# Supplementary material: Bubble connectivity in experimentally-sheared crystal-bearing silicic melts 

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## 1. Methods

The experiments consisted in three main phases: (i) synthesis of a crystal-bearing hydrated glass by melt hydration in an internally-heated pressure vessel and mixing of the obtained hydrated glass with plagioclase crystals, (ii) $\mathrm{H}_{2} \mathrm{O}$-bubble formation by decompression in the Paterson-type apparatus, and (iii) subsequent deformation in simple shear of the three-phase magma.

### 1.1. Experimental methods

### 1.1.1. Synthesis of crystal-bearing hydrated glasses

The anhydrous starting glass is a haplogranite (HPG8, prepared by Schott AG, Germany) with the eutectic composition of the quartz-albite-orthoclase system [Holtz et al., 1992; composition in wt\%: 78.6 $\mathrm{SiO}_{2}, 12.5 \mathrm{Al}_{2} \mathrm{O}_{3}, 4.6 \mathrm{Na}_{2} \mathrm{O}, 4.2 \mathrm{~K}_{2} \mathrm{O}$ ). About 10 g of the powdered ( $<90 \mu \mathrm{~m}$ ) anhydrous HPG8 glass was mixed with either about 1 g or 0.5 g deionized $\mathrm{H}_{2} \mathrm{O}$, and sealed in $20-\mathrm{mm}$ diameter and $30-\mathrm{mm}$ long Au capsules. The HPG8 hydrations were performed in

[^0]internally-heated pressure vessels pressurized with argon (at ISTO) at $T$ of 750 and $950^{\circ} \mathrm{C}$ and $P$ of 400 MPa (for the capsules containing $1 \mathrm{~g} \mathrm{H}_{2} \mathrm{O}$ ) and $P$ of 170 MPa (for the capsules containing $0.5 \mathrm{~g} \mathrm{H}_{2} \mathrm{O}$ ). The $\mathrm{H}_{2} \mathrm{O}$ contents introduced in the capsules were enough to ensure $\mathrm{H}_{2} \mathrm{O}$ solubilities at $P$ of 400 MPa and $170 \mathrm{MPa}\left(950^{\circ} \mathrm{C}\right)$ according to the $\mathrm{H}_{2} \mathrm{O}$ solubility model of Newman and Lowenstern [2002], i.e. 9.6 and $5.0 \mathrm{wt} \% \mathrm{H}_{2} \mathrm{O}$, respectively. Hydration durations were 48 to 96 h , which is long enough to homogenize $\mathrm{H}_{2} \mathrm{O}$ by diffusion in the HPG8 glass powder, according to Zhang and Behrens [2000]. The samples were isobarically quenched by shutting down the furnace, in order to avoid $\mathrm{H}_{2} \mathrm{O}$ exsolution from the melt. The recovered hydrated HPG8 glasses were ground in an agate mechanical grinder to obtain a $\sim 20-\mu \mathrm{m}$ grain size powder, to which plagioclase crystals were added. We purchased commercially a plagioclase block of labradorite (anorthite content of 50 to $70 \mathrm{~mol} \%$ ) whose composition was tested for chemical resistance at the contact of the HPG8 hydrated melt under the elected run conditions. The labradorite block was reduced into pieces using a high-voltage pulsed power fragmentation apparatus (Selfrag, at BRGM, Orléans, France). The main advantage of the Selfrag is to crush rocks at the grain joints, so that we were expecting more or less elongated bits,


Supplementary Figure S1. The $50-90 \mu \mathrm{~m}$ fraction size of the plagioclase crystals.
i.e. resembling the natural plagioclase shapes. The recovered fragments were sieved to $50-90 \mu \mathrm{~m}$ (Supplementary Figure S1), before manual mixing with the hydrated HPG8 glass powder following different weight proportions. Very minor amounts of crystals other than plagioclase (presumably $\mathrm{Fe}-\mathrm{Ti}$ oxides and pyroxenes) have been found in the fragments, likely coming from mineral inclusions trapped in the labradorite block. Recalculated to volume proportions using a 2.7 density for labradorite, four series based on their crystal contents ( $\Phi_{\text {c_melt_3D }}$ ) have been chosen: $0,21,50$, and $70 \mathrm{vol} \%$.

### 1.1.2. Synthesis of bubble-bearing magmas

About $1.6-2.0 \mathrm{~g}$ of the crystal-glass mixtures were sealed in $14-\mathrm{mm}$ diameter and $12-\mathrm{mm}$ long Cu capsules in order to prevent $\mathrm{H}_{2} \mathrm{O}$ loss. The capsules were sandwiched between alumina spacers, alumina and zirconia pistons, and the whole assembly was coated by an iron jacket (Figure 1b). The sample column was placed at the hot spot of the internal Mo-furnace of the gas-medium (argon) Paterson rig [Paterson and Olgaard, 2000; Australian Scientific Instruments Pty Ltd, at ISTO; Figure 1a]. The samples were (i) pressurized to 240 MPa , (ii) heated to $850{ }^{\circ} \mathrm{C}$ (pressure will reach 300 MPa ) at a rate of $10^{\circ} \mathrm{C} / \mathrm{min}$ and maintained during 15 min for thermal equilibration, then (iv) decompressed to 50 MPa within 9 to 20 min in order to generate $\mathrm{H}_{2} \mathrm{O}$ bubble nucleation, (v) maintained for 45 min to let bubbles grow, and (vi) cooled to $650{ }^{\circ} \mathrm{C}$ (crystal-free samples) or $750{ }^{\circ} \mathrm{C}$ (crystal-bearing
samples), in order to allow further deformation without inconvenient jacket breakage, followed by a 15min dwell for thermal equilibration (Figure 1c). In the Paterson rig, all samples were decompressed from 300 MPa (maximum pressure allowed in the Paterson rig), so that the samples pre-hydrated at 400 MPa ( $\sim 9.6 \mathrm{wt} \% \mathrm{H}_{2} \mathrm{O}$ ) nucleated between 300 and 50 MPa [possibly during annealing at 300 MPa , although the high supersaturations $>100 \mathrm{MPa}$ required for homogeneous nucleation in silica-rich melts would favour nucleation at pressure below 300 MPa ; MourtadaBonnefoi and Laporte, 2002]. The samples hydrated to $5.0 \mathrm{wt} \% \mathrm{H}_{2} \mathrm{O}$ nucleated at pressure between 170 and 50 MPa .

### 1.1.3. Torsion experiments

Keeping the experimental setup as it was after decompression, deformation in right-lateral simple shear was carried out at $T$ of $650^{\circ} \mathrm{C}$ (crystal-free samples) or $750{ }^{\circ} \mathrm{C}, P$ of 50 MPa , and shear rate $\gamma_{r}$ of $2 \times 10^{-4} \mathrm{~s}^{-1}$. Torsion durations were 1 or 2 h , which led to bulk finite shear $\gamma$ of 1 and 2 , respectively, [see Paterson and Olgaard, 2000, for $\gamma$ calculation]; note that in torsion, the sample centre experiences zero torque and, therefore, zero strain; both strain and strain rate increase radially toward the sample exterior. Temperature, pressure, shear stress and angular displacement were live recorded on a computer. The experiment was ended by relaxing the stress, followed by an isobaric quench (shut of the furnace while maintaining 50 MPa confining pressure) at a rate of $\sim 40^{\circ} \mathrm{C} / \mathrm{min}$ from 750 to $200^{\circ} \mathrm{C}$. According to Mader et al. [2013], the relaxation time $(\lambda)$ of a bubble writes as: $\lambda=\left(a \times \eta_{\text {melt }}\right) / \sigma$, where $a$ is the bubble's equivalent spherical radius, $\eta_{\text {melt }}$ is the viscosity of the hydrated melt, and $\sigma$ is the surface tension at the bubble-liquid interface. Considering $a=10$ and $100 \mu \mathrm{~m}$ (from the sample analyses), $\eta_{\text {melt }}=10^{6.3} \mathrm{~Pa} \cdot \mathrm{~s}$ [HPG8 melt with $2.9 \mathrm{wt} \% \mathrm{H}_{2} \mathrm{O}$ at 50 MPa and $750^{\circ} \mathrm{C}$; Hess and Dingwell, 1996], and $\sigma=0.2 \mathrm{~N} / \mathrm{m}$ at 50 MPa [Bagdassarov et al., 2000], $\lambda$ would be about 2 and 17 min , respectively. At $700^{\circ} \mathrm{C}, \eta_{\text {melt }}=10^{6.9} \mathrm{~Pa} \cdot \mathrm{~s}$ and $\lambda$ becomes 7 and 66 min for bubble radius of 10 and $100 \mu \mathrm{~m}$, respectively. During quenching, about 42 s are spent between 750 and $700{ }^{\circ} \mathrm{C}$, so that we infer that in our experiments, the small $10-\mu$ m radius bubbles fully relaxed (returned to sphericity), whereas the larger $100-\mu \mathrm{m}$ radius bubbles experienced limited relaxation during quenching. After experiment,


Supplementary Figure S2. After run sample preparation for analyses. (a) Cutting, (b) polish section with one outer piece of the sample, and (c) bore of a $3-\mathrm{mm}$ cylinder in the middle piece.
the sample column was extracted from the vessel and the extent of deformation was verified by the progress of the pen-markers between the non-deformed (piston) and deformed (sample) parts. The iron jacket was removed to release the Cu -capsule containing the sample. Note that shear stress could not be determined in-situ during deformation due to the low viscosity (high temperature) of the samples, so that bulk viscosity could not be measured.

### 1.2. Analytical methods

### 1.2.1. Microstructural analysis

After experiment, the Cu capsule containing the sample was cut following two sections parallel to the shear plane, in order to expose their longitudinal tangential surfaces, which represent the planes of maximum shear strain [Paterson and Olgaard, 2000] (Supplementary Figure S2a). One of the two sections was placed in epoxy, polished, and carbon coated for two-dimensional (2D) observations using a scanning electron microscope (SEM; Merlin Compact Zeiss at ISTO) (Supplementary Figure S2b).

The sample polished sections being about 510 mm long by $10-15 \mathrm{~mm}$ wide and often showing microtextural heterogeneities, the sample analysis was performed by processing 5 to 10 thumbnail images that covered the whole section. The SEM images were segmented using the SPO2003 image-processing software [Launeau and Robin, 1996, Launeau and Cruden, 1998], in order to determine the average 2D bubble and crystal contents
(accuracy of $\pm 3$ area\% determined on repeated measurements), bubble and crystal sizes, shapes, and orientations (following the method of intercepts; [Launeau and Robin, 1996], and bubble and crystal number densities, as follows:

- Crystal-free bubble content: $\Phi_{\mathrm{b} \_ \text {melt_2D }}=$ (bubble area)/(bubble area + glass area) $\times$ 100;
- 2D-bulk porosity: $\Phi_{\mathrm{b} \_ \text {bulk_2D }}=$ (bubble area)/(bubble area + glass area + crystal area) $\times 100$;
- 2D-bubble-free crystal content: $\Phi_{\text {c_melt_2D }}=$ (crystal area)/(crystal area + glass area) $\times$ 100;
- 2D-bulk crystal content: $\Phi_{\text {c_bulk_2D }}=$ (crystal area)/(bubble area + glass area + crystal area) $\times 100$;
- 2D-bulk glass content: $\Phi_{\mathrm{g} \_ \text {bulk_2D }}=$ glass area/ (bubble area + glass area + crystal area) $\times 100$;
- Crystal-free areal bubble number density: BND $=$ (number of bubbles) $/$ (glass area).
- Bubble-free areal crystal number density: CND = (number of crystals) $/$ (glass area).
- Bubble long and short axes; bubble eccentricity: $R=$ (long axis) / (short axis); the radius (a) equivalent to the bubble surface; bubble orientation to the horizontal $\left(\theta_{b}\right)$.


### 1.2.2. $X$-ray Computed Tomography (XCT)

After the removal of the two longitudinal tangential sections for the 2D analysis, the sample rest was bored perpendicularly to the shear plane ( 0 strain
in centre; Supplementary Figure S2c) in order to get an oriented 3-mm core sample for three-dimensional (3D) analysis using XCT (Phoenix NanoTOM at ISTO). The XCT images were reconstructed using a Phoenix 3D software with a voxel resolution of $1.4-\mu \mathrm{m}$ side. A qualitative analysis of the whole core sample was performed in order to segment the glass+crystal matrix, the isolated bubbles, and the bubbles connected to the outside of the core sample, using the commercial software VGStudio Max. Smaller sample volumes (cubes of 600 and $1400-\mu \mathrm{m}$ side) were defined to qualify bubble size and spatial distribution, as well as to quantify the 3D bulk porosity ( $\Phi_{\text {b_bulk_3D }}$ ) and the volume content of bubbles connected to the sample border ( $\Phi_{\mathrm{b}} \mathrm{connnect}^{2 \mathrm{D}}$ ), using the commercial software Blob3D. The porosity measurements, $\Phi_{\mathrm{b} \_ \text {bulk_3D }}$ and $\Phi_{\mathrm{b} \text { _connect_3D }}$, were determined with an accuracy of $\pm 3 \mathrm{vol} \%$. Because the small size of the experimental samples precludes porosity 3D measurement iterations, the assumption made here is that the volumes on which the measurements have been made are representative of the whole experimental sample.

### 1.2.3. Glass $\mathrm{H}_{2} \mathrm{O}$ contents

The $\mathrm{H}_{2} \mathrm{O}$ contents of the starting hydrated glasses were checked using an elemental analyser (ThermoFlash2000 at ISTO), given with a precision of $\pm 0.15 \mathrm{wt} \%$. The results confirmed the $\mathrm{H}_{2} \mathrm{O}$ solubility data from [Newman and Lowenstern, 2002], i.e. $\mathrm{H}_{2} \mathrm{O}$ contents of 9 to $10 \mathrm{wt} \%$ for the $400-\mathrm{MPa}$ hydrations and $\sim 5 \mathrm{wt} \%$ for the $170-\mathrm{MPa}$ hydrations. As the elemental analyser is a destructive method (sample pyrolyze), the $\mathrm{H}_{2} \mathrm{O}$ contents of the residual glasses from the run products were analysed using an electron microprobe (EMP; Cameca SX Five at ISTO) following the "by-difference" method of Devine et al. [1995], and using HPG8 glass standards with known $\mathrm{H}_{2} \mathrm{O}$ contents [samples from Martel et al., 2000]. The analysed elements were $\mathrm{Si}, \mathrm{Al}, \mathrm{Ca}, \mathrm{Na}, \mathrm{K}$, with alkalis analysed first, in order to minimize loss under the electron beam. The EMP conditions were set to an acceleration voltage of 15 kV , a beam current of 6 nA , peak/background counting times of $10 / 5 \mathrm{~s}$ for all elements, and a defocussed beam of $10 \times 10 \mu \mathrm{~m}$ size. The analytical errors on major elements were calculated at $\sim 1 \%$ (relative) for $\mathrm{SiO}_{2}, \mathrm{Al}_{2} \mathrm{O}_{3}$ and CaO , and $5 \%$ for $\mathrm{Na}_{2} \mathrm{O}$ and $\mathrm{K}_{2} \mathrm{O}$, and $\pm 0.7 \mathrm{wt} \%$ on the $\mathrm{H}_{2} \mathrm{O}$ content.

Some of the residual glasses were double-checked by microRaman spectroscopy. The Andor Shamrock 500 i spectrometer is coupled with a Nikon ECLIPSE Ni-U microscope uses a long working distance Nikon objective ( $100 \times$, numerical aperture of 0.8 ), which allows lateral resolution of $1-2 \mu \mathrm{~m}^{2}$. A monochromatic 532 nm Coherent Genesis MX SLM laser was used as exciting source (output laser power was set to 300 mW ). The 1200 lines/mm grating was used, providing two spectral windows spanning 200 to $1500 \mathrm{~cm}^{-1}$ (silicate network) and 2895 to $3800 \mathrm{~cm}^{-1}$ ( OH stretching region). For each analysis, the acquisition time was 60 s. In order to determine $\mathrm{H}_{2} \mathrm{O}$ content, the HPG8 glass standards were measured in the same analytical conditions as the samples. The Raman spectra were proceeded following the method of Behrens et al. [2006].

### 1.3. Calculations

### 1.3.1. Gas fraction

The gas fraction equation of Jaupart and Allegre [1991] calculates the gas volume ( $\alpha_{\text {melt }}$ ) resulting from degassing of a $\mathrm{H}_{2} \mathrm{O}$-saturated melt in closedsystem. The equation writes as follows:

$$
\alpha_{\text {melt }}=1 /\left\{1+\rho_{\text {gas }} /\left[\left(\mathrm{Cw}_{i}-\mathrm{Cw}_{f}\right) \times \rho_{\mathrm{liq}}\right]\right\} \times 100
$$

where $\rho_{\text {gas }}$ is the $\mathrm{H}_{2} \mathrm{O}$ density at $T$ and final $P$ calculated after Burnham et al. [1969], $\rho_{\text {liq }}$ is the melt density taken as $2400 \mathrm{~kg} / \mathrm{m}^{3}, \mathrm{Cw}_{i}$ and $\mathrm{Cw}_{f}$ are the $\mathrm{H}_{2} \mathrm{O}$ solubilities at initial and final pressures, respectively, calculated after Newman and Lowenstern [2002]. The uncertainty associated with the $\alpha_{\text {melt }}$ calculation mostly depends on the precision of the melt $\mathrm{H}_{2} \mathrm{O}$ contents $\left(\mathrm{Cw}_{i}\right.$ and $\left.\mathrm{Cw}_{f}\right)$. Assuming an uncertainty of $\pm 0.7 \mathrm{wt} \%$ on the EMP "by-difference" $\mathrm{H}_{2} \mathrm{O}$ measurements suggests uncertainties of $\pm 3 \mathrm{vol} \%$ on $\alpha_{\text {melt }}$ calculations.

### 1.3.2. Bulk viscosity

The bulk viscosity ( $\eta_{\text {bulk }}$ ) of our samples were calculated using the Equation (3.2) of Truby et al. [2015] that gives the relative viscosity ( $\eta_{r}$, with $\eta_{r}=$ $\eta_{\text {bulk }} / \eta_{\text {melt }}$ ) of a three-phase suspension of bubbles and crystals in a Newtonian liquid undergoing steady flow. The model adopts an "effective medium" approach in which the bubbly liquid is treated as a continuous medium which suspends the crystals. The model is valid for a low bubble capillary number (Ca)
regime. $C a$ describes the ratio of the viscous stress to the restoring stress and writes as follows: $C a=$ $\left(\eta_{\text {melt }} \times \gamma_{r}\right) /(\sigma / a)$, where $a$ is the bubble's equivalent spherical radius. For $\gamma_{r}$ of $2 \times 10^{-4} \mathrm{~s}^{-1}$, bubble radius of 10 and $100 \mu \mathrm{~m}, \sigma$ of $0.2 \mathrm{~N} / \mathrm{m}$ [Bagdassarov et al., 2000], and $\eta_{\text {melt }}$ of $10^{6.3} \mathrm{~Pa} \cdot \mathrm{~s}$ (HPG8 liquid with 2.9 $\mathrm{wt} \% \mathrm{H}_{2} \mathrm{O}$ at $750^{\circ} \mathrm{C}$; [Hess and Dingwell, 1996], Ca is
$\sim 0.02$ and 0.2 , respectively, which satisfies the low $C a$ regime $(C a<1)$ required for the viscosity calculation. The equation writes:

$$
\begin{align*}
\eta_{r}= & \left(1-\Phi_{\mathrm{b} \_ \text {melt_3D }} / 100\right)^{-1} \\
& \times\left(1-\Phi_{\mathrm{c} \_ \text {bulk_3D}} / \Phi_{\max }\right)^{-2} \tag{2}
\end{align*}
$$

where $\Phi_{\max }$ is the particle maximum packing of $66 \mathrm{vol} \%$ [Truby et al., 2015].


Supplementary Figure S3. 3D bubble size distributions.


Supplementary Figure S4. Crystal breakage. The red squares highlight crystal breakage in the undeformed $(\gamma=0)$ sample containing $50 \mathrm{vol} \%$ crystals (bottom left) and associated crystal size histogram showing a large population of $0-20 \mu \mathrm{~m}$ diameter crystals (bottom right), in contrast to non-broken crystals in the undeformed sample containing $10 \mathrm{vol} \%$ crystals (upper left; same scale bar) associated to a lower frequency of $0-20 \mu \mathrm{~m}$ crystals (upper right).

## References

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