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## Journal Pre-proofs

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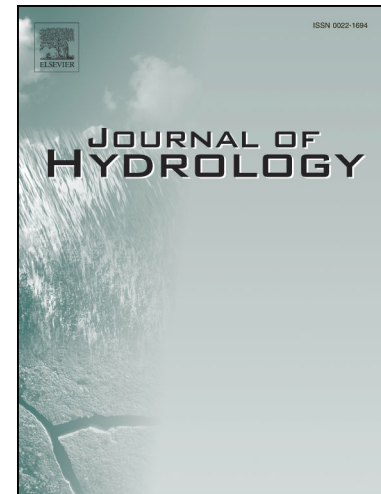
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# 1 Characterizing coastal aquifer heterogeneity from a single piezometer head 2 chronicle

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10 Hydraulic conductivity

## 11 1. Introduction

12 Climate change exerts particularly strong effects on coastal areas (Richardson et al., 2024). In this  
13 context, our focus is specifically on the risks associated with rising aquifer levels (Rotzoll and Fletcher,  
14 2013). With sea levels rising by a few millimeters to a few centimeters per year depending on climate  
15 change scenarios (Rignot et al., 2011), the levels of coastal aquifer are also increasing. This poses a  
16 threat to buried and low-lying infrastructures, nearshore ecosystems, and amplifies the risk of flooding  
17 (Habel et al., 2017; Knott et al., 2017). Fluctuations in aquifer level traduce the variations of its  
18 groundwater storage, and consequently the difference between recharge and discharge. For this  
19 reason, varying seasonal rainfall and evaporation can lead to temporary increased or decreased aquifer  
20 levels, depending on discharge conditions. Both marine and continental forcings, as well as the  
21 geometry of the coastline, distance from the coast, geologic depositional environments, and regional  
22 stream network contribute to groundwater-induced flood-risk evolution in coastal areas (Knott et al.,  
23 2019). Aquifer hydraulic properties were found to be a dominant factor in groundwater-rise  
24 vulnerability, with propagation projection of 10 km from the coast and main rivers in Netherlands  
25 (Oude Essink et al., 2010).

26 Diffusive aquifers extend the zone of tidal influence and their associated high levels (Jacob, 1950;  
27 Nielsen, 1990). They also moderate the influence of recharge, with reduced head gradients and limited  
28 aquifer levels. Conversely, less diffusive aquifers mitigate marine influences but increase the  
29 vulnerability to groundwater rise from the continental side. This initial qualitative analysis becomes  
30 significantly more complex for heterogeneous aquifers. This is particularly true for coastal areas where  
31 Quaternary sand deposits next to the shoreface separate inland less diffusive bedrock formations from  
32 marine boundaries, a common configuration found in coastal areas like on the Western Normandy  
33 coast (France) (Dupret et al., 1989). The dune ridge shields the adjacent low-lying area from most of  
34 the marine submersion risks but does not protect it from increasing groundwater levels. A few hundred  
35 meters to a few kilometers away inland, the bedrock rises significantly, protecting more distant coastal  
36 areas from any marine risk, but increasing the vulnerability to flooding induced by aquifer outlets.

37 To assess vulnerability to groundwater-induced flooding, one of the major challenges lies in  
38 characterizing hydraulic properties and their heterogeneity. Information derived from the aquifer's  
39 response to the tidal signal has been widely employed to determine these properties (e.g. Aguila et al.,  
40 2023; Fischer et al., 2020; Goyetche et al., 2022; Jha et al., 2008; Slooten et al., 2010; Zhang et al.,  
41 2021). They provide basic to advanced constraints on aquifer properties and flow structures (Rogers

et al., 2023). For homogeneous aquifers, piezometric tidal effects decrease exponentially with shore distance as a function of diffusivity (Ferris, 1952). Diffusivity can thus be determined by comparing the amplitude of piezometric head variations with that of tides (Carr and Vanderka, 1969; Slooten et al., 2010) and, for greater precision, by analyzing both signals together (Jha et al., 2008). Heterogeneous aquifers also exhibit spatial variations with hydraulic conductivity increasing linearly with the distance from the coastline in some cases (Monachesi and Guarracino, 2011), or vertically in other cases (Li and Jiao, 2003). Mapping these variations in diffusivity often requires several monitoring wells (Carol et al., 2009; Rogers et al., 2023; Yang et al., 2021). A review of methods also emphasizes the necessity to develop original approaches to independently estimate hydraulic conductivity and specific yield for water resources management (Zhang et al., 2021).

Here, we propose an alternative and innovative approach to characterize subsurface hydraulic properties (hydraulic conductivity and specific yield) and their heterogeneity, based on hydraulic head measured on a single piezometer. The method uses three aspects of aquifer response to marine and continental forcings: i) average head, which filters out the temporal variability and is linked to average recharge, sea level and hydraulic conductivity; ii) high-frequency head variations linked to tidal effects; iii) seasonal variations, which respond to hydrological cycle of aquifer recharge and discharge. We propose to characterize heterogeneous subsurface hydrodynamic properties by analyzing these three piezometric signal components, associated to characteristic time scales of weeks (spring and neap tides), months (hydrological cycle) and years (average recharge). We show that coastal aquifers may respond specifically to each of those forcings using data obtained on a coastal aquifer in Normandy, France (section 2). We propose a step-by-step approach to constrain the subsurface hydraulic properties relying on analytical and simplified 1D numerical models without considering any groundwater seepage (section 3). We compare the results obtained with a more advanced 2D numerical model, investigate the effects of seepage and of the distance of the observation piezometer to the lithological interface (section 4). We then discuss the most adapted identification method depending on the encountered conditions, and its domain of applicability. We eventually illustrate our methodology by presenting an application to groundwater-induced flooding in the studied coastal area (section 5). We believe that this is one of the key applications of our methodology, as this latter has to be applied to coastal areas, which are often prone to groundwater flooding as water table is likely to be shallow in such contexts.

## 2. Response of coastal hydraulic heads to tidal and recharge variations

Starting from a classic coastal context (2.1), we demonstrate the dual influence of continental and marine forcings on hydraulic head variations (2.2) and propose a quantification of their main characteristics (2.3).

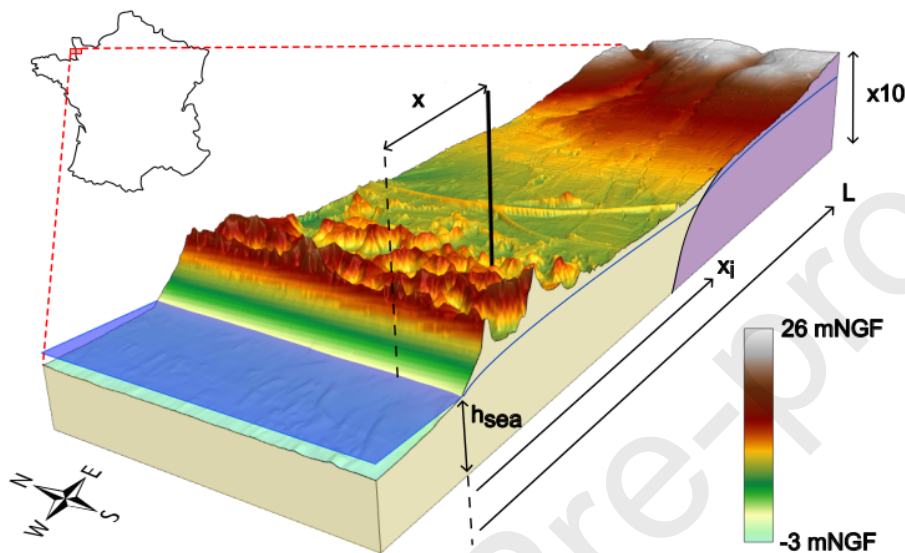
### 2.1. Geological and hydrogeological contexts

The study area is a coastal site located in the south-western part of the town of Gouville-sur-Mer, in western Normandy, France (Figure 1, insert). It is located in the downstream part of the Moulin-de-Gouville river catchment, the source of which lies 10 km to the East. The modelled area is 1 km wide and 3.3 km long (frame in Figure 2). This site is representative of coastal areas made up of a dune ridge, a retro-littoral palaeo-cliff and, between these two groups, a sea-marsh. The palaeo-cliffs of Normandy are polygenic structures, whose formation began in the Neogene (Pedoja et al., 2018). They contain different levels of marine terraces, most often masked by periglacial cover (Bigot, 1897; Coutard et al., 2006; Elhai, 1960; Lautridou, 1989). The most recent of these terraces is the Eemian (124,000 to 119,000 years ago), which is located in the basal parts of the paleo-cliffs and consists of perched fossil beaches of pebbles or sand (Dupret et al., 1989). Within the studied site, the dune belt reaches a

88 maximum elevation of 20 m. To the West, it overlooks a sea marsh, whose elevation is close to that of  
 89 the sea at high tide. The paleo-cliff has a gentle profile, a result of erosion of the last ice age. The  
 90 highest points of the modelled area, located to the East of the paleo-cliff, reach approximately 25 m  
 91 above sea level. Note that all elevation including hydraulic head are referenced as meters above sea  
 92 level shortened as "m".

93

94



95

96 *Figure 1: Topography and location of the study site within the Moulin-de-Gouville River watershed*  
 97 *(Normandy, France).*

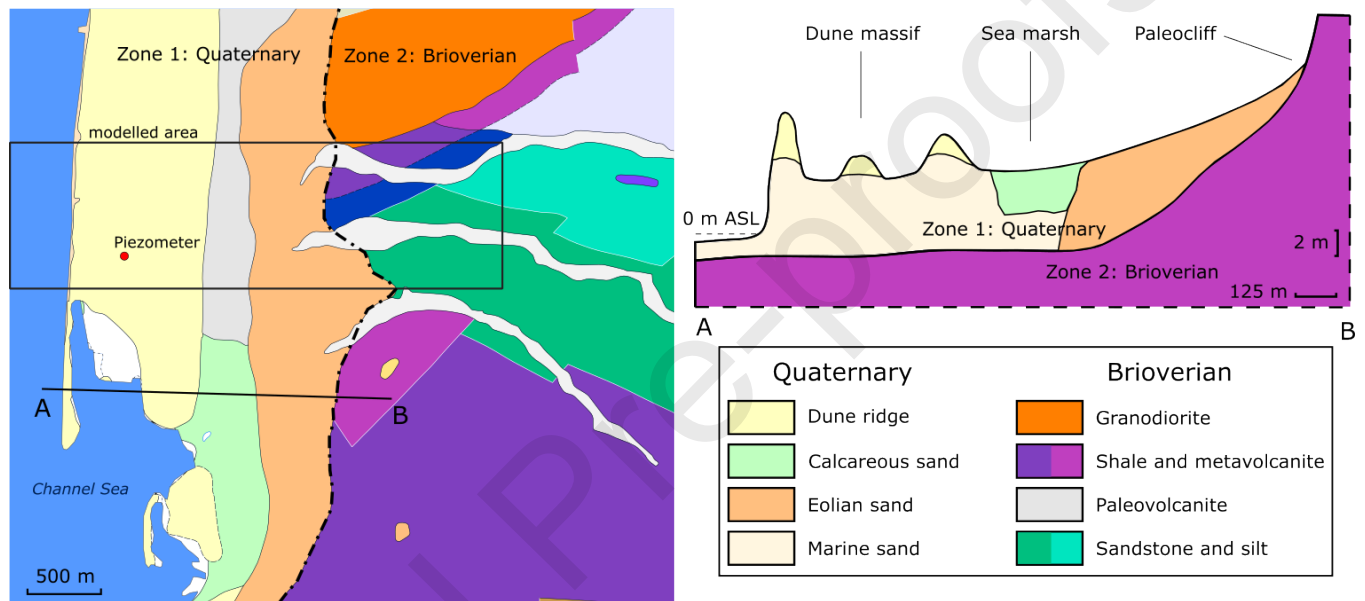
98 The study site is located in a complex geological context, both from a lithological and structural point  
 99 of view. It is located in the heart of the Cadomian island arc of Coutances (Dissler et al., 1988; Dupret  
 100 et al., 1990), whose main geological formations are of magmatic origin (Dupret et al., 1987; Dupret et  
 101 al., 1989). In the environment of the site, sedimentary formations of detrital origin are also present, of  
 102 lower and upper Brioverian age. Some Cambrian sandstones also crop out to the north and on the  
 103 rocky flat off the site, on the foreshore.

104 The geological bedrock at the study site is covered by more or less ancient Quaternary rocks, generally  
 105 sandy (zone 1 in Figure 2). They are of continental or marine origin depending on the case. Under the  
 106 dunes, the bedrock was reached by various drillings at a height of around ten meters. This Brioverian  
 107 bedrock outcrops on the foreshore and in the paleocliff (zone 2 in Figure 2). The description of the  
 108 rocks reached by the drilling does not make it possible to precisely characterize the composition of the  
 109 bedrock located under the dunes, in the vicinity of the study site. Understanding its structure in detail  
 110 would require high-precision geophysics coupled with close-up surveys. Nevertheless, this  
 111 environment is that of a strongly faulted site. It is likely that the paleocliff originated from the presence  
 112 of these structural discontinuities. The lithological differences observed between the rocks  
 113 outcropping on the foreshore or in the paleocliff can only be conceived in the presence of a bundle of  
 114 faults and folds masked by the dune massif and the sea marshes which border it at the foot of the  
 115 paleocliff.

116 Figure 2 synthesizes the site geological setup, with a well-marked heterogeneity characterized by two  
 117 juxtaposed distinct formations. In the western part (zone 1 on Figure 2), the site consists of recent,

118 loose rocks, mainly marine and eolian sands, up to 10 m thick. These sands are partially interbedded  
 119 with solifluction deposits or sandy clay peat. They are referred to as Quaternary sands in the next  
 120 sections. In the eastern part, the outcropping rocks (zone 2 on Figure 2) belong to the local Cadomo-  
 121 Variscan bedrock (Brioverian sequence). They are designated as Brioverian shales in the next sections.  
 122 They consist of variably metamorphosed sandstone and shale, as well as granite, showing fissures and  
 123 surface alteration. This bedrock forms the basement of the unconsolidated rocks in the western part  
 124 of the site. There is no clear discontinuity or impervious layer between the ancient rocks and the  
 125 overlying unconsolidated formations, due to a weathering layer affecting the upper part of the  
 126 bedrock. It is therefore not possible to clearly distinguish an upper aquifer from a lower, confined  
 127 aquifer. As a whole, the aquifer extends to a thickness of over 35 meters.

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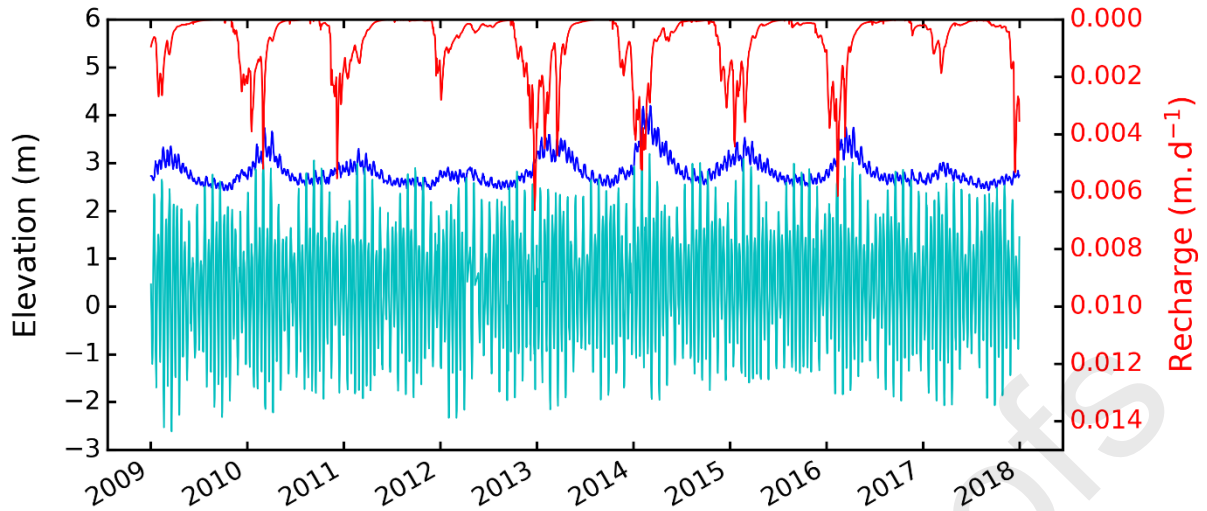


129

130 *Figure 2: Modelled area, geological map (left) and simplified geological cross-section (right). Modified*  
 131 *from Dupret et al. (1989).*

## 132 2.2. Piezometric, sea-level and recharge data

133 The Gouville piezometer (red circle on Figure 2) has been monitored at a daily frequency since 2005.  
 134 It is part of the French national network of groundwater measurements, whose information is  
 135 accessible online on the ADES database (Winckel et al., 2022). The piezometer is 11 metres deep,  
 136 drilled through sands within the Quaternary formation, and located 420 metres east of the shoreline.  
 137 The recorded head data is shown in dark blue on Figure 3 for the 2009-2017 period. It reacts to both  
 138 spring-and-neap tide and seasonal recharge forcings.



139

140 *Figure 3: Read on the left axis, daily hydraulic heads in dark blue recorded at the Gouville piezometer*  
 141 *and daily sea levels at the nearby Saint-Malo station in light blue. Read on the right axis, aquifer*  
 142 *recharge of the modelled area in red as given by the SURFEX national climate time series (Le Moigne et*  
 143 *al., 2020).*

144 The high frequency variations of the head data are to compare with the tidal signal (light blue curve  
 145 on Figure 3). It is obtained from the nearest oceanographic station of Saint-Malo operated by the  
 146 Hydrographic and Oceanographic Marine Service, which produces oceanographic data at several  
 147 coastal stations along the French shore (SHOM, 2020). Hourly levels were translated in daily levels to  
 148 focus on the bimonthly tidal fluctuations, which are the only ones observed in the piezometric data.  
 149 The high frequency variations of head data (dark blue) are well marked and have logically a significantly  
 150 smaller amplitude than the sea level ones (light blue).

151 The lower frequency variations of head data are well phased with aquifer recharge (red curve on Figure  
 152 3), obtained from the SURFEX national climate model (Le Moigne et al., 2020), produced by the French  
 153 meteorological institute. In SURFEX, aquifer recharge values are resulting from the exchanges of mass  
 154 and energy between the soil, the surface, the biosphere and the atmosphere accounting for the wide  
 155 diversity of surfaces.

### 156 2.3. Main characteristics of the hydraulic head signal

157 The head data display three main components: the mean pluriannual value, the amplitude of seasonal  
 158 recharge-induced variation, and the amplitude of weekly tidal variations. In order to identify aquifer  
 159 hydraulic properties based on these three components, we derive them from the head signal as  
 160 follows:

$$161 \quad h(\mathbf{x}, t) = \bar{h}(\mathbf{x}) + h_r(\mathbf{x}, t) + h_t(\mathbf{x}, t) \quad (1)$$

161 where  $\bar{h}(\mathbf{x})$  is the mean hydraulic head at a distance to shoreline  $\mathbf{x}$  within the aquifer,  $h_r(\mathbf{x}, t)$  and  $h_t$   
 162  $(\mathbf{x}, t)$  are the head components respectively associated to seasonal (recharge-induced) and weekly  
 163 (tide-induced) forcings.  $\bar{h}(\mathbf{x})$  is defined by:

$$\bar{h}(\mathbf{x}) = \frac{1}{t_f - t_i} \int_{t_i}^{t_f} h(\mathbf{x}, u) du \quad (2)$$

164 where  $[t_i, t_f]$  is the time interval over which the head data are available. In practice it should be one  
 165 to several years.  $h_r(\mathbf{x}, t)$  is obtained by filtering out the tidal signal using a moving average over the  
 166 tidal period of duration  $\tau=28$  days:

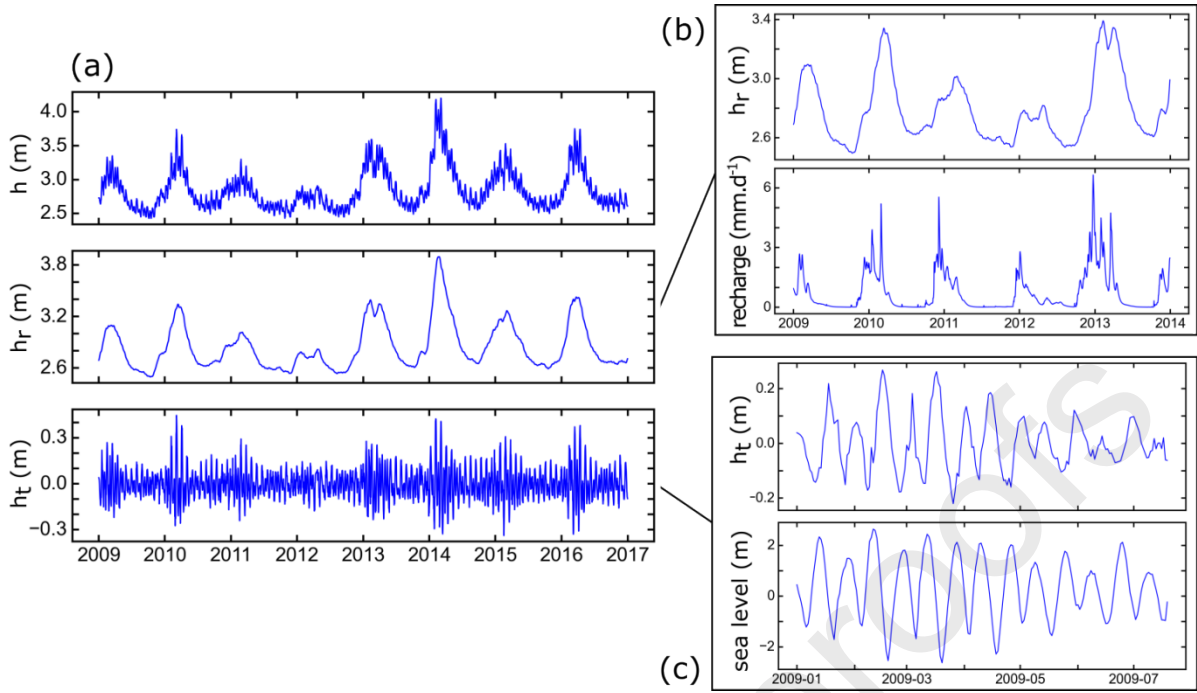
$$h_r(\mathbf{x}, t) = \frac{1}{\tau} \int_{t-\tau/2}^{t+\tau/2} (h(\mathbf{x}, u) - \bar{h}(\mathbf{x})) du. \quad (3)$$

167  $h_t(\mathbf{x}, t)$  is eventually obtained by removing the components previously determined:

$$h_t(\mathbf{x}, t) = \overline{h(\mathbf{x})} + h_r(\mathbf{x}, t) - h(\mathbf{x}, t). \quad (4)$$

168 Figure 4a shows the decomposition of the head levels of Gouville (Figure 2) in its recharge-induced and  
 169 tide-induced components  $h_r$  and  $h_t$ . Figure 4b and 4c show the comparison to the SURFEX recharge  
 170 rate and measured sea-level on a shorter time range. In order to ensure that the moving average  
 171 method efficiently filters the tide-induced head fluctuations, we analyzed the correlation between the  
 172 terms  $h_r$  and  $h_t$  on the one hand, and recharge and sea-level on the other hand. After applying a time  
 173 lag of 41 (and 5) days to  $h_r$  (and  $h_t$ ), we obtain a Pearson correlation coefficient value of 0.807 (and  
 174 0.804). This shows that SURFEX-derived recharge and measured sea-level explain more than 80 % of  
 175  $h_r$  and  $h_t$  terms, respectively. It also confirms that the 28-day moving average filter method does not  
 176 significantly erase any seasonal recharge signal that would have a wavelength similar to that of spring  
 177 and neap tide.





178

179 Figure 4: (a) Time series on the 2009-2016 period of measured head  $h$  in the Gouville piezometer and  
 180 derived recharge-induced  $h_r$ , and tide-induced  $h_t$  head components. (b) Time series on the 2009-2014  
 181 period of the recharge-induced head component  $h_r$ , and SURFEX recharge (c) Time series on the January  
 182 to August 2009 period of the tide-induced head component  $h_t$  and measured sea-level.

183

184 We additionally define specific model performance criteria, measuring the ability of any model to  
 185 match each of these components. For the mean hydraulic head, the criterion is built from the mean  
 186 simulated and observed heads  $h^{sim}(x)$  and  $h^{obs}(x)$ :

$$\alpha = 1 - \frac{\overline{h^{sim}(x)}}{\overline{h^{obs}(x)}} \quad (5)$$

187 The comparison of recharge- and tide-induced variations are obtained from the similar criteria  $\beta_r$  and  
 188  $\beta_t$ :

$$\beta_r = 1 - \frac{\sigma_r^{sim}(x)}{\sigma_r^{obs}(x)} \quad (6)$$

$$\beta_t = 1 - \frac{\sigma_t^{sim}(x)}{\sigma_t^{obs}(x)} \quad (7)$$

189 where  $\sigma_a^b(x)$  is the standard deviation of the head component  $a$ ,  $a$  being either recharge ( $r$ ) or tide ( $t$ ),  
 190 for the simulated or observed heads ( $b=sim$  and  $b=obs$ , respectively). For the head time series of the

191 Gouville piezometer on the 2009-2017 period,  $\overline{h^{obs}} = 2.85 \text{ m}$ ,  $\sigma_t^{obs} = 0.12 \text{ m}$ ,  $\sigma_r^{obs} = 0.27 \text{ m}$ . Tidal  
 192 fluctuations appear to be non-negligible compared to the recharge-induced variations.

### 193 3. Hydraulic properties derived with simplified analytical and 194 numerical models

195 In this section, we show how the mean hydraulic head and the tidal fluctuations can be approached by  
 196 analytical solutions and give a first approximation of the hydraulic properties of the Quaternary sands.  
 197 We assess and complete the identification with simple 1D numerical simulations of heterogeneous  
 198 free aquifers following the configuration given in section 2 and recalled in **Error! Reference source not  
 199 found..** Exploration ranges are 1 to 30 % and  $10^0$  to  $10^3 \text{ m.d}^{-1}$  for specific yield and hydraulic  
 200 conductivity, respectively. They are determined through global synthesis (Freeze and Cherry, 1979;  
 201 Gleeson et al., 2011; Rosas et al., 2014), confirmed by site-specific studies (Borehole file BSS000KUVT,  
 202 2017).

203 *Table 1: Main site configuration and recharge metrics.*

Mean aquifer extension	L	3000 m
Distance of the lithological interface to the coast	$x_i$	600 m
Distance of the piezometer to the coast	X	400 m
Aquifer thickness at the coast	$h_{sea}$	20 m
Mean recharge rate	R	286 mm.y <sup>-1</sup>

#### 204 3.1. Approximation of Quaternary sand hydraulic properties using analytical 205 solutions

206 The mean value can be compared to the value  $h(x)$  obtained at the position  $x$  from the coast in steady  
 207 state for a 1D heterogeneous aquifer of size  $L$  and thickness  $h_{sea}$  at the coast, hydraulic conductivities  
 208  $K_1$  and  $K_2$  respectively Quaternary sand and Brioverian shale, the heterogeneity separation at a distant  
 209  $x_i$  from the coast and a homogeneous recharge  $R$ :

$$\left\{ \begin{array}{l} 0 \leq x \leq x_i \quad h(x) = h_{sea} \sqrt{1 + \frac{R}{K_1} \left(\frac{L}{h_{sea}}\right)^2 \left(\frac{x}{L} - \frac{1}{2} \left(\frac{x}{L}\right)^2\right)} \\ x_i \leq x \leq L \quad h(x) = h_{sea} \sqrt{1 + \frac{R}{K_2} \left(\frac{L}{h_{sea}}\right)^2 \left(\frac{x}{L} - \frac{1}{2} \left(\frac{x}{L}\right)^2\right) + \left(\frac{R}{K_1} - \frac{R}{K_2}\right) \left(\frac{L}{h_{sea}}\right)^2 \left(\frac{x_i}{L} - \frac{1}{2} \left(\frac{x_i}{L}\right)^2\right)} \end{array} \right. \quad (8)$$

210 The head,  $h(x)$ , logically increases from its value at the coast,  $h_{sea}$ , as a square root function of  $x/L$ , a  
 211 dependence characteristic of free aquifers. In the Quaternary sands ( $0 \leq x \leq x_i$ ), it does not depend

212 on  $K_2$ . As the aquifer is not constrained by any interactions with the surface and does not have any  
 213 other outlet than the coast, the same incoming flux accumulated in the Brioverian shale  $R(L-x_i)$  is  
 214 transferred to the Quaternary sands, regardless of the value of  $K_2$ .  $K_1$  can be directly estimated from  
 215 the first equation of (8) as:

$$K_1 = R \frac{\left(\frac{L}{h_{sea}}\right)^2 \left(\frac{x}{L} - \frac{1}{2}\left(\frac{x}{L}\right)^2\right)}{\left(\frac{h(x)}{h_{sea}}\right)^2 - 1} \quad (9)$$

216 leading to a first approximation of  $K_1=17.61 \text{ m.d}^{-1}$  for the configuration given by **Error! Reference**  
 217 **source not found..** It should be noted that this value does not account for multiple important processes  
 218 including the interception of the aquifer water table with the surface, the potential existence of outlets  
 219 at the hydrographic network, which may be quite significant in this area downstream in the  
 220 hydrological system as well as differences between mean head levels and steady state levels, which  
 221 may occur because of the non-linearity of the free aquifer flow equation.

222 Tidal head fluctuations can be approached by the diffusion of the tidal signal within a homogeneous  
 223 confined aquifer given by (Nielsen, 1990) as:

$$h(x,t) = h_{sea} + \frac{A}{2} \cos\left(2\pi \frac{t}{\tau} - \frac{x}{l_c}\right) \exp\left(\frac{-x}{l_c}\right) + \frac{R}{K_1} x \quad \text{with} \quad l_c = \sqrt{(\tau K_1 e)/(\pi S y_1)} \quad (10)$$

224 where  $A$  and  $\tau$  are respectively the amplitude and period of the tidal forcing signal,  $Sy_1$  is the specific  
 225 yield of the Quaternary sands and  $e$  is the mean aquifer thickness.

226 We then use the terms of equation (10) relating to tidal wave propagation to calculate the variance of  
 227 tidal fluctuations  $\sigma_t^2$ :

$$\sigma_t^2 = \int_0^\tau \left[ \frac{A}{2} \cos\left(2\pi \frac{t}{\tau} - \frac{x}{l_c}\right) \right]^2 \exp\left(\frac{-x}{l_c}\right) dt \quad (11)$$

228 Equation (11) provides a new expression for  $l_c$ :

$$l_c = \frac{x}{\ln(A/(2^{3/2}\sigma_t))} \quad (12)$$

229

230 With the bimonthly tidal amplitude  $A = 5.8 \text{ m}$  and assuming (i) that the mean aquifer thickness  $e$  is  
 231 equal to  $h_{sea}$  and (ii) that it is large enough for the confined aquifer assumption to hold for the free  
 232 aquifer conditions, we can derive a first approximation of the specific yield  $Sy_1$  using expressions of  $l_c$   
 233 in both (10) and (12):

$$Sy_1 = \frac{\tau K_1 e}{\pi} \left( \frac{\ln\left(\left(A/(2^{3/2}\sigma_t^{obs})\right)\right)}{x} \right)^2 \quad (13)$$

234 Where we recall that  $\sigma_t$  is the standard deviation of the tidal fluctuations. Using the value of  $K_1$   
235 previously determined, we obtain a value of  $Sy_1$  of 10% ( $Sy_1 = 0.1$ ). As for  $K_1$ , this approximation is  
236 subject to several assumptions. As already mentioned, the free aquifer solution should not be too far  
237 from the confined one. The Brioverian shale of different hydraulic conductivity  $K_2$  and specific yield  $Sy_2$   
238 should also have a small enough influence on the diffusion of the tidal signal. We finally note that,  
239 using these first approximations, the characteristic amplitude of the bi-daily tidal signal would be of  
240 the order of  $10^{-5}$  m, a value that cannot in fact be observed.

241 Using these two analytical solutions, the hydraulic properties of the Quaternary sands can be  
242 approximated under the afore mentioned assumptions. The hydraulic properties of the Brioverian  
243 shales are more difficult to assess as they will influence the seasonal head fluctuations for which, to  
244 the best of our knowledge, no analytical solution is available for heterogeneous aquifers in transient  
245 state. We thus use a simplified numerical model to constrain the hydraulic properties of the Brioverian  
246 shale ( $K_2, Sy_2$ ).

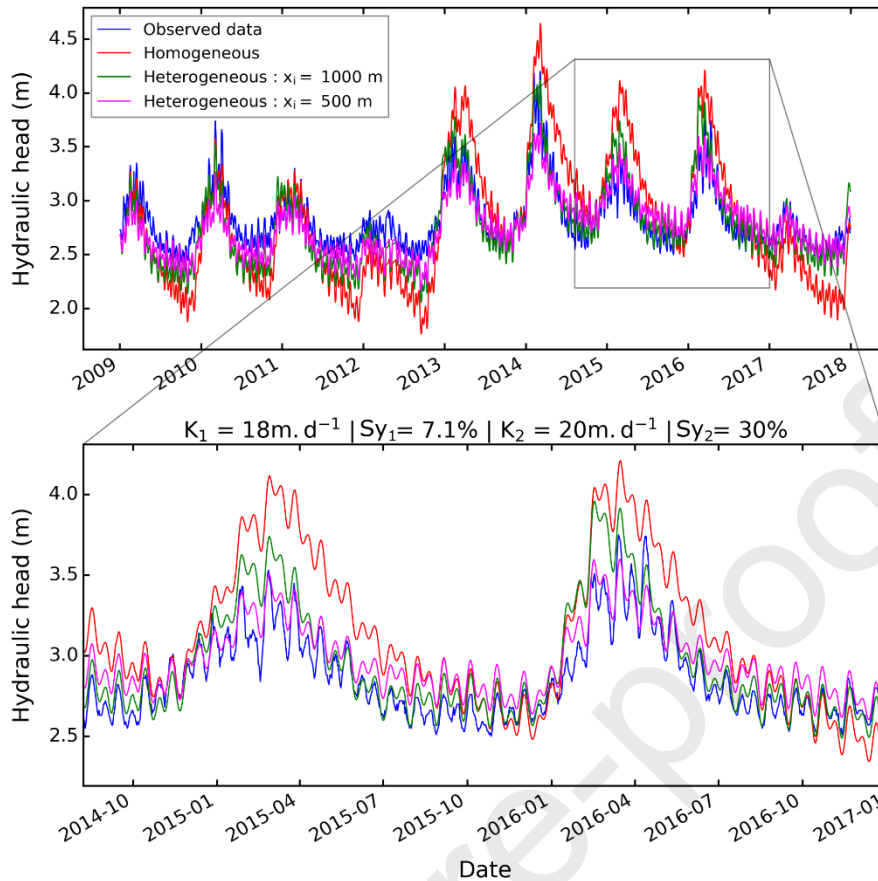
247 Table 2: Hydraulic properties obtained from the analytical, 1D and 2D numerical models.

	<b>Analytical</b>	<b>Numerical 1D</b>	<b>Numerical 1D</b>	<b>Numerical 2D</b>	<b>Numerical 2D</b>	<b>Numerical 2D</b>
<b>Distribution</b>	Homogeneous	Homogeneous	Heterogeneous	Heterogeneous	Heterogeneous	Heterogeneous
<b>Seepage</b>	Not allowed	Not allowed	Not allowed	Not observed	Observed	Observed
$x_i$ (m)	1 000	1 000	1 000	1 000	1 000	500
$K_1$ (m.d <sup>-1</sup> )	18	18	18	18	10 - 17	5.0 - 20
$Sy_1$ (%)	10	7.1	7.1	8.0	4.4 – 7.5	4.4 – 7.5
$D_1$ (m <sup>2</sup> .d <sup>-1</sup> )	$3.5 \cdot 10^3$	$5.2 \cdot 10^3$	$5.2 \cdot 10^3$	$4.5 \cdot 10^3$	$2.6 \cdot 10^3 - 7.7 \cdot 10^3$	$1.3 \cdot 10^3 - 9.0 \cdot 10^3$
$K_2$ (m.d <sup>-1</sup> )			$20 - 1.0 \cdot 10^3$	9.0 - 30	1.0 – 8.0	1.0 - 15
$Sy_2$ (%)			23 - 30	27 - 30	15 – 30	10 - 15
$D_2$ (m <sup>2</sup> .d <sup>-1</sup> )			$1.3 \cdot 10^2 - 8.7 \cdot 10^4$	$6.0^2 - 2.6 \cdot 10^3$	$7.0 \cdot 10^1 - 7.0 \cdot 10^2$	$7.0 \cdot 10^1 - 1.2 \cdot 10^3$

### 249 3.2. Constrains on Brioverian shale hydraulic properties with a 1D numerical model

250 To complete the identification, we set up a simplified 1D free aquifer perpendicular to the shoreline  
251 having the same characteristic as the one presented in the previous subsection. The head is fixed at  
252 the coast by the tidal signal (Figure 3, light blue curve). The recharge applied uniformly on the top of  
253 the model is taken from the SURFEX reanalysis (Figure 3, red curve). A no-flow boundary condition is  
254 applied upstream at  $x=L$  to represent the groundwater divide at the watershed limit. The minimal  
255 aquifer thickness is set at its value at the coast ( $h_{\text{sea}}=20$  m). The free-flow model is carried out using  
256 MODFLOW NWT (Harbaugh, 2005; Niswonger et al., 2011) with 1-meter-wide mesh cells and daily time  
257 steps. The initial head values are set to the steady-state solution obtained from the mean recharge  
258 and sea level.

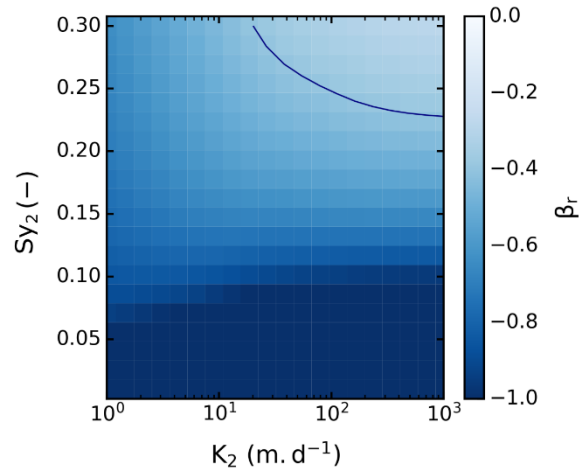
259 We first and synthetically evaluate the quality of the approximations given by the previous analytical  
260 solutions with a homogeneous numerical model with the values of  $K_1$  and  $Sy_1$  obtained previously by  
261 the analytical solutions. Results give values of  $\alpha = 0.014$  and  $\beta_t = 0.013$ , showing indeed close  
262 agreements. Calibrating directly with the numerical model instead of the analytical solutions following  
263 the same procedure would lead to close values  $K_1=18.33$  m.d<sup>-1</sup> and  $Sy_1=7.1\%$ . The relevance of the  
264 analytical solution was expected for the mean head. It is more conclusive on the confined assumption  
265 for the tidal fluctuations. Even though the homogeneous model captures well the mean head and the  
266 tide-induced signal (red curve), it remains far from the observed signal (blue curve, Figure 5). Seasonal  
267 variations are too large. For some of the later years (2013-2017), winter levels are overestimated by  
268 0.2-0.5 meters. For the earlier years (2009-2012) and the last year 2018, summer recessions are  
269 underestimated by around half a meter. It shows that the model calibrated on the mean level and on  
270 the tidal variations displays too large seasonal variations. In other words, the response to the tidal  
271 fluctuations and the mean level imposes that the aquifer is not capacitive enough to buffer the  
272 seasonal variations of recharge shown by the observations. We provide additional details in Section 5  
273 regarding the utilization of the earlier identification and comparison as a homogeneity test.



274

275 *Figure 5: Comparison of the hydraulic head chronicle observed at the Gouville piezometer shown by the*  
 276 *red point on Figure 1 (blue curve) with the results obtained by the 1D homogeneous analytical solution*  
 277 *(red curve), the 1D heterogeneous numerical model (green curve) and the 1D heterogeneous model*  
 278 *with the position of the interface closer at  $x_i=500$  m (pink curve). Model parameters are given in Table*  
 279 *2.*

280 We set up a heterogeneous model, derived from the homogeneous model, to accurately capture  
 281 seasonal variations while maintaining the calibration of the mean hydraulic head and tidal fluctuations.  
 282 To this end, we perform a sensitivity analysis of the recharge variations criterion  $\beta_r$  as a function of  $K_2$   
 283 and  $Sy_2$  at fixed values of the Quaternary sand hydraulic properties  $K_1$  and  $Sy_1$ , those values obtained  
 284 with the analytical solutions (Figure 6). The range of values of  $K_2$  is limited to a minimum value of  
 285  $20 \text{ m.d}^{-1}$  to restrain the piezometric values below the topography and avoid any significant seepage  
 286 not accounted by this simplified model. Results do not show a well-targeted minimum but a zone of  
 287 lower  $\beta_r$  values. Using a limit of 0.3 for  $\beta_r$ , the top right corner of Figure 6 limited by the blue line  
 288 corresponds to a narrow range of specific yield ( $Sy_2=23\text{-}30\%$ ) and a large range of hydraulic  
 289 conductivities ( $K_2=20\text{-}10^3 \text{ m.d}^{-1}$ ). For this range of values, the values of  $\alpha$  and  $\beta_r$  remain smaller in  
 290 absolute values to 0.1 (more precisely  $\alpha=0.02\text{-}0.05$  and  $\beta_r=0.08\text{-}0.1$ ) justifying the approach to first  
 291 determine  $K_1$  and  $Sy_1$  before looking for constraints on  $K_2$  and  $Sy_2$ . Seasonal variations are thus reduced  
 292 when  $Sy_2$  is significantly increased to 23-30% while the hydraulic conductivity is not limiting as long as  
 293 it remains larger than  $20 \text{ m.d}^{-1}$ . Variations are thus reduced thanks to the creation of an upstream  
 294 aquifer that is sufficiently capacitive to buffer the recharge signal as strongly as possible. Even with the  
 295 highest values of specific yield, however,  $\beta_r$  does not converge to zero. The upstream aquifer is too far  
 296 from the piezometer (600 m) to exert a strong influence on the seasonal variations. This and the  
 297 specific yield values found in the most upper part of possible values for shales indicate that the  
 298 interface between the geological units might be effectively closer to the piezometer than shown by  
 299 the geological map.

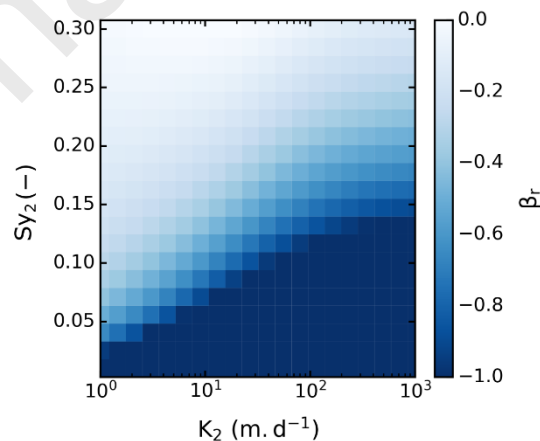


300

301 *Figure 6: Sensitivity analysis of the  $\beta_r$  criterion as a function of the Brioverian shale hydraulic*  
 302 *conductivity  $K_2$  and specific yield  $Sy_2$  ( $x_i=1000$  m).*

### 303 **3.3. Role of the position of the geological interface between the Quaternary sands** 304 **and Brioverian shales**

305 We repeat the previous method with an interface between Quaternary sands and Brioverian shales no  
 306 longer at  $x_i=1000$  m but at  $x_i=500$  m to determine to what extent such a configuration would enable a  
 307 better calibration of the piezometric signal with lower shale specific yield values.  $K_1$  and  $Sy_1$  are kept  
 308 equal to their previously determined values.  $\beta_r$  is shown as a function of  $K_2$  and  $Sy_2$ . It shows a better-  
 309 defined range of minimal values close to 0. It also leads to smaller specific yields  $Sy_2$  of 10-15 % more  
 310 in agreement with fractured shales. The hydraulic conductivity  $K_2$  remains poorly defined. The absolute  
 311 values of  $\alpha$  and  $\beta_t$  remain smaller than 0.1 (more precisely  $\alpha=0.02-0.05$  and  $\beta_t=0.08-0.1$ ). Even closer  
 312 to the piezometer, the upstream aquifer has only a minor influence on the average head and tidal  
 313 fluctuations. It still justifies the approach to first determine  $K_1$  and  $Sy_1$  before looking for constraints  
 314 on  $K_2$  and  $Sy_2$ . Seasonal variations in hydraulic head also suggest that the upstream aquifer is closer  
 315 than indicated on the geological map (Dupret et al., 1989).



316

317 *Figure 7: Sensitivity analysis of the  $\beta_r$  criterion as a function of the Brioverian shale hydraulic*  
 318 *conductivity  $K_2$  and specific yield  $Sy_2$  ( $x_i=500$  m).*

319 These results are surprising since, first, Quaternary sands are expected to be more porous and  
 320 permeable than Brioverian shales and second, the lithological interface is indicated further away from  
 321 the piezometer. Nonetheless, additional information supports the potential existence of highly



322 permeable formations East of the Quaternary sands. First, several boreholes at the study site show the  
323 existence of coarse sands containing pebbles beneath Quaternary eolian sands (Borehole file  
324 BSS000KUVT, 2017). Those coarse sands are probably Eemian sands (Dissler et al., 1988; Dupré et al.,  
325 1990), potentially extending further East and forming a more capacitive aquifer upstream. Second, a  
326 fault was observed and mapped 1.5 km east of the piezometer (Dupret et al., 1987; Rolet et al., 1994),  
327 oriented towards it and probably extending in its direction. This fault facilitates hydraulic connection  
328 between the low-permeability Brioverian shales and the lower Brioverian formations, which are known  
329 to be much more weathered and permeable. The presence of this fault in our study site, extending  
330 towards our observation point, could also explain the results indicating a closer interface. Finally, three  
331 boreholes drilled in the study area close to the coast show shales at depths averaging 6 m, contributing  
332 to explain the lower specific yield in zone 1 (Borehole file BSS000KUVT, 2017). Moreover, hydraulic  
333 tests performed in these boreholes give hydraulic conductivities of 7.5 to 22 m.d<sup>-1</sup> and specific yields  
334 of 4 to 15% confirming the ranges of values globally obtained for both formations (Table 2).

## 335 **4. Effects of spatialization and surface-subsurface interactions**

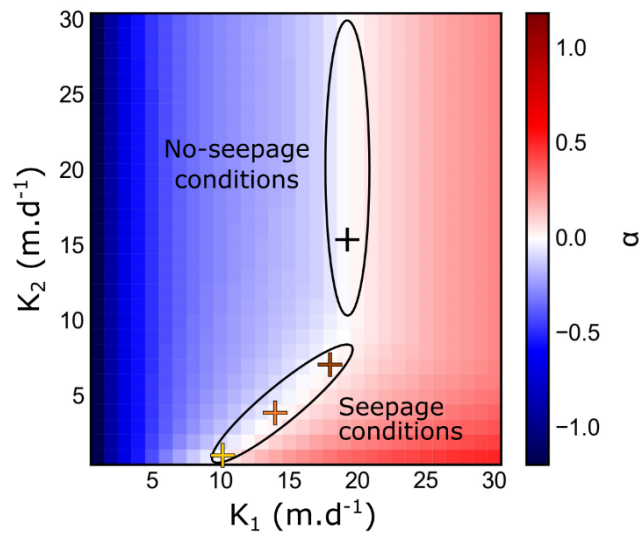
336 We investigate the specific effects of spatialization and of surface/subsurface interactions on the flow  
337 structures and identification process. To this end, we develop a more comprehensive 2D model,  
338 identify the hydraulic properties, and determine the similarities and differences with the properties  
339 identified in the previous section.

### 340 **4.1. 2D model characteristics and implementation**

341 The 2D model geometry is extracted from a 25-meter resolution DEM using HydroModPy, a Python  
342 toolkit allowing building MODFLOW models from GIS files (Gauvain et al., 2024, in prep.). The modelled  
343 area is a rectangular zone of 1 kilometer North-South width, extending 3.3 kilometers East  
344 perpendicular to the shoreline (black rectangle, Figure 2). The model has a square mesh configuration,  
345 a lateral resolution of 25 meters, and a single layer. Bottom of the model is at the constant elevation  
346 of -20 meters. Elevation of the model is ranging from 0 to 25 meters, corresponding to the DEM  
347 topography (Figure 1). Flows are computed with MODFLOW NWT using the same initial and boundary  
348 conditions as in the previous 1D model case at a daily time step. Initial conditions are defined after  
349 running the model in steady state using the mean recharge over the two years preceding the  
350 calibration year. Recharge is imposed homogeneously to the whole domain. Seepage is modelled using  
351 the DRAIN package (Harbaugh, 2005) and allows water to flow out of the aquifer when hydraulic head  
352 intersects topography. We take two assumptions for the location of the interface between Quaternary  
353 sand and Brioverian shale hydrogeological zones. The first one is based on the geological map and  
354 cross-section (Figure 2) at a distance  $x_i=1\ 000$  m from the coast. The second one is set closer to the  
355 coast at  $x_i=500$  m, based on the previous section findings.

### 356 **4.2. Hydraulic conductivities as determined by the mean hydraulic head**

357 We first analyze the dependence of the  $\alpha$  performance criterion (5) for the original position of the  
358 interface ( $x_i=1000$  m) with the Quaternary sands and Brioverian shale hydraulic conductivities  $K_1$  and  
359  $K_2$ . Instead of the mean hydraulic head, we use as a proxy the hydraulic head obtained in steady state.  
360 Indeed, complementary analyses show only marginal differences of  $\alpha$  values between them for the  
361 range of  $K_1$  and  $K_2$  values investigated. Results are obtained by an exploration on a 30 by 30 grid of  
362 regularly spaced value for  $K_1$  and  $K_2$  taken in the range of values identified by the 1D model (Figure 8).  
363 Optimal values of  $\alpha$  (white cells) are composed of two sections.



364

365 *Figure 8: Model to data comparison of steady-state hydraulic heads as measured by  $\alpha$  (equation (5))*  
 366 *for the 2D model ( $x_i=1000$  m). Crosses mark the  $(K_1, K_2)$  couples for which specific yields will be*  
 367 *calibrated with the response to the tidal and seasonal variations: yellow (10 m.d<sup>-1</sup>, 1 m.d<sup>-1</sup>), orange (14*  
 368 *m.d<sup>-1</sup>, 4 m.d<sup>-1</sup>), brown (17 m.d<sup>-1</sup>, 6.5 m.d<sup>-1</sup>), black (18 m.d<sup>-1</sup>, 15 m.d<sup>-1</sup>).*

369 The first section of optimal  $\alpha$  values is obtained for values of  $K_1=18$  m.d<sup>-1</sup> and  $K_2$  higher than 8 m.d<sup>-1</sup>.  
 370 For those simulations, it has been checked that seepage only occurs marginally in the modelled area.  
 371 This domain of  $(K_1, K_2)$  solutions is thus identified as the “no-seepage conditions” (Figure 8). It matches  
 372 the solutions obtained for the analytical and 1D numerical models.  $K_1$  is close at 10% to the analytical  
 373 solution, a good approximation given the coarse resolution of the exploration.  $K_2$  remains  
 374 unconstrained as long as it is high enough. The steady state piezometric level allows to identify the  
 375 Quaternary sands hydraulic conductivity  $K_1$ .

376 In the second section identified as the “seepage conditions” (Figure 8), the steady state piezometric  
 377 level depends not only on the Quaternary sand conductivity  $K_1$  but also on the Brioverian shale  
 378 conductivity  $K_2$ .  $K_1$  values range from 10 to 18 m.d<sup>-1</sup> and  $K_2$  from 1 to 8 m.d<sup>-1</sup>. Any reduction in  $K_1$  must  
 379 be matched by an equivalent reduction in  $K_2$ . To keep the same hydraulic head at the observation  
 380 piezometer, the lower capacity of the Quaternary sands to transmit the incoming flows to the sea  
 381 should be matched by lesser incoming flows and more seepage in the Brioverian shales. In such cases,  
 382 the mean hydraulic head constrains a relation between both hydraulic conductivities, which happens  
 383 to be linear in this case.

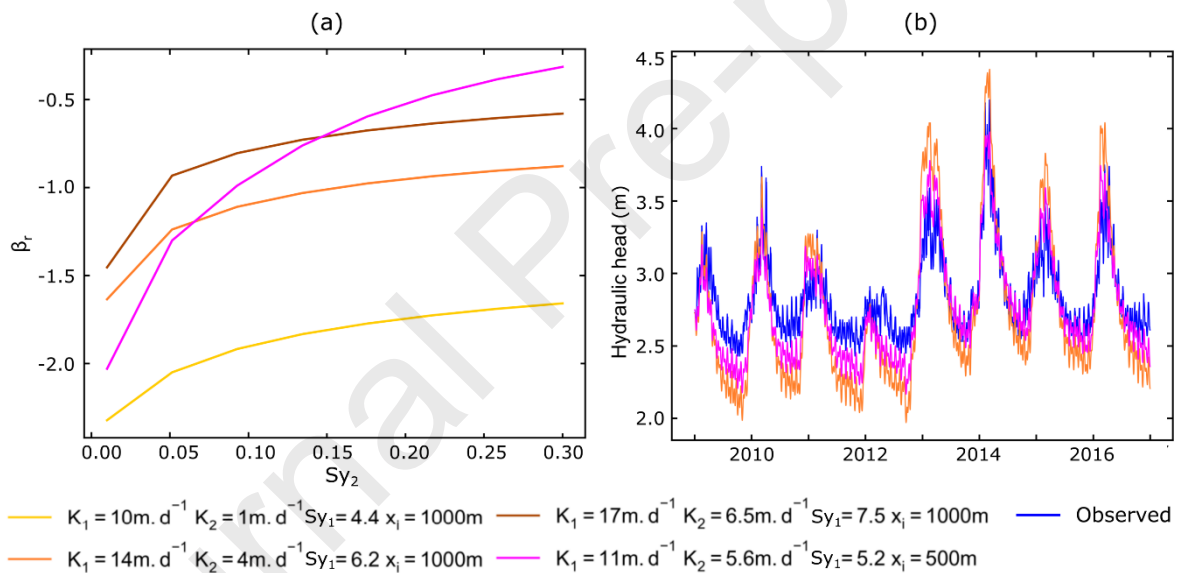
384 A similar pattern is obtained regarding the spatial distribution of  $\alpha$  values for the closer interface  
 385 location ( $x_i=500$  m). In this case, no-seepage conditions are restricted to  $K_1=22$  m.d<sup>-1</sup> and  $K_2$  higher than  
 386 15 m.d<sup>-1</sup>. The seepage conditions are obtained for lower  $K_1$  values ranging from 5 to 22 m.d<sup>-1</sup> and  $K_2$   
 387 values ranging from 1 to 15 m.d<sup>-1</sup>. Lower  $K_1$  values are explained by the larger groundwater seepage  
 388 area occurring in the Brioverian shale zone that is made 500 m wider. Indeed, this extension causes  
 389 more seepage and thus less water income to the Quaternary sand zone where the piezometer is  
 390 located. Lower  $K_1$  values are needed to counterbalance this smaller upstream groundwater flow.

### 391 4.3. Specific yields as determined by tidal fluctuations and seasonal variations

392 Simulations are run in transient state to explore the dependence of  $\beta_t$  and  $\beta_s$  with  $Sy_1$  and  $Sy_2$ . Hydraulic  
 393 conductivity  $K_1$  and  $K_2$  are set to their values identified in the previous step at the places identified by  
 394 crosses in Figure 8.

395 For the no-seepage conditions in the  $x_i=1\ 000\text{ m}$  case, we explore  $\beta_t$  and  $\beta_r$  over a 7 by 7 grid of specific  
 396 yield values  $Sy_1$  and  $Sy_2$ . Results are qualitatively similar to those obtained with the 1D model.  $\beta_t$   
 397 remains independent of  $Sy_2$  and leads to  $Sy_1$  value of 8%. For this value of  $Sy_1$ , the simulation of the  
 398 seasonal fluctuations imposes values of  $Sy_2$  in the higher range of values (27-30%) with associated  
 399 absolute  $\beta_r$  values ranging from 0.42 to 0.46. Comparison with the 1D model (Table 2) shows that the  
 400 identified values are close at 12 % for  $Sy_1$  and 15 % for  $Sy_2$ . In the absence of significant seepage, the  
 401 1D model can thus be used for the hydraulic parameter identification.

402 In the seepage conditions, we analyze the 3 cases marked by the crosses for the  $x_i=1000\text{ m}$  interface  
 403 case. As diffusivity of the Quaternary sands has been reported to be conserved in all previous cases  
 404 (Table 2), we set  $Sy_1$  to keep this same diffusivity ( $D_1=4.5\ 10^3\text{ m}^2.\text{d}^{-1}$ ). The resulting models still match  
 405 the tidal fluctuations whatever the investigated values of  $Sy_2$ , with  $\beta_t$  remaining lower than 0.28. With  
 406  $Sy_1$  respecting this constraint, the seasonal variations remain large whatever the value of  $Sy_2$  ( $\beta_r$   
 407  $< -0.5$ ) and even quite larger than in the absence of seepage (Figure 9a). The head variations remain  
 408 far from the observed ones especially in the recession and flooding periods (Figure 9b). The occurrence  
 409 of seepage limits even more the reduction of the seasonal variations. This can be explained by a partial  
 410 disconnection of the upstream and downstream zones by the seepage process, which limits the  
 411 influence of the hydraulic properties of the Brioverian shales. To counteract this effect, the interface  
 412 should be positioned even closer to the piezometer than in the no-seepage conditions.



413

414 *Figure 9: (a) Model to data comparison of the seasonal variations characterized by  $\beta_r$  as a function of*  
 415 *the Brioverian shale specific yield  $Sy_2$  for the three cases identified by crosses in Figure 8 within the*  
 416 *seepage conditions section.  $x_i=1000\text{ m}$  (yellow, orange and brown) and  $x_i=500\text{ m}$  (pink). Quaternary*  
 417 *sand specific yield  $Sy_1$  is fixed to keep the diffusivity determined in section 3.1 by the analytical solution.*  
 418 *(b) Simulated hydraulic heads obtained for corresponding simulations with Brioverian shale specific*  
 419 *yield  $Sy_2=30\%$ .*

420 The closer interface case ( $x_i=500\text{ m}$ ) gives better results, with  $\beta_r$  values closer to zero (Figure 9a). In  
 421 this latter configuration, the 3 performance criteria  $\alpha$ ,  $\beta_r$  and  $\beta_t$  can still be met simultaneously,  
 422 allowing to represent the main trends of the hydraulic head chronicle (Figure 9b, pink curve). Several  
 423 types of geological information can explain our hypothesis of a closer interface. As presented by  
 424 section 3.3, this can be due to lithological variations (Dissler et al., 1988; Dupré et al., 1990) or fault  
 425 hydraulic connection (Dupret et al., 1987; Rolet et al., 1994). Indeed, the bedrock of the study site is  
 426 polyphase and abundantly faulted, and uncertainties persist as to the precise characteristics of its  
 427 depth and nature.

## 428 5. Discussion

429 We propose to synthesize the parameter identification methods previously illustrated on the Gouville  
430 hydraulic head chronicle. The aim is to show how these methods can be applied to piezometric signals  
431 exhibiting both tidal fluctuations and seasonal variations in cases where (i) heterogeneity occurs  
432 between two geological formations separated by an interface globally aligned with the coast and (ii)  
433 the topographical gradient does not change much along the coast. The first step is to determine  
434 whether the aquifer formation is heterogeneous, by means of a homogeneity test (section 5.1). If  
435 heterogeneity is confirmed, the subsequent step is to define an identification method based on  
436 approaches that are as accessible as possible without requiring time-consuming calibration operations  
437 (section 5.2). We conclude by analyzing the significance of heterogeneity on the coastal vulnerability  
438 to groundwater flooding (section 5.3).

### 439 5.1. Homogeneity test

440 The homogeneity test is designed to determine whether the three components of the piezometric  
441 signal (mean hydraulic head, tidal fluctuations and seasonal variations) can be obtained simultaneously  
442 with a homogeneous model. The test can only be carried out in cases for which the interactions  
443 between surface and subsurface are sufficiently limited and do not require advanced spatial  
444 representation of the seepage. The test is performed in two steps, based on the decomposition of the  
445 piezometric signal into its three components using equations (1), (2), (3) and (4). In the first step,  
446 hydraulic conductivity and specific yield are obtained respectively from mean hydraulic head and tidal  
447 fluctuations, using the two analytical solutions given by equations (9) and (13). In the second step, a  
448 1D numerical model is developed with these two values of hydraulic conductivity and specific yield.  
449 The analytically calibrated model then undergoes a validation procedure, based on available sea-level  
450 and recharge data. The simulated seasonal variations are compared with the observed signal using the  
451 ratio of their variability given by  $\beta_r$ . If  $\beta_r$  is sufficiently close to 0, the homogeneity test is positive and  
452 the hydraulic parameters (conductivity and specific yield) as provided by the two analytical solutions  
453 can be applied to the whole domain to simulate hydraulic head variations.

### 454 5.2. Identification of the heterogeneous hydraulic properties

455 When the three components of the piezometric signal cannot be properly simulated using a  
456 homogeneous model, the identification method depends on whether seepage is significant. If seepage  
457 is not significant, the hydraulic conductivity and specific yield of the geological formation close to the  
458 coast can be approximated by their values provided by analytical solutions, based on average head and  
459 tide-induced fluctuations. As the hydrodynamic properties determined this way allow proper  
460 simulation of mean value and tidal fluctuations of hydraulic head, they can be assigned to the near-  
461 shore aquifer formation. The calibration of the seasonal variations (using  $\beta_r$  performance criterion)  
462 offers a way to identify some constraints on the hydraulic properties of the far-from-shore aquifer  
463 formation. Several identification methods can be used to explore the two-dimensional parameter  
464 space formed by its hydraulic conductivity and specific yield. If solutions can effectively be found, it  
465 makes sense to get a relationship between properties rather than a single pair of values, since only  
466 one constraint is available. In the absence of clear optimal solutions provided by parameter  
467 exploration, several causes can be investigated. As for the case presented above, the interface may  
468 have been misplaced, making the simulated piezometric signal too insensitive to the far-from-shore  
469 geological formation.

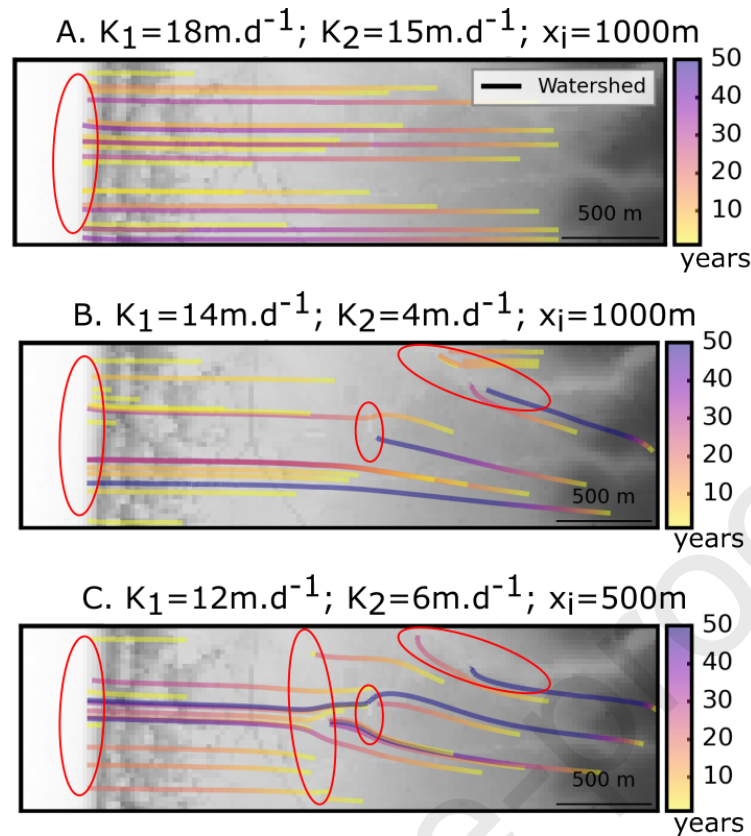
470 Interactions with the surface can impose boundary conditions that limit or, on the contrary, increase  
471 seasonal variations. This is especially the case when groundwater seepage occurs. In such cases, the  
472 identification method is different since the mean hydraulic head depends on hydraulic conductivity of

473 both proximal and distal geological formations. Indeed, low upstream hydraulic conductivity values  
474 can cause important seepage, leading to reduced downstream heads, which can in turn be  
475 counterbalanced by reduced hydraulic conductivity values, as shown in section 4.2. The relation  
476 between hydraulic conductivities can be obtained from the average hydraulic head using a transient  
477 model or a steady-state model if the steady-state hydraulic head can be shown to be close to the  
478 steady-state solution. For each identified valid couple of hydraulic conductivities (providing low  $\alpha$   
479 values), the specific yields can be determined by using the tidal and seasonal variations as shown in  
480 section 4.3, assuming that their effect on the mean hydraulic head remains limited.

### 481 **5.3. Seepage areas and vulnerability to aquifer-induced flooding**

482 From a single piezometer data, we infer the possible values of hydraulic conductivity of both  
483 Quaternary sands and Brioverian shales. Those values define two main flow regimes, associated to  
484 variable groundwater seepage occurrence. In this section, we discuss to what extent our methodology  
485 of heterogeneous aquifer property investigation can provide insights on a major issue of some coastal  
486 areas that is groundwater-induced flooding. To this end, we use the MODPATH particle tracking  
487 module (Pollock, 2016) to analyze the spatial variability of seepage areas. Seepage area location is  
488 controlled by time-variant boundary conditions (sea-level, recharge), as well as aquifer properties.  
489 Figure 10 shows the resulting flow lines and seepage areas for steady-state simulations using mean  
490 observed values of sea-level and recharge rate, and implementing previously inferred values of aquifer  
491 properties.

492 The first simulation (A.) corresponds to the no-seepage conditions (black cross on Figure 8). Associated  
493 results show seepage areas only at the shoreline. Groundwater flowlines go straight from the  
494 Brioverian foothill to the sea, indicating no surface/subsurface interaction. The second simulation (B.)  
495 corresponds to the seepage conditions as defined in section 4.2 (orange cross on Figure 8). Due to the  
496 lower hydraulic conductivity  $K_2$ , the water table rises up to the surface. While shoreline seepage areas  
497 are maintained (with lower rates), additional seepage areas show up along the low-lying points of the  
498 sea marsh. Some of the groundwater pathlines end up in these seepage areas, instead of flowing  
499 straight to the sea. The third simulation (C.) corresponds to seepage conditions with a lithological  
500 interface located at  $x_i=500$  m, i.e. closer to the shoreline. In this configuration, a larger zone of the  
501 modelled area is associated to low  $K_2$  values, leading to new seepage areas extending West and  
502 reinforcing surface-subsurface interactions.



503

504 *Figure 10: Seepage areas identified by red ellipses and main groundwater time pathlines for different*  
 505 *conditions.*

506 Land vulnerability to aquifer-induced flooding can be described as the likelihood of terrains to be part  
 507 of seepage areas (i.e. to be subject to flooding due to the groundwater rise), or to show high  
 508 groundwater levels (i.e. having water table at small depths). This analysis shows that a proper  
 509 identification of hydrodynamic parameter values is necessary to assess this vulnerability. Indeed, if  
 510 coastal groundwater level is linked to recharge rate, sea level and geomorphology, it is eventually  
 511 controlled by aquifer hydraulic properties. Our work shows that, in a heterogeneous aquifer made up  
 512 of two zones, the hydraulic conductivities of both zones control the mean hydraulic head. Hydraulic  
 513 conductivity controls the capacity of groundwater to drain incoming recharge to the sea and thus its  
 514 mean level. Low hydraulic conductivity values in the upstream zone can cause important groundwater  
 515 rise, leading to seepage areas and enhanced vulnerability. In association to hydraulic conductivity,  
 516 specific yield also impacts land vulnerability, as it controls the amplitude of the water table variations.  
 517 Lower conductivity increases the water table fluctuations and its probability to generate seepage  
 518 areas. Close to the shore, lower specific yield values also lead to increased diffusivity and thus to higher  
 519 tide-induced water table rise (Haehnel et al., 2023).

520 Identifying hydraulic parameters is essential to assess coastal vulnerability to aquifer saturation and  
 521 the induced risks on several types of infrastructure, even before reaching the surface. Buildings can  
 522 crack if water table fluctuations reach swelling clay, and water can rise up the walls by capillary action,  
 523 producing saltpeter (by bringing minerals from the soil, and drying back) and potentially leading to  
 524 sanitary issues. Farmlands can also be impacted by groundwater rise, with various effects such as  
 525 lowered bearing capacity of the soil, or disturbed root systems. Buried networks are also vulnerable to  
 526 groundwater rise, with damage such as electric wires corrosion, water supply breaking, or  
 527 groundwater intrusion into sewage networks leading to water treatment plant bypass.

528 In some cases, analytical and numerical solutions can yield various combinations of hydrodynamic  
529 properties, both in terms of values and spatial heterogeneity. In such configurations, seepage areas  
530 can be an efficient complementary observation to calibrate the models, as proposed in previous works  
531 (Abhervé et al., 2023).

## 532 **6. Conclusion**

533 We propose a new method for identifying the hydraulic conductivity and specific yield of  
534 heterogeneous coastal aquifers using time series of hydraulic heads observed in an isolated  
535 piezometer showing clear sensitivity of both marine and continental stresses. The method is based on  
536 the interpretation of three components of hydraulic head signal: weekly fluctuations, seasonal  
537 variations and multi-year mean levels. In order to calibrate hydraulic conductivity and specific yield  
538 values of the two zones that make up the main aquifer terrains, we define new performance criteria.  
539 We show that the average hydraulic head depends on the hydraulic conductivity of terrains and on the  
540 recharge rate. Weekly fluctuations are essentially determined by the diffusivity of formations between  
541 the coast and the piezometer. Seasonal variations are mainly controlled by the hydraulic properties of  
542 the upstream zone further away from the coast. In the absence of groundwater seepage, this method  
543 uses analytical solutions and numerical models. In the case of significant seepage, more advanced  
544 models must be used to separate the effect of heterogeneity from the effect of interactions between  
545 surface and subsurface.

546 Our method fundamentally relies on time-series approaches and multistress analyses to enhance  
547 characterization of groundwater systems in coastal areas with limited availability of hydrogeologic  
548 information. While other approaches analyze hydraulic response to multiple stresses to better  
549 understand groundwater level fluctuations (Bakker and Schaars, 2019; Yang and McCoy, 2023), we  
550 analyze this response to infer some essential information on hydrodynamic properties heterogeneity.  
551 Our method can be applied to any coastal site with an observation piezometer sensitive to both  
552 continental and marine stresses, and an identified lithological interface defining the heterogeneity  
553 location. Depending on the occurrence of surface/subsurface interactions, hydraulic properties can be  
554 identified using simplified 1D models or more complex spatialized 2D models. If the data do not allow  
555 to fully constrain hydraulic properties, a complementary calibration procedure can be performed using  
556 the seepage areas, assuming that they can be identified in the field. Conversely, if head data allow to  
557 identify hydraulic properties, seepage areas can be modelled using our method. This approach can  
558 have useful applications linked to surface/groundwater interactions in coastal contexts, such as  
559 groundwater flooding of low-lying areas or seawater intrusions.

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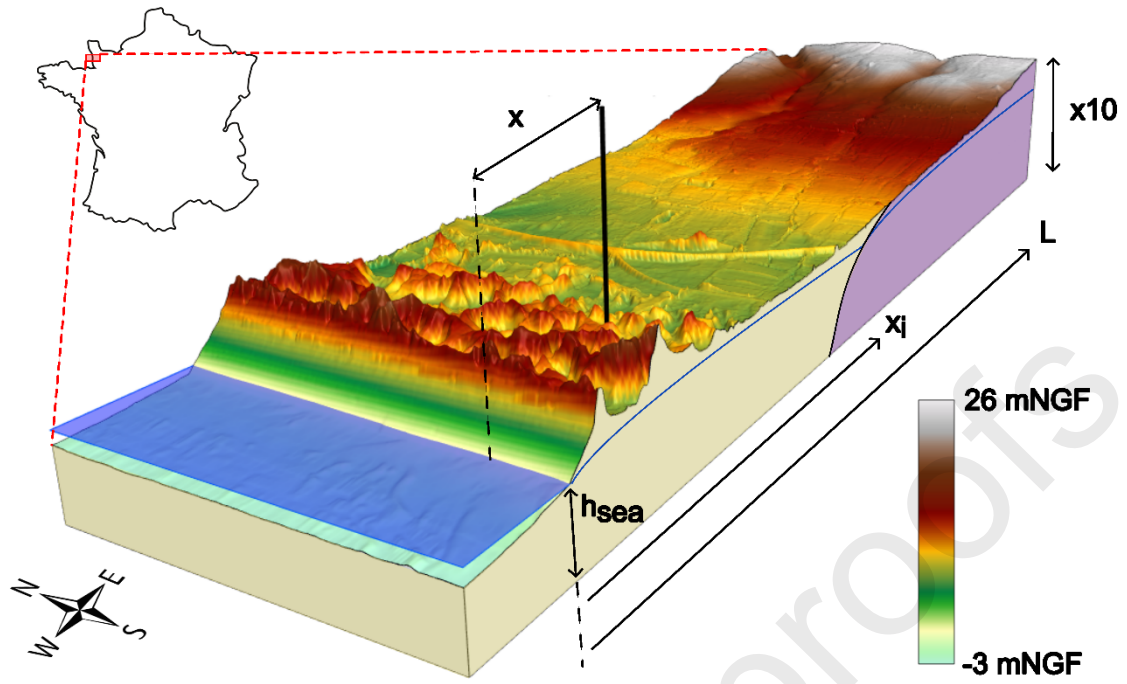
695 We propose a new method for identifying the hydraulic properties of coastal aquifers based on their  
696 response to continental and marine influences observed from isolated piezometers displaying both  
697 tidal and seasonal fluctuations. From a single piezometer, a first approximation of hydraulic  
698 conductivity and porosity can be derived analytically from the mean hydraulic head and its tidal  
699 fluctuations. If this approximation also allows a correct simulation of seasonal head variations, the  
700 aquifer can be modelled as homogeneous. Otherwise, the seasonal head variations provide constraints  
701 on the heterogeneity of hydraulic properties. This new method is applied to a coastal aquifer in  
702 Normandy, formed by a relatively flat, kilometer-wide coastal strip of Quaternary sands followed by a  
703 foothill of higher Brioverian shales. Hydraulic head variations monitored daily for 8 years in a  
704 piezometer located in the Quaternary sand formation enable us to constrain their hydraulic  
705 conductivity (5-20 m.d<sup>-1</sup>) and porosity (7-10 %) within restricted ranges. They also suggest the  
706 existence of a significantly more porous formation (15-30%) upstream of the observation piezometer,  
707 which could consist of more porous sands or fractured shales. In the case of limited surface-subsurface  
708 interactions, the identification method relies on a step-by-step combination of analytical solutions and  
709 simplified 1D numerical models. When more important surface-subsurface interactions are involved,  
710 a spatialized 2D model is used, that allows the analysis of seepage areas. Based on this case study, we  
711 gradually introduce 1D and 2D approaches, and discuss their applicability. We finally illustrate one  
712 major application of this approach by analyzing the interest of aquifer properties investigation on  
713 groundwater-induced flooding vulnerability.

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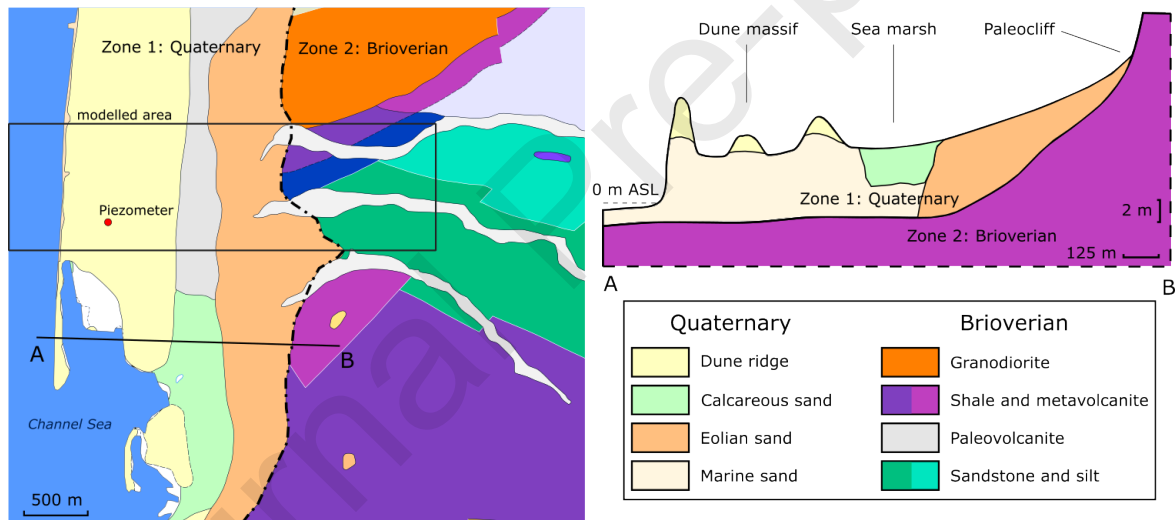
- 715 - Piezometric variations are linked to tidal fluctuations and recharge variations.
- 716 - Hydraulic conductivity and specific yield calibrated using multistress aquifer response.
- 717 - Heterogeneous hydraulic properties are identified from an isolated piezometer.
- 718 - Coastal groundwater flooding vulnerability is assessed using seepage areas analysis.

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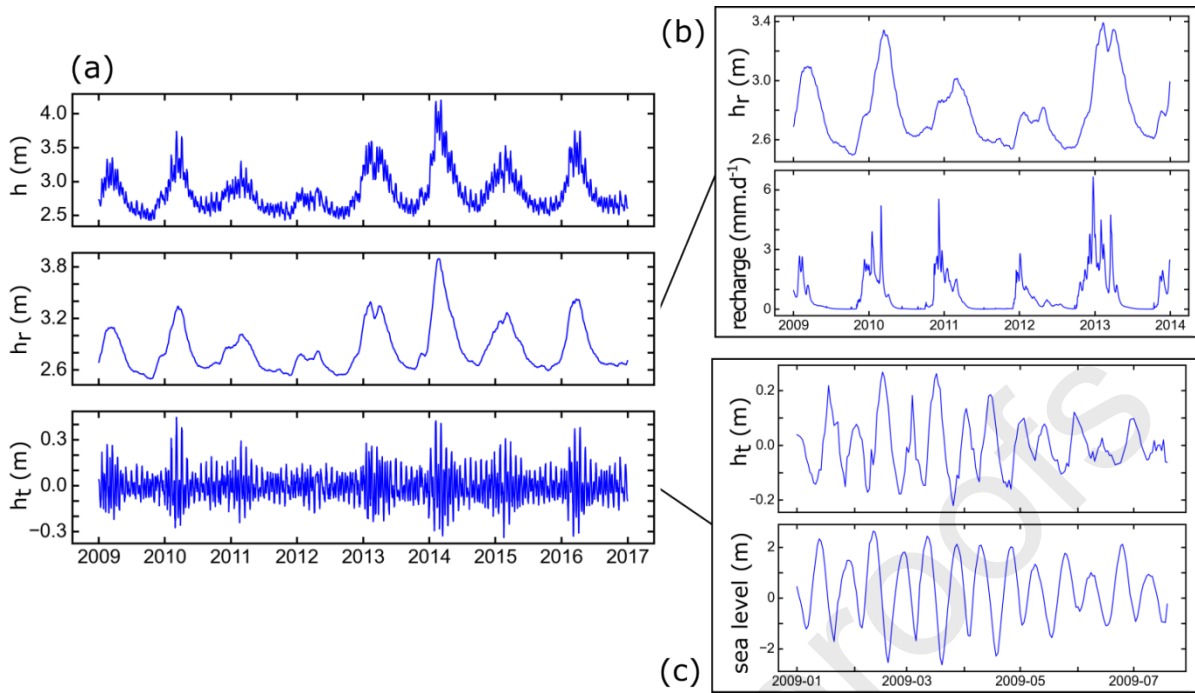
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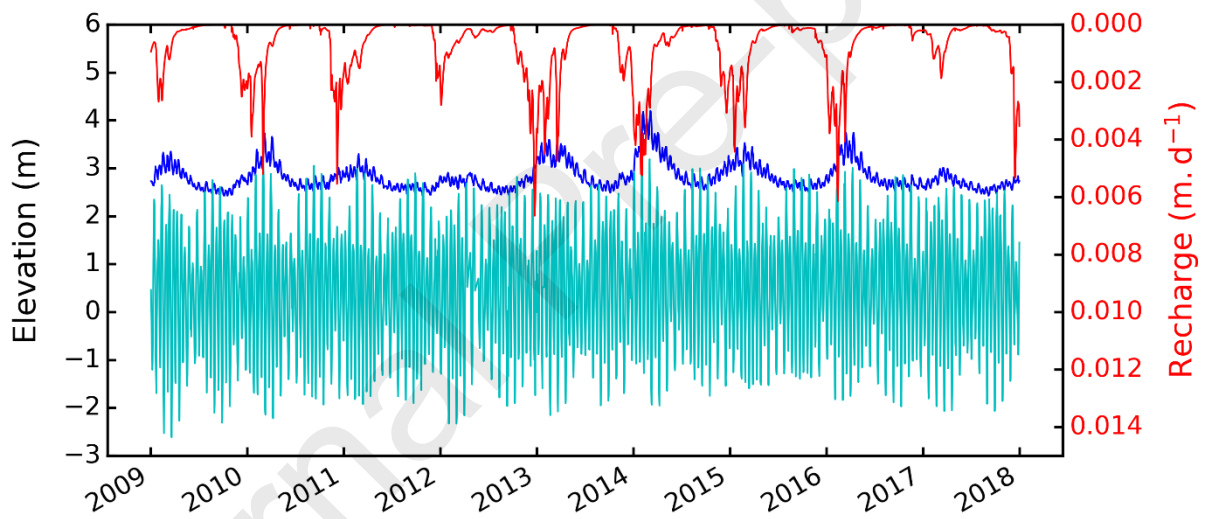
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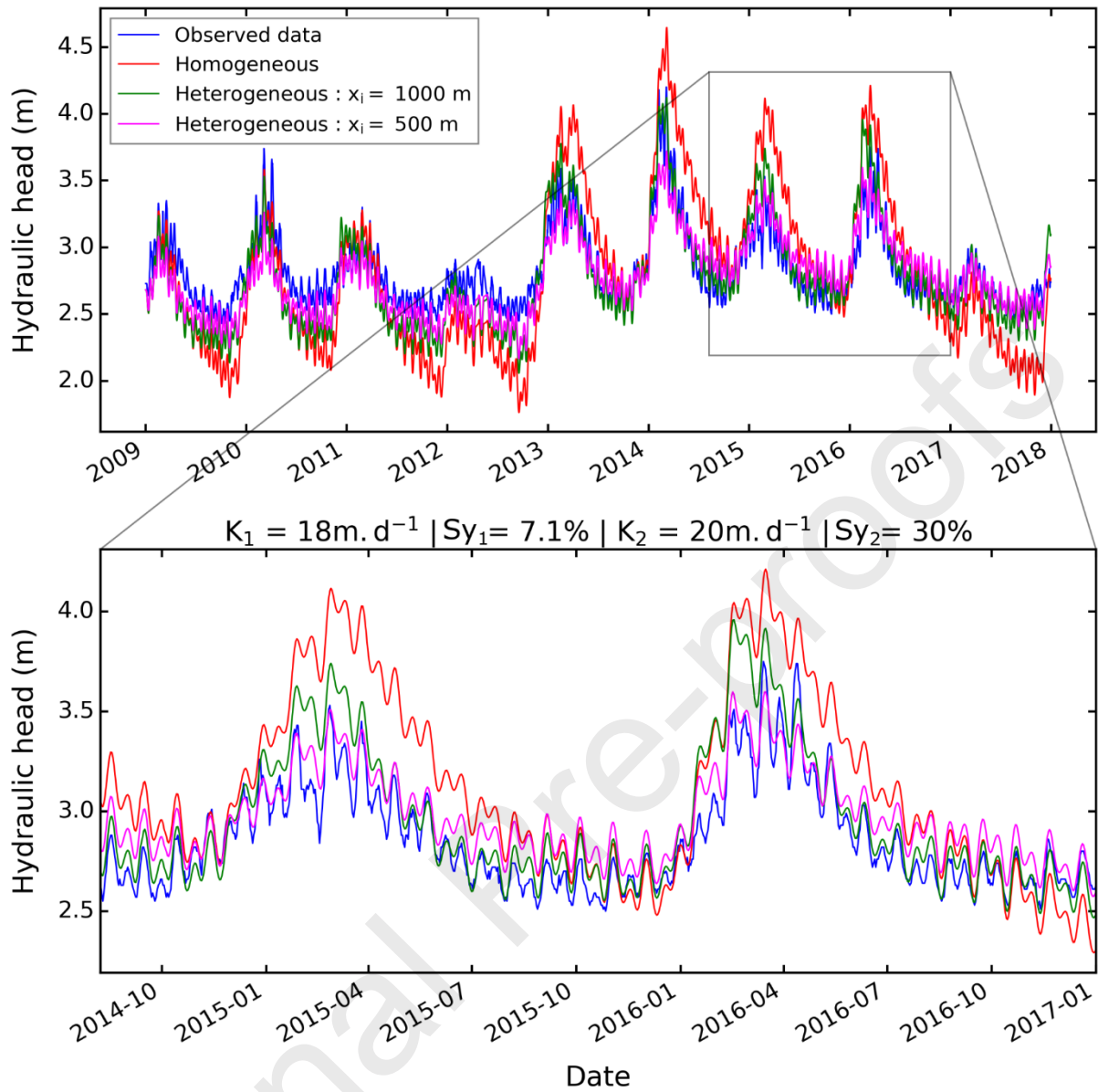
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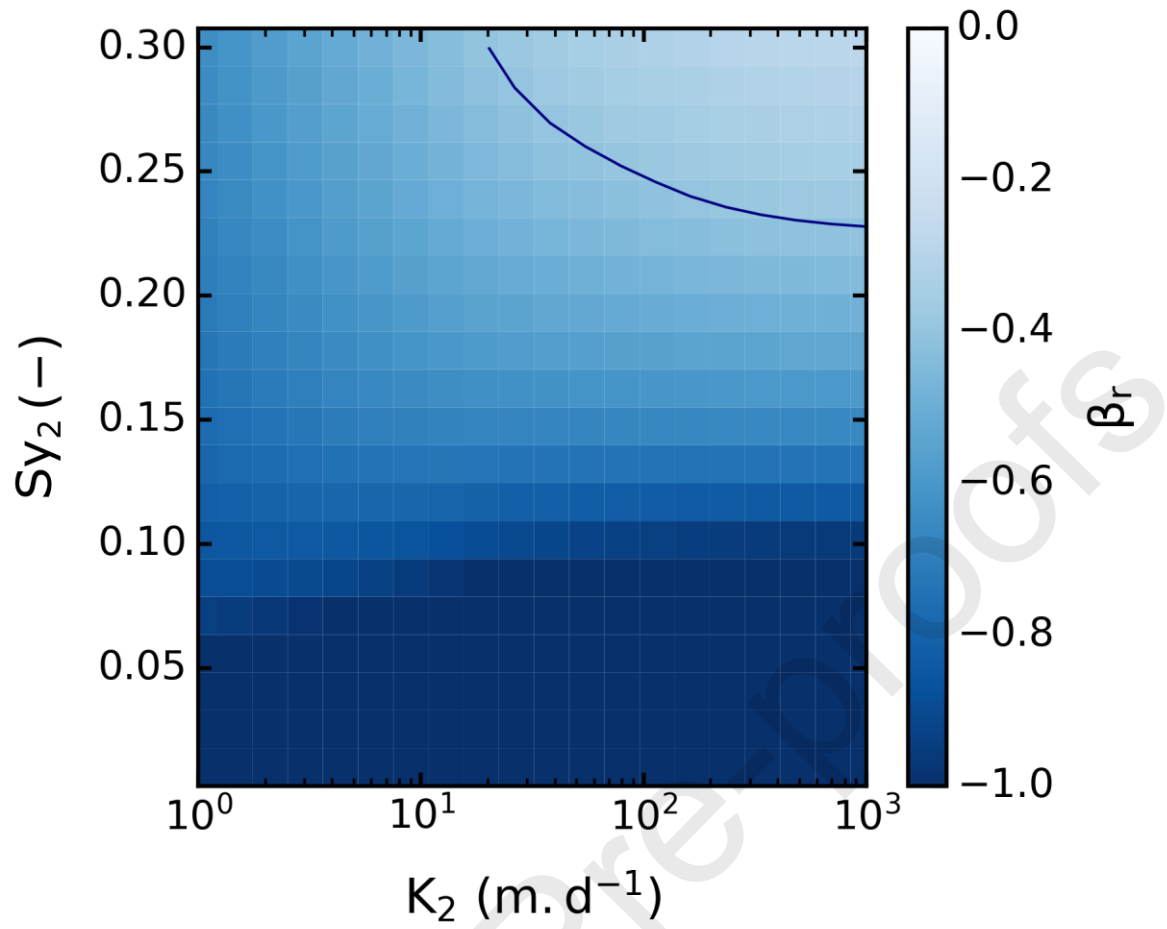
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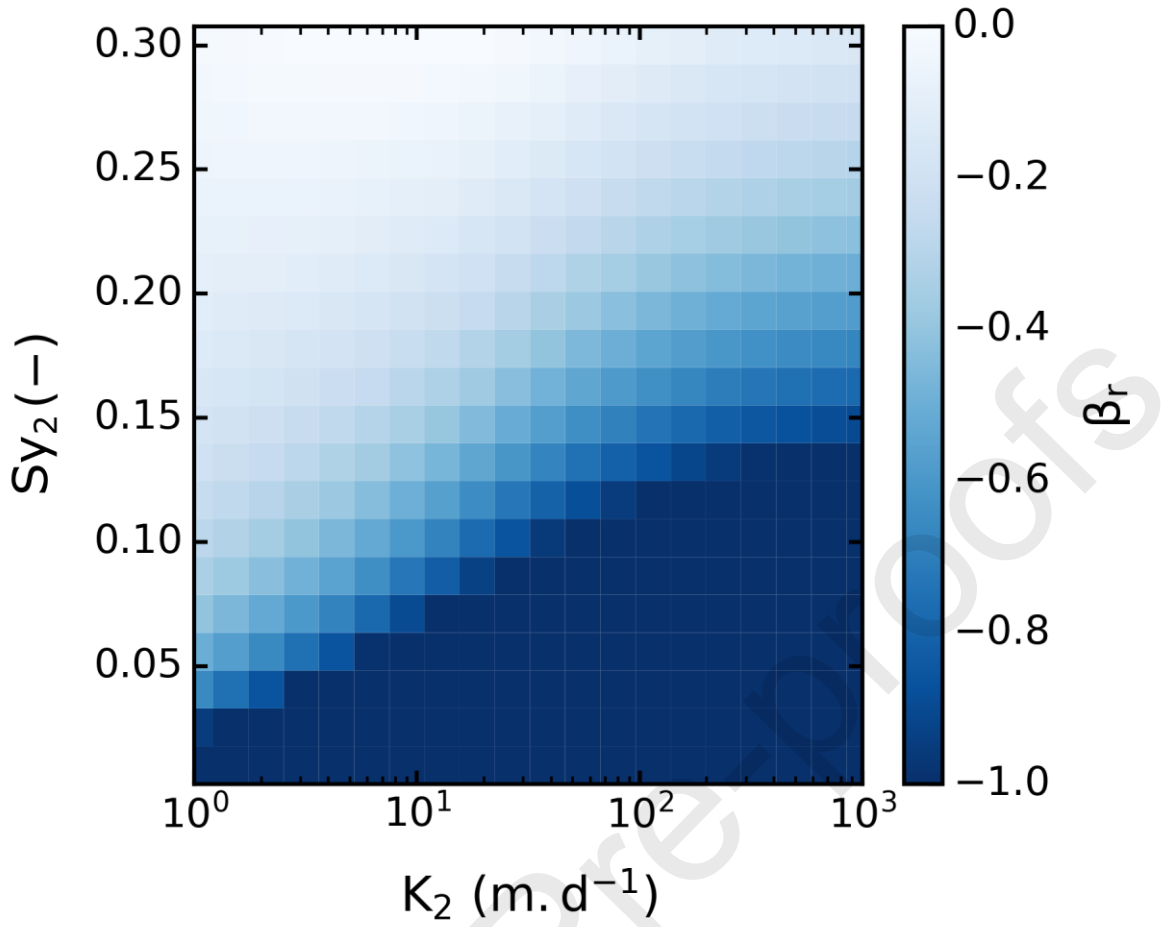
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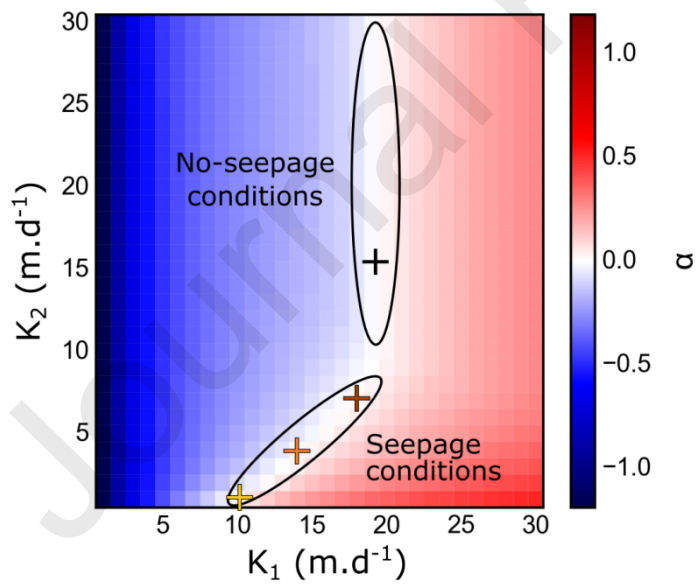
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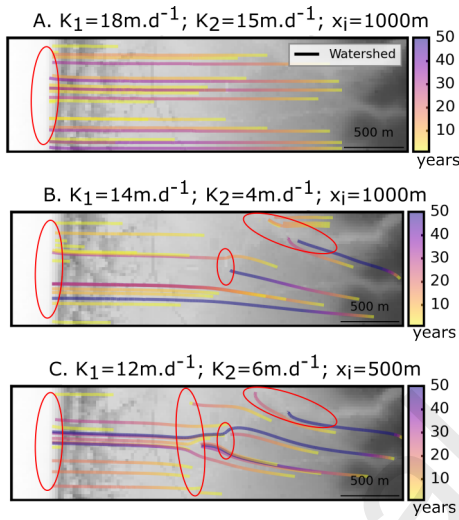
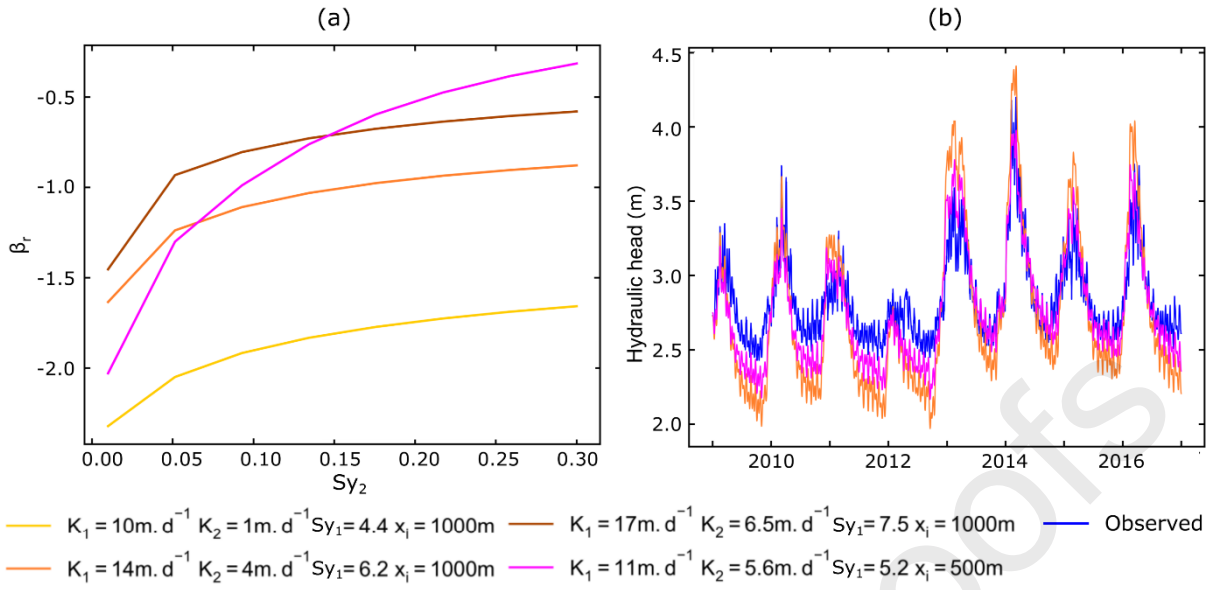


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Mean aquifer extension	L	3000 m
Distance of the lithological interface to the coast	$x_i$	600 m
Distance of the piezometer to the coast	X	400 m
Aquifer thickness at the coast	$h_{\text{sea}}$	20 m
Mean recharge rate	R	286 $\text{mm}\cdot\text{y}^{-1}$

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	Analytical	Numerical 1D	Numerical 1D	Numerical 2D	Numerical 2D	Numerical 2D
<b>Distribution</b>	Homogeneous	Homogeneous	Heterogeneous	Heterogeneous	Heterogeneous	Heterogeneous
<b>Seepage</b>	Not allowed	Not allowed	Not allowed	Not observed	Observed	Observed
$x_i$ (m)	1 000	1 000	1 000	1 000	1 000	500
$K_1$ (m.d <sup>-1</sup> )	18	18	18	18	10 - 17	5.0 - 20
$n_1$ (%)	10	7.1	7.1	8.0	4.4 – 7.5	4.4 – 7.5
$D_1$ (m <sup>2</sup> .d <sup>-1</sup> )	$3.5 \cdot 10^3$	$5.2 \cdot 10^3$	$5.2 \cdot 10^3$	$4.5 \cdot 10^3$	$2.6 \cdot 10^3 - 7.7 \cdot 10^3$	$1.3 \cdot 10^3 - 9.0 \cdot 10^3$
$K_2$ (m.d <sup>-1</sup> )			$20 - 1.0 \cdot 10^3$	9.0 - 30	1.0 – 8.0	1.0 - 15
$n_2$ (%)			23 - 30	27 - 30	15 – 30	10 - 15
$D_2$ (m <sup>2</sup> .d <sup>-1</sup> )			$1.3 \cdot 10^2 - 8.7 \cdot 10^4$	$6.0^2 - 2.6 \cdot 10^3$	$7.0 \cdot 10^1 - 7.0 \cdot 10^2$	$7.0 \cdot 10^1 - 1.2 \cdot 10^3$

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736 that could have appeared to influence the work reported in this paper.

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