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An empirical relation between velocity, mass discharge rate and vent area for normal through paroxysmal eruptions at Stromboli

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17 Abstract

Based on published and new data for explosive events at Stromboli (Italy), we propose an 18 19 empirical relation that links mass discharge rate (MDR) and at-vent gas jet velocity (G_v). We use 65 simultaneous measurements of MDR and G_{ν} and find two trends in both the cross-20 correlation and rank order statistics. Cross-correlation gives a power law relation: MDR =21 $10^{(0.015G_v+2.434)}$ kg/s, R²=0.81, and applies to ash-dominated emissions. Combining this 22 relation with the conservation of mass equation allows at-vent plume density and/or vent area 23 to be derived from MDR = $G_{\nu} \rho A$, ρ being plume density and A being vent cross-sectional area. 24 We find that while a vent radius of 2 m and plume density of 0.35 kg/m³ fits with the "normal" 25 activity at Stromboli, a 290×2.5 m vent area likely feeds a 10 kg/m³ jet during paroxysmal 26 activity. Initial tests on available data shows promise in extending the correlation beyond 27 Stromboli and/or to events with higher MDR ($>10^7$ kg/s). However, the exact relation will 28 depend on magma composition, temperature and volatile content, as well as conduit radius and 29 vent overpressure. 30

31 **Keywords:** Thermal imagery, Eruption intensity, Mass Discharge Rate, Particle Velocity,

32 Gas Jet Velocity, Stromboli

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43 **Conflicts of interest/Competing interests**

44 The authors declare no conflicts nor competing interest

45 Introduction

Mass Discharge Rate (MDR, kg/s) is commonly used to classify the "explosiveness" of a 46 volcanic eruption, especially through the Volcanic Explosivity Index (Newhall and Self, 1982). 47 Time-averaged MDR can be estimated from the total erupted mass divided by eruption duration 48 (e.g., Mason et al. 2004; Bryan et al. 2010; Pyle, 2015). Peak MDR has also been derived from 49 maximum plume height, as MDR is proportional to plume height to the power-of-four for 50 Vulcanian-to-Plinian eruptions (Wilson et al. 1978). Geophysical signals, such as seismicity, 51 52 infrasound and Doppler radar (e.g., Brodsky et al. 1999; Freret-Lorgeril et al. 2018; Perttu et al., 2020; Maki et al. 2021), as well as lightning intensity rates (Van Eaton et al., 2016), have 53 also been tested as a proxy for MDR. 54

We propose a further option for deriving MDR from thermal or visible video using an 55 56 empirical relation between MDR and gas jet velocity (G_v) . We initially explore this relation for explosive events at Stromboli (Italy) where there is excellent constraint on the plumbing system 57 (e.g., Bertagnini et al. 1999, 2013; Métrich et al. 2005, 2010, 2021), explosion source 58 mechanisms (e.g., Chouet et al. 1999; Ripepe and Gordeev 1999; Ripepe et al. 2001) and 59 emission dynamics (e.g., Patrick et al. 2007; Scharff et al. 2008; Gurioli et al. 2013). As a result 60 61 data are available to test a relation between MDR and G_{ν} . Stromboli also displays a range of explosive activity, which are commonly separated into three groups (Barberi et al. 1993). These 62 are, in order of increasing magnitude: normal, major and paroxysmal. Named by Barberi et al. 63 (1993) to describe the typical explosive activity that occurs at Stromboli, "normal" eruptions 64 send 10–10⁴ kg of bombs, gas and ash to a height of a few 10s to a few 100 m typically \sim 10 65 times an hour (Harris and Ripepe 2007; Patrick et al. 2007; Harris et al. 2013). Major eruptions 66 can occur several times a year, involve $10^5 - 10^7$ kg of bombs and ash, and send plumes to around 67 a kilometre in height (Gurioli et al. 2013). Paroxysms are rarer, with four having occurred 68 69 between 2003 and 2019, and form buoyant ash-rich plumes that ascend to several kilometres, and involve $>10^8$ kg (Rosi et al., 2006; Pistolesi et al. 2011; Giordano and De Astis 2020). 70

The wealth of data for explosions at Stromboli makes it an ideal location to test relations between a variety of eruption source terms (e.g., MDR and vent area) and plume ascent parameters (e.g., emission velocity and plume ascent velocity). We thus use Stromboli to explore an empirical relation between at-vent gas velocity and MDR using published and new datasets for which the two parameters can be simultaneously derived.

76 Method

We examined 65 eruptive events (59 normal, two major and four paroxysmal) for which suitable data were available (Table 1). Harris et al. (2013) obtained the mass (*m*) of 21 normal eruptions from thermal video using the amount of energy lost by the bomb field during cooling.

80	However, the duration (t) for these events was not assessed, so we revisited the data to obtain
81	emission duration so that time-averaged MDR could be obtained from m/t . Duration was taken
82	as the time between the first appearance of the plume and the last bomb to exit the vent. Videos
83	used were recorded at 30 frames per second, and in the compressed data 10 frames were
84	equivalent to one second of recording. The uncertainty is five frames (0.5 s), so that
85	(considering the same uncertainty for the start and end of the event) error on duration is ± 1 s.
86	We also used the mass, particle ejection velocity and duration 31 eruptions as obtained by
87	Bombrun et al. (2015) through particle tracking to convert to time-averaged MDR. In addition,
88	we included MDR and gas ejection velocities for transient ash-dominated normal eruptions at
89	Stromboli as derived from thermal and visible imagery by Tournigand et al. (2017).
90	Mass discharge rates for major and paroxysmal eruptions at Stromboli were taken from the
91	literature as follows:
92	• For the 8 and 24 November 2009 major eruptions MDR was taken from Gurioli et al.
93	(2013);
94	• For the 2003 and 2007 paroxysms, we used the MDR of Rosi et al. (2006) and Pistolesi
95	et al. (2011), respectively;
96	• MDR for the July and August 2019 paroxysms were calculated from maximum plume
97	height by Giordano and De Astis (2020) following the equation of Mastin et al. (2009).
98	A theoretical relation between ballistic exit velocity (Bv) and gas exit velocity (Gv) was
99	proposed by Steinberg and Babenko (1978). In this relation, Gv represents the speed of the gas
100	to which the finest particles are coupled, and Bv represents the velocity of particles large enough
101	to be affected by drag, as tested on and applied to normal eruptions at Stromboli by Ripepe et
102	al. (1993) and Harris et al. (2012b).

Ballistic velocities are obtained either through particle tracking and given by Harris et al. (2013) and Bombrun et al. (2015) for normal explosions, or ballistic trajectory modeling for major (Gurioli, Colo, et al., 2013; Pioli et al., 2014) and paroxysmal events (Rosi et al., 2006; Pistolesi et al., 2011; Andronico et al., 2013; Giordano & De Astis, 2020). We convert these ballistic velocities (B_v) to gas jet velocities (G_v^b) using equation (8) of Harris et al. (2012b):

108

$$G_{\nu}^{b} = 1.41 \times B_{\nu} + 15.3 \tag{1}$$

109 This relation is set for explosions at Stromboli and correlates well with directly measured gas 110 ejection velocities (Fig. 1). The literature-derived database is given in Table 1, and our 111 calculated MDR data are given in Table 2.

112 **Results**

The 21 normal explosions at Stromboli recorded by Harris et al. (2013) lasted between 3 and 113 114 28 seconds, giving MDRs ranging from 32 to 800 kg/s (Table 2). Eruptions from vent NE1 lasted longer (average of 18 s) than eruptions from NE2 (average of 6 s). This leads to a wider 115 range of MDR values for events at NE2 than NE1 (Fig. 2a). In Figure 2a, data from Bombrun 116 et al. (2015) fall in a cluster of low MDR and high gas velocities (150–250 m/s, MDR $< 10^4$ 117 118 kg/s), and data from Tournigand et al. (2017) have high MDR with low gas velocities (<150 m/s, MDR $\geq 10^4$ kg/s). MDR for these normal explosions show correlations with gas velocity 119 120 with an R² of between 0.5 and 0.83 depending on the data set used (Fig. 2a).

MDR for the major and paroxysmal events range between 10⁴ and 10⁷ kg/s, with gas jet velocities in the range 142–297 m/s (Table 1). The relation between MDR and gas velocity for the six major and paroxysmal explosions shows a positive, linear correlation with an R² of 0.79. Eruption magnitudes have a power-law dependence (Pyle, 1998). This can be expressed as a

125 rank order plot, as obtained by sorting the values from the highest to the lowest (Sornette et al.

126 1996). This method can be used to constrain whether the dataset is homogeneous (cf. Schneider

and Barbera, 1998) within a single volcanic system. The rank order plot for our Stromboli data 127 128 shows two trends representing two different populations (Fig. 3). These two populations are apparent in the rank order statistics for both gas velocity and MDR and involve a first group of 129 low gas velocity and MDR, and a second group of high gas velocity and MDR. We thus define 130 two main populations and treat them separately. The first involves ballistic-dominated normal 131 emissions (Fig. 2a). The second includes all major and paroxysmal events, plus one ash-132 133 dominated normal eruption, this population being of ash-rich emissions involving plume ascent dominated by buoyancy (Fig. 2b) 134

135 **Discussion**

The two trends apparent for Stromboli in the cross-correlation (Fig. 2) and rank order (Fig. 3) 136 plots result from the different plume types considered and differences in their associated ascent 137 dynamics. Normal explosions at Stromboli are associated with slug flow in the conduit 138 (Gonnermann and Manga, 2012) and are characterized by very low levels of fragmentation to 139 140 produce bomb-dominated plumes with particles that follow ballistic trajectories (e.g., Chouet et al. 1974; Patrick et al. 2007; Gurioli et al. 2013). In contrast, major and paroxysmal events 141 involve rapid ascent of magma coupled with a gas phase ascending from depths of 7–10 km 142 143 and are characterized by higher degrees of fragmentation (e.g., Bertagnini et al. 1999; Métrich et al. 2005, 2010, 2021; Pioli et al. 2014). The result is an ash-dominated plume whose ascent 144 145 is characterized by a longer steady convection-dominated phase (cf. Wilson and Self 1980; Rosi et al. 2006; Harris et al. 2008). 146

147 Cross-correlation using data for ballistic-dominated normal explosions at Stromboli gives a 148 relation between MDR and G_{ν} of (Fig. 2a, yellow regression line):

149

$$MDR = 10^{(0.003G_v + 1.933)} R^2 = 0.50 (2a)$$

150 Considering only a single vent improves the correlation, where the relation for vent NE1 (Fig.151 2a, blue regression line) is:

152
$$MDR = 10^{(0.004G_v+1.906)}$$
 $R^2 = 0.83$ (2b)
153 These two relations are consistent with differences in vent size, gas/particle ratio, crater

 $MDR - 10(0.004G_v + 1.906)$

geometry, overpressure and volatile content between craters and events. 154

Finally, the cross-correlation for ash-dominated normal, major and paroxysmal events gives 155

156
$$MDR = 10^{(0.015G_v + 2.434)}$$
 $R^2 = 0.81$ (3)

157 This is the black regression line of Figure 2b.

The next largest event at Stromboli? 158

Application of maximum likelihood statistics to our rank order plots (cf. Sornette et al. 1996; 159 Pyle 1998) can indicate the most probable MDR and gas velocity for the hypothetical, but next 160 161 largest, eruption not recorded in our data (i.e., an event larger than the 2003 paroxysm). On this basis an eruption at Stromboli larger than the 2003 paroxysm would have an MDR of $2.19 \times$ 162 10⁷ kg/s and a gas ejection velocity of 338 m/s. Our current data set for Stromboli is missing at 163 164 least two paroxysms, i.e., those of 1456 and 1930. Both have been described as being larger than the 2003 paroxysm (e.g., Rosi et al. 2006; Bertagnini et al. 2011; Métrich et al. 2021), but 165 both lack an assessment of MDR and G_{ν} . We thus speculate that the MDR and G_{ν} calculated 166 for the next largest eruption in our dataset are possibly representative of the 1456 and 1930 167 paroxysms. 168

Vent size during normal and paroxysmal activity 169

170 MDR is related to bulk average (V) velocity, gas-particle mixture density (ρ) and vent cross 171 sectional area, A:

172

$$MDR \approx \rho VA$$
 (4)

Given a vent radius typical for Stromboli, i.e., 2 m (Harris et al. 2012b), we use our range of 173 ejection velocities and MDR values to solve for mixture density. We find that the normal gas 174 and ballistic-dominated events fit with a cloud density of 0.35 kg/m³ (Fig. 2a). This corresponds 175

to the density of water vapor at 650 K. Instead, ash-dominated normal events fit with 10 kg/m³
(Fig. 2a). Note, that these values are for at-vent conditions and are hence in the gas-thrust region
of the jet before entrainment of air.

The lower and higher limits of the data set for major and paroxysmal eruptions can only be 179 reproduced with a cloud density of 10 and 2600 kg/m³, respectively (Fig. 2b). The latter density 180 is close to the dense-rock value of basaltic magma, and does not provide a realistic plume 181 density. For paroxysmal eruptions the conduit radius likely exceeds 2 m. Using the MDR and 182 G_{ν} for the July 2019 paroxysm (Table 1), with a cloud density of 10 kg/m³, gives a circular vent 183 radius of ~13 m. A 290 m long and 2.5 m wide source also provides a fit for the paroxysmal 184 events. This would represent an eruption from the entire length of a SW-NE trending dyke 185 underlying the crater terrace, and is consistent with emission from all three active craters during 186 187 a paroxysm (Rosi et al., 2006). It is also consistent with collapse of the crater terrace following paroxysms to create a continuous trench in place of the typical three-crater system that 188 189 characterizes Stromboli's crater terrace during normal activity (cf. Harris and Ripepe, 2007) and the ejection of meter-sized blocks of the "shattered shallow subvolcanic system" (Renzulli 190 et al., 2009). 191

We calculate the at-vent volume fraction of pyroclasts (f) within the plume using a simple mixture model:

$$\rho \approx f \times \rho_{pyroclast} + (1 - f) \times \rho_{gas}$$
⁽⁵⁾

An average pyroclast density ($\rho_{pyroclast}$) of ~800 kg/m³ (Pichavant et al. 2022), a gas density (ρ_{gas}) of 0.35 kg/m³ (Harris et al. 2013), and a plume density of 10 kg/m³ results in a mixture of ~1 % pyroclasts and ~99 % gas volumes (respectively ~97 % pyroclasts and ~3 % gas mass fraction). A low gas weight fraction indicates that the cloud was ejected out of the vent without any mixing with the atmosphere (Wilson and Self, 1980).

200 Towards a global predictive model for eruption intensity?

At-vent gas and particle velocities vary as a function of vent geometry, over-pressure, magma 201 temperature, volatile content, particle size and gas density (Steinberg and Babenko, 1978; 202 Woods and Bower, 1995). By restricting our consideration to a single system, we limit the 203 variation in volatile content, temperature, crater/vent geometry, pressure, ash/gas ratio, and gas 204 density. Our results for Stromboli indicate that, if eruption types and styles are considered 205 206 separately according to their dynamics, and measurements of mass eruption rate, gas velocity and particle velocity are available, then an empirical relation relating the three can be derived. 207 We assess whether this can be extended to other, higher magnitude systems by considering: 208

- 209
- Pinatubo 1991 (VEI = 6; based on the data from Simkin et al, 1981);
- 210
- Mt. St. Helens 1980 (VEI = 5; Venzke 2022);
- Fuego 2012 (VEI \leq 2; Venzke 2022);
- Sakurajima 2013 (VEI \leq 3; Venzke 2022).

For Fuego and Sakurajima we take the MDR and G_{ν} as derived from thermal and visible 213 imagery by Tournigand et al. (2017). For Pinatubo, an MDR ranging between 6.8×10^8 and 10^9 214 kg/s has been calculated from granulometry (Koyaguchi and Ohno 2001) and satellite data 215 (Koyaguchi and Tokuno 1993). MDR estimates for Mt. St. Helens range from an average of 2 216 $\times 10^7$ kg/s for the whole eruption (Carey and Sigurdsson, 1985; Pyle, 2015), to 2–6 $\times 10^9$ kg/s 217 for the initial lateral blast (Brodsky et al. 1999). In all cases, we use the full range. For Pinatubo 218 219 whether we calculate gas velocity using the at-vent decompressing jet model (6) or the freely 220 decompressing model (7) of Woods and Bower (1995) is debatable:

221
$$G_{\nu} = 0.95 \times (n_0 RT)^{1/2}$$
(6)

222
$$G_v = 1.85 \times (n_0 RT)^{1/2}$$
(7)

Here n_0 is the difference between melt inclusion volatile concentration (6.4–7 wt %, Rutherford 223 224 and Devine, 1996) and glass matrix average volatile concentration (1.45 wt.%, Hammer et al., 1999), *R* is the vapor-gas constant (461.5 J/kg K), and T is the magma temperature (1073 K). 225 The value we obtain is likely a maximum since experimental studies suggested disequilibrium 226 degassing for this eruption (Mangan and Sisson, 2000), which would delay nucleation and thus 227 decrease magma ascent rate and G_{ν} . For Mt. St. Helens we use the range of velocities for the 228 Plinian phase given by Carey and Sigurdsson (1985) and Woods and Bower (1995), i.e., 200-229 300 m/s. We use velocities as close as possible to the vent-leaving values, where the at-surface 230 231 decompression of the volcanic jet has the least impact (Woods and Bower, 1995) and where vent-leaving values can be compared between cases. 232

MDR values for Sakurajima, Pinatubo, and Mt. St. Helens are one-to-three orders of magnitude higher than those for Stromboli and Fuego at similar G_v (Fig. 4). However, the relationship between G_v and MDR remains linear and positive. This is consistent with the decompressing jet model of Woods and Bower (1995) for the emission dynamics of gas-particle mixtures, where variations in magma volatile content, over-pressure, vent geometry, and magma temperature account for the differences observed between each system (Fig. 4).

239 Conclusion

We derive an empirical relationship between gas jet velocity and MDR which applies to explosive events at Stromboli with VEI ranging from 0 to 3. At Stromboli, a network of continuously recording thermal cameras allows measurement of gas jet velocity (Delle Donne and Ripepe, 2012). This means that real-time measurements of G_v can potentially be converted to MDR for the two event types (ballistic and convective emissions) common at this wellmonitored site.

Extending the analysis to events with higher VEI suggest a wider applicability a linear relation between G_v and MDR. Our argument is thus for a database with simultaneous measurements

- of MDR and at-vent velocities for a variety of systems, allowing extension of this analysis.
- 249 Such data requires a video camera network targeting the vent, which is rarely possible. All the
- same, given the importance of MDR as a key source term in forward modeling (cf. Bonadonna
- et al. 2011), such a fast and straightforward empirical approach to potentially derive MDR in
- 252 near-real time shows promise.

253 **References**

- Andronico, D., Taddeucci, J., Cristaldi, A., Miraglia, L., Scarlato, P., & Gaeta, M. (2013). The 15
- 255 March 2007 paroxysm of Stromboli: video-image analysis, and textural and compositional
- 256 features of the erupted deposit. *Bulletin of Volcanology*, 75(7), 733.
- 257 https://doi.org/10.1007/s00445-013-0733-2
- 258 Bertagnini, A., Coltelli, M., Landi, P., Pompilio, M., & Rosi, M. (1999). Violent explosions yield new
- insights into dynamics of Stromboli volcano. *Eos, Transactions American Geophysical Union*,
 80(52), 633–636. https://doi.org/10.1029/99EO00415
- Bertagnini, Antonella, Di Roberto, A., & Pompilio, M. (2011). Paroxysmal activity at Stromboli:
 lessons from the past. *Bulletin of Volcanology*, *73*(9), 1229–1243.
- 263 https://doi.org/10.1007/s00445-011-0470-3
- 264 Bertagnini, Antonella, Méltrich, N., Francalanci, L., Landi, P., Tommasini, S., & Conticelli, S. (2013).
- 265 Volcanology and Magma Geochemistry of the Present-Day Activity: Constraints on the
- 266 Feeding System. In S. Calvari, S. Inguaggiato, G. Puglisi, M. Ripepe, & M. Rosi (Eds.),
- 267 *Geophysical Monograph Series* (pp. 19–37). Washington, D. C.: American Geophysical
- 268 Union. https://doi.org/10.1029/182GM04
- 269 Bevilacqua, A., Bertagnini, A., Pompilio, M., Landi, P., Del Carlo, P., Di Roberto, A., et al. (2020).
- 270 Major explosions and paroxysms at Stromboli (Italy): a new historical catalog and temporal
- 271 models of occurrence with uncertainty quantification. *Scientific Reports*, *10*(1), 17357.
- 272 https://doi.org/10.1038/s41598-020-74301-8
- Bombrun, M., Harris, A., Gurioli, L., Battaglia, J., & Barra, V. (2015). Anatomy of a Strombolian
 eruption: Inferences from particle data recorded with thermal video. *Journal of Geophysical*
- 275 Research: Solid Earth, 120(4), 2367–2387. https://doi.org/10.1002/2014JB011556
- Bonadonna, C., Genco, R., Gouhier, M., Pistolesi, M., Cioni, R., Alfano, F., et al. (2011). Tephra
 sedimentation during the 2010 Eyjafjallajökull eruption (Iceland) from deposit, radar, and
- 278 satellite observations. Journal of Geophysical Research: Solid Earth, 116(B12).
- 279 https://doi.org/10.1029/2011JB008462

- Brodsky, E. E., Kanamori, H., & Sturtevant, B. (1999). A seismically constrained mass discharge rate
 for the initiation of the May 18, 1980 Mount St. Helens eruption. *Journal of Geophysical Research: Solid Earth*, *104*(B12), 29387–29400. https://doi.org/10.1029/1999JB900308
- 283 Bryan, S. E., Peate, I. U., Peate, D. W., Self, S., Jerram, D. A., Mawby, M. R., et al. (2010). The
- 284 largest volcanic eruptions on Earth. *Earth-Science Reviews*, *102*(3–4), 207–229.
- 285 https://doi.org/10.1016/j.earscirev.2010.07.001
- Carey, S., & Sigurdsson, H. (1985). The May 18, 1980 eruption of Mount St. Helens: 2. Modeling of
 dynamics of the Plinian Phase. *Journal of Geophysical Research: Solid Earth*, 90(B4), 2948–
- 288 2958. https://doi.org/10.1029/JB090iB04p02948
- Chouet, B., Hamisevicz, N., & McGetchin, T. R. (1974). Photoballistics of volcanic jet activity at
 Stromboli, Italy. *Journal of Geophysical Research (1896-1977)*, 79(32), 4961–4976.
- 291 https://doi.org/10.1029/JB079i032p04961
- Chouet, B., Saccorotti, G., Dawson, P., Martini, M., Scarpa, R., De Luca, G., et al. (1999). Broadband
 measurements of the sources of explosions at Stromboli Volcano, Italy. *Geophysical Research Letters*, 26(13), 1937–1940. https://doi.org/10.1029/1999GL900400
- 295 Delle Donne, D., & Ripepe, M. (2012). High-frame rate thermal imagery of Strombolian explosions:
- Implications for explosive and infrasonic source dynamics. *Journal of Geophysical Research: Solid Earth*, *117*(B9). https://doi.org/10.1029/2011JB008987
- 298 Freret-Lorgeril, V., Donnadieu, F., Scollo, S., Provost, A., Fréville, P., Guéhenneux, Y., et al. (2018).
- 299 Mass Eruption Rates of Tephra Plumes During the 2011–2015 Lava Fountain Paroxysms at

300 Mt. Etna From Doppler Radar Retrievals. *Frontiers in Earth Science*, 6, 73.

- 301 https://doi.org/10.3389/feart.2018.00073
- Giordano, G., & De Astis, G. (2020). The summer 2019 basaltic Vulcanian eruptions (paroxysms) of
 Stromboli. *Bulletin of Volcanology*, 83(1), 1. https://doi.org/10.1007/s00445-020-01423-2
- Global Volcanism Program, & Venzke, E. (2022). Volcanoes of the World, v.5 [Data set]. Global
 Volcanism Program.
- Gonnermann, H., & Manga, M. (2012). Dynamics of magma ascent in the volcanic conduit Chapter 4
 Overview. https://doi.org/10.1017/cbo9781139021562.004

308	Gurioli, L., Harris, A. J. L., Colò, L., Bernard, J., Favalli, M., Ripepe, M., & Andronico, D. (2013).
309	Classification, landing distribution, and associated flight parameters for a bomb field
310	emplaced during a single major explosion at Stromboli, Italy. <i>Geology</i> , 41(5), 559–562.
311	https://doi.org/10.1130/G33967.1
312	Gurioli, L., Colo, L., Bollasina, A. J., Harris, A. J. L., Whittington, A., & Ripepe, M. (2013).
313	Dynamics of Strombolian explosions: Inferences from field and laboratory studies of erupted
314	bombs from Stromboli volcano. Journal of Geophysical Research, 27.
315	Hammer, J. E., Cashman, K. V., Hoblitt, R. P., & Newman, S. (1999). Degassing and microlite
316	crystallization during pre-climactic events of the 1991 eruption of Mt. Pinatubo, Philippines.
317	Bulletin of Volcanology, 60(5), 355–380. https://doi.org/10.1007/s004450050238
318	Harris, A., & Ripepe, M. (2007). Synergy of multiple geophysical approaches to unravel explosive
319	eruption conduit and source dynamics – A case study from Stromboli. Geochemistry, 67(1),
320	1-35. https://doi.org/10.1016/j.chemer.2007.01.003
321	Harris, A.J.L., Delle Donne, D., Dehn, J., Ripepe, M., & Worden, A. K. (2013). Volcanic plume and
322	bomb field masses from thermal infrared camera imagery. Earth and Planetary Science
323	Letters, 365, 77-85. https://doi.org/10.1016/j.epsl.2013.01.004
324	Harris, Andrew J. L., Ripepe, M., Calvari, S., Lodato, L., & Spampinato, L. (2013). The 5 April 2003
325	Explosion of Stromboli: Timing of Eruption Dynamics Using Thermal Data. In S. Calvari, S.
326	Inguaggiato, G. Puglisi, M. Ripepe, & M. Rosi (Eds.), Geophysical Monograph Series (pp.
327	305–316). Washington, D. C.: American Geophysical Union.
328	https://doi.org/10.1029/182GM25
329	Harris, Andrew J.L., Ripepe, M., & Hughes, E. A. (2012). Detailed analysis of particle launch
330	velocities, size distributions and gas densities during normal explosions at Stromboli. Journal
331	of Volcanology and Geothermal Research, 231–232, 109–131.

- 332 https://doi.org/10.1016/j.jvolgeores.2012.02.012
- Koyaguchi, T., & Ohno, M. (2001). Reconstruction of eruption column dynamics on the basis of grain
 size of tephra fall deposits: 2. Application to the Pinatubo 1991 eruption. *Journal of*

- 335 *Geophysical Research: Solid Earth*, 106(B4), 6513–6533.
- 336 https://doi.org/10.1029/2000JB900427
- Koyaguchi, T., & Tokuno, M. (1993). Origin of the giant eruption cloud of Pinatubo, June 15, 1991.
 Journal of Volcanology and Geothermal Research, 55(1), 85–96.
- 339 https://doi.org/10.1016/0377-0273(93)90091-5
- Leduc, L., Gurioli, L., Harris, A., Colò, L., & Rose-Koga, E. F. (2015a). Types and mechanisms of
 strombolian explosions: characterization of a gas-dominated explosion at Stromboli. *Bulletin*

342 of Volcanology, 77(1), 8. https://doi.org/10.1007/s00445-014-0888-5

- 343 Leduc, L., Gurioli, L., Harris, A., Colò, L., & Rose-Koga, E. F. (2015b). Types and mechanisms of
- 344 strombolian explosions: characterization of a gas-dominated explosion at Stromboli. *Bulletin* 345 *of Volcanology*, 77(1), 8. https://doi.org/10.1007/s00445-014-0888-5
- 346 Maki, M., Kim, Y., Kobori, T., Hirano, K., Lee, D.-I., & Iguchi, M. (2021). Analyses of three-
- 347 dimensional weather radar data from volcanic eruption clouds. *Journal of Volcanology and*348 *Geothermal Research*, 412, 107178. https://doi.org/10.1016/j.jvolgeores.2021.107178
- 349 Mangan, M., & Sisson, T. (2000). Delayed, disequilibrium degassing in rhyolite magma:
- decompression experiments and implications for explosive volcanism. *Earth and Planetary Science Letters*, 183(3), 441–455. https://doi.org/10.1016/S0012-821X(00)00299-5
- 352 Mason, B. G., Pyle, D. M., & Oppenheimer, C. (2004). The size and frequency of the largest explosive
- 353 eruptions on Earth. *Bulletin of Volcanology*, 66(8), 735–748. https://doi.org/10.1007/s00445354 004-0355-9
- 355 Mastin, L. G., Guffanti, M., Servranckx, R., Webley, P., Barsotti, S., Dean, K., et al. (2009). A
- 356 multidisciplinary effort to assign realistic source parameters to models of volcanic ash-cloud
- 357 transport and dispersion during eruptions. *Journal of Volcanology and Geothermal Research*,
- 358 *186*(1), 10–21. https://doi.org/10.1016/j.jvolgeores.2009.01.008
- 359 Métrich, N, Bertagnini, A., & Di Muro, A. (2010). Conditions of Magma Storage, Degassing and
- 360 Ascent at Stromboli: New Insights into the Volcano Plumbing System with Inferences on the
- 361 Eruptive Dynamics. *Journal of Petrology*, *51*(3), 603–626.
- 362 https://doi.org/10.1093/petrology/egp083

- Métrich, Nicole, Bertagnini, A., Landi, P., Rosi, M., & Belhadj, O. (2005). Triggering mechanism at
 the origin of paroxysms at Stromboli (Aeolian Archipelago, Italy): The 5 April 2003 eruption.
 Geophysical Research Letters, 32(10). https://doi.org/10.1029/2004GL022257
- 366 Métrich, Nicole, Bertagnini, A., & Pistolesi, M. (2021a). Paroxysms at Stromboli Volcano (Italy):
- 367 Source, Genesis and Dynamics. *Frontiers in Earth Science*, 9.
- 368 https://doi.org/10.3389/feart.2021.593339

370

369 Métrich, Nicole, Bertagnini, A., & Pistolesi, M. (2021b). Paroxysms at Stromboli Volcano (Italy):

Source, Genesis and Dynamics. Frontiers in Earth Science, 9. Retrieved from

- 371 https://www.frontiersin.org/articles/10.3389/feart.2021.593339
- 372 Newhall, C. G., & Self, S. (1982). The volcanic explosivity index (VEI) an estimate of explosive
- 373 magnitude for historical volcanism. *Journal of Geophysical Research*, 87(C2), 1231.
- 374 https://doi.org/10.1029/JC087iC02p01231
- 375 Patrick, M. R., Harris, A. J. L., Ripepe, M., Dehn, J., Rothery, D. A., & Calvari, S. (2007).
- 376 Strombolian explosive styles and source conditions: insights from thermal (FLIR) video.
- 377 *Bulletin of Volcanology*, 69(7), 769–784. https://doi.org/10.1007/s00445-006-0107-0
- 378 Pichavant, M., Di Carlo, I., Pompilio, M., & Le Gall, N. (2022). Timescales and mechanisms of
- 379 paroxysm initiation at Stromboli volcano, Aeolian Islands, Italy. *Bulletin of Volcanology*,
- 380 84(4), 36. https://doi.org/10.1007/s00445-022-01545-9
- Pioli, L., Pistolesi, M., & Rosi, M. (2014). Transient explosions at open-vent volcanoes: The case of
 Stromboli (Italy). *Geology*, 42(10), 863–866. https://doi.org/10.1130/G35844.1
- Pistolesi, M., Delle Donne, D., Pioli, L., Rosi, M., & Ripepe, M. (2011). The 15 March 2007 explosive
 crisis at Stromboli volcano, Italy: Assessing physical parameters through a multidisciplinary
- 385 approach. Journal of Geophysical Research, 116(B12), B12206.
- 386 https://doi.org/10.1029/2011JB008527
- Pyle, D. M. (1998). Forecasting sizes and repose times of future extreme volcanic events. *Geology*,
 26(4), 367–370. https://doi.org/10.1130/0091-7613(1998)026<0367:FSARTO>2.3.CO;2
- 389 Pyle, D. M. (2015). Sizes of Volcanic Eruptions. In *The Encyclopedia of Volcanoes* (pp. 257–264).
- 390 Elsevier. https://doi.org/10.1016/B978-0-12-385938-9.00013-4

- Renzulli, A., Del Moro, S., Menna, M., Landi, P., & Piermattei, M. (2009). Transient processes in
 Stromboli's shallow basaltic system inferred from dolerite and magmatic breccia blocks
- 393 erupted during the 5 April 2003 paroxysm. *Bulletin of Volcanology*, *71*(7), 795–813.

394 https://doi.org/10.1007/s00445-009-0265-y

- Ripepe, M., Rossi, M., & Saccorotti, G. (1993). Image processing of explosive activity at Stromboli.
 Journal of Volcanology and Geothermal Research, 54(3), 335–351.
- 397 https://doi.org/10.1016/0377-0273(93)90071-X
- 398 Ripepe, Maurizio, & Gordeev, E. (1999). Gas bubble dynamics model for shallow volcanic tremor at
- 399 Stromboli. *Journal of Geophysical Research: Solid Earth*, *104*(B5), 10639–10654.
- 400 https://doi.org/10.1029/98JB02734
- 401 Ripepe, Maurizio, Ciliberto, S., & Della Schiava, M. (2001). Time constraints for modeling source
 402 dynamics of volcanic explosions at Stromboli. *Journal of Geophysical Research: Solid Earth*,
 403 106(B5), 8713–8727. https://doi.org/10.1029/2000JB900374
- 404 Rosi, M., Bertagnini, A., Harris, A. J. L., Pioli, L., Pistolesi, M., & Ripepe, M. (2006). A case history
 405 of paroxysmal explosion at Stromboli: Timing and dynamics of the April 5, 2003 event. *Earth*

406 and Planetary Science Letters, 243(3), 594–606. https://doi.org/10.1016/j.epsl.2006.01.035

- 407 Rutherford, M. J., & Devine, J. D. (1996). Preeruption Pressure-Temperature Conditions and Volatiles
- 408 in the 1991 Dacitic Magma of Mount Pinatubo. Retrieved October 27, 2022, from
 409 https://pubs.usgs.gov/pinatubo/ruth/
- 410 Scharff, L., Hort, M., Harris, A. J. L., Ripepe, M., Lees, J. M., & Seyfried, R. (2008). Eruption
- 411 dynamics of the SW crater of Stromboli volcano, Italy An interdisciplinary approach.
- 412 *Journal of Volcanology and Geothermal Research*, *176*(4), 565–570.
- 413 https://doi.org/10.1016/j.jvolgeores.2008.05.008
- 414 Schneider, H., & Barbera, F. (1998). 18 Application of order statistics to sampling plans for inspection
- 415 by variables. In *Handbook of Statistics* (Vol. 17, pp. 497–511). Elsevier.
- 416 https://doi.org/10.1016/S0169-7161(98)17020-7

- 417 Sornette, D., Knopoff, L., Kagan, Y. Y., & Vanneste, C. (1996). Rank-ordering statistics of extreme
 418 events: Application to the distribution of large earthquakes. *Journal of Geophysical Research:*419 *Solid Earth*, *101*(B6), 13883–13893. https://doi.org/10.1029/96JB00177
- 420 Steinberg, G. S., & Babenko, J. I. (1978). Experimental velocity and density determination of volcanic
- 421 gases during eruption. *Journal of Volcanology and Geothermal Research*, *3*(1–2), 89–98.
- 422 https://doi.org/10.1016/0377-0273(78)90005-7
- 423 Tournigand, P.-Y., Taddeucci, J., Gaudin, D., Peña Fernández, J. J., Del Bello, E., Scarlato, P., et al.
- 424 (2017). The Initial Development of Transient Volcanic Plumes as a Function of Source
- 425 Conditions. *Journal of Geophysical Research: Solid Earth*, *122*(12), 9784–9803.
- 426 https://doi.org/10.1002/2017JB014907
- 427 Van Eaton, A. R., Amigo, Á., Bertin, D., Mastin, L. G., Giacosa, R. E., González, J., et al. (2016).
- 428 Volcanic lightning and plume behavior reveal evolving hazards during the April 2015 eruption
- 429 of Calbuco volcano, Chile. *Geophysical Research Letters*, 43(7), 3563–3571.
- 430 https://doi.org/10.1002/2016GL068076
- 431 Wilson, L., Sparks, R. S. J., Huang, T. C., & Watkins, N. D. (1978). The control of volcanic column
- 432 heights by eruption energetics and dynamics. *Journal of Geophysical Research: Solid Earth*,
- 433 83(B4), 1829–1836. https://doi.org/10.1029/JB083iB04p01829
- 434 Wilson, Lionel, & Self, S. (1980). Volcanic explosion clouds: Density, temperature, and particle
- 435 content estimates from cloud motion. *Journal of Geophysical Research: Solid Earth*, 85(B5),
 436 2567–2572. https://doi.org/10.1029/JB085iB05p02567
- Woods, A. W., & Bower, S. M. (1995). The decompression of volcanic jets in a crater during
 explosive volcanic eruptions. *Earth and Planetary Science Letters*, *131*(3), 189–205.
- 439 https://doi.org/10.1016/0012-821X(95)00012-2
- Barberi F, Rosi M, Sodi A (1993) Volcanic hazard assessment at Stromboli based on review of
 historical data. Acta Vulcanologica 3:173–187
- 442 Hort M, Seyfried R (1998) Volcanic eruption velocities measured with a micro radar. Geophys Res
- 443 Lett 25(1):113–116. https://doi.org/10. 1029/97GL03482

444	Hort M, Seyfried R, Vöge M (2003) Radar doppler velocimetry of volcanic eruptions: theoretical
445	considerations and quantitative documentation of changes in eruptive behaviour at stromboli
446	volcano, Italy. Geophys J Int 154(2):515-32. https://doi.org/10.1046/j.1365-
447	246X.2003.01982.x
448	Simkin T, Siebert L, McClelland L, Bridge D, Newhall C, Latter JH (1981) Volcanoes of the world: a
449	regional directory, gazetteer and chronology of volcanism during the last 10,000 years. US
450	Hutchinson Ross Publishing
451	Weill A, Brandeis G, Vergniolle S, Baudin F, Bilbille J, Fèvre JF, Piron B, Hill X (1992) Acoustic
452	sounder measurements of the vertical velocity of volcanic jets at Stromboli Volcano. Geophys
453	Res Lett 19(23):2357-2360. https://doi.org/10.1029/92GL0 2502

454

455 **Figure caption listing**

456 **Fig. 1** Comparison between max gas velocity, as derived from ballistic ejection velocity (G_v^b) , 457 and directly measured maximum gas velocities (G_v) for major to paroxysmal eruptions at 458 Stromboli. See Table 1 for data and sources.

Fig. 2 Relationships between MDR and maximum gas velocity (data points) and ballistic velocity (colored fields) for (a) normal, and (b) major and paroxysmal eruptions at Stromboli. Gray line gives fit obtained from Equation (4); red dashed lines represent the σ uncertainty envelope. The yellow trend is the fit to the data of Bombrun et al. (2015) and NE1 data of Harris et al. (2013), and the blue trend considers all NE crater data. Both trends look very similar, the difference with the correlation coefficient both lies in the amount of data used for each fit and because the NE2 vent data are scattered around the trendline.

Fig. 3 Rank order representation of Stromboli's normal, major and paroxysmal eruptions in terms of a) the mass discharge rate and b) the maximum gas ejection rate. Both MDR rank order and G_v rank order analyses display a gap between a higher and lower group. The dashed line marks the separation between the higher ranked group composed of paroxysmal, major and ashdominated emissions, and the lower ranked group of ballistic-dominated normal events.

Fig. 4 MDR and G_v relations. Orange field is that defined by the data for ash-dominated emissions at Stromboli, where the positive, linear increase as a function of gas density (d_{gas}), volatile content (C_{vol}), conduit size and vent overpressure (P_{vent}), magma temperature (T) and silica content (X). The blue "Vulcanian-Plinian" field falls on a similar trend but is at a level two orders of magnitude higher than the "Strombolian" trend. Sakurajima, Mt. St. Helens and Pinatubo data fall within this field, all three being volcanoes associated with higher magma volatile content (C_{vol}), silica content (X), conduit size and vent pressure (P_{vent}) than Stromboli.

478

479 **Table caption listing**

- 480 **Table 1** Data set for ballistic (B_v) and gas (G_v) velocities and mass discharge rate (MDR) for
- 481 normal, major, and paroxysmal eruptions at Stromboli. B_v and G_v re-calculated using
- 482 Equation (8) of Harris et al. (2012) are given in bold.
- 483 **Table 2** Mass and duration data obtained from thermal video for normal explosions at
- 484 Stromboli's NE1 and NE2 vents (derived MDR in bold).















Table 1

Date of eruption	Eruption type	Data type	Method	B _v (m/s)	Direct Gv independent measurement (m/s)	Literature derived Gv calculated (m/s)	Max derived G_v^b re-calculated (m/s)	Max derived Bv re-calculated (m/s)	Max Mass discharge rate (kg/s)	Ref.
4/5/2003	Parox	Radiometer Seismic	Waveform delay time	200	310		297		1.10E+07	Rosi et al. (2006)
4/5/2003	Parox	Radiometer - Seismic	Waveform delay time	185		324	276			Ripepe and Harris (2008)
3/15/2007	Parox	thermal video	Particle tracking	155	210		234		2.20E+06	Andronico et al. (2013), Pistolesi et al. (2011)
11/8/2009	Major	Bomb mapping	ballistic model	130	n.d		199		1.20E+04	Gurioli et al. (2013a), Pioli et al. (2014)
11/24/2009	Major	Bomb mapping	ballistic model	90	n.d		142		5.50E+04	Gurioli et al. (2013a), Pioli et al. (2014)
7/3/2019	Parox	Bomb mapping	ballistic model	160	n.d	200	241		1.40E+06	Giordano and De Astis (2020)
8/28/2019	Parox	Bomb mapping	ballistic model	130	n.d	200	199		3.60E+05	Giordano and De Astis (2020)
6/27/2004	Normal	thermal video	Gas cloud and particle tracking	129	213		197			Harris et al. (2012)
6/2/2010	Normal	thermal video	Gas cloud and particle tracking		8-48			23		Harris et al. (2013a,b)
6/8/2010	Normal	thermal video	Gas cloud and particle tracking		8-35			14		Harris et al. (2013a,b)
6/2004	Normal	thermal video	Particle tracking	3-101			158			Patrick et al. (2007)
9/27/1991	Normal	acoustic sounder	Waveform analysis	20-80			128			Weill et al. (1992)
9/1971	Normal	high speed camera	Particle tracking	2-72	94-112		117			Chouet et al. (1974)
4/2000	Normal	doppler radar	Waveform analysis	44-70			114			Hort et al. (2003)
9/1994	Normal	thermal video	Particle tracking	35-45	40-105		79			Ripepe et al. (2001)
1/29/1988 to 9/8/1989	Normal	thermal video	Particle tracking	16-22	70		46			Ripepe et al. (1993)
10/1/1996	Normal	doppler radar	Waveform analysis	7-13			34			Hort and Seyfried (1998)
27/9/2012 to 18/5/2014	Normal	thermal video	Gas cloud and particle tracking			240			1.30E+03	Bombrun et al. (2015)
26/5/2013 to 26/5/2016	Normal	Visible light and thermal video	Gas cloud and particle tracking			112			5.25E+04	Tournigand et al. (2017)

495 **Table 2**

Crater	Date	Time	Maximum Velocity*	Total	Mass*	Duration	MDR	Log ₁₀ (MDR)
	(dd/mm/yy)	(hh:mm:ss)	(m s ⁻¹)	(x 10 ³ kg)		(s)	(kg/s)	(kg/s)
NE1	2/6/2010	11:35:23	16.6	1.1	1.4	18.6	67	1.83
NE1	2/6/2010	11:57:51	39.5	3.5	3.8	22.9	160	2.20
NE1	2/6/2010	12:22:35	8.3	2.7	3	18.2	156	2.19
NE1	2/6/2010	14:08:51	39.5	1.7	1.8	19.0	92	1.96
NE1	2/6/2010	14:38:43	47.8	1.7	1.9	16.4	110	2.04
NE1	2/6/2010	14:59:53	37.4	3.3	3.7	28.1	125	2.10
NE1	2/6/2010	15:48:05	43.6	1.1	1.2	27.2	42	1.63
NE1	2/6/2010	16:08:17	33.3	0.9	1	9.4	101	2.00
NE1	2/6/2010	16:12:11	47.8	1.3	1.4	6.6	204	2.31
NE1	8/6/2010	13:50:46	33.3	1.3	1.4	10.2	132	2.12
Average			34.7	1.9	2.1	17.7	119	2.0
NE2	8/6/2010	12:43:43	22.9	2.3	2.6	5.0	489	2.69
NE2	8/6/2010	13:29:57	29.1	0.4	0.5	5.2	86	1.94
NE2	8/6/2010	14:03:17	20.8	0.32	0.35	3.4	99	1.99
NE2	8/6/2010	14:05:23	35.3	1.9	2.1	5.2	385	2.59
NE2	8/6/2010	14:20:28	27	1.1	1.2	4.8	239	2.38
NE2	8/6/2010	15:08:56	29.1	1.1	1.2	4.6	250	2.40
NE2	8/6/2010	15:19:10	33.3	1.3	1.4	5.0	270	2.43
NE2	8/6/2010	16:32:13	33.3	3.8	4.2	5.0	799	2.90
NE2	8/6/2010	17:00:32	8.3	0.09	0.1	3.0	32	1.50
NE2	8/6/2010	18:03:52	24.9	0.56	0.63	18.6	32	1.50
NE2	8/6/2010	18:20:31	27	0.13	0.15	4.2	33	1.52
Average			26.5	1.2	1.3	5.8	247	2.2

* data from Harris et al. (2013)

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