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Enrico M. Di Teodoro, Lorenzo Posti, S. Michael Fall, Patrick M. Ogle, Thomas Jarrett, et al.. Dark matter halos and scaling relations of extremely massive spiral galaxies from extended HI rotation curves. Monthly Notices of the Royal Astronomical Society, 2022, 10.1093/mnras/stac3424 . insu-03909767

HAL Id: insu-03909767

<https://insu.hal.science/insu-03909767>

Submitted on 6 Jul 2023

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Dark matter halos and scaling relations of extremely massive spiral galaxies from extended H I rotation curves

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Accepted 2022 November 19. Received 2022 November 17; in original form 2022 May 10

ABSTRACT

We present new and archival atomic hydrogen (H I) observations of 15 of the most massive spiral galaxies in the local Universe ($M_{\star} > 10^{11} M_{\odot}$). From 3D kinematic modeling of the datacubes, we derive extended H I rotation curves, and from these, we estimate masses of the dark matter halos and specific angular momenta of the discs. We confirm that massive spiral galaxies lie at the upper ends of the Tully–Fisher relation (mass vs velocity, $M \propto V^4$) and Fall relation (specific angular momentum vs mass, $j \propto M^{0.6}$), in both stellar and baryonic forms, with no significant deviations from single power laws. We study the connections between baryons and dark matter through the stellar (and baryon)-to-halo ratios of mass $f_M \equiv M_{\star}/M_h$ and specific angular momentum $f_{j,\star} \equiv j_{\star}/j_h$ and $f_{j,\text{bar}} \equiv j_{\text{bar}}/j_h$. Combining our sample with others from the literature for less massive disc-dominated galaxies, we find that f_M rises monotonically with M_{\star} and M_h (instead of the inverted-U shaped f_M for spheroid-dominated galaxies), while $f_{j,\star}$ and $f_{j,\text{bar}}$ are essentially constant near unity over four decades in mass. Our results indicate that disc galaxies constitute a self-similar population of objects closely linked to the self-similarity of their dark halos. This picture is reminiscent of early analytical models of galaxy formation wherein discs grow by relatively smooth and gradual inflow, isolated from disruptive events such as major mergers and strong active galactic nuclei feedback, in contrast to the more chaotic growth of spheroids.

Key words: galaxies: evolution – galaxies: haloes – galaxies: kinematics and dynamics – galaxies: spiral.

1 INTRODUCTION

Understanding the interplay between baryons and dark matter in galaxy evolution is one of the greatest challenges of modern astrophysics. In the standard Λ cold dark matter (Λ CDM) cosmological model, galaxies form when gas, trapped within the gravitational potential of dark matter (DM) halos, cools down, and collapses toward the centre of the potential well, settling in a disc-like, rotating structure and igniting star formation. Subsequently, galaxies grow by means of cosmological accretion and mergers. While hierarchical assembling of DM halos is reasonably simple and well understood (e.g. Mo, van den Bosch & White 2010), the physics of baryons is complex and involves a number of non-linear physical processes that galaxies experience during their evolution, such as gas dissipation, gas accretion, gravitational instabilities, star formation, feedback from massive stars and active galactic nuclei (AGN), galaxy mergers

and tidal interactions. These processes are expected to alter the properties of a galaxy, such as its mass, rotation velocity, and angular momentum.

It is remarkable that galaxies observed in the Universe none the less follow tight and approximately featureless power laws between their most basic structural properties (see van der Kruit & Freeman 2011, for a review). In particular, the most striking scaling relations for disc galaxies are the Tully & Fisher (1977) relation, between the stellar or baryonic¹ mass of a galaxy (M_{\star} or M_{bar}) and its rotation velocity V , and the Fall (1983) relation, between the stellar or baryonic specific angular momentum, $j_{\star} \equiv J_{\star}/M_{\star}$ or $j_{\text{bar}} \equiv J_{\text{bar}}/M_{\text{bar}}$, and the mass, M_{\star} or M_{bar} . Both the Tully–Fisher and the Fall relations are power laws, $M \propto V^{\beta}$ with $\beta \sim 3\text{--}4$ (e.g. Verheijen 2001; McGaugh 2012; Lelli, McGaugh & Schombert 2016a; Lelli et al. 2019) and $j \propto M^{\alpha}$ with

¹We follow others in this field and use the term ‘baryonic’ as a shorthand for the most readily observable constituents of galaxies, namely stars and atomic gas, thereby excluding molecular and ionized gas, and in particular, the circumgalactic medium.

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$\alpha \sim 0.5\text{--}0.7$ (e.g. Romanowsky & Fall 2012; Fall & Romanowsky 2013, 2018; Posti et al. 2018b; Di Teodoro et al. 2021; Mancera Piña et al. 2021a,b; Hardwick et al. 2022). In a similar way, DM halos in Λ CDM are fully rescalable and also follow simple, tight, power-law scaling relations with similar slopes, in particular $M_h \propto V_h^3$ and $j_h \propto M_h^{2/3}$, where M_h , V_h , and j_h are the mass, circular velocity, and specific angular momentum of the dark matter halo, respectively. This similarity between galaxy and DM scaling relations suggests that a simple connection between dark matter and baryons might still exist in today's disc galaxies, despite all the complexity of galaxy evolution in the cosmological context.

This connection between galaxy and halo properties is not easy to determine from observations (Wechsler & Tinker 2018). A standard way of parametrizing the dependence between baryons and DM is through the ratios $f_X \equiv X_*/X_h$, i.e. the stellar-to-halo ratio for a given quantity X , which can be mass M , circular velocity V , or specific angular momentum j . In particular, many studies in the last decade have been focused on constraining the variation of $f_M \equiv M_*/M_h$ or f_* $\equiv f_M/f_b$, where $f_b \simeq 0.156$ is the cosmological baryon fraction (Planck Collaboration 2020), as a function of M_* or M_h . This is also referred to as the ‘stellar-to-halo mass relation’ (SHMR). Various techniques have been used so far, including abundance matching (e.g. Vale & Ostriker 2004; Behroozi, Wechsler & Conroy 2013; Moster, Naab & White 2013), weak galaxy–galaxy lensing (Leauthaud et al. 2012; van Uitert et al. 2016), galaxy clustering (Zu & Mandelbaum 2015; Tinker et al. 2017), group catalogues (Zheng, Coil & Zehavi 2007; Yang, Mo & van den Bosch 2008), and empirical models (Rodríguez-Puebla et al. 2017; Behroozi et al. 2019). The general consensus is that f_M (or f_*) increases with mass, reaches a peak around $M_* \simeq 5 \times 10^{10} M_\odot$ ($M_h \simeq 10^{12} M_\odot$, near the mass of the Milky Way), and then decreases at larger masses. The standard interpretation of this form of the SHMR is that the rising and falling parts reflect mainly stellar and AGN feedback, respectively. A puzzling aspect of such a non-linear² relation is that a bend in the SHMR should induce a bend in the disc scaling relations at about the same mass (e.g. Navarro & Steinmetz 2000; Ferrero et al. 2017; Lapi, Salucci & Danese 2018; Posti et al. 2018a). Such a bend, however, is not observed (Di Teodoro et al. 2021).

A simple and elegant solution to this puzzle was recently put forward by Posti, Fraternali & Marasco (2019a), Posti et al. (2019b), and Posti & Fall (2021): that early-type galaxies (spheroids) and late-type galaxies (discs) in reality follow different SHMRs. In particular, Posti et al. (2019b) estimated DM halo masses from extended atomic hydrogen (HI) rotation curves in disc galaxies and found that the SHMR rises monotonically for all masses, at least up to $M_* \sim 10^{11} M_\odot$. Conversely, Posti & Fall (2021) derived the SHMR for early-type galaxies from position-velocity distributions of their globular clusters and found a SHMR that declines above $M_* \sim 5 \times 10^{10} M_\odot$, in agreement with the standard SHMR derived from abundance matching for the general population of galaxies, which is dominated by early-types at the highest masses (e.g. Kelvin et al. 2014). The linearity of the SHMR for discs suggests that, unlike in spheroids, AGN feedback is not efficient enough to turn over the SHMR relation (‘failed feedback’ problem). This likely happens because the super-massive black holes that power AGN feedback are associated more with spheroids than with discs (Kormendy & Richstone 1995). Differences in the SHMR of early-type and late-type galaxies have also been found in recent hydrodynamical

cosmological simulations (Grand et al. 2019; Correa & Schaye 2020; Marasco et al. 2020; Rodríguez-Gomez et al. 2022). These findings indicate that massive discs and spheroids are assembled in different ways, with the former being built by smooth inflows regulated by relatively weak stellar feedback, and the latter being assembled by a combination of merging and strong AGN feedback.

For disc-dominated galaxies, the other important property, next to mass, is specific angular momentum. This must ultimately derive from the tidal torques exerted by density perturbations on a wide range of scales in the linear and trans-linear phases of galaxy formation (Peebles 1969). As first emphasized by Fall & Efstathiou (1980), the torques, being gravitational, would act nearly equally on both the gas and dark matter in protogalaxies, thus endowing them initially with approximately the same specific angular momentum; and for discs especially, this equality would largely be preserved during the subsequent collapse and later evolution of galaxies. The assumption that galactic discs have the same specific angular momentum as their dark halos underlies practically all analytical and semi-analytical models of galaxy formation developed over the past 40 yr. There are, however, several processes that can alter this relationship, including transfer of angular momentum from galaxies to their dark halos, major mergers and tidal interactions with neighboring galaxies, and removal of gas by stellar and AGN feedback – thought to be dominant for spheroids but subdominant for discs (reviewed by Romanowsky & Fall 2012; see also DeFelippis et al. 2017). Thus, it is important to make robust empirical estimates of the ‘retained fractions’ of specific angular momentum, $f_{j,*} \equiv j_*/j_h$ and $f_{j,\text{bar}} \equiv j_{\text{bar}}/j_h$ for the stars and baryons in galaxies over wide ranges in M_* and M_h . Recent estimates are $f_{j,*} \simeq 0.7\text{--}0.8$ for disc-dominated galaxies (Fall & Romanowsky 2013, 2018; Huang et al. 2017; Posti et al. 2019b; Di Teodoro et al. 2021) and $f_{j,*} \simeq 0.1$ for spheroid-dominated galaxies (Romanowsky & Fall 2012; Fall & Romanowsky 2018), in general agreement with recent cosmological hydrodynamical simulations (Rodríguez-Gomez et al. 2022).

In this paper, we aim to study the connection between very massive discs and their DM halos, extending the stellar mass range well above $10^{11} M_\odot$, and to test their growth scenario. We use a combination of new and archival HI data to derive extended rotation curves of a sample of 15 galaxies that are among the most massive discs in the local Universe. These rotation curves are then decomposed into the contribution of the different mass components (cold gas, stars, and dark matter) and robust estimates of DM halo masses and specific angular momenta are obtained by imposing physically-motivated priors on the concentration and spin parameters of Λ CDM halos. We stress that HI rotation curves, which extend well beyond the stellar discs of galaxies, are crucial for estimating DM halo masses (e.g. Bosma 1978; van Albada et al. 1985; Kent 1988). Finally, we build and study the Tully–Fisher and Fall relations, in both their stellar and baryonic flavors, the SHMRs and the relation between stellar and halo specific angular momenta for disc galaxies with $M_* \gtrsim 10^{11} M_\odot$.

The remainder of this paper is structured as follows. Section 2 introduces our galaxy sample and the kinematical emission-line data used in this work, including our new HI observations. Section 3 describes our 3D kinematical modelling of the data and our rotation curve decomposition procedure to estimate the mass of dark matter halos in our galaxies. In Section 4, we present and discuss our results on scaling relations and dark matter halos of extremely massive spiral galaxies. The physical implications of our findings are discussed in Section 5. We summarize and conclude in Section 6. Throughout the paper, we use a fixed critical overdensity parameter $\Delta = 200$ for DM halos and we assume a flat Λ CDM cosmology with $\Omega_m = 0.314$, $\Omega_\Lambda = 0.686$, and $H_0 = 67.4 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (Planck Collaboration

²For brevity, we often use the terms ‘linear’ and ‘non-linear’ to refer to the power-law and non-power-law forms of relations in log-log space.

2020). In this cosmology, 1 arcsec corresponds to 212 pc and the lookback time is 143 Myr at $z \simeq 0.01$.

2 DATA

2.1 Galaxy sample and atomic hydrogen data

This work uses a mixture of new and archival H I interferometric data. Of the 15 galaxies that make up our final sample, seven come from new observations (out of eight galaxies actually observed) and eight from previous published studies.

For this project, we first selected a sample of eight new massive spiral galaxies to be observed with the Karl Jansky Very Large Array (VLA). These galaxies were chosen based on their stellar masses, their rotational velocities and their inclination angles. Galaxies were required to have stellar mass $M_* > 10^{11}$, based on the Sloan Digital Sky Survey (SDSS; Eisenstein et al. 2011) catalogue, and H I rotation speeds $V_{\text{rot}} > 300 \text{ km s}^{-1}$, based on their inclination-corrected H I line profile width from the Arecibo ALFALFA survey (Haynes et al. 2018). We note that ALFALFA galaxies typically have higher gas fractions, are more isolated, and have higher gas spin parameters than the general galaxy population (e.g. SDSS). Finally, we required an inclination angle $i > 40^\circ$ to minimize uncertainties on the kinematical modelling due to projection effects.

Aperture synthesis H I data for these galaxies were collected with the VLA in separate runs from July to September 2021 (project ID: 21A-191, PI: Ogle). The telescope was in configuration C, with a minimum baseline of 35 m and a maximum baseline of 3.4 km. A simple spectral setup for the L-band receiver was used, with a 16 MHz spectral window centred on the redshifted H I line and 512 channels of width 31.25 kHz, corresponding to about 6.5 km s^{-1} at the H I frequencies. This configuration guarantees sufficient bandwidth to include the broad integrated H I emission for these fast-rotating galaxies as well as enough baseline to subtract continuum emission. We used a standard observing sequence, in which a galaxy was targeted in 20–30 min intervals, separated by 3–5 min phase calibrator pointings. The flux/bandpass calibrator was observed at the start and at the end of each run. The total on-source integration time for each galaxy is approximately 9 h.

Calibration and imaging of the interferometric radio data was performed using the COMMON ASTRONOMY SOFTWARE APPLICATIONS (CASA; McMullin et al. 2007). In particular, we used stable version 6.1. Raw data were accurately cleaned using both automated algorithms (TFCROP or RFLAG) and manual flagging to remove undesired radio-frequency interference (RFI) and other bad data. For each observation run, we used standard CASA routines to perform flux, bandpass and complex gain calibrations. Calibration solutions and calibrated visibilities were visually inspected to ensure high-quality data for imaging. To increase the signal-to-noise ratio (SNR), calibrated sets were binned by either two or three channels, depending on the galaxy, achieving a channel width of 62.5 or 93.75 kHz ($\sim 13 \text{ km s}^{-1}$ and $\sim 20 \text{ km s}^{-1}$, respectively).

Continuum emission was removed from calibrated data in the uv -plane by fitting a first order polynomial to H I emission-free channels and subtracting it from visibility spectra over the entire spectral range. Continuum-subtracted spectra were imaged on a grid with pixel spacing of 4 arcsec using a natural weighting scheme to maximize the sensitivity of data. Finally, the emission in datacubes was cleaned of sidelobe contamination (Clark 1980) down to a $\text{SNR} = 3$ and corrected for the attenuation of the primary beam. Our final datacubes reach a typical root mean square (rms) sensitivity of $\sigma_{\text{rms}} \simeq 0.2\text{--}0.4 \text{ mJy per beam per channel}$ and have typical full width

at half maximum (FWHM) beam sizes of 17–21 arcsec. Of the eight new galaxies observed with the VLA, we had to discard UGC08902, which turned out to be a very strongly interacting system, thus unsuitable for our dynamical analysis.

Beside these new VLA data, we additionally re-analysed archival H I data of eight massive, fast-rotating, disc galaxies. In particular, we used VLA data from Spekkens & Giovanelli (2006) for three galaxies (NGC1324, NGC2862 and UGC2849), and *Westerbork Synthesis Radio Telescope* (WSRT) data from the Westerbork survey of neutral Hydrogen in Irregular and Spiral galaxies (WHISP; van der Hulst, van Albada & Sancisi 2001) for four systems (NGC338, NGC1167, NGC2599, and NGC5533). Finally, we also analysed WSRT data for UGC02885 from Hunter et al. (2013), also known as ‘Rubin’s galaxy’. Three of these galaxies (NGC1167, NGC5533, and UGC02885) are also included in the Spitzer Photometry & Accurate Rotation Curves catalogue (SPARC; Lelli et al. 2016a), but we decided to re-analyse these data with our latest modelling techniques. Archival data sets have beam FWHMs of 14–45 arcsec and channel widths of $4\text{--}13 \text{ km s}^{-1}$, while the rms sensitivity varies across the sample in the range $\sigma_{\text{rms}} = 0.3\text{--}1.1 \text{ mJy per beam}$ in a single channel.

Galaxies in our final sample have stellar masses that exceed $10^{11} M_\odot$, distances $D < 250 \text{ Mpc}$ ($z \lesssim 0.05$), and morphologies spanning from early-type discs (e.g. S0, Sa) to late-type discs (e.g. Sb, Sc). These galaxies are lower-redshift analogs of the ‘superluminous spiral galaxies’ catalogued by Ogle et al. (2016, 2019), except that, on average, they are slightly less massive. The reason for this is that interferometric H I observations are easily obtainable only in the nearby Universe, with RFI severely undermining the quality of data at $z > 0.05$. Thus, the volume of space readily accessible in H I is much smaller than that of the superspirals found in optical surveys up to $z \simeq 0.3$. We expect that it will not be possible to enlarge our current sample significantly until the advent of the Square Kilometer Array (SKA). Throughout this paper, we adopted homogenized distances and uncertainties from the Extragalactic Distance Database (EDD; Tully et al. 2009) and the CosmicFlows project (Tully, Courtois & Sorce 2016), when available. Alternatively, we used median distances from the literature as reported in the NASA Extragalactic Database (NED). Table 1 summarizes the main properties of the 15 galaxies in our final sample. An atlas of galaxies, including optical images, H I column-density maps and velocity fields, can be found in Appendix A (online supplementry).

2.2 Additional kinematical data

Besides H I data, for six galaxies, we also took advantage of publicly available kinematical data from integral field unit (IFU) observations. Optical recombination lines from the warm ionized gas are observed at a much higher spatial resolution than the H I line (although at lower spectral resolution) and are excellent to derive the inner rising part of the rotation curve of a galaxy and to constrain the contribution to the circular speed of the stellar component (see Section 3.3). For this work, we found archival IFU data from the Mapping Nearby Galaxies at Apache Point Observatory survey (MaNGA; Bundy et al. 2015) for NGC2599, NGC2713, and UGC08179 and data from the Calar Alto Legacy Integral Field Area Survey (CALIFA; Sánchez et al. 2012) for NGC1167, NGC1324, and NGC5635. In particular, we used datacubes from MaNGA DR7 and low spectral resolution datacubes (V500, channel width of 2 \AA) from CALIFA DR3.

To isolate gas emission lines from IFU datacubes, we fitted and subtracted the stellar continuum. We first performed a Voronoi binning to achieve a $\text{SNR} > 10$ per bin on the continuum (Cappellari &

Table 1. Properties of massive spiral galaxies analysed in this work. Columns: (1) Primary name; (2) Source of H I data, either new data, WHISP, from Spekkens & Giovanelli (2006; SG06) or from Hunter et al. (2013; H13); (3) Assumed distance (EDD or NED); (4) Stellar mass from W1 WISE aperture photometry (typical error is 0.2 dex); (5) Mass of cold gas from H I data, $M_{\text{gas}} = 1.36M_{\text{H I}}$ (typical error is 0.1 dex).

Name	H I data	D Mpc	$\log \frac{M_{\star}}{M_{\odot}}$	$\log \frac{M_{\text{gas}}}{M_{\odot}}$
(1)	(2)	(3)	(4)	(5)
NGC0338	WHISP	78 ± 11	11.2	10.3
NGC1167 ²	WHISP	73 ± 7	11.3	10.3
NGC1324 ²	SG06	72 ± 10	11.2	10.2
NGC2599 ¹	WHISP	73 ± 8	11.1	10.1
NGC2713 ¹	new	68 ± 9	11.4	10.2
NGC2862	SG06	68 ± 12	11.1	10.2
NGC5440	new	57 ± 4	11.1	10.5
NGC5533	WHISP	45 ± 6	11.0	10.4
NGC5635 ²	new	72 ± 13	11.1	10.2
NGC5790	new	164 ± 15	11.3	10.3
UGC02849	SG06	138 ± 25	11.2	10.4
UGC02885	H13	71 ± 9	11.2	10.6
UGC08179 ¹	new	232 ± 18	11.6	10.8
UGC12591	new	97 ± 7	11.7	10.0
UGC12811	new	174 ± 13	11.4	10.3

¹These galaxies also have MaNGA data.

²These galaxies also have CALIFA data.

Copin 2003). The continuum was fitted in each bin with the Penalized PiXel-Fitting software (Cappellari & Emsellem 2004) using MaStar Simple Stellar Population templates (MASTARSSP; Maraston et al. 2020). The best-fitting stellar continuum was then subtracted from the spectrum in each spatial pixel. Finally, from the continuum-subtracted datacubes, we isolated the strongest emission lines for the kinematical modelling, i.e. the H α line at 6564.63 Å and of the [N II] doublet at 6549.86 – 6585.27 Å.

3 METHODS

3.1 Photometry and baryonic masses

Deep multi-band images from publicly available surveys were used to derive stellar surface-density profiles and to estimate stellar masses of galaxies in our sample. In particular, for five galaxies (NGC1167, NGC1324, NGC5533, UGC02849, and UGC02885), we used z -band images from the Panoramic Survey Telescope and Rapid Response System Survey DR2 (Pan-STARRS1, Chambers et al. 2016), while for the remaining 10 galaxies we used z -band images from the Dark Energy Spectroscopic Instrument (DESI) Legacy Surveys DR9 (Dey et al. 2019). In addition, infrared W1-band images at 3.4 μm from the Wide-field Infrared Survey Explorer (WISE; Wright et al. 2010) were used to estimate the total stellar mass.

As in the analysis performed in Di Teodoro et al. (2021), we derived stellar surface-brightness profiles from sky-subtracted z -band images through the PHOTUTILS package (Bradley et al. 2020) implemented within the ASTROPY PYTHON library (Astropy Collaboration 2013, 2018). The light distribution of each galaxy was fitted with a set of elliptical annuli, each described by a centre (x_0, y_0) , a position angle ϕ and an ellipticity $\epsilon \equiv 1 - b/a$, where b/a is the ratio of the ellipse's minor axis b to the major axis a . The average surface-brightness $\Sigma_{\star}(R)$ was computed in each best-fitting annulus. Final errors for surface-brightness profiles were calculated by adding in quadrature the rms variation along each annulus and the error on

sky determination. Derived profiles for all galaxies can be found in Appendix A (online supplementary).

Stellar masses were estimated from background-subtracted 3.4 μm images, where dust obscuration is expected to be negligible. Following Jarrett et al. (2019), we fitted a double Sérsic function to radial profiles and extrapolated it out to $3R_d$, where R_d is the exponential scale length of the disc. The total W1-band flux within $3R_d$ was then K -corrected and stellar mass was calculated from the total W1 luminosity assuming a constant mass-to-light ratio $\Upsilon_{W1} = 0.6$ with a typical uncertainty of ~ 40 per cent (e.g. Norris et al. 2014; Röck et al. 2015). The fourth column of Table 1 lists derived stellar masses M_{\star} from W1 band, with typical errors of 0.2 dex, dominated by the uncertainty on the mass-to-light ratio.

Finally, the atomic hydrogen mass for each galaxy was calculated directly from the total integrated H I flux (Roberts 1975),

$$M_{\text{HI}}[M_{\odot}] = 2.36 D^2 \sum_{i=1}^N S_i \delta v \quad (1)$$

where D is the distance in Mpc and $S_i \delta v$ is the total flux in the i -th velocity channel expressed in Jy km s^{-1} . This equation assumes that H I gas is optically thin. The total baryonic mass (stars + cold gas), ignoring contributions from ionized and molecular gas, is $M_{\text{bar}} = M_{\star} + 1.36 M_{\text{HI}}$, where the factor 1.36 is to take into account the primordial abundance of Helium.

3.2 3D tilted-ring kinematical modelling

We modelled emission-line data with the kinematical fitting code ^{3D}BAROLO (Di Teodoro & Fraternali 2015).³ ^{3D}BAROLO builds 3D tilted-ring models of rotating disc galaxies and fits them directly to emission-line datacubes, taking into account well-known observational biases due to the finite spatial and spectral resolution of a telescope (e.g. beam smearing). This approach does not require the derivation of velocity maps and it proved to be very effective with a variety of emission-line data (e.g. Loiacono et al. 2019; Bewketu Belete et al. 2021; Ponomareva et al. 2021; Dye et al. 2022). ^{3D}BAROLO describes a galaxy as a set of concentric, rotating rings. The main quantities that characterize each ring are: (1) the centre coordinates (x_0, y_0) ; (2) the inclination angle i with respect to the plane of the sky (90° for an edge-on disc); (3) the position angle ϕ of the projected major axis, defined anticlockwise from the North direction; (4) the systemic recession velocity V_{sys} ; (5) the rotation velocity V_{rot} ; (6) the intrinsic gas velocity dispersion σ_{gas} . All these parameters but the galaxy centre and the systemic velocity were allowed to vary ring by ring during the kinematical modelling.

We used the same methodology in the kinematical analysis of radio and optical data. The modelling was performed on the H I line and, when available, on the H α -[N II] lines simultaneously (e.g. Di Teodoro et al. 2018). The kinematic centre was assumed to coincide with the photometric centre derived through the surface-density photometry (see Section 3.1) and fixed to this value throughout the entire procedure. Initial values for all other parameters were estimated automatically by ^{3D}BAROLO from the zeroth and first moment maps. A mask for the fit was created by using the source-finding masking algorithm with a primary threshold of $5 \times \sigma_{\text{rms}}$ and a secondary threshold of $3 \times \sigma_{\text{rms}}$, applied to datacubes smoothed by a factor of 1.5 (we refer to ^{3D}BAROLO's documentation and main paper for further details on these algorithms). An azimuthal normalization

³In particular, for this work we used non-stable version 1.6.3, which can be downloaded at github.com/editeodoro/Bbarolo.

scheme was adopted during the fit and, as a consequence, all models are fully symmetric in gas surface density and kinematics.

The fit was performed using a classical two-step approach. In the first step, all parameters were allowed to vary during the fit. Systemic velocity, inclination and position angles were then regularized and kept fixed during the second fitting step. In particular, V_{sys} was always fixed to a constant value, while ϕ and i were regularized with either a constant, a polynomial function or a Bezier curve, depending on the results of the first fitting step. Finally, a second fit was performed with only the rotation velocity and velocity dispersion kept free. In both fitting steps, we used a $(\cos \theta)^2$ weight, where θ is the azimuthal angle ($\theta = 0$ for major axis), to give more importance to pixels lying near the major axis of a galaxy. Errors on all parameters were calculated through the default Monte Carlo method implemented in ^{3D}BAROLO, which basically samples the variation of the parameter space around the minimum of the residuals (see Di Teodoro & Fraternali 2015, for details). Beside best-fitting kinematical parameters, ^{3D}BAROLO also returns the H I gas surface density $\Sigma_{\text{H I}}$ averaged along the best-fitting rings, which will be used for the mass modelling (Section 3.3) and calculation of the gas specific angular momentum (Section 4.1).

As an example, in Fig. 1 we show the best-fitting 3D kinematical model for the galaxy NGC2713. For this particular galaxy, we had both new extended VLA H I data (top rows) and IFU H α -[N II] data from MaNGA (bottom rows) for the very inner regions of the galaxy (red box in the uppermost left-hand panel). A selection of channel maps of the data (blue contours) are compared to the corresponding channel maps of the best-fitting model (red contours). For all velocity channels, the 3D model can accurately reproduce the line emission in both radio and optical data, signalling an optimal fit. The resulting hybrid H I-H α rotation curve for NGC2713 can be found in the left-hand panel of Fig. 2, where dots denote H I and stars denote H α -[N II]. In Appendix A (online supplementary), we show a comparison between best-fitting models and data for all galaxies through position-velocity slices taken along the apparent major and minor axes of the disc. Most galaxies in our sample have very regular and symmetrical kinematics. We also checked for non-circular motions using the procedure of Di Teodoro & Peek (2021), but we did not find any clear evidence of systematic streaming motions throughout these discs (with the exception of NGC5533, which has a long tidal tail in the external regions). This regularity allowed us to derive robust kinematical models and parameters for most galaxies. Notable exceptions are NGC5635 and UGC12591. The former has an asymmetric rotation curve and, on the approaching side, shows a significant amount of lagging extra-planar gas, which might indicate a recent accretion event (Saglia & Sancisi 1988), also supported by diffuse stellar tails in the optical images. The latter is an extremely massive, lenticular galaxy with relatively little gas, and it is barely detected in our new VLA H I data ($\text{SNR} \lesssim 3$ in most channels). Although we decided to model these two galaxies and we keep them in our sample, we note that their kinematics, and thus the following dynamical analysis, may be very uncertain, in particular for UGC12591.

3.3 Rotation curve decomposition and mass models

Rotation curves derived in Section 3.2 were decomposed into the contribution of the different mass components. Given that our sample is made up by extremely massive galaxies, for which $V_{\text{rot}} \gg \sigma_{\text{gas}}$, we neglected any asymmetric drift correction (e.g. Bureau & Carignan 2002) and we assumed $V_{\text{rot}}(R) \equiv V_c(R)$, where V_c is the circular velocity, i.e. the azimuthal component of the velocity induced in the equatorial plane by an axially symmetric gravitational potential $\phi(R,$

$z)$. The circular velocity profile can be written in terms of the matter components of a galaxy,

$$V_c^2(R) = -R \left. \frac{\partial \phi(R, z)}{\partial R} \right|_{z=0} = V_{\text{gas}}^2(R) + V_{\star}^2(R) + V_{\text{DM}}^2(R) \quad (2)$$

where V_{gas} and V_{\star} are the circular velocity induced by the gaseous and stellar discs, respectively, and V_{DM} is the circular velocity of the DM halo. The stellar circular velocity can be written as $V_{\star}^2 = \Upsilon_{\star} V_{\star,1}^2$, where Υ_{\star} is the mass-to-light ratio and $V_{\star,1}$ is the circular velocity obtained under the assumption that $\Upsilon_{\star} = 1$. In other words, Υ_{\star} normalizes the contribution of the stellar component and is needed because we measure the distribution of light rather than mass. Usually, the gas component V_{gas} and the shape of the stellar component $V_{\star,1}$ can be determined from the data, while the DM component V_{DM} and the mass-to-light ratio Υ_{\star} need to be fitted to the observed rotation curve of a galaxy.

The gravitational potential, thus the circular speed through equation (2), of the stellar and gaseous components can be directly calculated from the observed mass distributions via numerical integration (see e.g. Casertano 1983; Cuddeford 1993). We assumed that both stars and gas lie in discs with a classical vertical profile for an isothermal, self-gravitating layer, given by a squared hyperbolic secant,

$$\rho_d(R, z) = \frac{\Sigma_d(R)}{2z_0} \text{sech}^2 \left(\frac{z}{z_0} \right), \quad (3)$$

where $\Sigma_d(R)$ is the deprojected (i.e. face-on) radial profile for a given component, i.e. Σ_{\star} (Section 3.1) for stars and $\Sigma_{\text{gas}} = 1.36 \Sigma_{\text{H I}}$ (Section 3.2) for gas. Contributions from molecular and ionized gas are expected to be negligible, especially in the outer regions of a galaxy, and are usually not computed in rotation curve decompositions. For both the stellar and the gaseous disc, we assume a constant scale height of $z_0 = 300$ pc. We note that, for massive galaxies like those in our sample, the choice of a different vertical profile and/or scale height would have no significant effect on the rotation curve decomposition (Mancera Piña et al. 2022). Finally, for five galaxies with a clear bulge component in the rotation curve and optical images (NGC1167, NGC1324, NGC2713, NGC5635, and UGC08179), we also used a spheroidal stellar component in addition to the disc component, derived from a bulge-disc decomposition of the surface-brightness profiles.

The dark matter distribution is modelled as a Navarro, Frenk & White (1996; NFW) spherical halo profile:

$$\rho_{\text{DM}}(r) = \frac{4\rho_s}{(r/r_s)(1 + r/r_s)^2}, \quad (4)$$

where $r = \sqrt{R^2 + z^2}$ is the spherical radius, r_s is a scale radius and ρ_s is the density at r_s . The characteristic density ρ_s is given by

$$\rho_s = \frac{M_{200}}{16\pi r_s^3 [\ln(1 + c_{200}) - c_{200}/(1 + c_{200})]}, \quad (5)$$

where M_{200} is the DM mass within a radius R_{200} , where the average density is 200 times the critical density of the Universe, and $c_{200} \equiv R_{200}/r_s$ is the dimensionless concentration parameter. Cosmological DM simulations indicate that M_{200} anti-correlates with c_{200} (Dutton & Macciò 2014; Ludlow et al. 2014). For brevity, in the rest of the paper, we will use the notation M_h and c to indicate M_{200} and c_{200} , respectively.

Given the above parametrization, our rotation curve decomposition procedure has only three free parameters: $\mathbf{x} = (\Upsilon_{\star}, M_h, c)$. For each galaxy in our sample, we found the best-fitting Υ_{\star} , M_h and c via a Monte Carlo Markov chain (MCMC) sampling, using the PYTHON implementation EMCEE (Foreman-Mackey et al. 2013). We used a

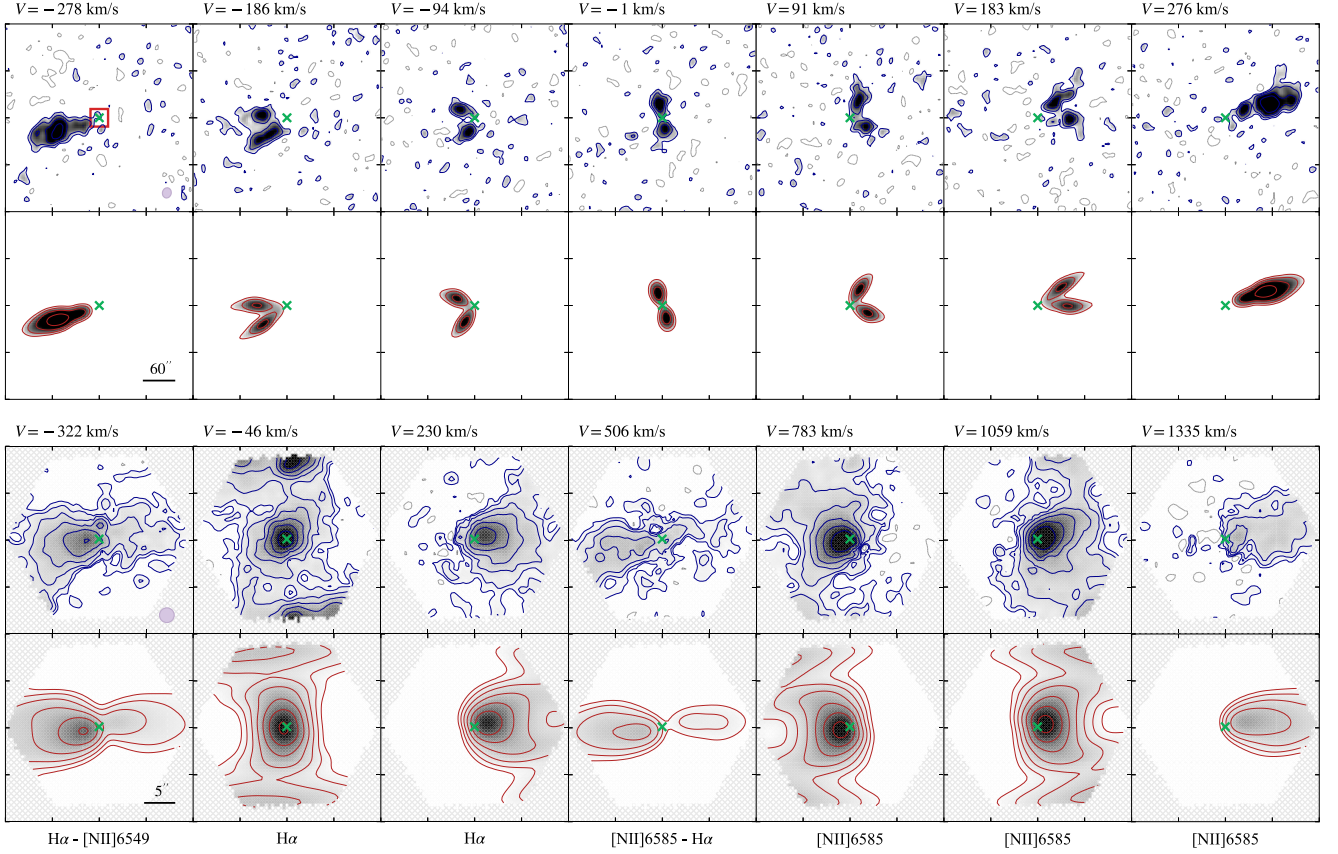


Figure 1. Comparison between observations (blue contours) and model (red contours) for the galaxy NGC2713. Top two rows show VLA H I data, while bottom two rows are MaNGA H α -[N II] data of the inner regions of the galaxy. On the first VLA channel map, a red rectangle denote the field of view of MaNGA data. The green cross in each panel identifies the galaxy centre. Contour levels are at $2.5\sigma_{\text{rms}} \times 2^n$, with $n = 0, 1, \dots, 6$. The beam is shown in the first channel map of both VLA and MaNGA data. For the MaNGA data, the first four channel maps include emission of the H α line, while the last four channel maps include the emission of the [N II] at 6585.27 Å. In the right part of the first channel, emission from the [N II] at 6549.86 Å is also visible. Velocity labels in the MaNGA data are centred on the systemic velocity of the H α line.

standard χ^2 likelihood function \mathcal{P} , defined as

$$\chi^2 = -\ln \mathcal{P}(V_{\text{rot}} | V_{\text{mod}}(\mathbf{x})) = \sum_{i=1}^N \left[\frac{V_{\text{rot}}(R_i) - V_{\text{mod}}(R_i)}{\Delta_i} \right]^2, \quad (6)$$

where $V_{\text{rot}}(R_i)$ and $V_{\text{mod}}(R_i)$ are the observed and model circular velocity at the i -th radius R_i , respectively, and Δ_i are the errors on the rotation velocity.

Appropriate priors on all free parameters were set during the MCMC sampling. With regard to Υ_* , spiral galaxies are known to have a range of mass-to-light ratios that can depend on galaxy morphological type (Bell & de Jong 2001; Portinari, Sommer-Larsen & Tantalo 2004; Fall & Romanowsky 2013), due to their different star formation histories and stellar populations. Testing different Gaussian priors for Υ_* , in a range of values predicted by stellar population models, we found that this has little effect on the resulting mass modeling of different galaxies. For simplicity, for all galaxies we therefore used a Gaussian prior with mean 0.8 and standard deviation 0.3, which broadly embraces values expected in the z -band (e.g. McGaugh & Schombert 2014; Meidt et al. 2014). The prior on M_h is, instead, flat over a wide range $6 < \log M_h/M_\odot \leq 15$. Finally, for the c parameter, we used a lognormal prior with mean given by the $c_{200}-M_{200}$ relation and standard deviation of 0.11 dex around the relation derived from Λ CDM simulations (equation 4

of Dutton & Macciò 2014).⁴ We stress that a strong non-uniform prior on the concentration parameter is necessary to infer reasonable constraints on the halo parameters (see e.g. Katz et al. 2017; Posti et al. 2019b). We sampled posterior probability distributions with 100 walkers running 10 000 steps, including a warm-up phase of 1000 steps. For each free parameter, we assumed the 50th percentile value of the 1D posterior distribution as central value, while lower and upper errors were taken at the 15.87th and 84.13th percentiles, corresponding to the standard deviation for a Gaussian distribution.

Fig. 2 illustrates the rotation curve decomposition for our example galaxy NGC2713. The right-hand panel shows a triangle plot with 1D joint posterior distributions and 2D marginalized posterior distributions.

⁴For simplicity and consistency with previous work in this field, we adopt the $c_{200}-M_{200}$ relation in Λ CDM simulations without baryons. Inflows of baryons within dark halos generally increase their concentration, while outflows decrease it. Thus, the net effect of these flows on the $c_{200}-M_{200}$ relation likely depends on the cooling rates in the protogalactic gas as well as the prescriptions for star formation, black hole growth, and stellar and AGN feedback – a situation that is difficult to quantify reliably. In some recent hydrodynamical simulations (EAGLE) the alteration of the $c_{200}-M_{200}$ relation by baryons is negligible (Schaller et al. 2015), while in others (ILLUSTRIS) it is significant (Chua et al. 2017).

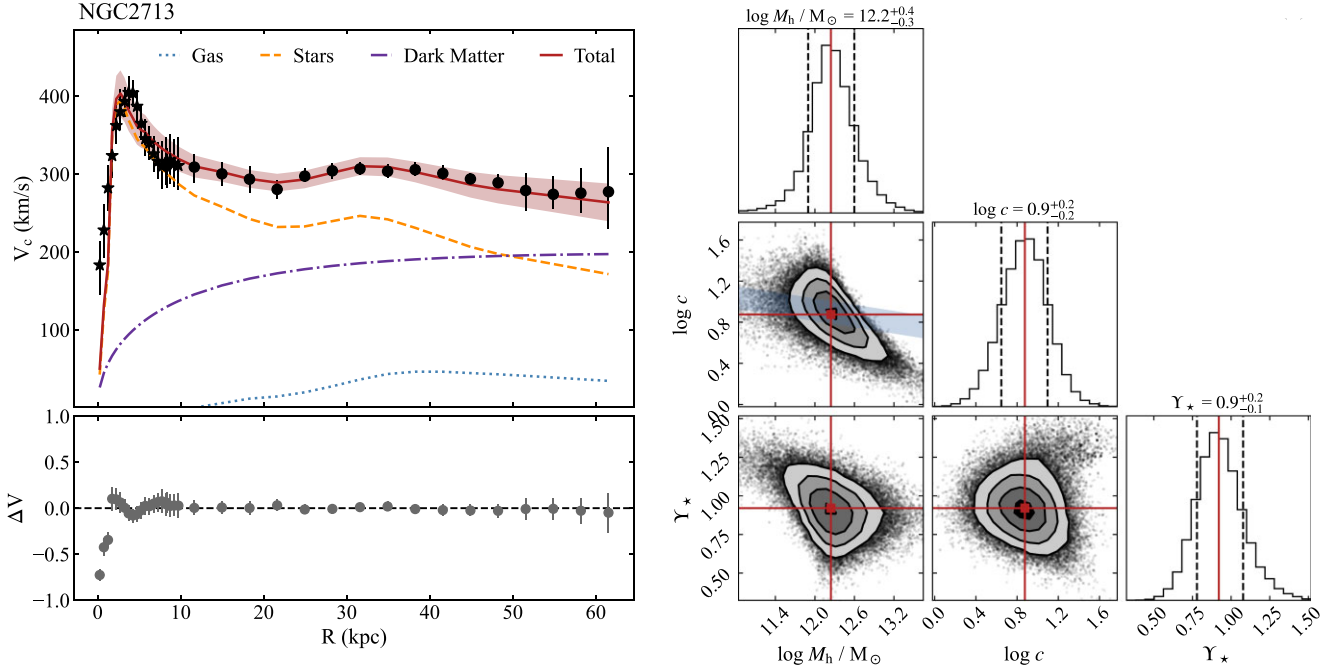


Figure 2. Rotation curve decomposition for the galaxy NGC2713. *Left:* Mass modelling of the hybrid H I–H α rotation curve (H I = dots, H α = stars). Mass components are gas (blue-dotted line), stars (bulge and disc, dashed orange line), and dark matter (dash-dotted purple line). The red-solid line represents the total circular velocity of the model. Bottom panel shows the fractional difference between the modelled and the measured circular velocity curve, $\Delta V = (V_{\text{tot}} - V_{\text{obs}})/V_{\text{obs}}$. *Right:* Triangle plot of the MCMC sampling. 2D posterior distributions are shown as contour plots, with contour drawn at 1σ , 2σ , and 3σ confidence levels. Histograms are the 1D posterior distributions. Full red lines denote the 50th percentile values, dashed black lines are the 15.87th and 84.13th percentiles. The blue band represents the $c_{200}-M_{200}$ relation by Dutton & Macciò (2014) used as a prior.

butions. Central best-fitting values for M_h , c and γ_\star are shown as red-solid lines, 1σ quantiles as black dashed lines on the 1D histograms. The posterior distributions indicate a well-attained sampling and converged chains. The resulting mass model and rotation curve decomposition is illustrated in the left-hand panel. The calculated gas and stellar velocity curves are shown as dotted-blue and dashed-orange lines, respectively, while the fitted DM velocity curve is the dash-dotted purple line. The total circular velocity curve of the model is the solid-red line, compared to the observed rotation curve (black dots and stars) derived as described in Section 3.2. Note the bump in the stellar circular velocity around 30 kpc in radius, caused by a similar feature in the stellar light profile, which corresponds to a bump in the rotation curve (‘Renzo’s rule’; Sancisi 2004). This rotation curve decomposition returned a DM halo mass for NGC2713 of $\log(M_h/M_\odot) \simeq 12.2 \pm 0.3$.

We obtained similarly good mass models for most galaxies in our sample. Rotation curve decompositions and MCMC corner plots for all galaxies are shown again in the atlas of Appendix A (online supplementary). Thanks to the extended H I rotation curves, we were able to put robust constraints on the dark matter halo masses of 13 out of 15 galaxies. Again, the most problematic galaxies are NGC5635 and UGC12591, for which the kinematic and mass modelling did not allow us to unequivocally decompose the contribution of the visible and dark matter.

The galaxies in our sample all lack publicly available CO observations, preventing us from including molecular gas in our calculations of baryonic quantities. However, we expect the contribution of molecules to be relatively minor, based on observations of other massive spirals, which typically have $M_{\text{mol}} \sim M_{\text{H I}} \sim 0.1M_\star$, mostly

concentrated toward the galactic centres (Saintonge & Catinella 2022). This will have little effect on the outer rotation curves, and thus on the derived mass of the halo and angular momentum of the disc. Finally, because the stellar component should always dominate the circular velocity in the inner regions, we do not expect any significant effect on the estimated total stellar mass either.

4 RESULTS

4.1 Tully–Fisher and Fall scaling relations

We placed our massive spiral galaxies on the two most important scaling relations for discs: the Tully & Fisher (1977) relation, between mass and rotation velocity, and the Fall (1983) relation, between mass and specific angular momentum $j = J/M$. We explored both the stellar and baryonic (stars + atomic gas) versions of these relations.

For the Tully–Fisher relations, we used the average velocity along the flat part of the rotation curve V_{flat} , which has been shown to minimize the scatter of the relation (Verheijen 2001; Lelli et al. 2019). This characteristic speed was computed following the iterative algorithm of Lelli et al. (2016a; see their equations 1 and 2), i.e. by requiring that the rotation velocities are flat within 5 per cent over at least the last three measured points. We note that all our galaxies have very flat rotation curves in the outer regions and many more points are usually included in the computation of V_{flat} . For consistency with the literature, we used stellar masses derived from the W1-band WISE photometry with a fixed $\gamma_{\text{W1}} = 0.6$ (Section 3.1) rather than those derived from the mass modelling. The stellar masses obtained

by these two different methods never differ more than the typical uncertainty of 0.1–0.2 dex (see Appendix B (online supplementry)). For the baryonic mass, we simply assume $M_{\text{bar}} = M_{\star} + 1.36M_{\text{HI}}$.

The left-hand panels of Fig. 3 show the stellar (top) and baryonic (bottom) Tully–Fisher relations. Together with our sample (red squares), we plot less massive galaxies from the SPARC sample (Lelli et al. 2016b, 2019; blue circles) and the higher- z sample ($0.04 \lesssim z \lesssim 0.28$) of superspiral galaxies by Di Teodoro et al. (2021; open triangles). The latter only have H α long-slit rotation curves, which typically do not extend further out than the optical disc, while H I rotation curves for most galaxies in this work reach radii 1.5–2 times larger than the optical disc. Throughout this paper, all data points derived from extended H I rotation curves (red and blue symbols), in all the relations presented, were determined by similar analysis techniques and with similar assumptions. In both the stellar and baryonic Tully–Fisher relations, our galaxies lie at the high-mass end of a single, unbroken power-law relation. We fit linear functions in the form $\log M = \beta \log V_{\text{flat}} + \log B$ to the Tully–Fisher relations in Fig. 3, using an orthogonal distance regression method to take into account errors on both axes. The best-fitting parameters are $(\beta, \log B) = (4.06 \pm 0.14, 1.26 \pm 0.32)$ for the stellar relation and $(\beta, \log B) = (3.58 \pm 0.10, 2.52 \pm 0.22)$ for the baryonic relation (black lines). These values are in good agreement with previous determinations of the relations at lower masses in the local Universe (e.g. McGaugh 2012; Zaritsky et al. 2014; Lelli et al. 2016a, 2019; Papastergis, Adams & van der Hulst 2016; Ponomareva et al. 2017, 2021). The best-fitting values and 1σ errors for all relations investigated in this paper are summarized in Table 2. Our new analysis therefore confirms the recent finding by Di Teodoro et al. (2021) that the Tully–Fisher relations extend at least up to $\log M/M_{\odot} \simeq 11.7$ as unbroken power laws.

Our sample includes the S0/Sa galaxy UGC12591, which has been known for decades as the fastest rotating disc in the local Universe (Giovanelli et al. 1986). Contrary to recent results by Ray et al. (2022), we find that this galaxy is consistent with the Tully–Fisher relation within the uncertainties. This discrepancy is ascribable to the fact that Ray et al. estimated a significantly lower stellar mass ($\log M_{\star}/M_{\odot} \simeq 11.2$ vs our 11.7) and they used the H α maximum rotation velocity from Giovanelli et al. (1986), which exceeds 500 km s^{−1} in the inner regions, while we use the flat part of the extended H I rotation curve ($V_{\text{flat}} \simeq 450$ km s^{−1}). We note that our stellar mass estimate is in agreement with other measurements in the literature (e.g. Dai et al. 2012; Li et al. 2017) and that our H I data, although noisy, seem to disfavour a flat velocity substantially larger than 450 km s^{−1}.

For the Fall relations, the specific angular momentum j_k for a given component k (stars, j_{\star} , or gas, j_{gas}) inside a radius R can be calculated as

$$j_k(< R) = \frac{J_k(< R)}{M_k(< R)} = \frac{\int_0^R \Sigma_k(R') R'^2 V_{k,\text{rot}}(R') dR'}{\int_0^R \Sigma_k(R') R' dR'}, \quad (7)$$

where Σ_k and $V_{k,\text{rot}}$ are the mass surface density and the azimuthal velocity of either the gas ($\Sigma_{\text{gas}}, V_{\text{gas,rot}}$) or the stars ($\Sigma_{\star}, V_{\star,\text{rot}}$). For gas, $V_{\text{gas,rot}}$ is simply the H I rotation curve V_{rot} , while for stars we also assume co-rotation with the gas, i.e. $V_{\star,\text{rot}} = V_{\text{rot}}$. Although stars usually have larger velocity dispersions and thus rotate slower than cold gas, this velocity lag is expected to be negligible in high-mass disc galaxies (Obreschkow & Glazebrook 2014; Posti et al. 2018b). For the total baryons, j_{bar} was calculated by using $\Sigma_{\text{bar}} = \Sigma_{\star} + 1.36\Sigma_{\text{HI}}$ and $V_{\text{bar}} = V_{\text{rot}}$. Equation (7) was used to compute the specific angular momentum of a given matter component as a function of radius. The total values of j_{\star} and j_{bar} for each galaxy were

then taken from the converged cumulative j profiles (for details, see Posti et al. 2018b; Di Teodoro et al. 2021).

The right-hand panels of Fig. 3 show the stellar (top) and baryonic (bottom) Fall relations. In addition to our sample (red squares), we plot galaxies from Mancera Piña et al. (2021a) (blue circles) and the higher- z H α sample from Di Teodoro et al. (2021; green triangles, only in the stellar relation). The black lines are linear fits in the form $\log j = \alpha \log M + \log A$, with best-fitting values $(\alpha, \log A) = (0.61 \pm 0.08, -3.31 \pm 0.26)$ for the stellar relation and $(\alpha, \log A) = (0.61 \pm 0.07, -3.27 \pm 0.24)$ for the baryonic relation, consistent with previous studies (e.g. Fall 1983; Fall & Romanowsky 2013, 2018; Posti et al. 2018b; Murugesan et al. 2019; Di Teodoro et al. 2021; Mancera Piña et al. 2021a, b; Hardwick et al. 2022). As with the Tully–Fisher relation, the baryonic form of the Fall relation is tighter than the stellar form, with an orthogonal scatter σ_{\perp} of the data points around the best-fitting power law decreasing from 0.21 dex to 0.18 dex. At the high-mass end, galaxies tend to lie slightly above these best-fitting relations. This might be a sign that the Fall relation has a weak bend at high masses, or it may be a bias due to our preference for selecting fast-rotating galaxies (see Section 2.1). However, both the Bayesian Information Criterion (BIC) and the Akaike Information Criterion (AIC) disfavour a double power-law model over a single power-law model. We note finally that our slope $\alpha \simeq 0.61$ for discs is very close to the value of 2/3 for DM halos in a Λ CDM cosmology, thus already indicating that the specific angular momentum ratio f_j is nearly independent of mass.

4.2 Stellar-to-halo mass relations

In this Section, we present the SHMRs for our sample of massive spiral galaxies. Fig. 4 shows the SHMR in the form $f_M \equiv M_{\star}/M_h$ as a function of M_{\star} (left) and as a function of M_h (right). The galaxies analysed in this work are represented by red squares. The two galaxies for which we could not obtain a good DM halo constraint (NGC5635 and UGC12591) are not shown in this and the following figures. We also plot the lower-mass disc galaxy sample of Posti et al. (2019a), derived with an identical mass decomposition procedure, as blue circles. The horizontal thick dashed line highlights the cosmic baryon fraction, i.e. $f_M = f_b = 0.156$. The grey band shows the SHMR estimated by Moster et al. (2013) using abundance matching, which represents the standard SHMR in the field (Wechsler & Tinker 2018). We note that other SHMRs in the literature (e.g. Rodríguez-Puebla et al. 2015; Mandelbaum et al. 2016; Behroozi et al. 2019) have qualitatively similar shapes to that of Moster et al. (2013). In both panels, the diagonal blue dot-dashed line denotes a simple linear fit to the data points. Fig. 5 shows instead the high-mass end of the M_{\star} – M_h relation, using the same symbols as Fig. 4. This represents a good alternative visualization of the SHMR because errors on the plotted quantities are not correlated by construction. In the M_{\star} – M_h diagram, as a reference, we also plot the positions of the Milky Way from Posti & Helmi (2019) and M31 from Corbelli et al. (2010).

The difference between abundance matching and our dynamical fits in the high-mass regime of the SHMR is evident, particularly from the f_M – M_{\star} and the M_h – M_{\star} relations. Our galaxy sample confirms a picture where f_M increases monotonically with M_{\star} , with no indication of a peak in the range $10.5 \leq \log M_{\star}/M_{\odot} \leq 11$, where the SHMR derived from abundance matching turns over. For example, for a galaxy with $M_{\star} = 2 \times 10^{11} M_{\odot}$, the Moster et al. (2013) SHMR implies $f_M \simeq 0.04$ and $M_h \simeq 6 \times 10^{13} M_{\odot}$, while with our linear relation we find $f_M \simeq 0.09$ and $M_h \simeq 2 \times 10^{12} M_{\odot}$. In other words, massive spirals inhabit less massive halos than galaxies in general, which tend to be lenticulars and ellipticals at high mass. These

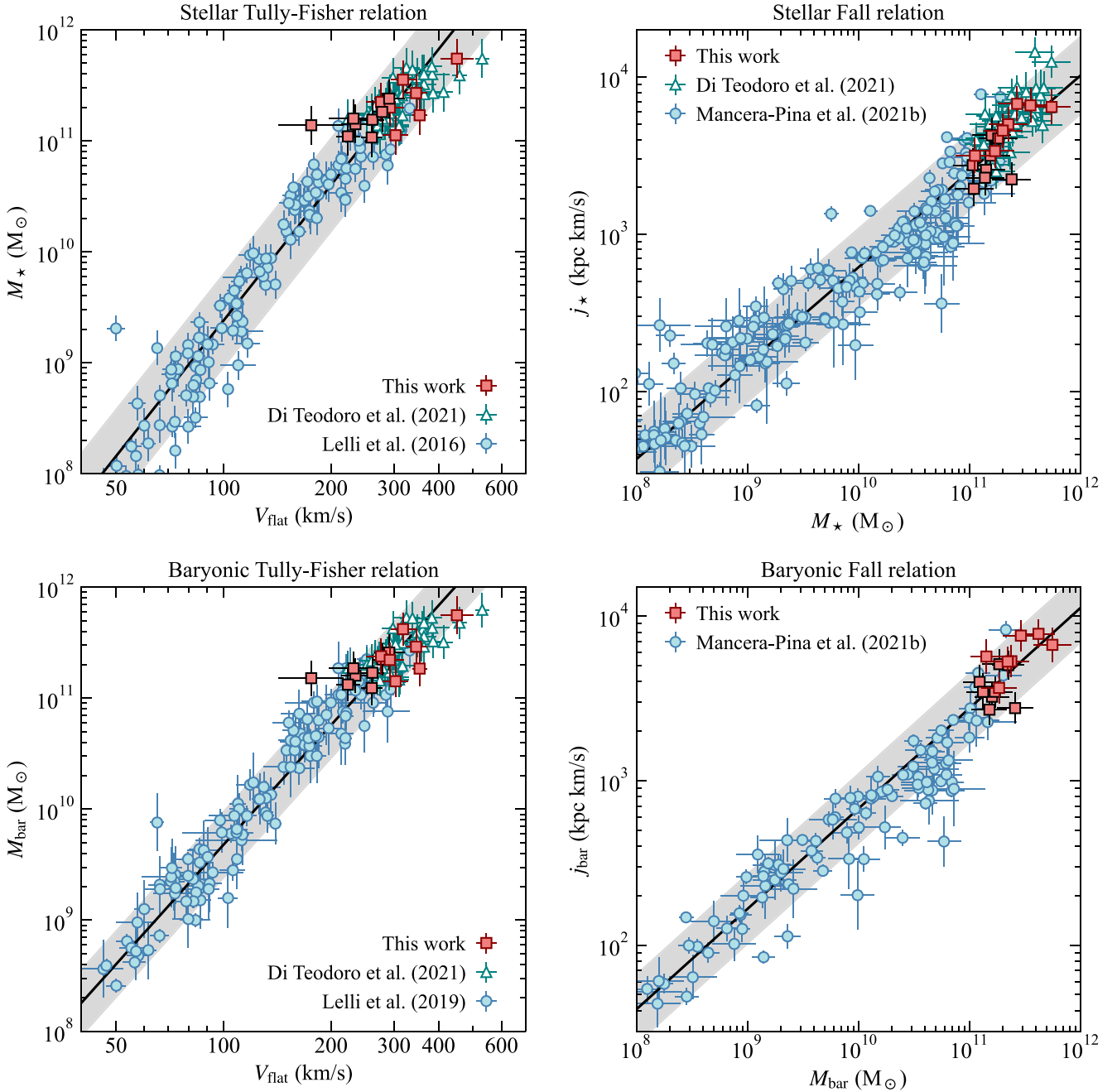


Figure 3. Tully–Fisher relations (left-hand panels) and Fall relations (right-hand panels) for our sample of extremely massive spiral galaxies with extended H I rotation curves (red squares). Markers of galaxies with new VLA data are shown with red edges, while archival galaxies with black edges. We also plot galaxies with measurements from H I rotation curves from the literature (blue circles; Lelli, McGaugh & Schombert 2016b; Lelli et al. 2019; Mancera Piña et al. 2021b). Open green triangles denote the high-mass sample of Di Teodoro et al. (2021), with measurements coming from long-slit H α rotation curves only. Black lines and grey shaded regions indicate best-fitting relations and orthogonal scatter around them, respectively. The best-fitting parameters and 1σ errors of these relations are listed in Table 2.

findings agree with and improve upon other recent studies of dark matter halos in late-type galaxies at slightly lower masses (M_* up to $1 - 2 \times 10^{11} M_\odot$; Posti et al. 2019a; Li et al. 2020).

Finally, we note that this difference holds regardless of the assumptions made during the mass modeling procedure. In particular, we tested the effect of using different DM halo profiles beside the NFW profile of equation (4), including pseudo-isothermal, cored Burkert (1995) and Einasto (1965) profiles. We also varied the centre

of the prior on the mass-to-light ratio in the z -band over the range $0.3 \lesssim Y_* \lesssim 1.3$ indicated by stellar population synthesis models (e.g. McGaugh & Schombert 2014; Schombert, McGaugh & Lelli 2019). We found that, although changing the above assumptions may marginally modify our DM halo mass estimates, the overall picture of the SHMR shown in Fig. 4 does not change significantly (see also appendix A2 in Posti et al. 2019a for similar tests on the SHMR).

Table 2. Best-fitting parameters γ and $\log C$ for relations in the form $\log(y) = \gamma \log(x) + \log C$. For the Tully–Fisher and Fall relations, we also list the orthogonal perpendicular scatter σ_\perp around the best-fitting relation.

Relation ($y-x$)	γ	$\log C$	σ_\perp
<i>Tully–Fisher relations</i>			
$M_\star-V_{\text{flat}}$	4.06 ± 0.14	1.26 ± 0.32	0.10
$M_{\text{bar}}-V_{\text{flat}}$	3.58 ± 0.10	2.52 ± 0.22	0.07
<i>Fall relations</i>			
$j_\star-M_\star$	0.61 ± 0.08	-3.31 ± 0.26	0.21
$j_{\text{bar}}-M_{\text{bar}}$	0.61 ± 0.07	-3.27 ± 0.24	0.18
<i>Stellar-to-halo mass relations</i>			
f_M-M_\star	0.46 ± 0.08	-6.23 ± 0.38	–
f_M-M_h	0.82 ± 0.16	-11.13 ± 1.72	–
$M_\star-M_h$	0.59 ± 0.06	5.74 ± 0.32	–
<i>Retained specific angular momentum relations</i>			
$f_{j,\star}-M_\star$	0.16 ± 0.07	-1.70 ± 0.39	–
$f_{j,\star}-M_h$	0.13 ± 0.09	-1.62 ± 0.46	–
$f_{j,\text{bar}}-M_{\text{bar}}$	0.04 ± 0.03	-0.14 ± 0.39	–
$f_{j,\text{bar}}-M_h$	-0.02 ± 0.04	-1.62 ± 0.48	–

4.3 Angular momentum retention

As a final step, we studied how the specific angular momentum of stars j_\star and baryons j_{bar} relates to the specific angular momentum of DM halos j_h through the ratios $f_{j,\star} \equiv j_\star/j_h$ and $f_{j,\text{bar}} \equiv j_{\text{bar}}/j_h$, also known as ‘retained fractions of angular momentum’. In particular, for each galaxy, we estimated the average value of $f_{j,k}$ for a given component k (stars or baryons) as

$$\langle f_{j,k} \rangle = j_k \left\langle \frac{1}{j_h} \right\rangle = j_k \frac{\int_0^{+\infty} [j_h(\lambda)]^{-1} p(\lambda) d\lambda}{\int_0^{+\infty} p(\lambda) d\lambda} \approx \frac{j_k}{\sqrt{2} R_h V_h} \left\langle \frac{1}{\lambda} \right\rangle \approx 32.5 \frac{j_k}{\sqrt{2} R_h V_h}. \quad (8)$$

Here, $R_h = R_{200}$ and $V_h = V_{200}$ are the virial radius and circular velocity of the DM halo, where its mean enclosed density is 200 times the cosmic critical density, and we have used the Bullock et al. (2001) approximate relation $j_h(\lambda) \approx \sqrt{2} \lambda R_h V_h$ between the spin parameter λ and specific angular momentum j_h of the halo. The distribution of spin parameters $p(\lambda)$ for halos in Λ CDM is known to be very close to a log-normal distribution with mean $\log \lambda = -1.456$ and $\sigma_{\log \lambda} = 0.22$ dex, independent of halo mass (Bullock et al. 2001; Bett et al. 2007). This implies $\langle 1/\lambda \rangle \simeq 32.5$. Errors on $f_{j,k}$ were calculated by bootstrapping, i.e. taking the standard deviation over 10k realizations of $f_{j,k}$ obtained by randomly sampling j_k , R_h , V_h and λ according to their distributions. We remark that the calculation of f_j is analogous to that of f_M . In both ratios, the numerator (M_\star or j_k) is determined from observations, while the denominator (M_h or j_h) is inferred by imposing physically-motivated priors, i.e. the lognormal priors on the concentration c for M_h (Section 3.3) and on the spin parameter λ for j_h .

The upper panels of Fig. 6 show how $f_{j,\star}$ varies as a function of M_\star (left) and M_h (right), while the lower panels display $f_{j,\text{bar}}$ as a function of M_{bar} (left) and M_h (right). As in previous plots, the red squares represent the 13 massive galaxies analysed in this work for which we could obtain robust estimates of DM halo masses. The blue circles represent SPARC galaxies, for which we cross-matched j_\star and/or j_{bar} from Posti et al. (2018b) and Mancera Piña

et al. (2021b) to j_h calculated from rotation curve decomposition by Posti et al. (2019a). The tilted blue dot-dashed lines represent linear fits to the relations. Although the data points have significant errors and scatter, $f_{j,\star}$ increases only marginally with stellar and halo mass. This dependence is very weak, with best-fitting slopes of 0.16 (vs M_\star) and 0.13 (vs M_h). The baryonic ratio $f_{j,\text{bar}}$ is even flatter, basically constant with mass. The mean and median of $f_{j,\star}$ across the entire spiral sample are 0.70 and 0.75, while those of $f_{j,\text{bar}}$ are 0.93 and 0.96, respectively. This ~ 20 per cent offset between the specific angular momentum of stars and baryons can be understood in terms of gas-to-stellar ratios of specific angular momentum and mass. Because, on average, $j_{\text{gas}} \simeq 2j_\star$ (Mancera Piña et al. 2021a) and $M_{\text{gas}} \simeq 0.1M_\star$, the gas adds approximately 20 per cent to the total specific angular momentum, accounting for the difference between $f_{j,\star}$ and $f_{j,\text{bar}}$. Moreover, because low mass galaxies have in general larger gas fractions than more massive galaxies, the relative contribution of j_{gas} decreases with mass, causing the flattening of the baryonic relation with respect to the stellar relation. Our galaxies sit at the high-mass end of the relations and show $f_{j,\text{bar}}$ (and $f_{j,\star}$) values consistent with unity, i.e. $j_\star \simeq j_{\text{bar}} \simeq j_h$. In other words, galactic discs have retained essentially all the initial specific angular momentum they acquired from tidal torques, with little or no dependence on stellar and halo mass. Our findings agree with other recent estimates of $f_{j,\star}$ in spiral galaxies (Fall & Romanowsky 2013; Huang et al. 2017; Posti et al. 2019b; Di Teodoro et al. 2021).

The most important quantities estimated in this work are summarized in Table 3.

4.4 Constraining the galaxy–halo connection with the observed scaling relations

In the Λ CDM cosmology, the formation of DM halos is relatively simple and well understood, leading to the scaling relations $M_h \propto V_h^3$ and $j_h \propto M_h^{2/3}$ (e.g. Mo et al. 2010). In contrast, the formation of the baryonic components of galaxies by dissipative collapse, star formation, feedback, and other processes within the dark halos is much more complex and still under active investigation. The net effects of these formation processes are conveniently summarized by the stellar fractions $f_M \equiv M_\star/M_h$, $f_{j,\star} \equiv j_\star/j_h$, and $f_V \equiv V_{\text{flat}}/V_h$ and their baryonic counterparts. The stellar Tully–Fisher and Fall relations can then be rewritten in this notation as $M_\star \propto f_M (V_{\text{flat}}/f_V)^3$ and $j_\star \propto f_{j,\star} (M_\star/f_M, \star)^{2/3}$.

In the previous section, we derived the (logarithmic) slopes of these linear scaling relations and the corresponding mass dependencies of the fractions f_M and $f_{j,\star}$ assuming that the measured quantities M_\star , j_\star , and V_{flat} are all independent of each other (with results listed in Table 2). In the Λ CDM cosmology, however, M_\star , j_\star , and V_{flat} are linked by the fractions f_M , $f_{j,\star}$, and f_V to the halo spin parameter λ induced by tidal torques, which, as mentioned in Section 4.3, has a well-known, nearly log-normal probability distribution $p(\lambda)$, independent of halo mass M_h and overdensity Δ (Bullock et al. 2001). In a recent work, Posti et al. (2019b) have designed a novel statistical procedure that simultaneously fits for the dependencies of f_M , $f_{j,\star}$, and f_V on M_\star or V_{flat} while also enforcing the required $p(\lambda)$ as a prior. For a complete description of the method and results, we refer interested readers to the Posti et al. (2019b) paper.

Posti et al. (2019b) applied this procedure to a sample of 138 nearby galaxies with near-infrared images and H I rotation curves (mostly from Lelli et al. 2016a), covering a wide range of stellar masses. We have repeated this analysis with the addition of the 15 high-mass spirals with new H I rotation curves presented in this

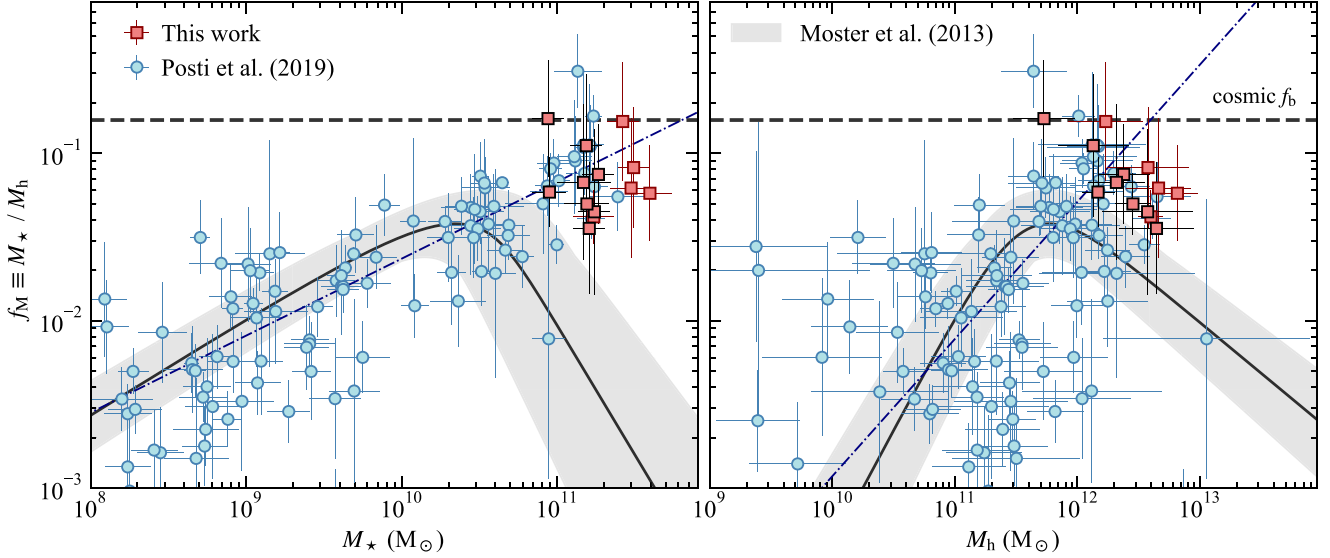


Figure 4. Stellar-to-halo mass relations f_M – M_* (left) and f_M – M_h (right). In both panels, we plot our galaxy sample (red squares) and the spiral galaxy sample by Posti et al. (2019a), obtained with an identical technique and the same priors. As in Fig. 3, galaxies with archival data have black edges. The horizontal black-dashed lines denote the cosmic baryon fraction, i.e. $f_M = f_b = 0.156$. The black full curves are the mean SHMR from abundance matching by Moster et al. (2013), with grey bands representing 1σ deviations. The diagonal blue dash-dotted lines are best-fitting linear relations to the entire galaxy sample. The best-fitting parameters and 1σ errors of these relations are listed in Table 2.

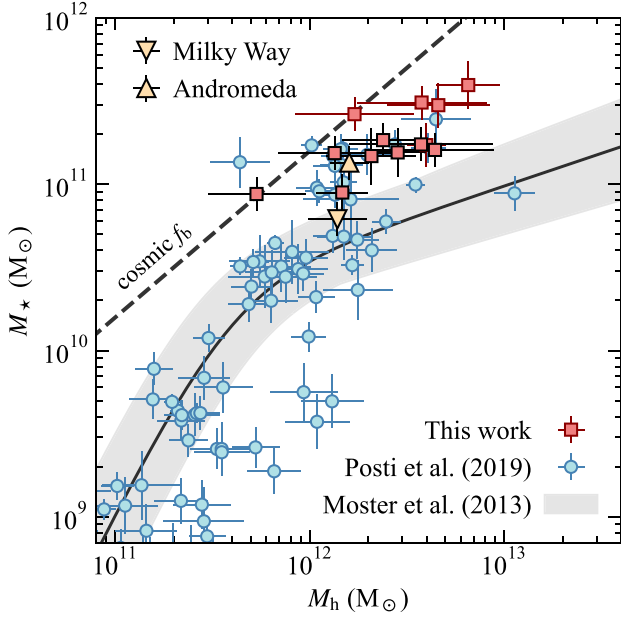


Figure 5. Stellar-to-halo mass relation M_* – M_h . Symbols as in Fig. 4. In this plot we also show the Milky Way (downfacing triangle; Posti & Helmi 2019) and the Andromeda galaxy (upfacing triangle; Corbelli et al. 2010).

paper.⁵ The results are $f_M \propto M_*^{0.31 \pm 0.08}$, $f_{j,*} \propto M_*^{0.02 \pm 0.06}$, and $f_V \propto M_*^{-0.01 \pm 0.04}$ (for the linear model), i.e. a significant increase of f_M with M_* but no dependence of $f_{j,*}$ or f_V on M_* , in excellent

⁵We have adopted this approach in order to test whether the extension of the sample to higher masses alters the results significantly. We have also checked that the results are not sensitive to the exact definition of the sample at lower masses.

agreement with the findings of Posti et al. (2019b) (see their Table B.1). These fits also agree reasonably well with those listed here in Table 2 given the different assumptions involved, i.e. one with independent M_* , j_* , and V_{flat} and the other with these quantities linked by $p(\lambda)$. Thus, this formalism, which returns a nearly constant $f_{j,*} \sim 0.8$ – 1 and $f_V \sim 1$, and a linearly increasing f_M , reinforces our conclusions that the power-law forms of the Tully–Fisher and Fall relations descend naturally from the scaling relations of their parent DM halos.

5 DISCUSSION

Our analysis clearly shows that massive discs sit on the continuation of the most important scaling relations for late-type galaxies (Tully–Fisher and Fall relations) and that they live in dark matter halos that scale almost linearly with stellar mass. This implies that disc galaxies are a self-similar population of objects closely related to their dark matter halos over a wide range of mass, i.e. high-mass discs are simply scaled up versions of low-mass discs. Moreover, we find that galactic discs, on average, have almost as much specific angular momentum as their halos, i.e. they retain nearly all the initial angular momentum imparted by tidal torques.

We observe that massive discs have systematically lower halo masses, corresponding to higher stellar-to-halo mass ratios f_M , than those expected from conventional abundance matching prescriptions (Wechsler & Tinker 2018). For example, our spiral galaxies typically have DM masses a factor 3–8 smaller than those implied by the Moster et al. (2013) relation. A likely explanation for this discrepancy was recently put forward by Posti & Fall (2021), who argued that the SHMR has a secondary correlation with galaxy type, i.e. the relation splits in two different branches at high masses, a rising one for late-type galaxies and a falling one for early-type galaxies. Abundance matching prescriptions are mostly based on the general galaxy population; however, the ratio of early-type to late-type galaxies varies significantly with stellar and halo mass. In particular,

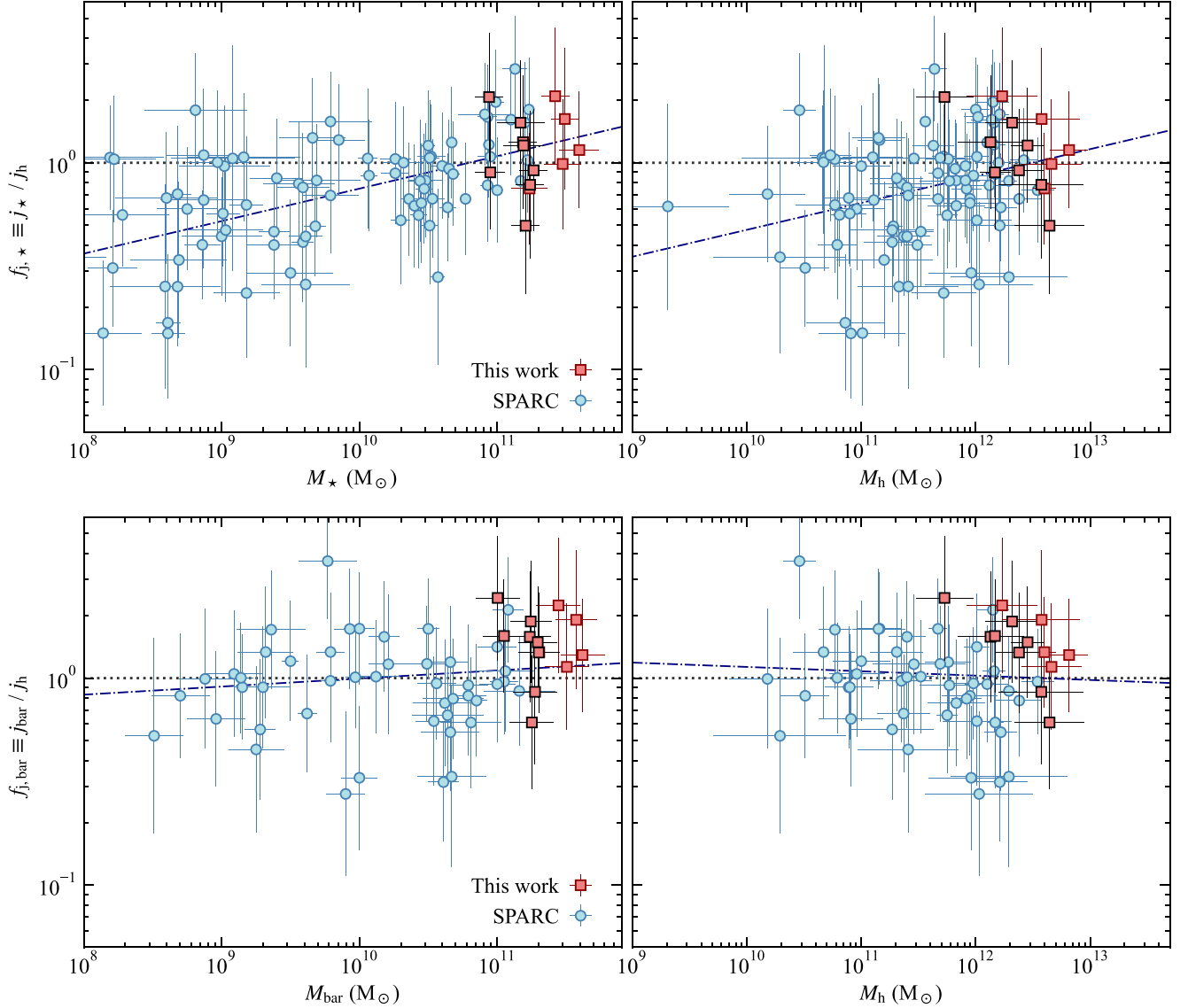


Figure 6. Retained fraction of angular momentum of stars ($f_{j,*} \equiv j_{*}/j_h$, upper panels) and baryons ($f_{j,\text{bar}} \equiv j_{\text{bar}}/j_h$, lower panels) as a function of stellar/baryonic mass (left) and DM halo mass (right). We plot our galaxy sample (red squares, archival data with black edges) and the SPARC sample with measurements from Posti et al. (2018b, 2019a) and Mancera Piña et al. (2021b). The horizontal black dotted lines indicate $f_j = 1$. The tilted blue dash-dotted lines are best-fitting linear relations to the entire galaxy sample. The best-fitting parameters and 1σ errors of these relations are given in Table 2.

the galaxy population is heavily dominated by massive early-type spheroids for $M_* \gtrsim 5 \times 10^{10} M_\odot$ (Kelvin et al. 2014). In this context, it is not surprising that massive discs, which are rare at high masses and not well represented by abundance matching prescriptions, are discrepant with respect to those predictions. Recent cosmological simulations of galaxy formation also find morphology-dependent SHMRs (Correa & Schaye 2020; Marasco et al. 2020; Rodriguez-Gomez et al. 2022), although these differences are somewhat weaker than the empirically based SHMRs presented here.

Our findings further support this idea of a splitting at high-masses of the SHMR, which implies the existence of two distinct evolutionary pathways for building up massive discs and massive spheroids. Massive spiral galaxies like the ones in our sample must have been evolving in near isolation, continuing to grow in mass and gradually transforming gas into stars, with their star formation mainly sustained through a relatively smooth accretion of gas from the

surroundings and/or minor mergers, and with a regulation mechanism dictated by feedback from young stars. Such gradual evolution would move galaxies up to the high-mass ends of the scaling laws and up to the rising branch of the SHMR, without introducing a prominent feature like a break or a bend. These galaxies somehow avoided disruptive events (see also Saburova 2018; Saburova et al. 2021), like major mergers and strong AGN feedback in the form of outflows and radiation, capable of drastically impeding gas inflows and star formation, hence reducing f_M , and at the same time causing the dynamical heating of the stellar body and the growth of the spheroidal component (e.g. Hopkins et al. 2006, 2010; Martin et al. 2018). These events would have moved massive discs off the scaling relations and off the rising branch of the SHMR. In simplified terms, discs mostly know about hierarchical assembly, which gives them their self-similarity, and are mainly regulated by gas accretion and star-formation feedback. They have relatively small spheroids, thus

Table 3. Physical quantities derived through kinematical and dynamical modelling. Columns: (1) Primary name; (2) Velocity of the flat part of the rotation curve V_{flat} ; (3) Specific angular momentum of stars j_* ; (4) Specific angular momentum of baryons j_{bar} ; (5) Stellar mass M_* from rotation curve decomposition; (6) Dark-matter halo mass M_h ; (7) Concentration parameter c ; (8) Stellar-to-halo mass ratio $f_M \equiv M_*/M_h$; (9) Retained fraction of specific angular momentum of stars $f_{j,*} = j_*/j_h$; (10) Retained fraction of specific angular momentum of baryons $f_{j,\text{bar}} = j_{\text{bar}}/j_h$. Kinematical and/or mass decompositions for NGC5635 and UGC12591 are extremely uncertain. We do not use these two galaxies in the SHMRs and in the f_j – M relations.

Name (1)	$V_{\text{flat}}/\text{km s}^{-1}$ (2)	$\log \frac{j_*}{\text{kpc km s}^{-1}}$ (3)	$\log \frac{j_{\text{bar}}}{\text{kpc km s}^{-1}}$ (4)	$\log \frac{M_*}{M_\odot}$ (5)	$\log \frac{M_h}{M_\odot}$ (6)	$\log c$ (7)	f_M (8)	$f_{j,*}$ (9)	$f_{j,\text{bar}}$ (10)
NGC0338	234 ± 21	3.41 ± 0.11	3.51 ± 0.10	11.2 ± 0.1	12.1 ± 0.3	0.9 ± 0.1	0.11 ± 0.09	1.26 ± 0.94	1.58 ± 1.16
NGC1167	291 ± 28	3.35 ± 0.10	3.44 ± 0.10	11.2 ± 0.1	12.7 ± 0.3	0.9 ± 0.1	0.04 ± 0.02	0.49 ± 0.37	0.61 ± 0.45
NGC1324	261 ± 20	3.50 ± 0.09	3.54 ± 0.10	11.2 ± 0.1	12.6 ± 0.4	0.9 ± 0.1	0.04 ± 0.03	0.78 ± 0.64	0.86 ± 0.69
NGC2599	176 ± 36	3.36 ± 0.11	3.43 ± 0.11	10.9 ± 0.1	11.7 ± 0.2	1.0 ± 0.1	0.16 ± 0.12	2.07 ± 1.46	2.44 ± 1.70
NGC2713	276 ± 26	3.70 ± 0.11	3.73 ± 0.11	11.5 ± 0.1	12.2 ± 0.3	0.9 ± 0.2	0.15 ± 0.12	2.10 ± 1.59	2.25 ± 1.69
NGC2862	260 ± 18	3.44 ± 0.09	3.60 ± 0.10	11.3 ± 0.1	12.4 ± 0.2	0.9 ± 0.1	0.07 ± 0.05	0.92 ± 0.63	1.33 ± 0.89
NGC5440	303 ± 25	3.50 ± 0.08	3.75 ± 0.09	11.2 ± 0.1	12.6 ± 0.1	1.0 ± 0.1	0.04 ± 0.02	0.75 ± 0.46	1.34 ± 0.82
NGC5533	223 ± 17	3.29 ± 0.10	3.54 ± 0.10	10.9 ± 0.1	12.2 ± 0.1	1.0 ± 0.1	0.06 ± 0.03	0.89 ± 0.56	1.59 ± 1.01
NGC5635	354 ± 18	3.53 ± 0.11	3.57 ± 0.11	11.2 ± 0.1	13.4 ± 0.5	0.8 ± 0.1	0.01 ± 0.01	0.25 ± 0.22	0.28 ± 0.24
NGC5790	292 ± 27	3.66 ± 0.11	3.72 ± 0.10	11.5 ± 0.1	12.7 ± 0.3	0.9 ± 0.1	0.06 ± 0.05	0.99 ± 0.71	1.13 ± 0.80
UGC02849	231 ± 36	3.63 ± 0.10	3.71 ± 0.10	11.2 ± 0.2	12.3 ± 0.3	1.0 ± 0.1	0.07 ± 0.06	1.56 ± 1.08	1.88 ± 1.27
UGC02885	278 ± 16	3.61 ± 0.10	3.70 ± 0.10	11.2 ± 0.2	12.5 ± 0.2	0.9 ± 0.1	0.05 ± 0.02	1.21 ± 0.77	1.49 ± 0.93
UGC08179	318 ± 25	3.82 ± 0.11	3.89 ± 0.11	11.4 ± 0.1	12.6 ± 0.4	0.9 ± 0.1	0.08 ± 0.06	1.63 ± 1.27	1.91 ± 1.48
UGC12591	450 ± 47	3.81 ± 0.11	3.82 ± 0.11	11.6 ± 0.1	14.0 ± 0.8	0.9 ± 0.1	0.01 ± 0.01	0.18 ± 0.23	0.19 ± 0.24
UGC12811	346 ± 24	3.83 ± 0.11	3.88 ± 0.11	11.6 ± 0.2	12.8 ± 0.2	0.9 ± 0.1	0.06 ± 0.03	1.15 ± 0.74	1.29 ± 0.81

relatively small black holes (e.g. Kormendy & Richstone 1995), and weak AGN feedback. Conversely, massive elliptical galaxies mostly know about major mergers and strong AGN feedback, which can drastically inhibit stellar growth and move these galaxies toward the falling branch of the SHMR (see Posti & Fall 2021 for further discussion of this picture).

Another interesting aspect of this evolutionary picture for massive spirals is their high overall efficiency in converting available baryons into stars. Galaxies in our sample typically have very high stellar fractions $f_* = f_M/f_b \simeq 0.3$ – 0.9 , often referred to as ‘global star formation efficiencies’. In contrast, L_* galaxies ($M_h \simeq 10^{12} M_\odot$), which are usually considered to be at the maximum star formation efficiency (Wechsler & Tinker 2018), typically only have $f_* \simeq 0.2$ – 0.3 . More massive elliptical and lenticular galaxies have even lower baryon conversion efficiencies. Furthermore, the fraction of baryons in massive discs is also extremely high, compared to lower mass discs and to spheroids. If, in addition to the stellar fraction f_* , we consider also the fraction of atomic gas $f_{\text{at}} = 1.36 f_{\text{HI}}$, of molecular gas f_{mol} (for example through the $M_{\text{HI}} - M_{\text{H}_2}$ relation; Catinella et al. 2018), and of ionized gas in the hot CGM $f_{\text{ion}} \simeq 0.1$ – $0.3 f_b M_h$ (e.g. Bregman et al. 2018), we obtain a total baryonic fraction $f_{\text{bar}} = f_* + f_{\text{at}} + f_{\text{mol}} + f_{\text{ion}} \sim 1$ for most galaxies in our sample. In other words, consistent with the findings by Posti et al. (2019a), we confirm that the most massive disc galaxies have remarkably little, if any, missing baryons.

Finally, our work indicates that baryons in discs retain a large fraction of the halo specific angular momentum, i.e. $f_{j,\text{bar}} \simeq 1$, independent of mass. Such a behavior was already predicted by early models of disc formation on the basis of simple conservation arguments, starting with Fall & Efstathiou (1980) and then adopted in essentially all analytical and semi-analytical models of galaxy formation (see also Dalcanton, Spergel & Summers 1997; Mo, Mao & White 1998, and many subsequent papers). We do not yet have a full understanding of this noteworthy result ($f_j \simeq 1$) because there are several physical processes that can change the specific angular momentum of baryons over galactic lifetimes (e.g. Romanowsky & Fall 2012; DeFelippis et al. 2017). We remark, however, that smooth inflow of gas from a gradually settling hot halo does promote the

conservation of specific angular momentum (Hafen et al. 2022). It is also worth noting that $f_* \simeq 1$ for massive spiral galaxies makes the apparent conservation of j_{bar} less puzzling: if most baryons are in the disc, there is then little circumgalactic medium in which to hide additional mass and angular momentum.

6 SUMMARY AND CONCLUSIONS

In this paper, we studied the dark matter halos and the main scaling relations of some of the most massive spiral galaxies in the local Universe. These discs have stellar masses $M_* > 10^{11} M_\odot$, are relatively gas-rich and have typical outer rotation velocities that approach or exceed 300 km s^{-1} . This is probably the most complete sample of very massive spiral galaxies with H I interferometric data that will be available for the next decade. Taking advantage of our new VLA H I data, together with other archival H I data, we derived extended rotation curves through 3D kinematical modelling for a sample of 15 massive galaxies. We then obtained constraints on their dark matter halos by using a MCMC approach to decompose their rotation curves into the contribution of stars, cold gas, and dark matter halo. We used the results from our dynamical modelling to build the two most important scaling relations for discs, namely the Tully–Fisher relation (M – V) and the Fall relation (j – M), in both their stellar and baryonic versions. Finally, we derived the stellar-to-halo mass relation (SHMR, e.g. M_* vs M_h) and we investigated how the stellar and baryonic-to-halo specific angular momentum ratios vary as functions of stellar and halo masses.

Our investigation reinforces recent findings that massive discs lie on the high-mass ends of both the Tully–Fisher and the Fall relations. These relations appear to be unbroken power laws spanning roughly five orders of magnitude in mass, from dwarf galaxies ($M_* \sim 10^7 M_\odot$) to the most massive spiral galaxies ($M_* \sim 10^{12} M_\odot$). We also show that the ratio $f_M \equiv M_*/M_h$ increases monotonically with mass and does not turn over above $M_* \simeq 5 \times 10^{10}$, in sharp contrast with widely-used SHMRs from abundance matching. Finally, we showed that the ratio between specific angular momentum of baryons and halos ($f_{j,\text{bar}} \equiv j_{\text{bar}}/j_h$) is close to unity not only for massive spiral galaxies, but for discs in general, with little or no dependence on

galaxy mass. This is a remarkable vindication of the basic premise, adopted in early models of galaxy formation, that galactic discs have approximately the same specific angular momentum as their surrounding dark matter halos.

This work demonstrates that discs, like the dark matter halos they live in, are a fully scaleable population of objects up to the very highest masses. Our results show that massive spirals are the most efficient galaxies in turning gas into stars in the Universe and that they have very few missing baryons. We also highlight how the evolutionary paths of discs and spheroids must diverge above a certain mass ($M_{\star} \simeq 10^{10.7} M_{\odot}$). Strong AGN feedback and/or major mergers most likely are responsible for this divergence. While spheroids grow mostly through episodes of merging and AGN feedback, massive discs grow in near isolation through star formation fed by smooth accretion from their halos, without experiencing disrupting events like major mergers and/or strong AGN feedback.

ACKNOWLEDGEMENTS

The authors thank T. Oosterloo, K. Spekkens, and T. van der Hulst for providing reduced H I data of some archival galaxies. EMDT was supported by the US National Science Foundation under grant 1616177 and by the European Research Council (ERC) under grant agreement no. 101040751. LP acknowledges support from the ERC under the European Union Horizon 2020 research and innovation program (grant agreement No. 834148). MPH acknowledges support from NSF/AST-1714828 and grants from the Brinson Foundation. UL acknowledges support from project PID2020-114414GB-I00, financed by MCIN/AEI/10.13039/501100011033, from project P20_00334 financed by the Junta de Andalucía, and from FEDER/Junta de Andalucía-Consejería de Transformación Económica, Industria, Conocimiento y Universidades/Proyecto A-FQM-510-UGR20. Data analysed in this work include multiband images from WISE, Legacy, and Pan-STARRS surveys and spectroscopic datacubes from MaNGA and CALIFA surveys. This research made use of Photutils, an ASTROPY package for detection and photometry of astronomical sources. This work relied on the NASA/IPAC Extragalactic Database, operated by the Jet Propulsion Laboratory, California Institute of Technology, under contract with NASA.

DATA AVAILABILITY

The data underlying this article will be shared on reasonable request to the corresponding author.

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SUPPORTING INFORMATION

Supplementary data are available at *MNRAS* online.

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