Teyssier 2002), with a total of 1024^3 dark matter particles with mass $M_{\text{dm}} = 8 \times 10^7 M_{\odot}$, and a force softening of ~ 2 kpc. It has an initial number of 1024^3 gas cells, which are refined up to seven times reaching a maximum physical resolution of ~ 1 kpc. It includes gas cooling, heating from a uniform redshift-dependent ultraviolet background, star formation, stellar feedback driven by supernovae Type Ia and II, and stellar winds. Black holes (BHs) grow according to a Bondi–Hoyle–Lyttleton accretion scheme capped at the Eddington

accretion rate, and a two-mode active galactic nucleus (AGN) feedback is explicitly implemented as an isotropic thermal energy injection at accretion rates greater than 1 percent the Eddington accretion, and as a bipolar outflow otherwise (see Dubois et al. 2010, 2012, 2014, for further details); these implementations produce BH populations that reproduce the observed evolution of the BH mass density and mass functions (Volonteri et al. 2016).

Horizon-AGN produces galaxy populations whose luminosity and stellar mass functions, as well as star formation main sequence, are in good agreement with the observed ones (Kaviraj et al. 2017). It has also been used to demonstrate that AGN feedback is crucial to produce the observed morphology diversity and kinematic properties of massive galaxies (Dubois et al. 2016), and to show how AGN feedback affects the total density profile of galaxies and dark matter haloes (Peirani et al. 2017, 2019). In addition, the simulation has been used to investigate the alignment between cosmic web filaments and the spins of galaxies, and how mergers change the spin orientation of galaxies (Dubois et al. 2014; Welker et al. 2014).

2.2 Identification of structures

Structure is identified using the code VELOCIRAPTOR, first introduced in Elahi et al. (2011) and subsequently upgraded in Cañas et al. (2019) and Elahi et al. (2019a). Here, we describe the identification process for dark matter haloes, galaxies, and the IHSC.

2.2.1 Galaxies

Galaxies are identified using a phase-space (6D) Friends-of-Friends (FOF, Davis et al. 1985) search to identify phase-space dense structures. The algorithm is described in detail in Cañas et al. (2019), but here we summarize key features. The first step consists of obtaining a configuration space (3D) FOF, which is done using the commonly adopted $b = 0.2$ dark matter interparticle spacing as linking length, l_x . Subsequently a 6DFOF search is done, where l_x is shrunk as galaxies are expected to be more concentrated than dark matter haloes; the velocity space linking length is chosen to be equal to the 3DFOF object velocity dispersion, $l_v = \sigma_v$. Substructures are identified by performing an iterative 6DFOF search, as is used for core-finding in dark matter haloes. A key feature of this process for galaxies is the selection of the initial and iterative parameters used for this search, and properly assigning particles to each of these cores. The most massive galaxy in each 3DFOF object is considered to be the central, and the remaining objects to be substructures/satellites.

2.2.2 Dark matter haloes

Dark matter haloes and their substructure can also be identified with VELOCIRAPTOR. However, because we focus on the stellar mass content in galaxies and the IHSC, dark matter haloes will only be used to refer to the total matter content (stars + BH + gas + dark matter) in the region of interest. Haloes are therefore defined as spherical regions centred at the centre of mass of the most massive galaxy of an FOF object, in which the total mass average overdensity is 200 times the critical density of the universe. Throughout the paper, we use the subscript 200c to refer to properties of these objects, e.g M_{200c} .

¹Referring either to light or mass, which can be interchangeable if a constant mass-to-light ratio, M/L , is assumed.

2.2.3 Defining the IHSC

The IHSC is composed of all the background particles that were not assigned to galaxies in the field 6DFOF search. The parameters that define the IHSC are therefore the linking lengths used for the field 3DFOF and 6DFOF search. Because galaxies and tidal features are identified using a phase-space FOF algorithm, the IHSC is composed of particles that are too far in phase space to be linked to any structure. Physically, this means that the component is diffuse and kinematically hot. This definition allows us to estimate robustly the IHSC for systems of different masses in a cosmological simulation. In Cañas et al. (2019), we showed that our galaxy finding algorithm has also the capability to recover streams and other tidal features. These, however, are a by-product of the algorithm and at this point their robust identification have not been tested yet.²We, therefore, do not include these as part of the IHSC; however, if desired, it is straightforward to include these structures into the IHSC. From preliminary analysis, the mass content in these stellar tidal structures is typically less than a few per cent the IHSC mass.

Moreover, the outer extent of the background particles that compose the IHSC can be defined either by the region delimited by the 3DFOF field search, or by the virial radius R_{200c} . While the second approach provides a theoretical point of comparison with simulations and observations, in the case of merging groups and clusters, some of the diffuse material between such systems might be left out. Throughout this paper, we use the former definition, although we note that both definitions give equivalent results. See Appendix A for a comparison of the total and IHSC stellar mass content using both of these definitions.

In Fig. 1, we give a visual impression of the projected stellar density of all stellar particles (first and third rows) and the IHSC (second and fourth rows) of MW-like mass systems, as well as galaxy groups and clusters. For reference, we show the extent of *fixed spherical* apertures of radius $R_{\text{IHSC}} = \{30, 100\}$ kpc commonly used to separate the central galaxy from the IHSC (e.g. Pillepich et al. 2018b). While fixed spherical apertures are a simple way of separating the mass content in the central galaxy and the IHSC, they do not necessarily provide a robust definition that works for systems displaying a variety of mass distributions that depart from a spherical symmetry, as well as systems of a wide range of masses. For example, a spherical aperture of 30 kpc might be reasonable for MW-like mass systems to separate the stellar content of the central galaxy from that of the IHSC (e.g. systems A and B in Fig. 1). However, for galaxies at the centre of groups and clusters, this aperture can in fact truncate the outer parts of the galaxy (e.g. D, E, and F). In contrast, a larger aperture, for example 100 kpc, could work for massive systems, but will be too large for smaller galaxies encompassing most of the stellar material within the aperture; this can lead to measurements of IHSC mass fraction that are too low as a result of the measurement method. See also Appendix A for a comparison between these different definitions.

To solve these issues, previous studies have implemented adaptive spherical apertures based on the central galaxy + IHSC (CG + IHSC) mass distribution; for example a sphere with radius proportional to the CG + IHSC half-mass radius, $R_{\text{IHSC}} = \beta R_{50}$ (e.g. $\beta = 2.0$, Pillepich et al. 2018b; Elias et al. 2018). However, it is not straightforward to know which value of β should be used to give consistent answers across the mass range covered by

hydrodynamical simulations. Moreover, for this particular choice of R_{IHSC} , the amount of mass that is assigned to the IHSC is likely to depend on the specific distribution of the central galaxy rather than on the properties of the IHSC. For example, the R_{IHSC} of a system with a spiral central galaxy will be larger than that of an elliptical galaxy with same stellar mass only because of their intrinsic mass distribution (e.g. van der Wel et al. 2014); in this case, a lower mass fraction in the IHSC would be expected for spirals compared to ellipticals *because of the method* rather than the properties of the IHSC.

By defining the IHSC as the kinematically hot component, we are able to address all the issues that spherical aperture definitions have, as is seen in the IHSC projections of Fig. 1. Moreover, by having the capability to consistently define the IHSC for systems with a wide range of masses, we can perform statistical studies of the IHSC in entire cosmological simulations, as well as systematically following the evolution of the IHSC for both individual systems and complete entire populations.

For simplicity, throughout this paper we refer to 3DFOF objects as ‘systems’, which would typically be composed by a central galaxy, its satellite galaxies, and the IHSC.

2.3 Calculated properties

In this section, we describe how we calculate the properties of systems and galaxies used in upcoming sections.

2.3.1 Number of satellites

The number of satellites of a given system (3DFOF) is the count of substructures found by VELOCIRAPTOR composed of more than 50 stellar particles.

2.3.2 Mass content

The stellar mass of objects will be denoted by the subscript ‘*’ and a label. This quantity refers to the sum of the mass of all stellar particles in that object/component as identified by VELOCIRAPTOR. For the total mass content inside R_{200c} , i.e. stars + gas + BH + dark matter, we will simply refer to as M_{200c} , and $M_{*, 200c}$ for the stellar mass only within R_{200c} .

2.3.3 V/σ

For the kinematic morphology parameter V/σ of the central galaxies, we first calculate the spherical radius that encloses 50 per cent of the stellar mass of the central galaxy,³ R_{50} . Then, we calculate the specific angular momentum, \mathbf{j} , for all the particles within R_{50} , i.e.

$$\mathbf{j} = \frac{1}{M_{*, R_{50}}} \sum_i^{r_i \leq R_{50}} \mathbf{r}_i \times m_i \mathbf{v}_i, \quad (1)$$

where \mathbf{r}_i and \mathbf{v}_i are the position and velocity vectors of stellar particle i , with mass m_i , measured with respect to the galaxy’s centre of mass; and $M_{*, R_{50}}$ is the mass inside R_{50} , or equivalently $M_{*, R_{50}} = 0.5 M_{*, \text{ctrl}}$.

²Within VELOCIRAPTOR there is built-in code that has been used to identify dark matter tidal structures (e.g. Elahi et al. 2013), the implementation of this tool within the IHSC is beyond the scope of this work.

³Note that we consider the central galaxy and the IHSC as separate components, therefore no IHSC particles are included in the computation of the half-mass radius.

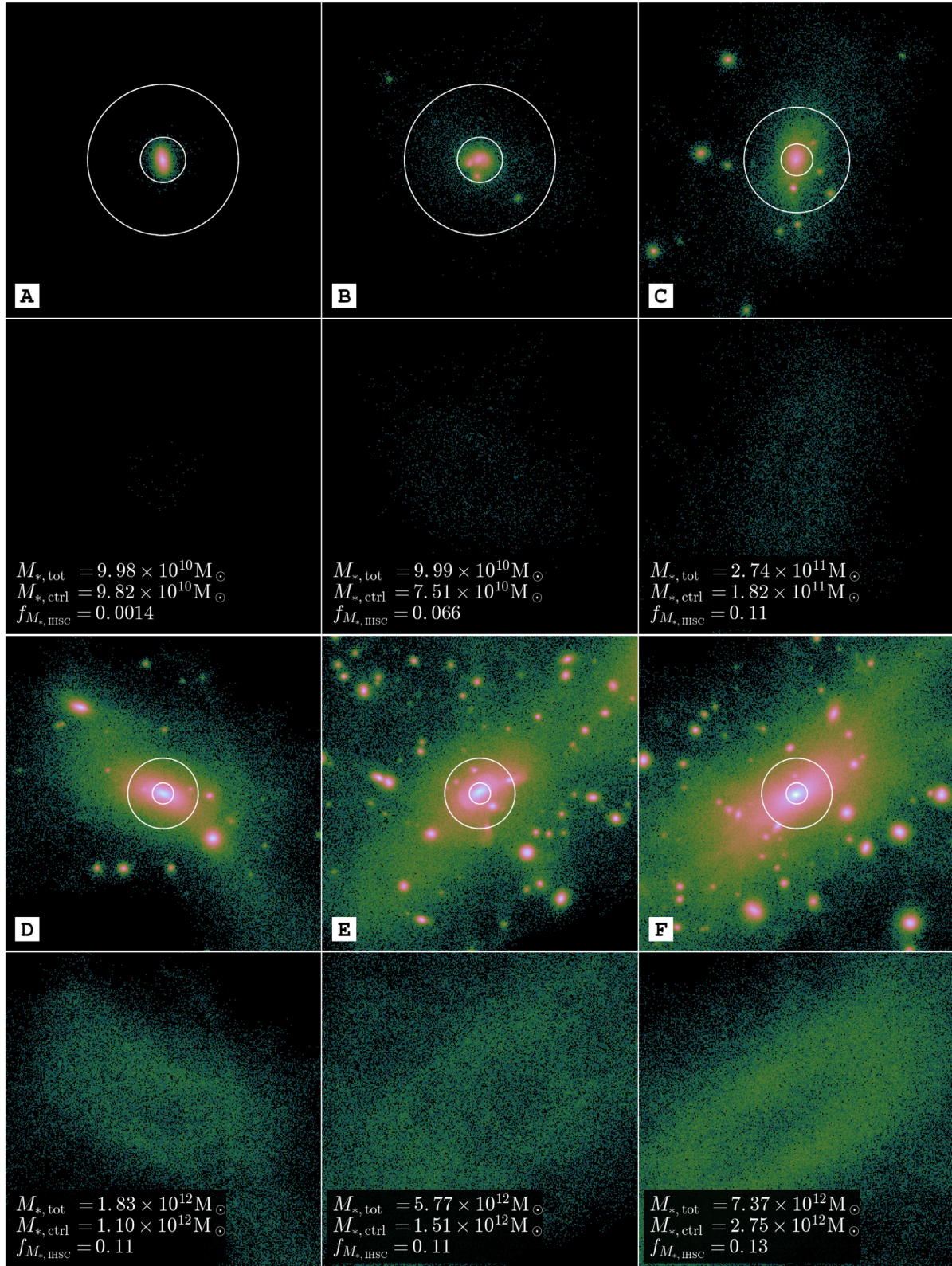


Figure 1. Projected stellar mass density of all the stellar particles inside 3DFOF objects (first and third rows), and its IHSC as identified using VELOCIRAPTOR (second and fourth rows). 3DFOF total stellar mass, $M_{*, \text{tot}}$, central galaxy stellar mass, $M_{*, \text{ctrl}}$, and IHSC mass fraction $f_{M_{*, \text{IHSC}}} = M_{*, \text{IHSC}}/M_{*, \text{tot}}$ are shown for each object. Circles show 30 and 100 kpc apertures commonly used in the literature to separate the central galaxy from the stellar halo/ICL.

The rotational velocity V is calculated as

$$V = \frac{|\mathbf{j}|}{R_{50}}. \quad (2)$$

The velocity dispersion σ is calculated as the average 3D velocity dispersion of all stellar particles within R_{50} ,

$$\sigma_{v_x}^2 = \frac{1}{M_{*,R50}} \sum_i^{r_i \leq R_{50}} m_i v_{x,i}^2, \quad (3)$$

$$\sigma = \frac{1}{3} \sqrt{\sigma_{v_x}^2 + \sigma_{v_y}^2 + \sigma_{v_z}^2}, \quad (4)$$

where $v_{x,i}$ is the velocity of particle i along the Cartesian axis x , and σ_{v_x} , σ_{v_y} , and σ_{v_z} are the velocity dispersions along the x -, y -, and z -axes, respectively. Finally, the kinematic morphology parameter V/σ is simply the ratio between these quantities.

2.3.4 Star formation rate

The star formation rate (SFR) of a galaxy is calculated by summing the mass of all its stellar particles with age, t_{age} , smaller than a given Δt window from the time of the snapshot analysed,

$$\text{SFR} = \frac{1}{\Delta t} \sum_i^{t_{\text{age},i} < \Delta t} m_i. \quad (5)$$

Throughout this paper, we adopt a $\Delta t = 50$ Myr to calculate this quantity. SFRs calculated using windows of $\Delta t = \{20, 100\}$ Myr, are consistent with that of $\Delta t = 50$ Myr. Mass loss due to stellar evolution is neglected, however; if included, it would represent a systematic shift of the estimated SFRs, and would not change our conclusions.

3 PRESENT-DAY $f_{M_*,\text{IHSC}} - M_*$ RELATION

The IHSC mass fraction, $f_{M_*,\text{IHSC}}$, is calculated as

$$f_{M_*,\text{IHSC}} = \frac{M_{*,\text{IHSC}}}{M_{*,\text{tot}}}, \quad (6)$$

where $M_{*,\text{IHSC}}$ is the stellar mass of the IHSC, and $M_{*,\text{tot}}$ is the total stellar mass of the system that includes all the stellar mass in the galaxies (central and satellites) and the IHSC. As shown in Cañas et al. (2019), VELOCIRAPTOR's galaxy finding algorithm is also capable of identifying tidal structures, such as stellar streams and shells, as separate objects that are distinct in phase space from the galaxies and are kinematically colder than the IHSC envelope. These structures are often incorporated into the IHSC because of their diffuse and accreted nature, in the sense that their stars do not form in the main galaxy/dark matter halo branch, similar to the outskirts of galaxies and clusters (*in situ* versus *ex situ*, e.g. Pillepich et al. 2015; Dubois et al. 2016). We argue, however, that it is important to separate such structures from the IHSC as some of that material may be accreted on to the galaxy at later times. Although these tidal structures can be found with ease by VELOCIRAPTOR, for the purposes of this study we consider all kinematically distinct stellar structures as satellite galaxies, while the IHSC is only the *diffuse* stellar background.

In Fig. 2, we show the $f_{M_*,\text{IHSC}} - M_*$ relation in Horizon-AGN at $z = 0$. The measurements for individual systems (i.e. entire 3DFOF objects) are shown as black dots. Dashed and dotted-dashed blue lines delimit regions where, at fixed total stellar mass, the IHSC is composed of ≤ 100 and ≤ 10 particles, respectively. At $10^{10.5} \lesssim M_{*,\text{tot}}/M_\odot \lesssim 10^{12} M_\odot$, $f_{M_*,\text{IHSC}}$ increases with increasing $M_{*,\text{tot}}$, with the scatter decreasing as $M_{*,\text{tot}}$ increases. At $M_{*,\text{tot}} > 10^{12} M_\odot$, the

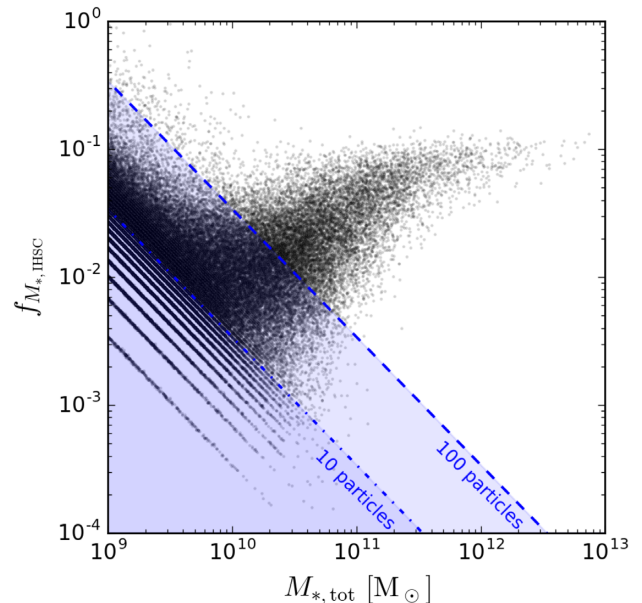


Figure 2. Mass fraction in the IHSC, $f_{M_*,\text{IHSC}}$, as identified by VELOCIRAPTOR, as a function of total stellar mass $M_{*,\text{tot}}$ at $z = 0$ for all systems in the Horizon-AGN simulation, shown as black dots. Blue dashed and dotted-dashed lines delimit regions where the IHSC at a given $M_{*,\text{tot}}$ is composed by ≤ 100 and ≤ 10 particles, respectively. See the text for more details.

relation flattens, while the scatter keeps decreasing out to the most massive system resolved in Horizon-AGN, $M_{*,\text{tot}} \sim 10^{13} M_\odot$.

The variation in $f_{M_*,\text{IHSC}}$ at fixed $M_{*,\text{tot}}$ is ~ 2 dex at $M_{*,\text{tot}} \simeq 3 \times 10^{10} M_\odot$ ($M_{200c} \simeq 10^{12} M_\odot$), and gradually decreases towards higher $M_{*,\text{tot}}$. This is caused by changes in the principle mode of growth of a system. At $M_{*,\text{tot}} < 10^{12} M_\odot$ ($M_{200c} < 10^{13} M_\odot$) systems grow either via continuous infall of gas and star formation; accretion of multiple satellite galaxies; or a combination of these two. The large dispersion observed at these masses is therefore a consequence of the various growth mechanisms these systems can undergo (this is demonstrated in Section 5). In contrast, mass growth at $M_{*,\text{tot}} > 10^{12} M_\odot$ is expected to be dominated by interactions and galaxy mergers (Oser et al. 2010; Rodriguez-Gomez et al. 2016; Dubois et al. 2013, 2016). Because this is the dominant growth mechanism, we expect that these systems will display a tighter distribution in the $f_{M_*,\text{IHSC}} - M_*$ relation. It is important to note, however, that the limited volume of Horizon-AGN means that it contains only a handful of systems with $M_{*,\text{tot}} > 10^{12} M_\odot$, and so the tight distribution observed at these masses may be due to poor statistics.

At $M_{*,\text{tot}} < 10^{10} M_\odot$, there is an apparent anticorrelation between $M_{*,\text{tot}}$ and $f_{M_*,\text{IHSC}}$. This is a consequence of the resolution limit of the simulation. In Horizon-AGN, stellar particles have a mass resolution of $M_* \simeq 3 \times 10^6 M_\odot$, which means that in a galaxy composed by 300 particles (i.e. $M_* = 10^9 M_\odot$), an $f_{M_*,\text{IHSC}} = 0.01$ will be composed by only three particles. Such features are visible as diagonal patterns at $f_{M_*,\text{IHSC}} < 0.01$ and $M_{*,\text{tot}} < 10^{10} M_\odot$, which extends to the upturn observed in the relation and is delimited by the 100 particle limit (blue dashed line). This upturn towards lower $M_{*,\text{tot}}$ is also an effect caused by the method used: at spatial scales close to the resolution limit of the simulation, 3DFOF objects can often be decomposed into sparse particle distributions with interparticle distances comparable to the 3DFOF linking length; by construction such particles are not linked to galaxies by the 6DFOF

search, and are therefore assigned to the IHSC, giving high $f_{M_*,\text{IHSC}}$ for 3DFOF objects close to the resolution limit.

The overall shape of the relation is similar to the *accreted* stellar mass fraction total stellar mass relation (e.g. Cooper et al. 2013; Rodríguez-Gomez et al. 2016), but it is important to note that these two quantities are not the same. We expect this similarity because the mass budget in the outskirts of galaxies and clusters, included in the IHSC, is dominated by stars that originated in satellite galaxies, i.e. were accreted into the host galaxy/dark matter halo. However, accreted mass estimates also take into account the stellar mass bound to satellites, as well as stars in the central galaxy that were not formed along the main galaxy branch, and is the reason why the amplitude of accreted stellar mass fractions is larger than $f_{M_*,\text{IHSC}}$ at similar $M_{*,\text{tot}}$.

3.1 Parameter dependence of the IHSC

We mentioned in Section 2.2 that the IHSC is determined by the choice of linking lengths used for the 6DFOF field search. As the velocity linking length in the 6DFOF search is chosen to be proportional to the velocity dispersion of each system, the only user-defined parameter is the configuration space linking length, $l_{x,6D}$. This parameter sets a phase-space density cut on the particles that are linked to galaxies, excising them from the IHSC. Therefore, larger values of $l_{x,6D}$ will assign more mass to the galaxies and less to the IHSC and vice versa, as was qualitatively explored in appendix A of Cañas et al. (2019). Here, we study in detail the effects different choices of $l_{x,6D}$ have on the estimated IHSC mass, $M_{*,\text{IHSC}}$. Recalling step 2 of the galaxy identification method used in Cañas et al. (2019, section 3.1.2), the configuration space linking lengths are defined as

$$l_{x,3D} = b \Delta x,$$

$$l_{x,6D} = f_{l_{x,6D}} l_{x,3D}, \quad (7)$$

where Δx is the mean interparticle spacing of dark matter particles in the simulation, and b and $f_{l_{x,6D}}$ are constants <1 ; we adopt the commonly used value of $b = 0.2$.

In Fig. 3, we show the effect that changing $f_{l_{x,6D}}$ has on the $f_{M_*,\text{IHSC}} - M_*$ relation, as estimated using different values of $f_{l_{x,6D}}$; solid lines show medians in equal log-spaced mass bins, and shaded regions delimit the 16th and 84th percentiles of the distribution in each mass bin. Increasing $f_{l_{x,6D}}$ has the effect of changing the overall normalization of the $f_{M_*,\text{IHSC}} - M_*$ relation, in a way that increasing $f_{l_{x,6D}}$ leads to a lower $f_{M_*,\text{IHSC}}$. In addition, the scatter of the relation below $10^{12} M_\odot$ also depends on $f_{l_{x,6D}}$, with higher values leading to larger scatter. Despite these differences, the overall behaviour of the $f_{M_*,\text{IHSC}} - M_*$ relation is qualitatively the same: $f_{M_*,\text{IHSC}}$ increases with $M_{*,\text{tot}}$ up to $M_{*,\text{tot}} \sim 10^{12} M_\odot$, followed by a flattening at higher masses. The scatter also decreases monotonically with increasing $M_{*,\text{tot}}$, which is in part caused by the limited volume of Horizon-AGN. The increasing $f_{M_*,\text{IHSC}}$ at fixed mass with decreasing linking length is expected as higher $f_{l_{x,6D}}$ values result in assigning more particles to galaxies, reducing the mass in the IHSC. It should be noted that for small $f_{l_{x,6D}}$ values, resolution effects (i.e. upturn in the relation) become important at smaller $M_{*,\text{tot}}$ (vertical dotted–dashed line). Observations at this stage are shown for reference.⁴

In Fig. 4, we compare the estimated mass in the IHSC to that in

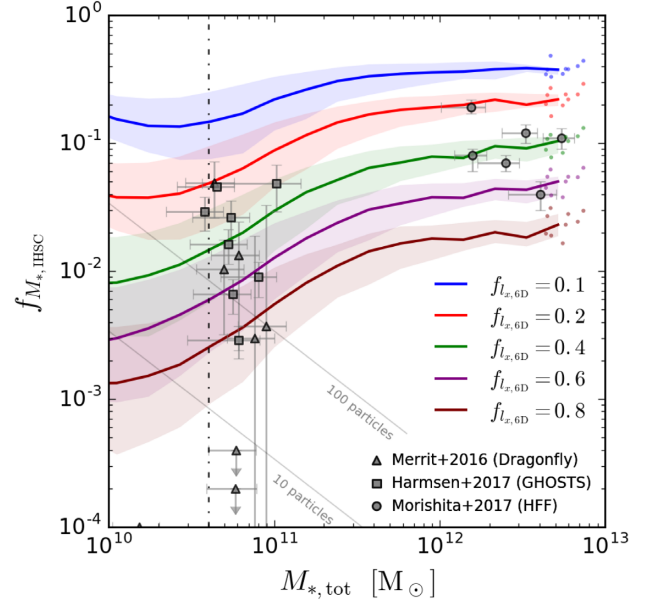


Figure 3. Mass fraction in the IHSC $f_{M_*,\text{IHSC}}$ (top left), and mass content in the IHSC and central as estimated using $f_{l_{x,6D}} = \{0.1, 0.2, 0.4, 0.6, 0.8\}$, coloured as labelled. Solid lines represent the median $f_{M_*,\text{IHSC}}$ for each $M_{*,\text{tot}}$ bin and shaded regions delimit the 16th and 84th percentile of the distribution in that bin; vertical dotted–dashed line indicate the $M_{*,\text{tot}}$ where measurements are considered not to be affected by resolution. Observational estimates of mass fraction in stellar haloes from Merritt et al. (2016) and Harmsen et al. (2017) and ICL (Morishita et al. 2017) are shown as symbols, as labelled.

the central galaxy, $M_{*,\text{ctrl}}$, and to the total stellar mass in satellites, $M_{*,\text{sats}}$. For each $f_{l_{x,6D}}$, we fit a power law as $M_{*,\text{IHSC}} \propto M_*^\alpha$, to the mean $M_{*,\text{IHSC}}$ per M_* bin, shown as dashed coloured lines, with power-law index α as labelled; bins are required to have at least five systems and an $M_{*,\text{tot}} > 4 \times 10^{10} M_\odot$ to avoid consideration of systems affected by resolution; points show individual measurements of resolved systems in bins with less than five systems. The mass relations between these components are strikingly similar for different values of $f_{l_{x,6D}}$, with power-law index variations smaller than 5 per cent. This agreement is remarkable due to the large range of $f_{l_{x,6D}}$ and stellar masses explored. Moreover, the extrapolation of the fit to each distribution does seem to be in agreement as well with mass estimations of high-mass systems where statistics are low.

The agreement between the mass relations shows that the robustness of our results rely on the methodology and not on a specific choice of $f_{l_{x,6D}}$.⁵ This consistency can also be used to make predictions that can easily be tested by observations. For example, the fact that $\alpha \sim 1$ for the $M_{*,\text{IHSC}} - M_{*,\text{sats}}$ relation tells us that *on average* the IHSC mass is a constant fraction of the total mass in satellites. In fact, although in Fig. 4 $M_{*,\text{sats}}$ includes all substructures found by VELOCIRAPTOR composed of at least 50 particles (i.e. $M_* \geq 10^7 M_\odot$), the power-law index α is also consistent if mass

space-based approach that we take. We show them to indicate to the reader as an approximate comparison, illustrating how published estimates of $f_{M_*,\text{IHSC}}$ vary with mass; a more careful, like-for-like, comparison is beyond the scope of this paper.

⁵We must remember that as with any other method, poorly chosen parameters affect properties of individual galaxies, e.g. extremely short values of $f_{l_{x,6D}}$ are likely to identify only the cores of galaxies. See appendix A of Cañas et al. (2019) for a visual example.

⁴Each of the observational data sets shown in Fig. 3 are based on estimates of the $f_{M_*,\text{IHSC}}$ using different approaches, which are distinct from the phase-

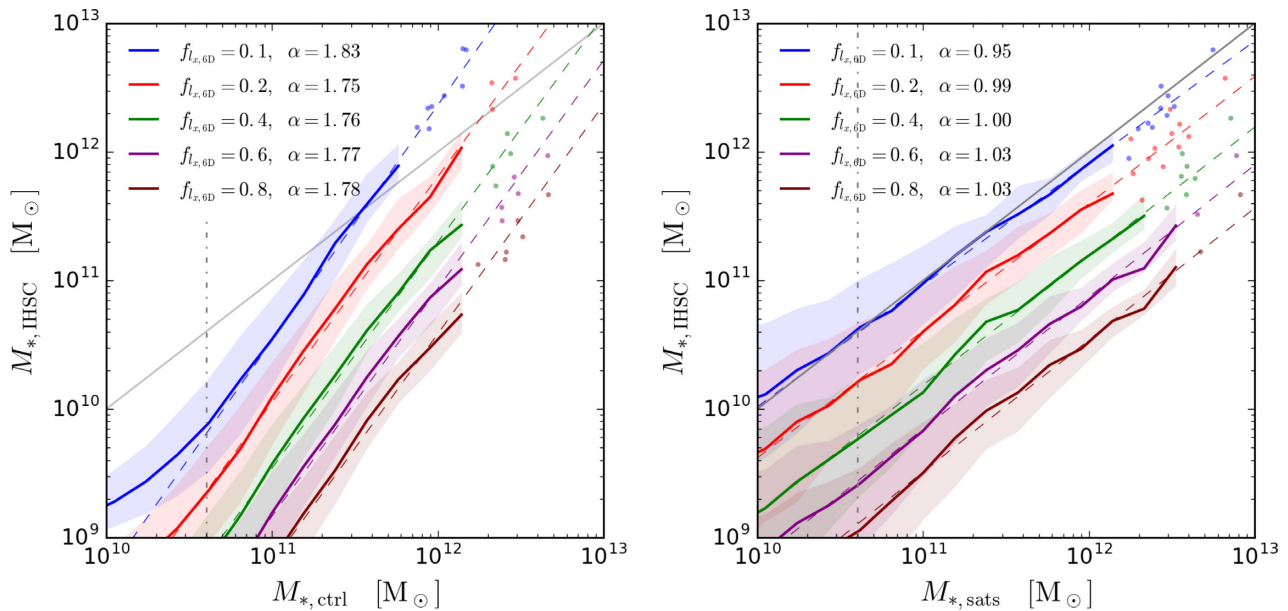


Figure 4. Stellar mass content of the IHSC as a function of the central galaxy stellar mass (left-hand panel), and the total stellar mass in satellite galaxies (right-hand panel) as estimated using $f_{i,x,6D} = \{0.1, 0.2, 0.4, 0.6, 0.8\}$, as labelled. Solid lines represent the median $f_{M_*,\text{IHSC}}$ for each $M_{*,\text{tot}}$ bin and shaded regions delimit the 16th and 84th percentiles. Dashed lines show power-law fit to the *mean* $M_{*,\text{IHSC}}$ (power-law index α as labelled) in equally log-spaced resolved M_* bins; bins with less than five measurements are not considered, systems in such bins are shown as dots; diagonal grey lines show a 1-to-1 correspondence. These relations are remarkably consistent and independent of the specific $f_{i,x,6D}$ used. The latter demonstrates the robustness of our method to define the IHSC and sets strong predictions that can be easily tested against observations.

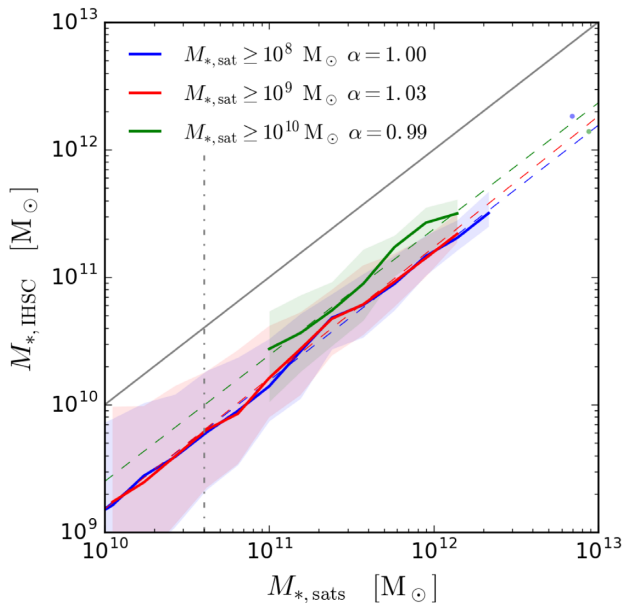


Figure 5. IHSC mass as a function of the total stellar mass in satellites with stellar masses $>10^8$, 10^9 , and $10^{10} M_\odot$, for $f_{i,x,6D} = 0.4$. Solid lines shows the median in each mass bin, and shaded regions delimit the 16th and 84th percentiles. Similarly to Fig. 4 dashed lines show a power-law fit to the median. The mass relation between $M_{*,\text{sats}}$ and $M_{*,\text{IHSC}}$ is consistent even when only satellites with $M_* > 10^8$ and $10^9 M_\odot$ are used. For a mass threshold of $10^{10} M_\odot$, the relation has a similar slope but is shifted towards the left.

thresholds of 10^8 and $10^9 M_\odot$ are used, as shown in Fig. 5. These results highlight the advantage of using phase-space iso-density cuts over fixed spherical aperture definitions of the IHSC, where the choice of parameter R_{IHSC} does affect the slope measured (e.g.

Pillepich et al. 2018b). The latter can be understood because the stellar mass distributions of systems of different mass (e.g. MW-like and cluster) are not self-similar, nor necessarily spherically symmetric; therefore, the mass enclosed within spherical shells assigned to the central (IHSC) for an increasing (a decreasing) R_{IHSC} correspond to a varying fraction across $M_{*,\text{tot}}$, and consequently they will not preserve the mass relation between these components. See Appendix A for complementary comparisons to spherical apertures.

The observed behaviour of our method is quite a useful finding for both simulations and observations because definition of the IHSC (i.e. stellar halo, IGL, and ICL) often relies on defining or delimiting the extent of galaxies, which is not a straightforward task because there is no ‘true’ definition of where galaxies end. In this study, we adopt $f_{i,x,6D} = 0.4$, because it predicts a $f_{M_*,\text{IHSC}} - M_*$ relation that is in better agreement with the estimated stellar halo mass fractions for MW-like galaxies from Merritt et al. (2016) and Harmsen et al. (2017), and recent ICL mass estimations of Morishita et al. (2017). Although the exact method to measure the stellar halo and ICL mass fraction differs between our method and previous observational studies, this comparison provides an equivalent phase-space density threshold (i.e. $f_{i,x,6D}$ value) for the particular characteristics of a given set of observations. The latter is useful as reference in cases where a one-to-one comparison is not possible, such as individual stellar counts.

3.2 Comparison to IHSC definitions in literature

As mentioned above, for simplicity and ease of comparison, studies in the literature have used geometrical definitions of the IHSC. In Fig. 6, we compare the $f_{M_*,\text{IHSC}}$ obtained with our method to that of spherical apertures with $R_{\text{IHSC}} = 30 \text{ kpc}$, 100 kpc , $2 R_{50}$. To properly compare the methods we show the $f_{M_*,\text{IHSC}}$ as a function of the total stellar mass within R_{200c} , i.e. $M_{*,200c}$. A visual represen-

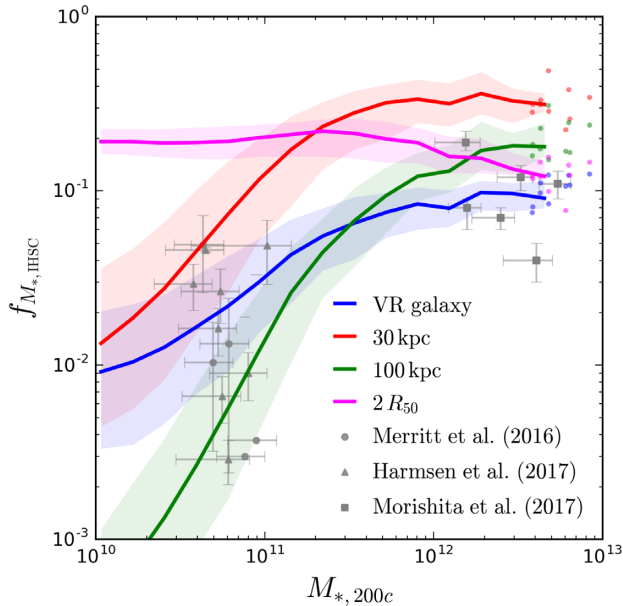


Figure 6. Mass fraction in the IHSC, $f_{M_*, \text{IHSC}}$, as a function of total stellar mass within spherical overdensity $M_{*, 200c}$ (top) and total halo mass M_{200c} (bottom). At $M_{*, 200c} < 10^{11} M_{\odot}$ compared to observations $2 R_{50}$ overestimates the estimated $f_{M_*, \text{IHSC}}$, 100 kpc aperture underestimates it, and VELOCIRAPTOR and 30 kpc aperture are in better agreement. At $M_{*, 200c} > 10^{12} M_{\odot}$, fixed apertures overestimate the $f_{M_*, \text{IHSC}}$ estimated by observations, while a better agreement is shown by VELOCIRAPTOR and $2 R_{50}$ aperture. Our adaptive phase-space method allows us to get IHSC mass fractions in better agreement with observations in the whole mass range.

tation and a comparison of the mass content with these definitions is shown in Appendix A. Observations are shown for reference. At MW scales, i.e. $M_{*, 200c} \sim 10^{11} M_{\odot}$, $2 R_{50}$ overestimates the $f_{M_*, \text{IHSC}}$, as the median of their distribution goes through the galaxies with the highest $f_{M_*, \text{IHSC}}$ of the observed sample; the 30 kpc aperture median is in slight better agreement, while the 100 kpc aperture underestimates the $f_{M_*, \text{IHSC}}$ at these masses. At the high mass both fixed apertures overestimate the $f_{M_*, \text{IHSC}}$ compared to the estimated from the Frontier Field clusters, while $2 R_{50}$ is in better agreement with these measurements.

Our method has the particular advantage over ones based on spherical apertures in so far as it is capable of predicting IHSC mass fractions on both MW and galaxy cluster scales. This is because it is designed to adapt to the physical scale of the system being investigated, and so offers a physically motivated, shape independent, consistent definition of the IHSC, representing a considerable improvement over previous studies. While there exist other methods in the literature that make use of the velocity information of the particles (e.g. Dolag et al. 2010; Cui et al. 2014), these only apply for a given population, while our method provides a consistent definition of the IHSC across a wide range of masses.

4 UNVEILING THE NATURE OF THE $f_{M_*, \text{IHSC}} - M_*$ RELATION

One of the aims of this study is to understand the origin of the scatter observed in the $f_{M_*, \text{IHSC}} - M_*$ relation (e.g. Merritt et al. 2016; Harmsen et al. 2017). In this section, we explore how the mass fraction in the IHSC, $f_{M_*, \text{IHSC}}$, correlates with observables, specifically with those that relate directly to environment and

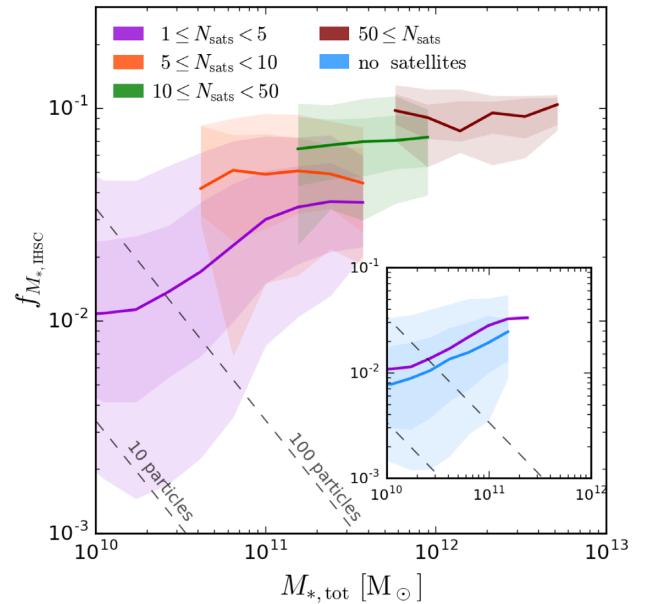


Figure 7. $f_{M_*, \text{IHSC}} - M_*$ relation separating it into subsamples of systems with different total number of satellites, N_{sats} . Solid lines show the median of the distribution, and shaded regions delimit the 1σ and 2σ , respectively. Colours show the subsamples using different N_{sats} thresholds. Inset in the top panel show the contribution of systems with no identified satellites.

accretion history. We remind the reader that throughout this paper we refer to a ‘system’ as the ensemble of components in a 3DFOF object, composed of a central galaxy, satellites, and its IHSC. Here, we focus on *static* properties of systems, i.e. properties that can be measured at a fixed time-step, to provide guidance on possible third parameters that could be explored in observations that would help to interpret the observed scatter. All the measurements presented in this section are done at $z = 0$; in subsequent sections we will focus on their temporal evolution.

4.1 Number of satellites

As the IHSC is built from the tidal debris of orbiting satellites and mergers, we expect that the mass in the IHSC should correlate with the accretion history of a halo, as well as with the availability of material that can be deposited into the IHSC. In Fig. 7, we show the $f_{M_*, \text{IHSC}} - M_*$ relation for subsamples according to the *current* number of satellites, N_{sats} , as identified by VELOCIRAPTOR.

Overall, more massive systems tend to have a higher number of satellites, as expected from hierarchical growth. However, in the range in which there is overlap between the samples with different number of satellites, we see that a system with a larger total number of satellites display a higher $f_{M_*, \text{IHSC}}$ at fixed $M_{*, \text{tot}}$. Although the scatter around the $f_{M_*, \text{IHSC}} - M_*$ relation in each subsample is large, the correlation between $f_{M_*, \text{IHSC}}$ and N_{sats} is noticeable at $2 \times 10^{11} \lesssim M_{*, \text{tot}}/M_{\odot} \lesssim 4 \times 10^{11}$, in which the distribution of three subsamples of different N_{sats} overlap. However, the 1σ regions are typically large enough that they overlap, and hence a point in the $f_{M_*, \text{IHSC}} - M_*$ plane cannot be robustly associated with a single value of N_{sats} .

It is important to note that for lower masses and less populated systems, the scatter is quite large, ~ 0.5 dex (~ 1 dex) for 1σ (2σ). This can be caused by a variety of factors. For example, at fixed $M_{*, \text{tot}}$ a system with only one satellite that has just accreted is likely to have a very different $f_{M_*, \text{IHSC}}$ than another one-satellite

system in which the satellite has had enough time to interact with the central galaxy, and therefore deposit material into the IHSC. In fact, after only one orbit, an average subhalo is expected to lose ~ 50 per cent of its infall mass after its first pericentric passage, and up to ~ 80 per cent after its second (Poultou et al. 2020). For this reason, we expect to be within a given subsample’s scatter in the $f_{M_*,\text{IHSC}} - M_*$ relation. Moreover, a system without satellites could have a quiescent accretion history, or its satellites may have already merged with the central galaxy. This possibility can be seen in the inset where the distribution of systems without satellites is shown; although the overall amplitude of $f_{M_*,\text{IHSC}}$ is lower than we see in the $1 < N_{\text{sats}} < 5$ sample, both the medians and the size of scatter are comparable, almost overlapping.

If we repeat the exercise of Fig. 7, but limit it to satellites above $10^9 M_\odot$ (which is a typical value adopted to avoid resolution effects; see e.g. Dubois et al. 2016), we find that the relation between $f_{M_*,\text{IHSC}} - M_*$ and N_{sats} prevails, but becomes weaker. If we limit ourselves to only the massive satellites, $M_* > 10^{10} M_\odot$, we find no dependence of the scatter of the $f_{M_*,\text{IHSC}} - M_*$ on N_{sats} . This is not necessarily surprising because the dynamical friction time-scale of massive galaxies is much shorter than low-mass ones, and hence the current number of massive satellites is not necessarily a good indication of the overall assembly history of a system.

4.2 Dynamical state

While the abundance of substructures give information about the environment of a system, there is no evolutionary information that can be obtained by a satellite count. Because the IHSC is built from disrupted material from ongoing and past interactions between galaxies, as mentioned above, the expected $f_{M_*,\text{IHSC}}$ of a system is likely to be different at the time a satellite has just been accreted compared to a later epoch when interactions have already taken place and mass has been deposited into the IHSC. We explore this idea by using the ratio between the masses of the largest satellite (or second most massive galaxy), $M_{*,\text{scnd}}$, and the central galaxy, $M_{*,\text{ctrl}}$, as a proxy for the dynamical age of a system. This definition is widely used in observations because it is readily accessible (e.g. Davies et al. 2019). As dynamical friction is more efficient on massive satellites, their orbits are expected to decay more quickly than those of less massive satellites, and they will have more significant interactions with the central galaxy more quickly than less massive substructures; this suggests that a higher $M_{*,\text{scnd}}/M_{*,\text{ctrl}}$ should indicate that the system is young, and debris from interactions are yet to be deposited into the IHSC. On the other hand, smaller $M_{*,\text{scnd}}/M_{*,\text{ctrl}}$ are typically associated with dynamically old systems, indicating that interactions with larger satellites might have already occurred, and mass has been deposited on to the IHSC.

In Fig. 8, we show the $f_{M_*,\text{IHSC}} - M_*$ relation for subsamples of different $M_{*,\text{scnd}}/M_{*,\text{ctrl}}$; using mass ratios of $[0.001,0.05]$, $[0.05,0.3]$, and $[0.3,1.0]$, which mimic commonly adopted thresholds to classify mergers as mini, minor, and major, respectively. At $M_{*,\text{tot}} < 10^{11.6} M_\odot$, we find that the three samples of $M_{*,\text{scnd}}/M_{*,\text{ctrl}}$ have similar medians as well as 1σ and 2σ contours. It is only at $M_{*,\text{tot}} > 10^{11.6} M_\odot$ that we start to see the expected dependence of a higher $f_{M_*,\text{IHSC}}$ as $M_{*,\text{scnd}}/M_{*,\text{ctrl}}$ decreases at fixed $M_{*,\text{tot}}$. The fact that $M_{*,\text{scnd}}/M_{*,\text{ctrl}}$ disentangles the distributions only at larger $M_{*,\text{tot}}$ is because mergers are the principal mechanisms through which these systems grow (see e.g. Oser et al. 2010; Dubois et al. 2016; Rodriguez-Gomez et al. 2016 for simulations, Robotham et al. 2014 for observational evidence). While these results are indicative,

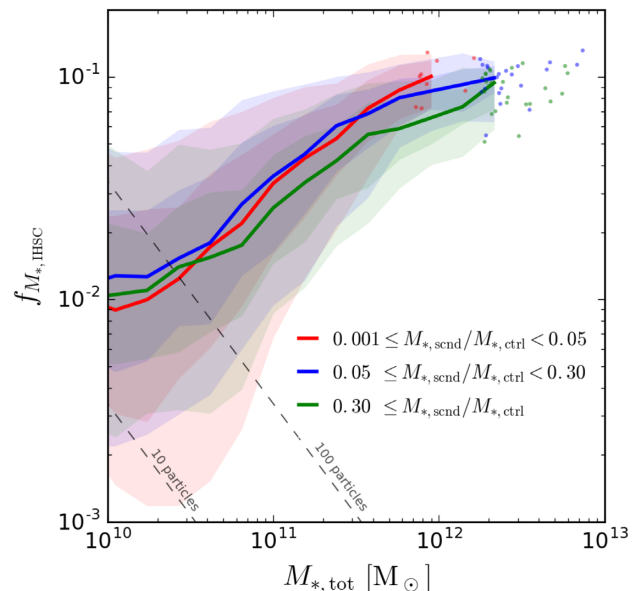


Figure 8. Same as Fig. 7, the $f_{M_*,\text{IHSC}} - M_*$ relation into subsamples of galaxies of different $M_{*,\text{scnd}}/M_{*,\text{ctrl}}$, as labelled. The overlap between the medians and σ contours of different subsamples, indicates that there is no correlation between $f_{M_*,\text{IHSC}}$ and $M_{*,\text{scnd}}/M_{*,\text{ctrl}}$ for systems with $M_{*,\text{tot}} > 10^{11.5}$. At the high-mass end, the distribution of subsamples suggest that in fact this proxy for dynamical age is a good indicator of the expected IHSC mass fraction of a system, with dynamically younger systems displaying a lower $f_{M_*,\text{IHSC}}$, and vice versa; the latter being consequence of the dominant growth mechanisms at this mass range. See the text for further details.

stronger conclusions cannot be made because of the small number of systems with $M_{*,\text{tot}} > 10^{12} M_\odot$ that can be resolved by the Horizon-AGN simulation box ($L_{\text{box}} = 100 h^{-1}$ Mpc).

4.3 Kinematic morphology

The internal properties of the central galaxy provide additional information about the accretion history of a system. Previous studies have found that galaxies with low V/σ are mostly formed by mergers (Dubois et al. 2013, 2016), particularly dry mergers (Lagos et al. 2018b). Although several routes can lead the formation of the so-called slow rotators (Naab et al. 2014), large cosmological hydrodynamical simulations have allowed the statistical inference of the dominant mechanism behind their formation (Penoyre et al. 2017; Lagos et al. 2018b). Therefore, we expect that kinematic morphology gives us an indication of the merger history of the galaxy. Here, we use the kinematic morphology V/σ of the central galaxy as an indicator of the accretion history experienced by a system. We note that V/σ for Horizon-AGN galaxies does indeed reflect the properties expected for a galaxy given its visual morphology; see for instance fig. 2 of Dubois et al. (2016).⁶

In Fig. 9, we show the $f_{M_*,\text{IHSC}} - M_*$ relation, separating systems into subsamples according to the V/σ of their central galaxy, as labelled. At all masses, systems with high $f_{M_*,\text{IHSC}}$ host a highly dispersion-supported galaxy, while a lower $f_{M_*,\text{IHSC}}$ corresponds to systems hosting a rotationally supported galaxy. There is a clear

⁶Note that although the exact way of calculating V/σ for this study differs from that of Dubois et al. (2016), low (high) V/σ values correspond to spheroidal (disc) dominated galaxies for both methods.

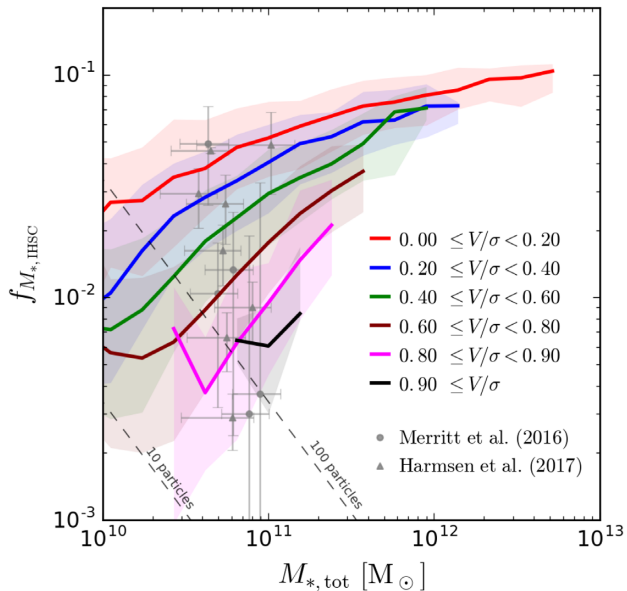


Figure 9. Same as Fig. 7, but the $f_{M_*, \text{IHSC}} - M_*$ relation into subsamples of galaxies of different V/σ , as labelled. For clarity, we only show only 16th–84th percentiles shaded regions. Observational estimates from Merritt et al. (2016) and Harmsen et al. (2017) are shown as grey symbols. It is clear that the $f_{M_*, \text{IHSC}}$ does show an anticorrelation with the kinematic morphology V/σ of the central galaxy; the medians of each subsample do not overlap and show a continuous transition from high V/σ and low $f_{M_*, \text{IHSC}}$ towards low V/σ and high $f_{M_*, \text{IHSC}}$. The observed behaviour is consistent with the expected active assembly history of galaxies supported mainly by dispersion, and a more quiescent one for rotationally supported ones. See the text for a more extensive discussion.

distinction between different subsamples as their medians do not overlap or cross each other; moreover, there is a gradual transition between subsamples from low $f_{M_*, \text{IHSC}}$ and high V/σ , to high $f_{M_*, \text{IHSC}}$ and low V/σ . These results are consistent with the notion that rotationally supported galaxies should have had quiescent accretion histories, and consequently lower $f_{M_*, \text{IHSC}}$. Lagos et al. (2018b) found that the highest V/σ galaxies can only be obtained in the absence of mergers. On the other hand, a dispersion-supported galaxy is expected to have experienced multiple mergers and interactions, which in turn should deposit higher amounts of mass into the IHSC, increasing its $f_{M_*, \text{IHSC}}$.

We find that of the properties explored, the kinematic morphology of the central galaxy displays the strongest (anti)correlation with the $f_{M_*, \text{IHSC}}$ at $M_{*, \text{tot}} < 10^{12} M_\odot$. This may be surprising because other parameters studied here are typically used in observations to separate dynamically young and old systems. This means that, in Horizon-AGN, kinematic morphology is the best indicator of how the IHSC was built up. Previous simulation results suggest that the IHSC could be easily built up by dry mergers, because the mass of satellites is preferentially deposited in the outskirts (see e.g. Lagos et al. 2018a). This, combined with the fact that simulations predict dry mergers to be the most effective way of producing slow rotators, may be the reason behind our findings. For higher masses, the dynamical state of the system gives us a handle on the scatter in a way that morphology cannot, because at $M_{*, \text{tot}} > 10^{12} M_\odot$ all the centrals are mainly supported by dispersion. Note that there is a difference between the V/σ calculated (which uses the 3D velocity information of galaxies) with what is recovered from a 2D projection of that information. This is partly due to inclination and partly due

to limitations in resolution in observations that affect the inferred velocity dispersion in observations (see van de Sande et al. 2019 for a detailed analysis of how hydrodynamical simulations compare to integral field spectroscopic surveys).

In recent work, Elias et al. (2018) found an anticorrelation between the mass fraction in the stellar halo and the morphology parameter κ in the Illustris simulation. While in principle this is consistent with the anticorrelation observed in Fig. 9, we argue that these are not completely equivalent because of the spherical aperture of $2 R_{50}$ (magenta line in Fig. 6) used to separate the stellar halo. This definition not only overestimates the IHSC/stellar halo at MW masses, but also fails to reproduce the observed $f_{M_*, \text{IHSC}}$ scatter. Consequently the $f_{M_*, \text{IHSC}}$ scatter at fixed κ is comparable to that of the entire population.

We can, in principle, connect this result with those found in recent observations by Merritt et al. (2016) and Harmsen et al. (2017, shown as symbols in Fig. 9), who, using different observational techniques, found that the estimated $f_{M_*, \text{IHSC}}$ for MW-like galaxies can vary up to 2 dex in a similar mass range. Because of their disc morphology, we would expect all the galaxies in these studies to have a high V/σ , and consequently a low $f_{M_*, \text{IHSC}}$ according to the behaviour observed in our results. However, their location in the relation overlaps with the entire simulated population, even for simulated galaxies mainly supported by dispersion. While this can be in conflict with the trend observed in our measurements, we have to take into account that the observational data do not include ellipsoidal galaxies which are needed to test if the V/σ correlation is displayed by observations. The ‘tension’ can be alleviated by shifting the $f_{M_*, \text{IHSC}} - M_*$ relation measured from the simulation towards higher $f_{M_*, \text{IHSC}}$ values, which can be achieved by using a different choice of $f_{l_x, 6D}$, as shown in Section 3.1; however, this would then introduce a conflict with estimated mass fraction in the ICL, and would also reduce the extent and mass of the galaxies (see Section 3.1, and appendix A of Cañas et al. 2019). Another factor that comes into play is the uncertainty in the measurements as well as the scatter that individual V/σ subsamples have; 1σ of contours of consecutive V/σ subsamples overlap and 2σ contours as large as ~ 0.5 dex, indicating that, although unlikely, a galaxy with high V/σ can have high $f_{M_*, \text{IHSC}}$ as well, and vice versa.

4.4 Specific star formation rate

We have shown that V/σ can be used to estimate the mass fraction in the IHSC. However, observational estimates of this parameter require expensive spectroscopic observations, and while surveys such as MaNGA (Drory et al. 2015), CALIFA (Sánchez et al. 2012), and SAMI (Croom et al. 2012) have been capable of estimating kinematic properties of thousands of galaxies, there are no estimates of the IHSC of these galaxies to date. Here, we explore a possible correlation between specific star formation rate (sSFR) of the central galaxy and the $f_{M_*, \text{IHSC}}$. SFR and V/σ of a galaxy are strongly correlated, and it is easier to estimate sSFR from observations that will be readily accessible via Spectral Energy Distribution (SED) fitting to a survey such as LSST (Robertson et al. 2019).

In Fig. 10, we show the $f_{M_*, \text{IHSC}} - M_*$ relation for subsamples of sSFR. Although the median of each subsample indicates that there is anticorrelation between the sSFR and $f_{M_*, \text{IHSC}}$, the scatter observed is quite large. A larger number of subsamples shows a similar behaviour; because of highly overlapping distributions, we only show two subsamples that are most distinct for clarity. We repeated this calculation using bins in SFR instead of sSFR, and found similar results. The observed behaviour is a consequence of

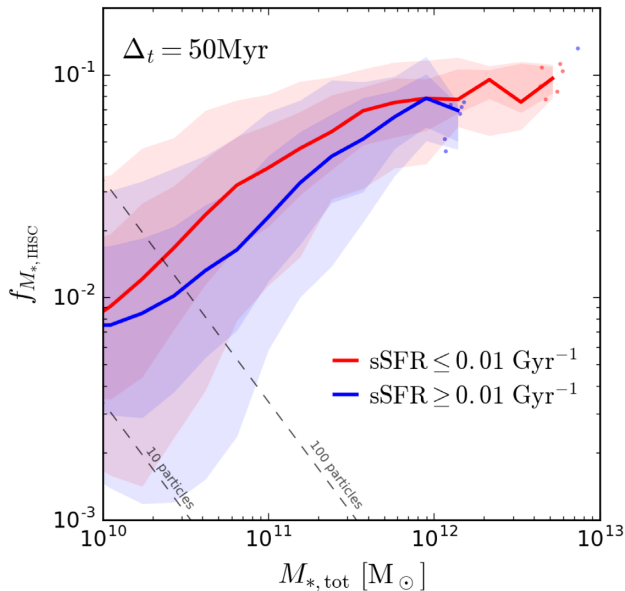


Figure 10. Same as Fig. 7, but separating the $f_{M_*, \text{IHSC}} - M_*$ relation into subsamples of galaxies of different sSFRs, as labelled. The sSFR shows a weak trend with $f_{M_*, \text{IHSC}}$ compared to V/σ . There is, however, a slight indication that higher sSFR have lower $f_{M_*, \text{IHSC}}$. A higher number of sSFR bins give similar results, for clarity we show only two subsamples where the relations are more distinct.

several factors. One is the way in which we estimate the SFR; by using only stellar particles to determine the SFR, it is likely that our estimate is affected by particle discreteness and mass resolution, because we cannot measure SFR below one stellar particle formed in the Δt used. Another is that spheroidal and disc galaxies of similar masses can have similar SFRs; this can arise if star formation quenching occurs because of feedback or because the available reservoir of gas has been exhausted. We note that while the exact values of V/σ and sSFR change from simulation to simulation, all simulations tend to predict qualitatively similar relations between sSFR- M_* (Somerville & Davé 2015) and V/σ versus M_* (van de Sande et al. 2019).

4.5 Two distinct regimes for the IHSC and observational prospects in the local Universe

Our results suggest that there are two broad, distinct, populations of haloes, with a transition at $M_{*, \text{tot}} \sim 10^{12} M_{\odot}$. At $M_{*, \text{tot}} < 10^{12} M_{\odot}$, properties of central galaxies are highly correlated with $f_{M_*, \text{IHSC}}$, with more dispersion-dominated galaxies being a strong indicator for high $f_{M_*, \text{IHSC}}$. Weaker correlations are seen with star formation activity, likely rising from the more fundamental correlation with V/σ . Halo properties at these masses do not seem to be good indicators of the overall $f_{M_*, \text{IHSC}}$. At $M_{*, \text{tot}} > 10^{12} M_{\odot}$, a very different picture emerges. All centrals at these masses are similar: they have little star formation activity and are dispersion dominated, and so they offer little insight into the IHSC. Instead, the dynamical state of the correlations studied are readily available in the observations and hence offer a great opportunity to test our predictions. Moreover, observations have so far sampled only a handful of galaxies, which is insufficient to unveil a correlation like the one reported here. Surveys such as those possible with Hyper-Suprime Cam (Miyazaki et al. 2012) and LSST (Robertson et al. 2019) are likely to change

this, because their deep photometry over half the sky will provide the required statistics and data quality.

5 TEMPORAL EVOLUTION OF THE IHSC

So far we have studied the mass content in the IHSC and how it correlates with observable properties of its system at $z = 0$. We have, however, not yet explored the temporal information available from the simulation. In this section, we explore the evolution of the $f_{M_*, \text{IHSC}}$ of the entire Horizon-AGN population with the aim of understanding how different regions of the $f_{M_*, \text{IHSC}} - M_*$ plane are populated as a function of time. Additionally, we study the evolution of systems of interest, specifically galaxy clusters and MW-mass systems, using their individual evolutionary paths.

5.1 Individual paths

In this section, we follow the evolution of individual systems through cosmic time by tracking their location in the $f_{M_*, \text{IHSC}} - M_*$ plane. We focus on three sets of objects of interest: MW-mass systems with low and high $f_{M_*, \text{IHSC}}$ and galaxy clusters.

We follow the evolution of each system by tracking its central galaxy across snapshots using TREEFROG (Poulton et al. 2018; Elahi et al. 2019b), a code that constructs merger trees for simulations. The progenitor of each galaxy is defined as the structure that shares most of its particles in the previous snapshot. This is found by comparing IDs of the stellar particles, and computing a merit function

$$\mathcal{M}_{ij} = \frac{N_{\text{sh}}^2}{N_i N_j}, \quad (8)$$

where N_i and N_j are the total number of particles in galaxies i and j respectively, and N_{sh} is the number of particles that exist in both structures. The main progenitor is chosen to be the one with the highest \mathcal{M}_{ij} . Systems are traced by following the main progenitors of the system's most massive galaxy at $z = 0$, i.e. the one with the highest merit.

To understand the evolutionary paths, we first note that horizontal displacements in the $f_{M_*, \text{IHSC}} - M_*$ plane tend to be towards higher $M_{*, \text{tot}}$ increments, which can either be caused by the accretion of systems or by the creation of new stars from gas accreted on an already existing interstellar medium; negative horizontal displacements are infrequent, and are caused by other galaxies or systems ‘flying by’. Vertical positive displacements correspond to mass being deposited from galaxies in the system (either central or satellites) into the IHSC. Negative vertical displacements result from either increments in $M_{*, \text{tot}}$ for a fixed $M_{*, \text{IHSC}}$, or the ‘re-capture’ of particles from the IHSC to galaxies at fixed $M_{*, \text{tot}}$.

5.1.1 Milky Way mass – low $f_{M_*, \text{IHSC}}$

In Fig. 11, we show the evolutionary paths in the $f_{M_*, \text{IHSC}} - M_*$ plane for a sample of systems with $M_{*, \text{tot}} \simeq 10^{11} M_{\odot}$ and $f_{M_*, \text{IHSC}} \simeq 10^{-3}$ at $z = 0$. At $z = 2.12$ (magenta squares) these systems have total stellar masses between $M_{*, \text{tot}} \simeq 10^{10}$ and $10^{10.5} M_{\odot}$, and an $f_{M_*, \text{IHSC}} \simeq 0.03$. Their evolution is mainly characterized by displacements towards higher $M_{*, \text{tot}}$ and lower $f_{M_*, \text{IHSC}}$. We highlight the evolution of object A (see Section 2.2.3) shown as a thick blue line, coloured symbols indicate its location in the plane at different redshifts, as labelled; in the bottom panels, we show the projected

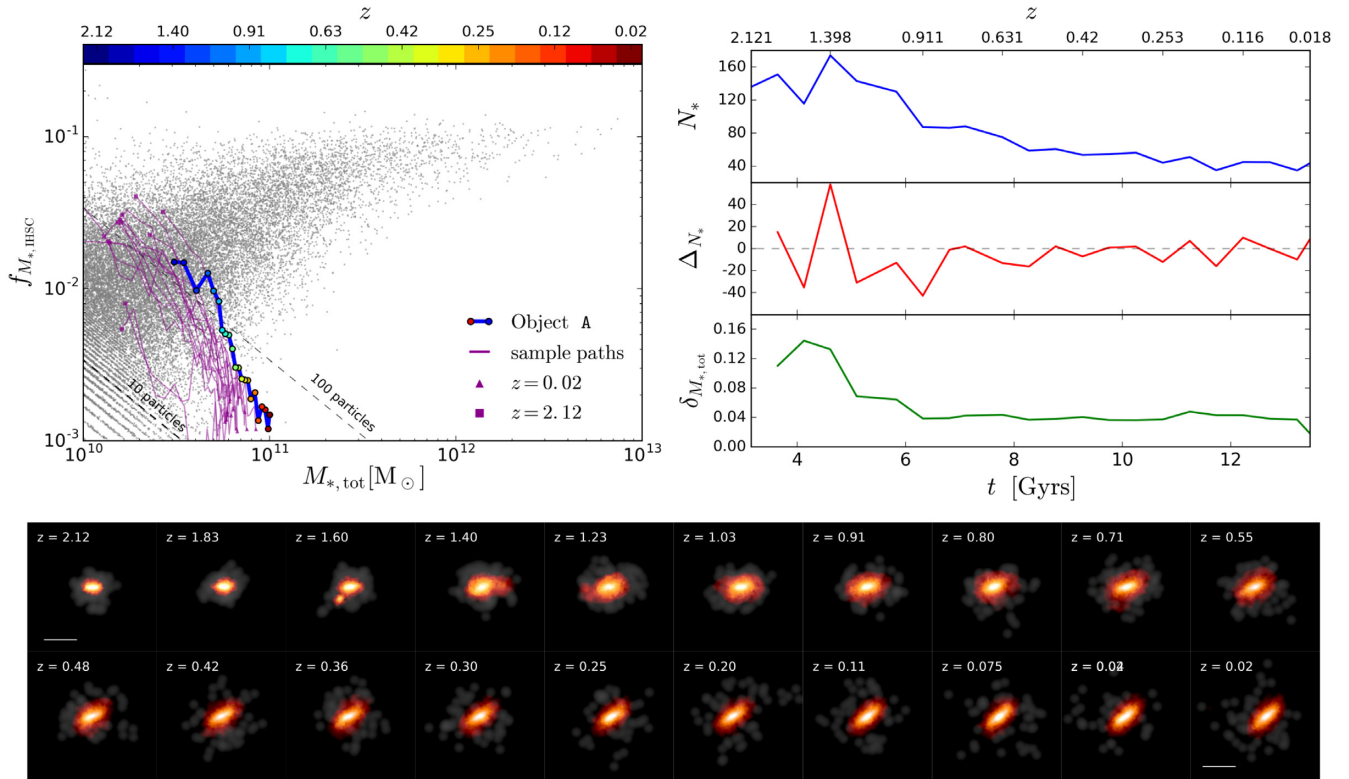


Figure 11. Evolution of MW-mass systems with low $f_{M_*,\text{IHSC}}$. Top left panel: evolutionary paths of a sample of galaxies (thin magenta lines) from $z = 2.12$ (square symbols) to $z = 0$ (triangle symbols). In blue is highlighted the path of object A, with its location at each snapshot denoted by symbols coloured according to redshift. In the background, the $z = 0$ $f_{M_*,\text{IHSC}} - M_*$ relation is shown as scatter points; diagonal dashed lines delimit regions where the IHSC is composed by 10 and 100 particles, as labelled. Top right panels: number of particles in the IHSC, $N_{*,\text{IHSC}}$, difference of $N_{*,\text{IHSC}}$ between snapshots, $\Delta N_{*,\text{IHSC}}$, and relative difference of $M_{*,\text{tot}}$, $\delta M_{*,\text{tot}} = M_{*,\text{tot}}(t + \Delta t)/M_{*,\text{tot}}(t) - 1$, as a function of time. Bottom panels: stellar surface density projections showing the evolution of the IHSC (grey) and the stellar mass in galaxies (red). Brighter colours denote higher densities. Colour intensities are different for each component to highlight their distribution. Systems with $M_{*,\text{tot}} \simeq 10^{11} M_\odot$ and $f_{M_*,\text{IHSC}} \simeq 10^{-3}$ are characterized by having a rather quiescent accretion history. The absence of mergers reduces the mass deposited into the IHSC, that in addition to the mass growth of the galaxy through the formation of new stars decreases the $f_{M_*,\text{IHSC}}$ of these systems. See the text for detailed discussion.

stellar density of the IHSC in grey, and the stellar mass in galaxies particles in red.⁷

This system starts with $f_{M_*,\text{IHSC}} \simeq 0.01$, decreasing for a couple of snapshots before showing a sudden growth, followed by a monotonic decrease reaching $f_{M_*,\text{IHSC}} \sim 0.001$. This behaviour is a consequence of the interaction between an infalling satellite with the central galaxy. At $z = 1.6$, the dip in the track is caused by the accretion of the satellite which increases $M_{*,\text{tot}}$, as seen in $\delta M_{*,\text{tot}} = M_{*,\text{tot}}(t + \Delta t)/M_{*,\text{tot}}(t) - 1$ (top right panels), without yet depositing material on to the IHSC. At a subsequent snapshot, the number of particles in the IHSC increases, as seen in $N_{*,\text{IHSC}}$ and $\Delta N_{*,\text{IHSC}}$, due to the disruption of stellar material from the interaction, causing the bump in the track. At subsequent times, $f_{M_*,\text{IHSC}}$ keeps decreasing up until $z = 0.02$, which is due to the decreasing number of particles in the IHSC, and an ongoing increment of $M_{*,\text{tot}}$, i.e. positive values of $\delta M_{*,\text{tot}}$, due to continuing star formation in the galaxy. The decreasing number of particles in the IHSC is also explained by mass being ‘re-accreted’ on to the galaxy from the IHSC as the system relaxes due to the

particular orbit that the infalling satellite had. This is in agreement with Peñarrubia, McConnachie & Babul (2006), and more recently, Karademir et al. (2019), who have shown that stellar debris from the disruption of galaxies on orbits close to the plane of the disc are expected to relax into an extended rotating disc; this extended disc would therefore occupy a similar region in phase space and therefore be assigned to the galaxy in our method. Finally, we note that the bumps displayed by all systems at later times are caused by the low number of particles that compose the IHSC, as is shown by $\Delta N_{*,\text{IHSC}}$. All of the other highlighted galaxies in magenta show a similar behaviour, interacting with a single satellite and continuous star formation activity in the central.

5.1.2 Milky Way mass – high $f_{M_*,\text{IHSC}}$

In Fig. 12, we show evolutionary paths of systems with $M_{*,\text{tot}} \simeq 10^{11} M_\odot$ and high $f_{M_*,\text{IHSC}}$ at $z = 0$. The paths that these galaxies display in the $f_{M_*,\text{IHSC}} - M_*$ plane are characterized by large displacements and variations in the $f_{M_*,\text{IHSC}}$, a consequence of the interactions that these systems experience. Contrary to the low $f_{M_*,\text{IHSC}}$ cases, these systems show a large variety of paths across cosmic time, due to the diversity of accretion histories. This is seen in the visualization of the highlighted path (bottom panels), as well

⁷Note that the colour intensity differs for the IHSC and for galaxies. This is done to better highlight the IHSC, which tends to have a low number of particles. For comparison, the visualization of Fig. 1 has the same colour and intensity palette for both components.

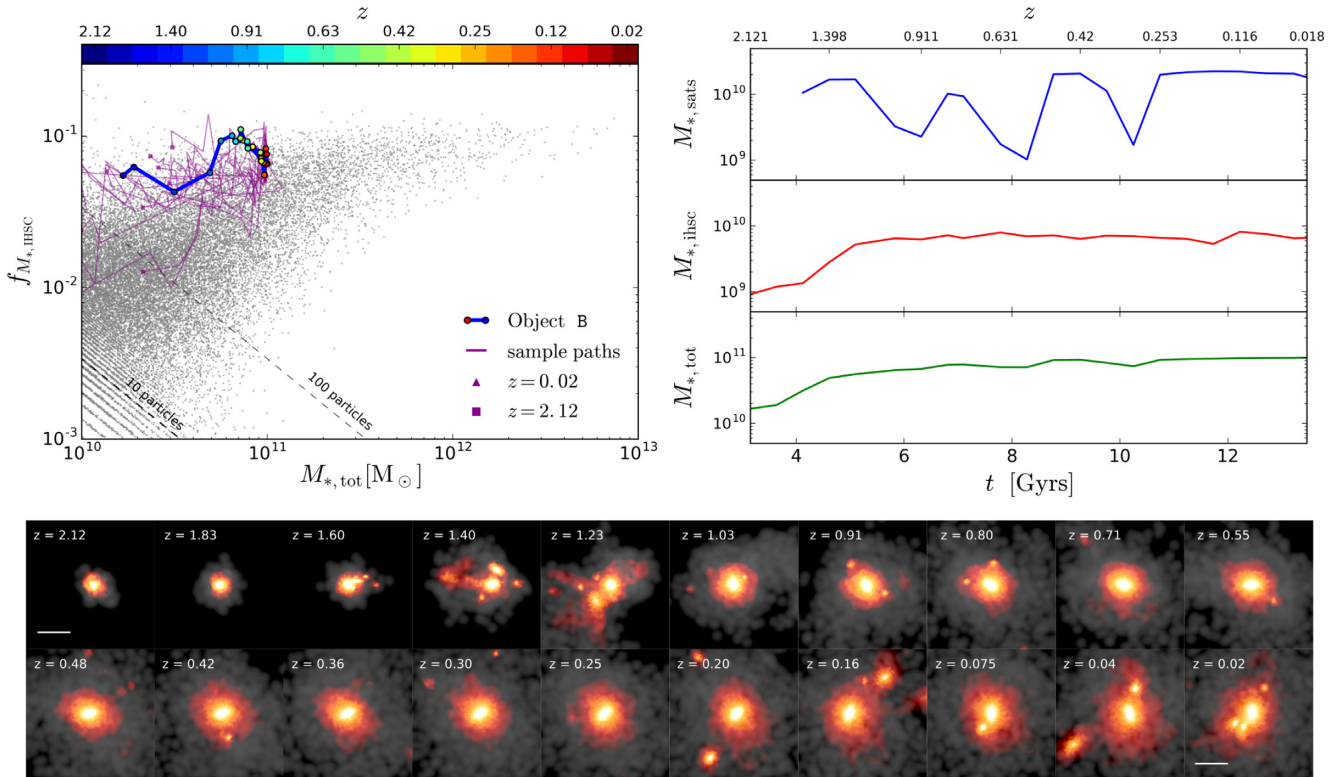


Figure 12. Same as Fig. 11, but for MW-mass galaxies with high $f_{M_*,\text{IHSC}}$. Top right panels show the total stellar mass, $M_{*,\text{tot}}$, IHSC mass, $M_{*,\text{IHSC}}$, and the mass in satellites $M_{*,\text{sats}}$, as a function of time. Visualizations in the bottom panel have the same spatial scale, colour palettes, and intensities as the example shown in Fig. 11. Systems with high $f_{M_*,\text{IHSC}}$ have an active accretion history which is responsible for depositing a large amount of mass into the IHSC. The diversity of paths in the $f_{M_*,\text{IHSC}} - M_*$ plane described by these systems is the result of the variety of infall epochs and satellite masses that each system experiences.

as the evolution of the mass in satellites, $M_{*,\text{sats}}$ (top right panels), where bumps across time represent the infall (peaks) and disruption (valleys) of satellites. These multiple interactions experienced by the central galaxy at different times result in a higher mass fraction in the IHSC. For comparison, the spatial scale and colour schemes of the projections is the same as for the low $f_{M_*,\text{IHSC}}$ case in Fig. 11. These results are consistent with the relation observed between the $f_{M_*,\text{IHSC}}$ of a system and V/σ of its central galaxy. Moreover, these results demonstrate the robustness of our method, and highlight the advantage of defining the IHSC as the kinematically hot component in each system.

5.1.3 Galaxy clusters

In the top panel of Fig. 13, we show evolutionary paths in the $f_{M_*,\text{IHSC}} - M_*$ plane of systems with $M_{*,\text{tot}} > 10^{12} M_\odot$ at $z = 0$, all of which have $f_{M_*,\text{IHSC}} > 5 \times 10^{-2}$ (magenta triangles). These objects display a variety of locations in the $f_{M_*,\text{IHSC}} - M_*$ plane at $z = 2.12$ (magenta squares), differing by ~ 1 dex in both $M_{*,\text{tot}}$ and $f_{M_*,\text{IHSC}}$ for this particular sample. Regardless of their initial location, all systems move towards higher $M_{*,\text{tot}}$ with time and display a series of peaks and valleys in the $f_{M_*,\text{IHSC}} - M_*$ plane throughout their evolution, a consequence of the multiple interactions that drive the growth of these systems. For systems that at $z = 2.12$ have a high $f_{M_*,\text{IHSC}}$, the displacements are on average horizontal through cosmic time, as shown by the highlighted case. Systems that start with low $f_{M_*,\text{IHSC}}$ and $M_{*,\text{tot}}$ show a tendency to move towards increasing $f_{M_*,\text{IHSC}}$ and $M_{*,\text{tot}}$, until reaching

$M_{*,\text{tot}} \simeq 10^{12} M_\odot$ where the displacements become on average horizontal.

While for MW-mass systems, this evolution can be described by the accretion of satellites on to a dominant central galaxy, for groups and clusters this evolution is more complex, because they grow mainly by accretion of entire smaller groups and clusters. These infalling systems carry with them their own IHSC, which after accretion is added to the IHSC of the larger system. During these events, the total $f_{M_*,\text{IHSC}}$ is not expected to increase, simply because of how mass fractions add; for example, a cluster with an initial IHSC mass fraction of 10 per cent that accretes a group whose $f_{M_*,\text{IHSC}}$ is 10 per cent, will have, post-accretion, the same mass fraction in the IHSC. Although mathematically the infall of a group can also increase the total $f_{M_*,\text{IHSC}}$ if the infalling group has a higher $f_{M_*,\text{IHSC}}$, this is somewhat unlikely, as our results indicate that the $f_{M_*,\text{IHSC}}$ of such a system is either equal to or lower than that of high-mass end systems. Displacements towards higher $f_{M_*,\text{IHSC}}$ can therefore only arise because mass is disrupted from galaxies and transferred to the IHSC. On average, systems describe horizontal paths because of the interplay between the disruption timescales of the galaxies already in the cluster and the accretion time-scale of other clusters.

Overall these results indicate that, for systems with $M_{*,\text{tot}} > 10^{12} M_\odot$, there is no apparent correlation between $f_{M_*,\text{IHSC}}$ and $M_{*,\text{tot}}$, and there should be no strong evolution of $f_{M_*,\text{IHSC}}$ with time. The lack of evolution of $f_{M_*,\text{IHSC}}$ with time is consistent with observational results of Krick & Bernstein (2007), who found no trend between ICL fraction and cluster mass for a sample of Abell

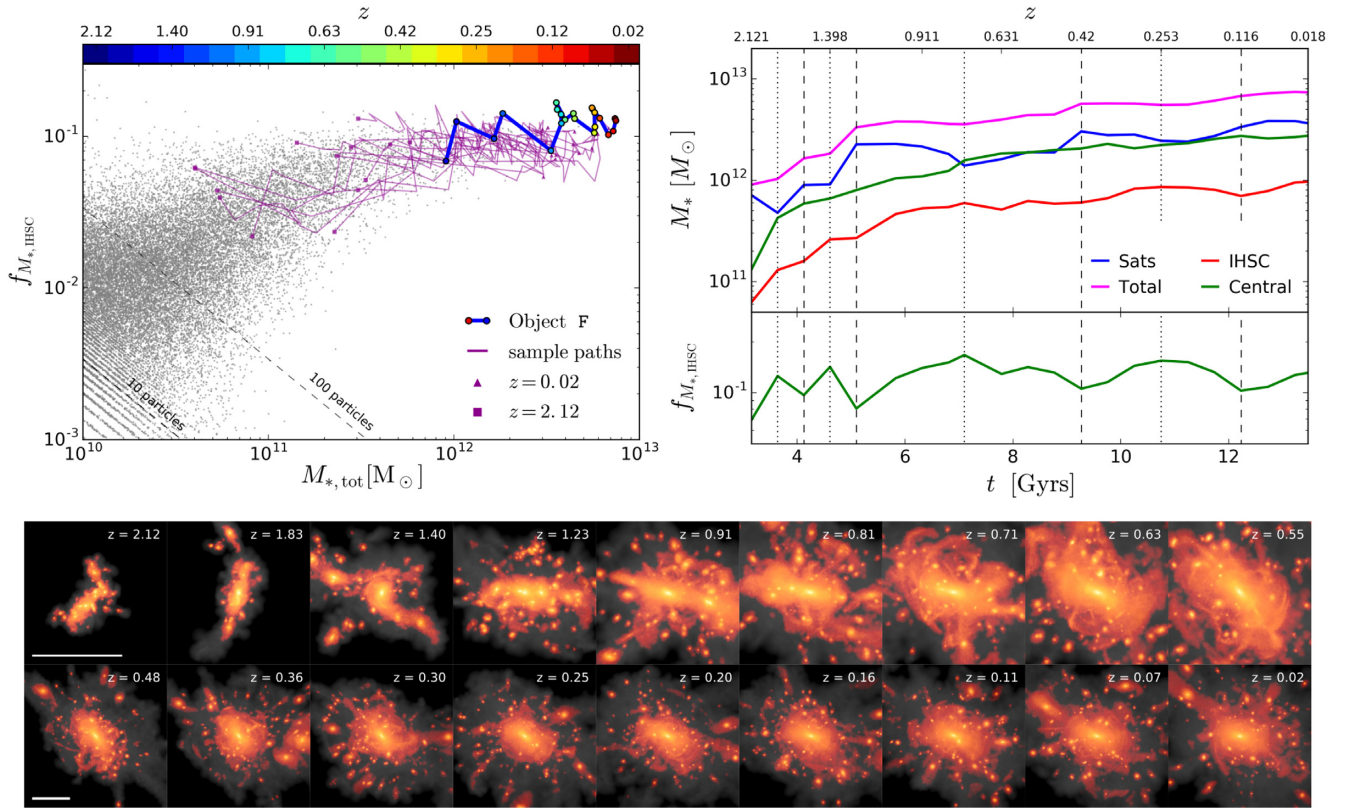


Figure 13. Same as Fig. 11, but showing the evolution of the IHSC at galaxy groups and clusters scales. Note that the spatial scale is different for the top and bottom rows of the projections, in both cases the white horizontal line has a length of 430 kpc. Colour intensity is different from that of Figs 11 and 12 for clarity purposes. Top right panels show the evolution of the stellar mass in satellites, IHSC, central and total, as well as the evolution of the IHSC. For reference vertical dotted (dashed) lines are shown at peaks (valleys) of the $f_{M_*, \text{IHSC}}$. The horizontal displacements in the $f_{M_*, \text{IHSC}} - M_*$ plane are the consequence of the interplay between the disruption galaxies and the accretion of other groups and clusters.

clusters, and a weak or non-existent evolution across redshifts. This has also been noted more recently by Montes & Trujillo (2018), using data from the Hubble Frontier Fields. In previous theoretical studies, Cui et al. (2014) found no correlation between cluster mass and the mass fraction in the ICL, using simulations that did not include AGN feedback and only when the ICL was defined using surface density thresholds. This was not observed however when AGN feedback was included, as well as when a dynamical definition of the ICL was used. This contradicts our results, and warrants further research at cluster masses. In a future paper we focus specifically on this regime using the Cluster-EAGLE (Bahé et al. 2017; Barnes et al. 2017) suite (Cañas et al., in preparation).

5.1.4 Comments

In this section, we have focused on three different populations, which the authors consider to be particularly relevant and interesting for comparison with observational data sets. While an in-depth and statistical analysis of the entire population is important, this is not possible with Horizon-AGN alone because of its characteristics. At MW masses and low $f_{M_*, \text{IHSC}}$, we are at the resolution limit of the simulation; therefore to provide stronger constraints on these systems, we need larger samples at much higher resolution. Similarly, at the massive end of the $f_{M_*, \text{IHSC}} - M_*$ plane, the current study is limited by the box size of Horizon-AGN which does not include larger perturbation modes that can give rise to more massive

clusters. These limitations are in fact present for any state-of-the-art simulation of similar characteristics, such as EAGLE, Illustris, and Illustris-TNG (Schaye et al. 2015; Vogelsberger et al. 2014; Pillepich et al. 2018a), and reflect the limits imposed by present-day computational resources. Such analysis is, therefore, only possible using a mixture of simulations whose characteristics are suitable to resolve the systems of interest.

5.2 Galaxy population

In Fig. 14, we show the temporal evolution of the $f_{M_*, \text{IHSC}} - M_*$ relation from $z = 2.12$ to 0.02. At $z = 2.12$, the relation shows a mass dependence of the $f_{M_*, \text{IHSC}}$ with $M_{*, \text{tot}}$ up to $M_{*, \text{tot}} \sim 2 \times 10^{11} M_\odot$, where the relation appears to flatten. At $M_{*, \text{tot}} \simeq 10^{10} M_\odot$, the scatter in the $f_{M_*, \text{IHSC}}$ can be greater than 1 dex, and decreases with increasing $M_{*, \text{tot}}$. At subsequent redshifts, the evolution is characterized by a shift of the relation towards higher $M_{*, \text{tot}}$, and is accompanied by a steepening of the mean for $M_{*, \text{tot}} < 10^{11.5} M_\odot$, as well as a stronger distinction between a mass dependence of the $f_{M_*, \text{IHSC}}$ and a weaker or non-existent one at the high-mass end. This steepening of the relation is partially caused by systems populating low $f_{M_*, \text{IHSC}}$ regions at ever high $M_{*, \text{tot}}$, which, as seen in Section 5.1, correspond to systems that had a quiescent accretion history and whose IHSC ceased to grow. The other factor that causes this steepening is the horizontal displacement of systems with initially high $f_{M_*, \text{IHSC}}$, which also contribute to the flattening of the relation at $M_{*, \text{tot}} > 10^{11.5} M_\odot$.

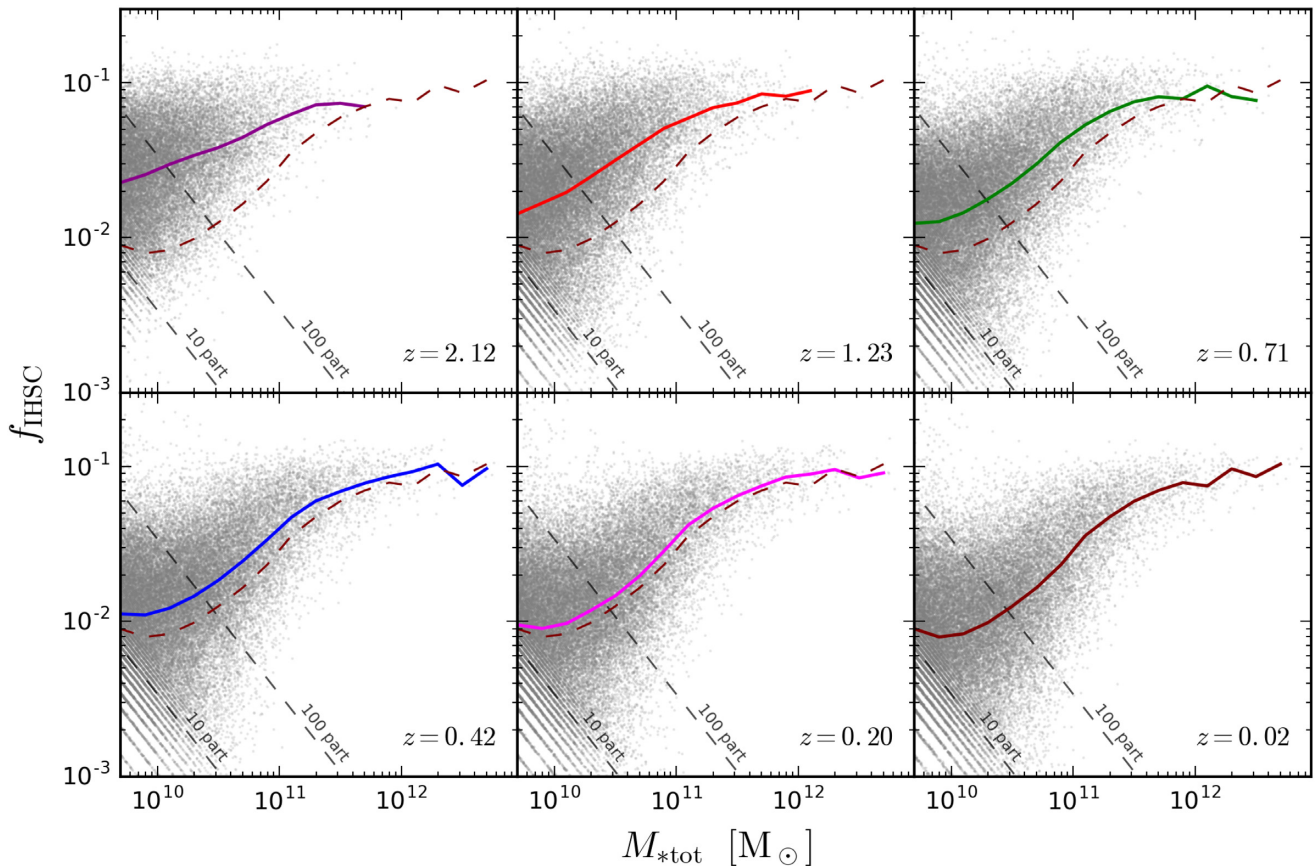


Figure 14. Temporal evolution of the $f_{M_*,\text{IHSC}} - M_*$ relation from $z = 2.12$ to 0.02 , as labelled. Grey points are the measurements for individual systems; solid lines indicate the median $f_{M_*,\text{IHSC}}$ per mass bin, and dashed line indicates the median at $z = 0$ for reference. Diagonal dashed lines indicate $f_{M_*,\text{IHSC}}$ limits for IHSC composed 10 and 100 particles at a given $M_{*,\text{tot}}$, as labelled.

6 SUMMARY AND CONCLUSIONS

We presented the first results of a new method to define the IHSC in cosmological hydrodynamical simulations. This method relies on robust identification of galaxies using an adaptive phase-space structure finder VELOCIRAPTOR (Cañas et al. 2019; Elahi et al. 2019a). The IHSC is then defined to be all the stellar material that is sufficiently distinct from galaxies in phase space to be considered separate from them, i.e. a diffuse, kinematically hot stellar component. A critical feature of this method is the use of local properties of each system to separate the IHSC from the rest of the galaxies. This allows us to robustly define the IHSC from MW mass systems up to galaxy groups and clusters, and consequently to consistently follow the assembly of the IHSC through cosmic time.

A novelty of this method is that it is capable of producing consistent relations between the stellar mass of the central galaxy, $M_{*,\text{ctrl}}$; the IHSC, $M_{*,\text{IHSC}}$; and satellites, $M_{*,\text{sats}}$, independently of the phase-space density thresholds used, determined by the search parameter $f_{l_{x,6D}}$. Modifying this parameter does not affect the shape of the relations, but only changes their zero-point. We argue that this feature allows the user to choose the $f_{l_{x,6D}}$ value that better matches observations of given characteristics, e.g. surface-brightness limit, to make appropriate theoretical predictions.

We find that the $f_{M_*,\text{IHSC}}$ increases with the system’s mass, on average, with the scatter being a strong function of the latter: low-mass systems display variations of up to 2 orders of magnitude in

their $f_{M_*,\text{IHSC}}$, while the scatter gets systematically smaller, being 0.3 dex at group masses.

We explored the nature of the scatter observed in the $f_{M_*,\text{IHSC}} - M_*$ relation at MW masses by looking for possible correlations between properties of systems that are easily accessible in observations and their $f_{M_*,\text{IHSC}}$:

Number of satellites: at $M_{*,\text{tot}} > 10^{11} M_\odot$, systems with higher N_{sats} are expected to have a higher $f_{M_*,\text{IHSC}}$ at fixed $M_{*,\text{tot}}$, but at lower masses, there is no evident correlation between N_{sats} with $f_{M_*,\text{IHSC}}$.

Dynamical age: in the case of $M_{*,\text{scnd}}/M_{*,\text{ctrl}}$, it is only at $M_{*,\text{tot}} > 10^{12} M_\odot$ that this quantity is indicative of the $f_{M_*,\text{IHSC}}$ in a system. At a fixed $M_{*,\text{tot}}$, dynamically younger systems with higher $M_{*,\text{scnd}}/M_{*,\text{ctrl}}$ have lower $f_{M_*,\text{IHSC}}$ than older, more dynamically relaxed ones.

Kinematic morphology: we found that V/σ is the parameter that most strongly (anti)correlates with $f_{M_*,\text{IHSC}}$ at fixed mass in systems with $M_{*,\text{tot}} < 10^{12} M_\odot$.

At MW masses, we see a clear transition from low $f_{M_*,\text{IHSC}}$ in systems with more rotationally supported galaxies, i.e. higher V/σ , to high $f_{M_*,\text{IHSC}}$ for those with a central galaxy mainly supported by dispersion, low V/σ .

This is consistent with the picture that dispersion-supported galaxies have a more active accretion history and therefore a larger amount

of mass deposited into the IHSC; this is in comparison with disc galaxies, which have on average a more quiescent accretion history.

Star formation rate: at fixed $M_{*,\text{tot}}$, the SFR of the central galaxy can be indicative of the expected $f_{M_*,\text{IHSC}}$ of the system, with lower $f_{M_*,\text{IHSC}}$ in systems with more star forming central galaxies. However, there is not a continuous transition from low $f_{M_*,\text{IHSC}}$ and high SFRs to high $f_{M_*,\text{IHSC}}$ and low SFRs, as strong as we obtained for V/σ .

Our method also allows us to follow the evolution and assembly of the IHSC through cosmic time for individual objects as well as for the entire galaxy population. We explored individual paths in the $f_{M_*,\text{IHSC}} - M_*$ plane for cases of interest:

Milky Way mass – low $f_{M_,\text{IHSC}}$:* the evolution of these systems is characterized by smooth displacements towards higher $M_{*,\text{tot}}$ and lower $f_{M_*,\text{IHSC}}$ which are the result of the absence of accretion of satellites, the continuous formation of new stars from gas, and the relaxation of IHSC stars into the outskirts of the growing central galaxy.

Milky Way mass – high $f_{M_,\text{IHSC}}$:* these galaxies display a variety of evolutionary paths in the $f_{M_*,\text{IHSC}} - M_*$ plane. Contrary to low $f_{M_*,\text{IHSC}}$ cases, these systems have different locations in the plane at $z = 2$, but finish with similar $M_{*,\text{tot}}$ and $f_{M_*,\text{IHSC}}$ at $z = 0$.

Their paths are characterized by increments in the $f_{M_*,\text{IHSC}}$, which are a consequence of episodes of satellite accretion and interactions, that occur at different epochs for each system.

Galaxy groups and clusters: the evolutionary paths of high-mass systems are characterized by a series of increments and decrements in the $f_{M_*,\text{IHSC}}$.

While for MW mass systems, the evolution of these features are attributed to the accretion and disruption of individual satellites, for groups and clusters such features are caused by the accretion of smaller groups/clusters and the disruption of all the members within those structures.

Overall these systems display increasing $f_{M_*,\text{IHSC}}$ with time until they reach a $M_{*,\text{tot}} \sim 10^{11.5} M_\odot$ and $f_{M_*,\text{IHSC}} \simeq 10 - 20$ per cent, from where the evolution indicates to be weak or non-existent due to the interplay between group accretion episodes, which decreases $f_{M_*,\text{IHSC}}$, and disruptions of individual galaxies that increase it.

The evolution of the galaxy population is characterized by a steepening of the median $f_{M_*,\text{IHSC}}$ at $M_{*,\text{tot}} < 10^{11} M_\odot$, which is caused by galaxies with $f_{M_*,\text{IHSC}}$ at high redshifts that subsequently have a quiescent accretion history, populating the low $f_{M_*,\text{IHSC}}$ region in increasing numbers as time goes by. For $M_{*,\text{tot}} > 10^{11} M_\odot$, the population evolution shows a mild to negligible increment in the $f_{M_*,\text{IHSC}}$. For our preferred 6D finder parameters, the $f_{M_*,\text{IHSC}}$ appears to peak around ~ 10 per cent, however such value changes depend on the phase-space density cut used.

Overall, the scatter displayed by the $f_{M_*,\text{IHSC}} - M_*$ relation is driven by the large diversity in accretion histories that galaxies can experience. The difference in the scatter observed at MW masses and at groups and cluster scales is mainly due to the various factors that play a role in the growth and evolution of an MW-mass system, compared to that of clusters, which are dominated by hierarchical growth. While some properties of the system can be used as indicators of the stellar content in the IHSC, the specific location in the $f_{M_*,\text{IHSC}} - M_*$ plane ultimately depends on the specific assembly history a system has, because specific locations in the $f_{M_*,\text{IHSC}} - M_*$ plane can be reached by a variety of paths, explaining why there

is a non-negligible scatter even when studying subsamples of the population with more similar accretion histories.

The method and results presented in this paper give insight into open questions about the IHSC, and provide a consistent picture of the properties of the IHSC across a wide range of masses and its evolution throughout cosmic time. There is, however, still work to be done, more specifically exploring in detail MW mass system using higher resolution simulations, as well simulations that can resolve multiple massive galaxy clusters. We should remember as well the effect that subgrid models may have in the estimated IHSC, while the hierarchical formation of galaxies is in principle equivalent in all simulations, the diversity of subgrid models may produce as well different IHSC contents, which we will address in future work. Finally, a detailed and careful comparison between observations and different theoretical models is crucial to help us understand better the physics of galaxy formation.

ACKNOWLEDGEMENTS

The authors thank Aaron Robotham, Bob Abraham, Aaron Ludlow, Mireia Montes, Rhea-Silvia Remus, Rhys Poulton, and the theory and computing group at ICRAR for helpful discussions. RC is supported by the Mobilising European Research in Astrophysics and Cosmology foundation postdoctoral grant awarded to CL and by the Consejo Nacional de Ciencia y Tecnología CONACYT CVU 520137 Scholar 290609 Overseas Scholarship 438594. CL is funded by a Australian Research Council Discovery Early Career Researcher Award (DE150100618). Parts of this research were conducted by the Australian Research Council Centre of Excellence for All Sky Astrophysics in 3Dimensions (ASTRO 3D), through project number CE170100013. This research is part of Spin(e) (ANR-13-BS05-0005, <http://cosmicorigin.org>). This work has made use of the Horizon Cluster hosted by Institut d’Astrophysique de Paris. We thank Stephane Rouberol for running smoothly this cluster for us.

REFERENCES

- Abraham R. G., van Dokkum P. G., 2014, *PASP*, 126, 55
 Bahé Y. M. et al., 2017, *MNRAS*, 470, 4186
 Barker M. K., Ferguson A. M. N., Irwin M., Arimoto N., Jablonka P., 2009, *AJ*, 138, 1469
 Barnes D. J. et al., 2017, *MNRAS*, 471, 1088
 Barnes J. E., Hernquist L. E., 1991, *ApJ*, 370, L65
 Puchwein E., Springel V., Sijacki D., Dolag K., 2010, *MNRAS*, 406, 936
 Bullock J. S., Johnston K. V., 2005, *ApJ*, 635, 931
 Burke C., Hilton M., Collins C., 2015, *MNRAS*, 449, 2353
 Cañas R., Elahi P. J., Welker C., del P Lagos C., Power C., Dubois Y., Pichon C., 2019, *MNRAS*, 482, 2039
 Contini E., De Lucia G., Villalobos Á., Borgani S., 2014, *MNRAS*, 437, 3787
 Cooper A. P., D’Souza R., Kauffmann G., Wang J., Boylan-Kolchin M., Guo Q., Frenk C. S., White S. D. M., 2013, *MNRAS*, 434, 3348
 Cooper A. P., Gao L., Guo Q., Frenk C. S., Jenkins A., Springel V., White S. D. M., 2015, *MNRAS*, 451, 2703
 Cooper A. P. et al., 2010, *MNRAS*, 406, 744
 Croom S. M. et al., 2012, *MNRAS*, 421, 872
 Cui W. et al., 2014, *MNRAS*, 437, 816
 Da Rocha C., Mendes de Oliveira C., 2005, *MNRAS*, 364, 1069
 Davies L. J. M. et al., 2019, *MNRAS*, 483, 5444
 Davis M., Efstathiou G., Frenk C. S., White S. D. M., 1985, *ApJ*, 292, 371
 Dolag K., Murante G., Borgani S., 2010, *MNRAS*, 405, 1544
 Drory N. et al., 2015, *AJ*, 149, 77
 Dubois Y., Devriendt J., Slyz A., Teyssier R., 2010, *MNRAS*, 409, 985

- Dubois Y., Devriendt J., Slyz A., Teyssier R., 2012, *MNRAS*, 420, 2662
- Dubois Y., Gavazzi R., Peirani S., Silk J., 2013, *MNRAS*, 433, 3297
- Dubois Y., Peirani S., Pichon C., Devriendt J., Gavazzi R., Welker C., Volonteri M., 2016, *MNRAS*, 463, 3948
- Dubois Y. et al., 2014, *MNRAS*, 444, 1453
- Durbala A. et al., 2008, *AJ*, 135, 130
- D'Souza R., Kauffman G., Wang J., Vegetti S., 2014, *MNRAS*, 443, 1433
- Elahi P. J., Cañas R., Poulton R. J. J., Tobar R. J., Willis J. S., Lagos C. d. P., Power C., Robotham A. S. G., 2019a, *PASA*, 36, e021
- Elahi P. J., Poulton R. J. J., Tobar R. J., Canas R., Lagos C. d. P., Power C., Robotham A. S. G., 2019b, *PASA*, 36, e028
- Elahi P. J., Thacker R. J., Widrow L. M., 2011, *MNRAS*, 418, 320
- Elahi P. J. et al., 2013, *MNRAS*, 433, 1537
- Elias L. M., Sales L. V., Creasey P., Cooper M. C., Bullock J. S., Rich R. M., Hernquist L., 2018, *MNRAS*, 479, 4004
- Feldmeier J. J., Mihos J. C., Morrison H. L., Harding P., Kaib N., Dubinski J., 2004, *ApJ*, 609, 617
- Font A. S., McCarthy I. G., Crain R. A., Theuns T., Schaye J., Wiersma R. P. C., Dalla Vecchia C., 2011, *MNRAS*, 416, 2802
- Gauthier J.-R., Dubinski J., Widrow L. M., 2006, *ApJ*, 653, 1180
- Greggio L., Rejkuba M., Gonzalez O. A., Arnaboldi M., Iodice E., Irwin M., Neeser M. J., Emerson J., 2014, *A&A*, 562, A73
- Harmen B., Monachesi A., Bell E. F., de Jong R. S., Bailin J., Radburn-Smith D. J., Holwerda B. W., 2017, *MNRAS*, 466, 1491
- Ibata R., Chapman S., Ferguson A. M. N., Lewis G., Irwin M., Tanvir N., 2005, *ApJ*, 634, 287
- Karademir G. S., Remus R.-S., Burkert A., Dolag K., Hoffmann T. L., Moster B. P., Steinwandel U. P., Zhang J., 2019, *MNRAS*, 487, 318
- Kaviraj S. et al., 2017, *MNRAS*, 467, 4739
- Komatsu E. et al., 2011, *ApJS*, 192, 18
- Krick J. E., Bernstein R. A., 2007, *AJ*, 134, 466
- Lagos C. d. P., Schaye J., Bahé Y., Van de Sande J., Kay S. T., Barnes D., Davis T. A., Dalla Vecchia C., 2018b, *MNRAS*, 476, 4327
- Lagos C. d. P. et al., 2018a, *MNRAS*, 473, 4956
- Martínez-Delgado D., Peñarrubia J., Gabany R. J., Trujillo I., Majewski S. R., Pohlen M., 2008, *ApJ*, 689, 184
- Martínez-Delgado D. et al., 2010, *AJ*, 140, 962
- McConnachie A. W. et al., 2009, *Nature*, 461, 66
- Merritt A., van Dokkum P., Abraham R., Zhang J., 2016, *ApJ*, 830, 62
- Mihos J. C., Harding P., Feldmeier J., Morrison H., 2005, *ApJ*, 631, L41
- Mihos J. C., Harding P., Feldmeier J. J., Rudick C., Janowiecki S., Morrison H., Slater C., Watkins A., 2017, *ApJ*, 834, 16
- Mihos J. C., Hernquist L., 1996, *ApJ*, 464, 641
- Miyazaki S. et al., 2012, in McLean, I. S., Ramsay, S. K., Takami, H., eds, Proc. SPIE Conf. Ser. Vol. 8446, Ground-based and Airborne Instrumentation for Astronomy IV, SPIE, Bellingham. p. 84460Z
- Monachesi A., Bell E. F., Radburn-Smith D. J., Bailin J., de Jong R. S., Holwerda B., Streich D., Silverstein G., 2016, *MNRAS*, 457, 1419
- Monachesi A. et al., 2019, *MNRAS*, 485, 2589
- Montes M., Trujillo I., 2014, *ApJ*, 794, 137
- Montes M., Trujillo I., 2018, *MNRAS*, 474, 917
- Morishita T., Abramson L. E., Treu T., Schmidt K. B., Vulcani B., Wang X., 2017, *ApJ*, 846, 139
- Mouhcine M., Ferguson H. C., Rich R. M., Brown T. M., Smith T. E., 2005, *ApJ*, 633, 810
- Murante G., Giovalli M., Gerhard O., Arnaboldi M., Borgani S., Dolag K., 2007, *MNRAS*, 377, 2
- Murante G. et al., 2004, *ApJ*, 607, L83
- Naab T. et al., 2014, *MNRAS*, 444, 3357
- Oser L., Ostriker J. P., Naab T., Johansson P. H., Burkert A., 2010, *ApJ*, 725, 2312
- Peirani S. et al., 2017, *MNRAS*, 472, 2153
- Peirani S. et al., 2019, *MNRAS*, 483, 4615
- Penoyre Z., Moster B. P., Sijacki D., Genel S., 2017, *MNRAS*, 468, 3883
- Peñarrubia J., McConnachie A., Babul A., 2006, *ApJ*, 650, L33
- Pillepich A., Madau P., Mayer L., 2015, *ApJ*, 799, 184
- Pillepich A. et al., 2014, *MNRAS*, 444, 237
- Pillepich A. et al., 2018a, *MNRAS*, 473, 4077
- Pillepich A. et al., 2018b, *MNRAS*, 475, 648
- Poulton R. J. J., Power C., Robotham A. S. G., Elahi P. J., 2020, *MNRAS*, 491, 3820
- Poulton R. J. J., Robotham A. S. G., Power C., Elahi P. J., 2018, *PASA*, 35, e042
- Radburn-Smith D. J. et al., 2011, *ApJS*, 195, 18
- Remus R.-S., Dolag K., Hoffmann T., 2017, *Galaxies*, 5, 49
- Robertson B. E. et al., 2019, *Nature Rev. Phys.*, 1, 450
- Robotham A. S. G. et al., 2014, *MNRAS*, 444, 3986
- Rodríguez-Gomez V. et al., 2016, *MNRAS*, 458, 2371
- Rudick C. S., Mihos J. C., McBride C., 2006, *ApJ*, 648, 936
- Rudick C. S., Mihos J. C., McBride C. K., 2011, *ApJ*, 732, 48
- Schaye J. et al., 2015, *MNRAS*, 446, 521
- Somerville R. S., Davé R., 2015, *ARA&A*, 53, 51
- Sánchez S. F. et al., 2012, *A&A*, 538, A8
- Sérsic J. L., 1963, *Bol. Asoc. Argentina Astron. La Plata Argentina*, 6, 41
- Teyssier R., 2002, *A&A*, 385, 337
- Toomre A., Toomre J., 1972, *ApJ*, 178, 623
- van der Wel A. et al., 2014, *ApJ*, 788, 28
- van de Sande J. et al., 2019, *MNRAS*, 484, 869
- Vogelsberger M. et al., 2014, *MNRAS*, 444, 1518
- Volonteri M., Dubois Y., Pichon C., Devriendt J., 2016, *MNRAS*, 460, 2979
- Watkins A. E., Mihos J. C., Harding P., 2015, *ApJ*, 800, L3
- Welker C., Devriendt J., Dubois Y., Pichon C., Peirani S., 2014, *MNRAS*, 445, L46
- White S. D. M., Rees M. J., 1978, *MNRAS*, 183, 341
- Zhang Y. et al., 2019, *ApJ*, 874, 165
- Zibetti S., White S. D. M., Schneider D. P., Brinkmann J., 2005, *MNRAS*, 358, 949
- Zwicky F., 1952, *PASP*, 64, 242

APPENDIX A: IHSC EXTENT AND SPHERICAL APERTURES

Here, we present how our definition of the IHSC compares to the one defined by spherical overdensity and spherical apertures widely used in the literature (see Introduction for a discussion). In Fig. A1, we show surface density projections of the stellar mass content using M_{200c} (left-hand column) and 3DFOF (right-hand column) mass conventions. Top row shows the total stellar mass, middle row the stellar mass in the central galaxy and IHSC (CG + IHSC), and bottom row the stellar mass in the IHSC only, as identified by VELOCIRAPTOR. The total mass content (top row) shows that 3DFOF convention does not capture the presence of some satellites in the vicinity of the central galaxy, as well as some diffuse stellar mass, differing by ~ 15 per cent. This difference is similar to the excess of ~ 10 per cent mass content in the M_{200c} IHSC and 3DFOF definitions. For this particular example, the mass fraction in the IHSC is $f_{M_*, \text{IHSC}} = 0.059$ for M_{200c} and $f_{M_*, \text{IHSC}} = 0.062$. This behaviour is consistent for the entire population of objects resolved in the Horizon-AGN simulation, as can be seen in Fig. A2, where the total stellar mass content, $M_{*, \text{tot}}$ (top panel), and the mass in the IHSC, $M_{*, \text{IHSC}}$ (middle panel), follow an almost 1-to-1 correspondence with only notable variations at $M_* < 10^{11} M_\odot$. Finally, the $f_{M_*, \text{IHSC}} - M_*$ relation (bottom panel) is consistent in shape and amplitude at all stellar masses for both conventions.

In the middle panel of Fig. A1, we show the combination of CG + IHSC components, along with concentric circles representing spherical apertures of 30 and 100 kpc (solid circles) and $2R_{50}$ (dashed circle) used in the literature to separate the central galaxy from the IHSC (e.g. Pillepich et al. 2018b; Elias et al. 2018). We show in the top panel of Fig. A3, the stellar mass of the central galaxy, $M_{*, \text{ctrl}}$ as a function of total stellar mass inside spherical overdensity, $M_{*, 200c}$; note that for the VELOCIRAPTOR measurement

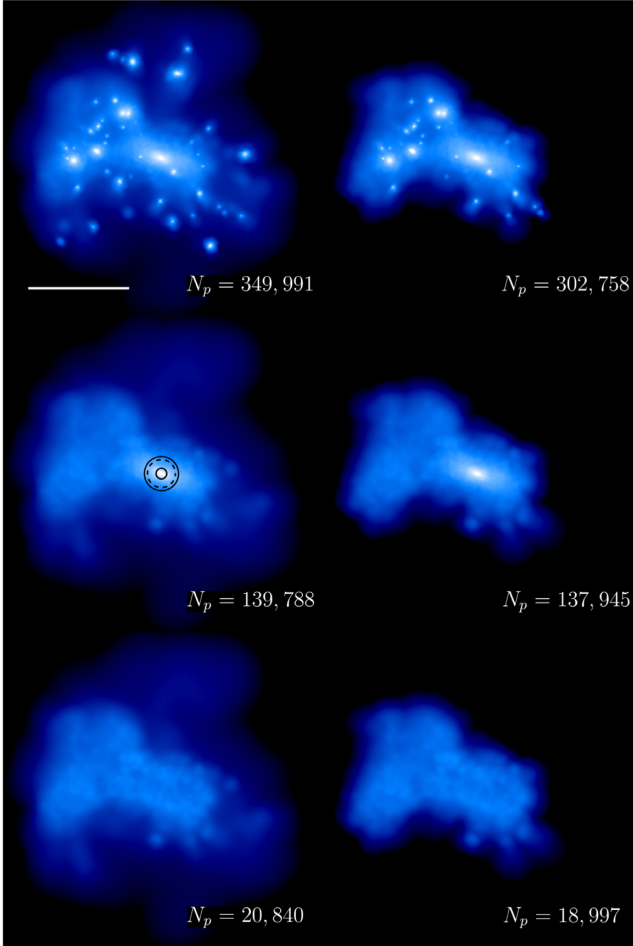


Figure A1. Surface density projections of total stellar content (top row), central galaxy and IHSC (CG + IHSC, middle row), and IHSC only (bottom row), for spherical overdensity M_{200c} (left-hand column) and 3DFOF conventions for a group in Horizon-AGN at $z = 0$. The total number of stellar particles, N_p , in the object is indicated in each panel; and solid white line represents a spatial scale of 570 kpc. Concentric circles denote the extent of spherical apertures used in the literature to separate the central galaxy from the IHSC. For the M_{200c} CG + IHSC, we also show spherical apertures of 30 and 100 kpc (solid circle), and $2R_{50}$ (dashed circle), for which the stellar material inside the aperture is considered as the central galaxy, and the outer to be the IHSC (e.g. Pillepich et al. 2018b; Elias et al. 2018). See the text for a detailed description.

we use the definition of the bottom left panel of Fig. A1, instead of the 3DFOF for consistency. All definitions show a consistent relation between $M_{*,\text{ctrl}}$ and M_{200c} for $M_{200c} < 10^{11} M_{\odot}$, which is expected as the mass budget is contained mainly in the central galaxy, which at this masses can be well defined by spherical apertures of 30 and 100 kpc. At larger masses, the relations deviate from the 1-to-1 relation. This is in part because most of the mass comes from satellites, which is particularly noticeable for the 30 kpc aperture as the central galaxy is also likely to extend beyond this aperture. A similar trend is visible at $M_{200c} > 10^{12.5} M_{\odot}$ for the 100 kpc aperture for the same reason. Contrary to the $M_{*,\text{ctrl}}$, the relation between M_{200c} and $M_{*,\text{IHSC}}$ is different for all definitions at all mass ranges. The $2R_{50}$ relation has a power-law index < 1 at all masses. In the case of the 30 kpc aperture, there is an evident change in the power-law index which goes from being ≥ 1 at $M_{200c} < 2 \times 10^{11} M_{\odot}$ to ≈ 1 for higher masses. The 100 kpc

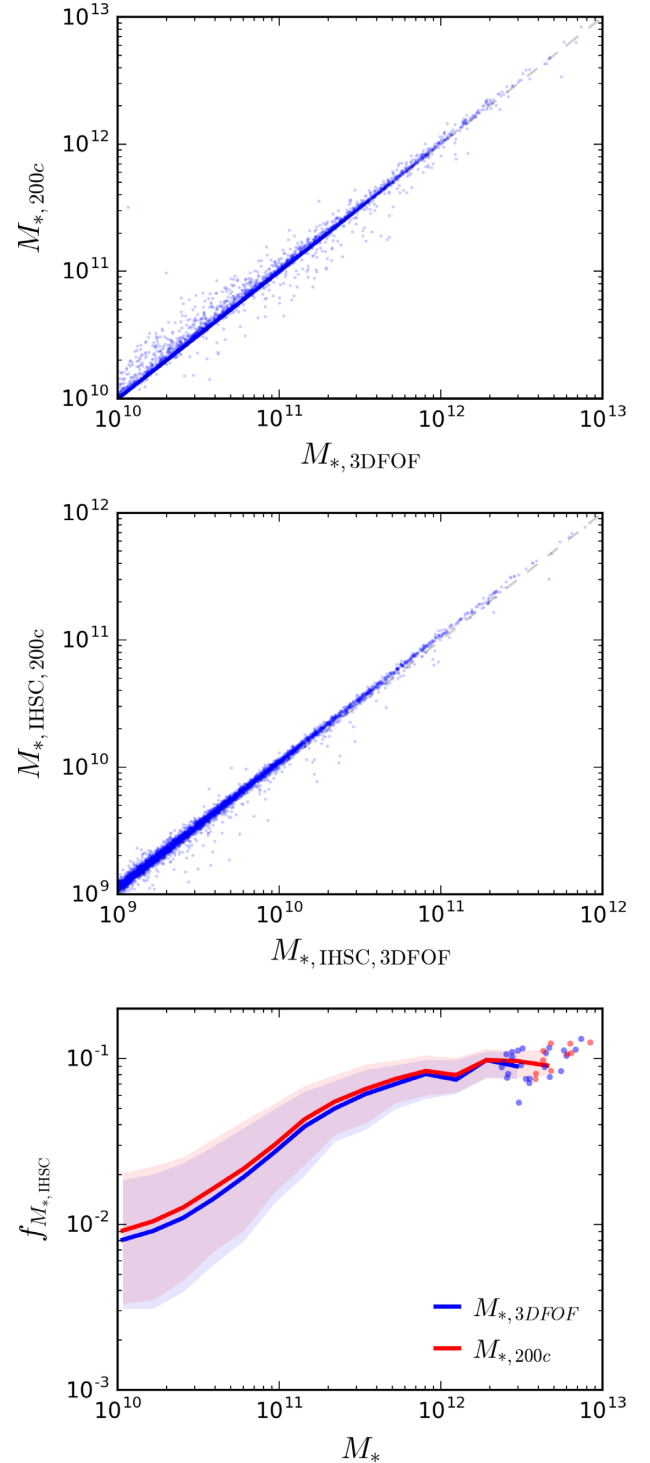


Figure A2. Total stellar mass content (top), mass in the IHSC (middle), and $f_{M_{*,\text{IHSC}}} - M_*$ relation of 3DFOF objects compared to its correspondent spherical overdensity of 200 times the critical density of the universe (bottom), for all 3DFOF objects in Horizon-AGN at $z = 0$. Solid lines and shaded regions in the bottom panel represent the median, and extent of 16th and 84th percentiles, respectively. The stellar mass content is in agreement for both conventions, displaying an almost 1-to-1 correspondence and a consistent $f_{M_{*,\text{IHSC}}} - M_*$ relation in the whole mass range.

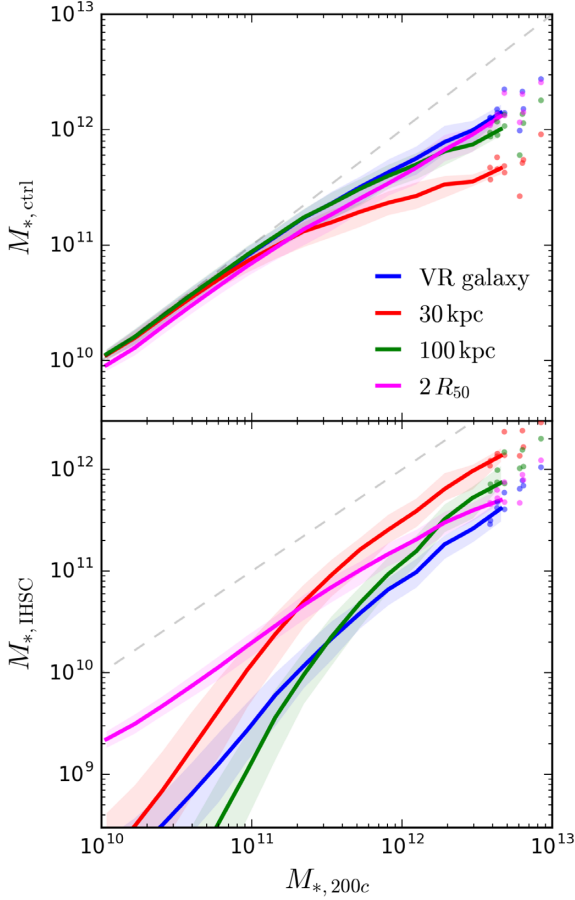


Figure A3. Stellar mass of the central galaxy (top) and IHSC mass (bottom) as a function of total stellar mass within spherical a overdensity for all systems in Horizon-AGN at $z = 0$.

aperture also shows a change in the power-law index at a similar mass, but with a value > 1 ; finally for our method the initial slope is slightly > 1 for $M_{200c} < 10^{11.5} M_{\odot}$ and ~ 1 at higher masses.

Lastly, in Fig. A4, we show the $f_{M_*, \text{IHSC}}$ as a function of the total halo mass M_{200c} . This plot is complementary to that of Fig. 6. While the $M_*, 200c$ relation is observable for low-mass systems, the M_{200c}

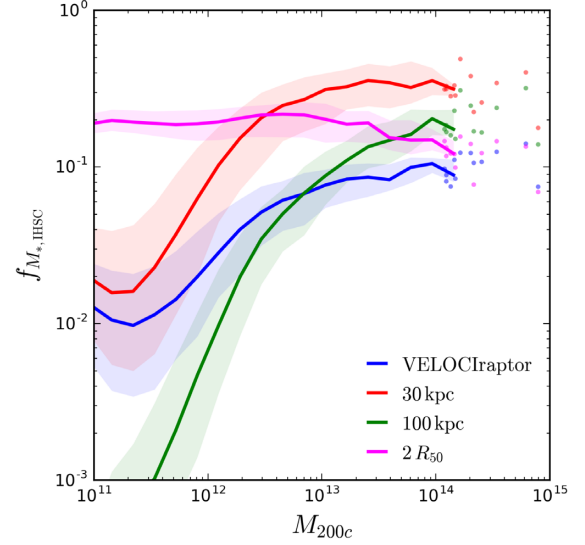


Figure A4. Mass fraction in the IHSC, $f_{M_*, \text{IHSC}}$, as a function of total halo mass M_{200c} (bottom).

is useful for theoretical predictions, and can also be estimated via lensing at cluster scales. The behaviour of both relations is very similar, which is expected from the 1-to-1 comparison shown in Fig. A2.

Overall, we argue that while there is a difference in the stellar mass content of different components from 3DFOF and spherical overdensity definitions, our method gives consistent $f_{M_*, \text{IHSC}}$ and $f_{M_*, \text{IHSC}} - M_*$ relations. We also argue that our method not only provides a consistent definition of the IHSC over a wide range of masses, but for the central galaxy as well. As mentioned in the main body of the paper, a fixed aperture of 30 kpc may provide a good definition of the central galaxy at lower masses, but at larger masses, the 100 kpc one might be a better option. While in principle an adaptive aperture could solve this issue, we argue that the $2 R_{50}$ choice is not ideal as it clearly overestimates the $f_{M_*, \text{IHSC}}$ at the low-mass end, and shows a decreasing trend towards higher masses.

This paper has been typeset from a $\text{\TeX}/\text{\LaTeX}$ file prepared by the author.